

Numpy_ed

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Numpy is the fundamental package for numeric computing with Python. It provides powerful ways to create, store, and/or manipulate data, which makes it able to seamlessly and speedily integrate with a wide variety of databases. This is also the foundation that Pandas is built on, which is a high-performance data-centric package that we will learn later in the course.

In this lecture, we will talk about creating array with certain data types, manipulating array, selecting elements from arrays, and loading dataset into array. Such functions are useful for manipulating data and understanding the functionalities of other common Python data packages.

```
[3]: # You'll recall that we import a library using the `import` keyword as numpy's
      ↪ common abbreviation is np
import numpy as np
import math
```

1 Array Creation

```
[4]: # Arrays are displayed as a list or list of lists and can be created through
      ↪ list as well. When creating an
      # array, we pass in a list as an argument in numpy array
a = np.array([1, 2, 3])
print(a)
# We can print the number of dimensions of a list using the ndim attribute
print(a.ndim)
```

```
[1 2 3]
```

```
1
```

```
[5]: # If we pass in a list of lists in numpy array, we create a multi-dimensional
      ↪ array, for instance, a matrix
b = np.array([[1,2,3],[4,5,6]])
b
```

```
[5]: array([[1, 2, 3],
           [4, 5, 6]])
```

```
[6]: # We can print out the length of each dimension by calling the shape attribute,
      ↪ which returns a tuple
b.shape
```

[6]: (2, 3)

```
[7]: # We can also check the type of items in the array
a.dtype
```

[7]: dtype('int64')

```
[8]: # Besides integers, floats are also accepted in numpy arrays
c = np.array([2.2, 5, 1.1])
c.dtype.name
```

[8]: 'float64'

```
[9]: # Let's look at the data in our array
c
```

[9]: array([2.2, 5. , 1.1])

```
[10]: # Note that numpy automatically converts integers, like 5, up to floats, since
      ↳ there is no loss of precision.
      # Numpy will try and give you the best data type format possible to keep your
      ↳ data types homogeneous, which
      # means all the same, in the array
```

```
[11]: # Sometimes we know the shape of an array that we want to create, but not what
      ↳ we want to be in it. numpy
      # offers several functions to create arrays with initial placeholders, such as
      ↳ zero's or one's.
      # Lets create two arrays, both the same shape but with different filler values
d = np.zeros((2,3))
print(d)

e = np.ones((2,3))
print(e)
```

```
[[0. 0. 0.]
 [0. 0. 0.]]
[[1. 1. 1.]
 [1. 1. 1.]]
```

```
[12]: # We can also generate an array with random numbers
np.random.rand(2,3)
```

[12]: array([[0.81967966, 0.24861747, 0.1324781],
[0.10917913, 0.61025551, 0.87901984]])

```
[13]: # You'll see zeros, ones, and rand used quite often to create example arrays,
      ↳ especially in stack overflow
      # posts and other forums.
```

```
[14]: # We can also create a sequence of numbers in an array with the arrange()
      ↳ function. The first argument is the
```

```
# starting bound and the second argument is the ending bound, and the third
→argument is the difference between
# each consecutive numbers

# Let's create an array of every even number from ten (inclusive) to fifty
→(exclusive)
f = np.arange(10, 50, 2)
f
```

```
[14]: array([10, 12, 14, 16, 18, 20, 22, 24, 26, 28, 30, 32, 34, 36, 38, 40, 42,
         44, 46, 48])
```

```
[15]: # if we want to generate a sequence of floats, we can use the linspace()
→function. In this function the third
# argument isn't the difference between two numbers, but the total number of
→items you want to generate
np.linspace( 0, 2, 15 ) # 15 numbers from 0 (inclusive) to 2 (inclusive)
```

```
[15]: array([0.          , 0.14285714, 0.28571429, 0.42857143, 0.57142857,
         0.71428571, 0.85714286, 1.          , 1.14285714, 1.28571429,
         1.42857143, 1.57142857, 1.71428571, 1.85714286, 2.          ])
```

2 Array Operations

```
[16]: # We can do many things on arrays, such as mathematical manipulation (addition,
→subtraction, square,
# exponents) as well as use boolean arrays, which are binary values. We can
→also do matrix manipulation such
# as product, transpose, inverse, and so forth.
```

```
[17]: # Arithmetic operators on array apply elementwise.
```

```
# Let's create a couple of arrays
a = np.array([10,20,30,40])
b = np.array([1, 2, 3,4])

# Now let's look at a minus b
c = a-b
print(c)

# And let's look at a times b
d = a*b
print(d)
```

```
[ 9 18 27 36]
[ 10  40  90 160]
```

```
[18]: # With arithmetic manipulation, we can convert current data to the way we want
      ↪ it to be. Here's a real-world
      # problem I face - I moved down to the United States about 6 years ago from
      ↪ Canada. In Canada we use celcius
      # for temperatures, and my wife still hasn't converted to the US system which
      ↪ uses farenheit. With numpy I
      # could easily convert a number of farenheit values, say the weather forecase,
      ↪ to ceclius
```

```
# Let's create an array of typical Ann Arbor winter farenheit values
farenheit = np.array([0,-10,-5,-15,0])
```

```
# And the formula for conversion is ((°F - 32) * 5/9 = °C)
celcius = (farenheit - 31) * (5/9)
celcius
```

```
[18]: array([-17.22222222, -22.77777778, -20.          , -25.55555556,
          -17.22222222])
```

```
[19]: # Great, so now she knows it's a little chilly outside but not so bad.
```

```
[20]: # Another useful and important manipulation is the boolean array. We can apply
      ↪ an operator on an array, and a
      # boolean array will be returned for any element in the original, with True
      ↪ being emitted if it meets the condition and False oetherwise.
      # For instance, if we want to get a boolean array to check celcius degrees that
      ↪ are greater than -20 degrees
      celcius > -20
```

```
[20]: array([ True, False, False, False,  True])
```

```
[21]: # Here's another example, we could use the modulus operator to check numbers in
      ↪ an array to see if they are even. Recall that modulus does division but
      ↪ throws away everything but the remainder (decimal) portion
      celcius%2 == 0
```

```
[21]: array([False, False,  True, False, False])
```

```
[22]: # Besides elementwise manipulation, it is important to know that numpy supports
      ↪ matrix manipulation. Let's
      # look at matrix product. if we want to do elementwise product, we use the "*"
      ↪ sign
      A = np.array([[1,1],[0,1]])
      B = np.array([[2,0],[3,4]])
      print(A*B)

      # if we want to do matrix product, we use the "@" sign or use the dot function
      print(A@B)
```

```
[[2 0]
```

```
[0 4]]
[[5 4]
 [3 4]]
```

[23]: *# You don't have to worry about complex matrix operations for this course, but*
→it's important to know that
numpy is the underpinning of scientific computing libraries in python, and
→that it is capable of doing both
element-wise operations (the asterix) as well as matrix-level operations (the
→@ sign). There's more on this
in a subsequent course.

[24]: *# A few more linear algebra concepts are worth layering in here. You might*
→recall that the product of two
matrices is only plausible when the inner dimensions of the two matrices are
→the same. The dimensions refer
to the number of elements both horizontally and vertically in the rendered
→matrices you've seen here. We
can use numpy to quickly see the shape of a matrix:
`A.shape`

[24]: (2, 2)

[25]: *# When manipulating arrays of different types, the type of the resulting array*
→will correspond to
the more general of the two types. This is called upcasting.

Let's create an array of integers
`array1 = np.array([[1, 2, 3], [4, 5, 6]])`
`print(array1.dtype)`

Now let's create an array of floats
`array2 = np.array([[7.1, 8.2, 9.1], [10.4, 11.2, 12.3]])`
`print(array2.dtype)`

```
int64
float64
```

[26]: *# Integers (int) are whole numbers only, and Floating point numbers (float) can*
→have a whole number portion
and a decimal portion. The 64 in this example refers to the number of bits
→that the operating system is
reserving to represent the number, which determines the size (or precision)
→of the numbers that can be
represented.

[27]: *# Let's do an addition for the two arrays*
`array3=array1+array2`

```
print(array3)
print(array3.dtype)
```

```
[[ 8.1 10.2 12.1]
 [14.4 16.2 18.3]]
float64
```

[28]: *# Notice how the items in the resulting array have been upcast into floating_*
→point numbers

[29]: *# Numpy arrays have many interesting aggregation functions on them, such as _*
→sum(), max(), min(), and mean()

```
print(array3.sum())
print(array3.max())
print(array3.min())
print(array3.mean())
```

```
79.3
18.3
8.1
13.216666666666667
```

[30]: *# For two dimensional arrays, we can do the same thing for each row or column*
let's create an array with 15 elements, ranging from 1 to 15,
with a dimension of 3X5

```
b = np.arange(1,16,1).reshape(3,5)
print(b)
```

```
[[ 1  2  3  4  5]
 [ 6  7  8  9 10]
 [11 12 13 14 15]]
```

[31]: *# Now, we often think about two dimensional arrays being made up of rows and_*
→columns, but you can also think
*# of these arrays as just a giant ordered list of numbers, and the *shape* of_*
→the array, the number of rows
and columns, is just an abstraction that we have for a particular purpose._
→Actually, this is exactly how
basic images are stored in computer environments.

Let's take a look at an example and see how numpy comes into play.

[32]: *# For this demonstration I'll use the python imaging library (PIL) and a_*
→function to display images in the
Jupyter notebook

```
from PIL import Image
from IPython.display import display
```

```
# And let's just look at the image I'm talking about
im = Image.open('chris.tiff')
display(im)
```

```

      □
↳ -----

FileNotFoundError                                Traceback (most recent call↳
↳ last)

<ipython-input-32-12896d20ac91> in <module>
      5
      6 # And let's just look at the image I'm talking about
----> 7 im = Image.open('chris.tiff')
      8 display(im)

/opt/conda/lib/python3.7/site-packages/PIL/Image.py in open(fp, mode)
2768
2769     if filename:
-> 2770         fp = builtins.open(filename, "rb")
2771         exclusive_fp = True
2772
```

```
FileNotFoundError: [Errno 2] No such file or directory: 'chris.tiff'
```

```
[ ]: # Now, we can conver this PIL image to a numpy array
array=np.array(im)
print(array.shape)
array
```

```
[ ]: # Here we see that we have a 200x200 array and that the values are all uint8.↳
↳ The uint means that they are
# unsigned integers (so no negative numbers) and the 8 means 8 bits per byte.↳
↳ This means that each value can
# be up to 2*2*2*2*2*2*2*2=256 in size (well, actually 255, because we start at↳
↳ zero). For black and white
# images black is stored as 0 and white is stored as 255. So if we just wanted↳
↳ to invert this image we could
# use the numpy array to do so

# Let's create an array the same shape
mask=np.full(array.shape,255)
```

mask

```
[ ]: # Now let's subtract that from the modified array
modified_array=array-mask

# And lets convert all of the negative values to positive values
modified_array=modified_array*-1

# And as a last step, let's tell numpy to set the value of the datatype
    ↳correctly
modified_array=modified_array.astype(np.uint8)
modified_array

[ ]: # And lastly, lets display this new array. We do this by using the fromarray()
    ↳function in the python
# imaging library to convert the numpy array into an object jupyter can render
display(Image.fromarray(modified_array))

[ ]: # Cool. Ok, remember how I started this by talking about how we could just
    ↳think of this as a giant array
# of bytes, and that the shape was an abstraction? Well, we could just decide
    ↳to reshape the array and still
# try and render it. PIL is interpreting the individual rows as lines, so we
    ↳can change the number of lines
# and columns if we want to. What do you think that would look like?
reshaped=np.reshape(modified_array,(100,400))
print(reshaped.shape)
display(Image.fromarray(reshaped))

[ ]: # Can't say I find that particularly flattering. By reshaping the array to be
    ↳only 100 rows high but 400
# columns we've essentially doubled the image by taking every other line and
    ↳stacking them out in width. This
# makes the image look more stretched out too.

# This isn't an image manipulation course, but the point was to show you that
    ↳these numpy arrays are really
# just abstractions on top of data, and that data has an underlying format (in
    ↳this case, uint8). But further,
# we can build abstractions on top of that, such as computer code which renders
    ↳a byte as either black or
# white, which has meaning to people. In some ways, this whole degree is about
    ↳data and the abstractions that
# we can build on top of that data, from individual byte representations
    ↳through to complex neural networks of
# functions or interactive visualizations. Your role as a data scientist is to
    ↳understand what the data means
```



```
# (it's context an collection), and transform it into a different
→representation to be used for sensemaking.
```

```
[ ]: # Ok, back to the mechanics of numpy.
```

3 Indexing, Slicing and Iterating

```
[ ]: # Indexing, slicing and iterating are extremely important for data manipulation
→and analysis because these
# techinques allow us to select data based on conditions, and copy or update
→data.
```

3.1 Indexing

```
[ ]: # First we are going to look at integer indexing. A one-dimensional array,
→works in similar ways as a list -
# To get an element in a one-dimensional array, we simply use the offset index.
a = np.array([1,3,5,7])
a[2]
```

```
[33]: # For multidimensional array, we need to use integer array indexing, let's
→create a new multidimensional array
a = np.array([[1,2], [3, 4], [5, 6]])
a
```

```
[33]: array([[1, 2],
           [3, 4],
           [5, 6]])
```

```
[34]: # if we want to select one certain element, we can do so by entering the index,
→which is comprised of two
# integers the first being the row, and the second the column
a[1,1] # remember in python we start at 0!
```

```
[34]: 4
```

```
[35]: # if we want to get multiple elements
# for example, 1, 4, and 6 and put them into a one-dimensional array
# we can enter the indices directly into an array function
np.array([a[0, 0], a[1, 1], a[2, 1]])
```

```
[35]: array([1, 4, 6])
```

```
[36]: # we can also do that by using another form of array indexing, which essentiall
→"zips" the first list and the
# second list up
print(a[[0, 1, 2], [0, 1, 1]])
```

```
[1 4 6]
```

3.2 Boolean Indexing

```
[37]: # Boolean indexing allows us to select arbitrary elements based on conditions.
      → For example, in the matrix we
      # just talked about we want to find elements that are greater than 5 so we set
      → up a condition a > 5
      print(a > 5)
      # This returns a boolean array showing that if the value at the corresponding
      → index is greater than 5
```

```
[[False False]
 [False False]
 [False  True]]
```

```
[38]: # We can then place this array of booleans like a mask over the original array
      → to return a one-dimensional
      # array relating to the true values.
      print(a[a > 5])
```

```
[6]
```

```
[39]: # As we will see, this functionality is essential in the pandas toolkit which
      → is the bulk of this course
```

3.3 Slicing

```
[40]: # Slicing is a way to create a sub-array based on the original array. For
      → one-dimensional arrays, slicing
      # works in similar ways to a list. To slice, we use the : sign. For instance,
      → if we put :3 in the indexing
      # brackets, we get elements from index 0 to index 3 (excluding index 3)
      a = np.array([0,1,2,3,4,5])
      print(a[:3])
```

```
[0 1 2]
```

```
[41]: # By putting 2:4 in the bracket, we get elements from index 2 to index 4
      → (excluding index 4)
      print(a[2:4])
```

```
[2 3]
```

```
[42]: # For multi-dimensional arrays, it works similarly, let's see an example
      a = np.array([[1,2,3,4], [5,6,7,8], [9,10,11,12]])
      a
```

```
[42]: array([[ 1,  2,  3,  4],
           [ 5,  6,  7,  8],
           [ 9, 10, 11, 12]])
```

```
[43]: # First, if we put one argument in the array, for example a[:2] then we would
      ↪ get all the elements from the
      # first (0th) and second row (1th)
      a[:2]
```

```
[43]: array([[1, 2, 3, 4],
           [5, 6, 7, 8]])
```

```
[44]: # If we add another argument to the array, for example a[:2, 1:3], we get the
      ↪ first two rows but then the
      # second and third column values only
      a[:2, 1:3]
```

```
[44]: array([[2, 3],
           [6, 7]])
```

```
[45]: # So, in multidimensional arrays, the first argument is for selecting rows, and
      ↪ the second argument is for
      # selecting columns
```

```
[46]: # It is important to realize that a slice of an array is a view into the same
      ↪ data. This is called passing by
      # reference. So modifying the sub array will consequently modify the original
      ↪ array
```

```
# Here I'll change the element at position [0, 0], which is 2, to 50, then we
↪ can see that the value in the
# original array is changed to 50 as well
```

```
sub_array = a[:2, 1:3]
print("sub array index [0,0] value before change:", sub_array[0,0])
sub_array[0,0] = 50
print("sub array index [0,0] value after change:", sub_array[0,0])
print("original array index [0,1] value after change:", a[0,1])
```

```
sub array index [0,0] value before change: 2
sub array index [0,0] value after change: 50
original array index [0,1] value after change: 50
```

4 Trying Numpy with Datasets

```
[47]: # Now that we have learned the essentials of Numpy let's use it on a couple of
      ↪ datasets
```

```
[48]: # Here we have a very popular dataset on wine quality, and we are going to only
      →look at red wines. The data
      # fields include: fixed acidity, volatile acidity, citric acid, residual sugar,
      →chlorides, free sulfur dioxide,
      # total sulfur dioxide, density, pH, sulphates, alcohol, quality
```

```
[49]: # To load a dataset in Numpy, we can use the genfromtxt() function. We can
      →specify data file name, delimiter
      # (which is optional but often used), and number of rows to skip if we have a
      →header row, hence it is 1 here

      # The genfromtxt() function has a parameter called dtype for specifying data
      →types of each column this
      # parameter is optional. Without specifying the types, all types will be casted
      →the same to the more
      # general/precise type

      wines = np.genfromtxt("datasets/winequality-red.csv", delimiter=";",
      →skip_header=1)
      wines
```

```
[49]: array([[ 7.4   ,  0.7   ,  0.    , ...,  0.56 ,  9.4   ,  5.    ],
              [ 7.8   ,  0.88  ,  0.    , ...,  0.68 ,  9.8   ,  5.    ],
              [ 7.8   ,  0.76  ,  0.04  , ...,  0.65 ,  9.8   ,  5.    ],
              ...,
              [ 6.3   ,  0.51  ,  0.13  , ...,  0.75 ,  11.    ,  6.    ],
              [ 5.9   ,  0.645 ,  0.12  , ...,  0.71 ,  10.2  ,  5.    ],
              [ 6.    ,  0.31  ,  0.47  , ...,  0.66 ,  11.    ,  6.    ]])
```

```
[50]: # Recall that we can use integer indexing to get a certain column or a row. For
      →example, if we want to select
      # the fixed acidity column, which is the first column, we can do so by
      →entering the index into the array.
      # Also remember that for multidimensional arrays, the first argument refers to
      →the row, and the second
      # argument refers to the column, and if we just give one argument then we'll
      →get a single dimensional list
      # back.

      # So all rows combined but only the first column from them would be
      print("one integer 0 for slicing: ", wines[:, 0])
      # But if we wanted the same values but wanted to preserve that they sit in
      →their own rows we would write
      print("0 to 1 for slicing: \n", wines[:, 0:1])
```

```
one integer 0 for slicing: [7.4 7.8 7.8 ... 6.3 5.9 6. ]
0 to 1 for slicing:
[[7.4]
```

```
[7.8]
[7.8]
...
[6.3]
[5.9]
[6. ]]
```

```
[51]: # This is another great example of how the shape of the data is an abstraction,
      → which we can layer
      # intentionally on top of the data we are working with.
```

```
[52]: # If we want a range of columns in order, say columns 0 through 3 (recall, this
      → means first, second, and
      # third, since we start at zero and don't include the training index value), we
      → can do that too
      wines[:, 0:3]
```

```
[52]: array([[7.4  , 0.7  , 0.   ],
             [7.8  , 0.88 , 0.   ],
             [7.8  , 0.76 , 0.04 ],
             ...,
             [6.3  , 0.51 , 0.13 ],
             [5.9  , 0.645, 0.12 ],
             [6.   , 0.31 , 0.47 ]])
```

```
[53]: # What if we want several non-consecutive columns? We can place the indices of
      → the columns that we want into
      # an array and pass the array as the second argument. Here's an example
      wines[:, [0,2,4]]
```

```
[53]: array([[7.4  , 0.   , 0.076],
             [7.8  , 0.   , 0.098],
             [7.8  , 0.04 , 0.092],
             ...,
             [6.3  , 0.13 , 0.076],
             [5.9  , 0.12 , 0.075],
             [6.   , 0.47 , 0.067]])
```

```
[54]: # We can also do some basic summarization of this dataset. For example, if we
      → want to find out the average
      # quality of red wine, we can select the quality column. We could do this in a
      → couple of ways, but the most
      # appropriate is to use the -1 value for the index, as negative numbers mean
      → slicing from the back of the
      # list. We can then call the aggregation functions on this data.
      wines[:, -1].mean()
```

```
[54]: 5.6360225140712945
```

```
[55]: # Let's take a look at another dataset, this time on graduate school admissions.
      ↪ It has fields such as GRE
      # score, TOEFL score, university rating, GPA, having research experience or
      ↪not, and a chance of admission.
      # With this dataset, we can do data manipulation and basic analysis to infer
      ↪what conditions are associated
      # with higher chance of admission. Let's take a look.
```

```
[56]: # We can specify data field names when using genfromtxt() to loads CSV data.
      ↪Also, we can have numpy try and
      # infer the type of a column by setting the dtype parameter to None
graduate_admission = np.genfromtxt('datasets/Admission_Predict.csv',
      ↪dtype=None, delimiter=',', skip_header=1,
      names=('Serial No', 'GRE Score', 'TOEFL
      ↪Score', 'University Rating', 'SOP',
      'LOR', 'CGPA', 'Research', 'Chance of
      ↪Admit'))
graduate_admission
```

```
[56]: array([( 1, 337, 118, 4, 4.5, 4.5, 9.65, 1, 0.92),
      ( 2, 324, 107, 4, 4. , 4.5, 8.87, 1, 0.76),
      ( 3, 316, 104, 3, 3. , 3.5, 8. , 1, 0.72),
      ( 4, 322, 110, 3, 3.5, 2.5, 8.67, 1, 0.8 ),
      ( 5, 314, 103, 2, 2. , 3. , 8.21, 0, 0.65),
      ( 6, 330, 115, 5, 4.5, 3. , 9.34, 1, 0.9 ),
      ( 7, 321, 109, 3, 3. , 4. , 8.2 , 1, 0.75),
      ( 8, 308, 101, 2, 3. , 4. , 7.9 , 0, 0.68),
      ( 9, 302, 102, 1, 2. , 1.5, 8. , 0, 0.5 ),
      (10, 323, 108, 3, 3.5, 3. , 8.6 , 0, 0.45),
      (11, 325, 106, 3, 3.5, 4. , 8.4 , 1, 0.52),
      (12, 327, 111, 4, 4. , 4.5, 9. , 1, 0.84),
      (13, 328, 112, 4, 4. , 4.5, 9.1 , 1, 0.78),
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 (305, 313, 106, 2, 2.5, 2. , 8.43, 0, 0.62),
 (306, 321, 109, 3, 3.5, 3.5, 8.8 , 1, 0.74),
 (307, 323, 110, 3, 4. , 3.5, 9.1 , 1, 0.79),
 (308, 325, 112, 4, 4. , 4. , 9. , 1, 0.8),
 (309, 312, 108, 3, 3.5, 3. , 8.53, 0, 0.69),
 (310, 308, 110, 4, 3.5, 3. , 8.6 , 0, 0.7),

(311, 320, 104, 3, 3. , 3.5, 8.74, 1, 0.76),
 (312, 328, 108, 4, 4.5, 4. , 9.18, 1, 0.84),
 (313, 311, 107, 4, 4.5, 4.5, 9. , 1, 0.78),
 (314, 301, 100, 3, 3.5, 3. , 8.04, 0, 0.67),
 (315, 305, 105, 2, 3. , 4. , 8.13, 0, 0.66),
 (316, 308, 104, 2, 2.5, 3. , 8.07, 0, 0.65),
 (317, 298, 101, 2, 1.5, 2. , 7.86, 0, 0.54),
 (318, 300, 99, 1, 1. , 2.5, 8.01, 0, 0.58),
 (319, 324, 111, 3, 2.5, 2. , 8.8 , 1, 0.79),
 (320, 327, 113, 4, 3.5, 3. , 8.69, 1, 0.8),
 (321, 317, 106, 3, 4. , 3.5, 8.5 , 1, 0.75),
 (322, 323, 104, 3, 4. , 4. , 8.44, 1, 0.73),
 (323, 314, 107, 2, 2.5, 4. , 8.27, 0, 0.72),
 (324, 305, 102, 2, 2. , 2.5, 8.18, 0, 0.62),
 (325, 315, 104, 3, 3. , 2.5, 8.33, 0, 0.67),
 (326, 326, 116, 3, 3.5, 4. , 9.14, 1, 0.81),
 (327, 299, 100, 3, 2. , 2. , 8.02, 0, 0.63),
 (328, 295, 101, 2, 2.5, 2. , 7.86, 0, 0.69),
 (329, 324, 112, 4, 4. , 3.5, 8.77, 1, 0.8),
 (330, 297, 96, 2, 2.5, 1.5, 7.89, 0, 0.43),
 (331, 327, 113, 3, 3.5, 3. , 8.66, 1, 0.8),
 (332, 311, 105, 2, 3. , 2. , 8.12, 1, 0.73),
 (333, 308, 106, 3, 3.5, 2.5, 8.21, 1, 0.75),
 (334, 319, 108, 3, 3. , 3.5, 8.54, 1, 0.71),
 (335, 312, 107, 4, 4.5, 4. , 8.65, 1, 0.73),
 (336, 325, 111, 4, 4. , 4.5, 9.11, 1, 0.83),
 (337, 319, 110, 3, 3. , 2.5, 8.79, 0, 0.72),
 (338, 332, 118, 5, 5. , 5. , 9.47, 1, 0.94),
 (339, 323, 108, 5, 4. , 4. , 8.74, 1, 0.81),
 (340, 324, 107, 5, 3.5, 4. , 8.66, 1, 0.81),
 (341, 312, 107, 3, 3. , 3. , 8.46, 1, 0.75),
 (342, 326, 110, 3, 3.5, 3.5, 8.76, 1, 0.79),
 (343, 308, 106, 3, 3. , 3. , 8.24, 0, 0.58),
 (344, 305, 103, 2, 2.5, 3.5, 8.13, 0, 0.59),
 (345, 295, 96, 2, 1.5, 2. , 7.34, 0, 0.47),
 (346, 316, 98, 1, 1.5, 2. , 7.43, 0, 0.49),
 (347, 304, 97, 2, 1.5, 2. , 7.64, 0, 0.47),
 (348, 299, 94, 1, 1. , 1. , 7.34, 0, 0.42),
 (349, 302, 99, 1, 2. , 2. , 7.25, 0, 0.57),
 (350, 313, 101, 3, 2.5, 3. , 8.04, 0, 0.62),
 (351, 318, 107, 3, 3. , 3.5, 8.27, 1, 0.74),
 (352, 325, 110, 4, 3.5, 4. , 8.67, 1, 0.73),
 (353, 303, 100, 2, 3. , 3.5, 8.06, 1, 0.64),
 (354, 300, 102, 3, 3.5, 2.5, 8.17, 0, 0.63),
 (355, 297, 98, 2, 2.5, 3. , 7.67, 0, 0.59),
 (356, 317, 106, 2, 2. , 3.5, 8.12, 0, 0.73),
 (357, 327, 109, 3, 3.5, 4. , 8.77, 1, 0.79),

```

(358, 301, 104, 2, 3.5, 3.5, 7.89, 1, 0.68),
(359, 314, 105, 2, 2.5, 2. , 7.64, 0, 0.7 ),
(360, 321, 107, 2, 2. , 1.5, 8.44, 0, 0.81),
(361, 322, 110, 3, 4. , 5. , 8.64, 1, 0.85),
(362, 334, 116, 4, 4. , 3.5, 9.54, 1, 0.93),
(363, 338, 115, 5, 4.5, 5. , 9.23, 1, 0.91),
(364, 306, 103, 2, 2.5, 3. , 8.36, 0, 0.69),
(365, 313, 102, 3, 3.5, 4. , 8.9 , 1, 0.77),
(366, 330, 114, 4, 4.5, 3. , 9.17, 1, 0.86),
(367, 320, 104, 3, 3.5, 4.5, 8.34, 1, 0.74),
(368, 311, 98, 1, 1. , 2.5, 7.46, 0, 0.57),
(369, 298, 92, 1, 2. , 2. , 7.88, 0, 0.51),
(370, 301, 98, 1, 2. , 3. , 8.03, 1, 0.67),
(371, 310, 103, 2, 2.5, 2.5, 8.24, 0, 0.72),
(372, 324, 110, 3, 3.5, 3. , 9.22, 1, 0.89),
(373, 336, 119, 4, 4.5, 4. , 9.62, 1, 0.95),
(374, 321, 109, 3, 3. , 3. , 8.54, 1, 0.79),
(375, 315, 105, 2, 2. , 2.5, 7.65, 0, 0.39),
(376, 304, 101, 2, 2. , 2.5, 7.66, 0, 0.38),
(377, 297, 96, 2, 2.5, 2. , 7.43, 0, 0.34),
(378, 290, 100, 1, 1.5, 2. , 7.56, 0, 0.47),
(379, 303, 98, 1, 2. , 2.5, 7.65, 0, 0.56),
(380, 311, 99, 1, 2.5, 3. , 8.43, 1, 0.71),
(381, 322, 104, 3, 3.5, 4. , 8.84, 1, 0.78),
(382, 319, 105, 3, 3. , 3.5, 8.67, 1, 0.73),
(383, 324, 110, 4, 4.5, 4. , 9.15, 1, 0.82),
(384, 300, 100, 3, 3. , 3.5, 8.26, 0, 0.62),
(385, 340, 113, 4, 5. , 5. , 9.74, 1, 0.96),
(386, 335, 117, 5, 5. , 5. , 9.82, 1, 0.96),
(387, 302, 101, 2, 2.5, 3.5, 7.96, 0, 0.46),
(388, 307, 105, 2, 2. , 3.5, 8.1 , 0, 0.53),
(389, 296, 97, 2, 1.5, 2. , 7.8 , 0, 0.49),
(390, 320, 108, 3, 3.5, 4. , 8.44, 1, 0.76),
(391, 314, 102, 2, 2. , 2.5, 8.24, 0, 0.64),
(392, 318, 106, 3, 2. , 3. , 8.65, 0, 0.71),
(393, 326, 112, 4, 4. , 3.5, 9.12, 1, 0.84),
(394, 317, 104, 2, 3. , 3. , 8.76, 0, 0.77),
(395, 329, 111, 4, 4.5, 4. , 9.23, 1, 0.89),
(396, 324, 110, 3, 3.5, 3.5, 9.04, 1, 0.82),
(397, 325, 107, 3, 3. , 3.5, 9.11, 1, 0.84),
(398, 330, 116, 4, 5. , 4.5, 9.45, 1, 0.91),
(399, 312, 103, 3, 3.5, 4. , 8.78, 0, 0.67),
(400, 333, 117, 4, 5. , 4. , 9.66, 1, 0.95)],
dtype=[('Serial_No', '<i8'), ('GRE_Score', '<i8'), ('TOEFL_Score', '<i8'),
('University_Rating', '<i8'), ('SOP', '<f8'), ('LOR', '<f8'), ('CGPA', '<f8'),
('Research', '<i8'), ('Chance_of_Admit', '<f8')]]

```

```
[57]: # Notice that the resulting array is actually a one-dimensional array with 400
      ↪ tuples
      graduate_admission.shape
```

```
[57]: (400,)
```

```
[58]: # We can retrieve a column from the array using the column's name for example,
      ↪ let's get the CGPA column and
      # only the first five values.
      graduate_admission['CGPA'][0:5]
```

```
[58]: array([9.65, 8.87, 8.    , 8.67, 8.21])
```

```
[59]: # Since the GPA in the dataset range from 1 to 10, and in the US it's more
      ↪ common to use a scale of up to 4,
      # a common task might be to convert the GPA by dividing by 10 and then
      ↪ multiplying by 4
      graduate_admission['CGPA'] = graduate_admission['CGPA'] /10 *4
      graduate_admission['CGPA'][0:20] #let's get 20 values
```

```
[59]: array([3.86 , 3.548, 3.2   , 3.468, 3.284, 3.736, 3.28 , 3.16 , 3.2   ,
        3.44 , 3.36 , 3.6   , 3.64 , 3.2   , 3.28 , 3.32 , 3.48 , 3.2   ,
        3.52 , 3.4   ])
```

```
[60]: # Recall boolean masking. We can use this to find out how many students have
      ↪ had research experience by
      # creating a boolean mask and passing it to the array indexing operator
      len(graduate_admission[graduate_admission['Research'] == 1])
```

```
[60]: 219
```

```
[61]: # Since we have the data field chance of admission, which ranges from 0 to 1,
      ↪ we can try to see if students
      # with high chance of admission (>0.8) on average have higher GRE score than
      ↪ those with lower chance of
      # admission (<0.4)

      # So first we use boolean masking to pull out only those students we are
      ↪ interested in based on their chance
      # of admission, then we pull out only their GPA scores, then we print the mean
      ↪ values.
      print(graduate_admission[graduate_admission['Chance_of_Admit'] > 0.
      ↪ 8] ['GRE_Score'].mean())
      print(graduate_admission[graduate_admission['Chance_of_Admit'] < 0.
      ↪ 4] ['GRE_Score'].mean())
```

```
328.7350427350427
302.2857142857143
```

```
[62]: # Take a moment to reflect here, do you understand what is happening in these
      ↪ calls?

      # When we do the boolean masking we are left with an array with tuples in it
      ↪ still, and numpy holds underneath
      # this a list of the columns we specified and their name and indexes
      graduate_admission[graduate_admission['Chance_of_Admit'] > 0.8]
```

```
[62]: array([( 1, 337, 118, 4, 4.5, 4.5, 3.86 , 1, 0.92),
             ( 6, 330, 115, 5, 4.5, 3. , 3.736, 1, 0.9 ),
             (12, 327, 111, 4, 4. , 4.5, 3.6 , 1, 0.84),
             (23, 328, 116, 5, 5. , 5. , 3.8 , 1, 0.94),
             (24, 334, 119, 5, 5. , 4.5, 3.88 , 1, 0.95),
             (25, 336, 119, 5, 4. , 3.5, 3.92 , 1, 0.97),
             (26, 340, 120, 5, 4.5, 4.5, 3.84 , 1, 0.94),
             (33, 338, 118, 4, 3. , 4.5, 3.76 , 1, 0.91),
             (34, 340, 114, 5, 4. , 4. , 3.84 , 1, 0.9 ),
             (35, 331, 112, 5, 4. , 5. , 3.92 , 1, 0.94),
             (36, 320, 110, 5, 5. , 5. , 3.68 , 1, 0.88),
             (44, 332, 117, 4, 4.5, 4. , 3.64 , 0, 0.87),
             (45, 326, 113, 5, 4.5, 4. , 3.76 , 1, 0.91),
             (46, 322, 110, 5, 5. , 4. , 3.64 , 1, 0.88),
             (47, 329, 114, 5, 4. , 5. , 3.72 , 1, 0.86),
             (48, 339, 119, 5, 4.5, 4. , 3.88 , 0, 0.89),
             (49, 321, 110, 3, 3.5, 5. , 3.54 , 1, 0.82),
             (71, 332, 118, 5, 5. , 5. , 3.856, 1, 0.94),
             (72, 336, 112, 5, 5. , 5. , 3.904, 1, 0.96),
             (73, 321, 111, 5, 5. , 5. , 3.78 , 1, 0.93),
             (74, 314, 108, 4, 4.5, 4. , 3.616, 1, 0.84),
             (82, 340, 120, 4, 5. , 5. , 3.8 , 1, 0.96),
             (83, 320, 110, 5, 5. , 4.5, 3.688, 1, 0.92),
             (84, 322, 115, 5, 4. , 4.5, 3.744, 1, 0.92),
             (85, 340, 115, 5, 4.5, 4.5, 3.78 , 1, 0.94),
             (98, 331, 120, 3, 4. , 4. , 3.584, 1, 0.86),
             (99, 332, 119, 4, 5. , 4.5, 3.696, 1, 0.9 ),
            (107, 329, 111, 4, 4.5, 4.5, 3.672, 1, 0.87),
            (108, 338, 117, 4, 3.5, 4.5, 3.784, 1, 0.91),
            (109, 331, 116, 5, 5. , 5. , 3.752, 1, 0.93),
            (121, 335, 117, 5, 5. , 5. , 3.824, 1, 0.94),
            (122, 334, 119, 5, 4.5, 4.5, 3.792, 1, 0.94),
            (127, 323, 113, 3, 4. , 3. , 3.728, 1, 0.85),
            (129, 326, 112, 3, 3.5, 3. , 3.64 , 1, 0.84),
            (130, 333, 118, 5, 5. , 5. , 3.74 , 1, 0.92),
            (131, 339, 114, 5, 4. , 4.5, 3.904, 1, 0.96),
            (135, 333, 113, 5, 4. , 4. , 3.712, 1, 0.89),
            (136, 314, 109, 4, 3.5, 4. , 3.508, 1, 0.82),
            (141, 329, 110, 2, 4. , 3. , 3.66 , 1, 0.84),
```


(142, 332, 118, 2, 4.5, 3.5, 3.744, 1, 0.9),
 (143, 331, 115, 5, 4. , 3.5, 3.776, 1, 0.92),
 (144, 340, 120, 4, 4.5, 4. , 3.968, 1, 0.97),
 (146, 320, 113, 2, 2. , 2.5, 3.456, 1, 0.81),
 (148, 326, 114, 3, 3. , 3. , 3.644, 1, 0.83),
 (149, 339, 116, 4, 4. , 3.5, 3.92 , 1, 0.96),
 (151, 334, 114, 4, 4. , 4. , 3.772, 1, 0.93),
 (152, 332, 116, 5, 5. , 5. , 3.712, 1, 0.94),
 (153, 321, 112, 5, 5. , 5. , 3.624, 1, 0.86),
 (165, 329, 111, 4, 4.5, 4. , 3.604, 1, 0.81),
 (172, 334, 117, 5, 4. , 4.5, 3.628, 1, 0.89),
 (173, 322, 110, 4, 4. , 5. , 3.652, 1, 0.86),
 (174, 323, 113, 4, 4. , 4.5, 3.692, 1, 0.89),
 (175, 321, 111, 4, 4. , 4. , 3.588, 1, 0.87),
 (176, 320, 111, 4, 4.5, 3.5, 3.548, 1, 0.85),
 (177, 329, 119, 4, 4.5, 4.5, 3.664, 1, 0.9),
 (178, 319, 110, 3, 3.5, 3.5, 3.616, 0, 0.82),
 (186, 327, 113, 4, 4.5, 4.5, 3.644, 1, 0.89),
 (187, 317, 107, 3, 3.5, 3. , 3.472, 1, 0.84),
 (188, 335, 118, 5, 4.5, 3.5, 3.776, 1, 0.93),
 (189, 331, 115, 5, 4.5, 3.5, 3.744, 1, 0.93),
 (190, 324, 112, 5, 5. , 5. , 3.632, 1, 0.88),
 (191, 324, 111, 5, 4.5, 4. , 3.664, 1, 0.9),
 (192, 323, 110, 5, 4. , 5. , 3.592, 1, 0.87),
 (193, 322, 114, 5, 4.5, 4. , 3.576, 1, 0.86),
 (194, 336, 118, 5, 4.5, 5. , 3.812, 1, 0.94),
 (203, 340, 120, 5, 4.5, 4.5, 3.964, 1, 0.97),
 (204, 334, 120, 5, 4. , 5. , 3.948, 1, 0.97),
 (212, 328, 110, 4, 5. , 4. , 3.656, 1, 0.82),
 (213, 338, 120, 4, 5. , 5. , 3.864, 1, 0.95),
 (214, 333, 119, 5, 5. , 4.5, 3.912, 1, 0.96),
 (215, 331, 117, 4, 4.5, 5. , 3.768, 1, 0.94),
 (216, 330, 116, 5, 5. , 4.5, 3.744, 1, 0.93),
 (217, 322, 112, 4, 4.5, 4.5, 3.704, 1, 0.91),
 (218, 321, 109, 4, 4. , 4. , 3.652, 1, 0.85),
 (219, 324, 110, 4, 3. , 3.5, 3.588, 1, 0.84),
 (230, 324, 111, 4, 3. , 3. , 3.604, 1, 0.82),
 (235, 330, 113, 5, 5. , 4. , 3.724, 1, 0.91),
 (236, 326, 111, 5, 4.5, 4. , 3.692, 1, 0.88),
 (237, 325, 112, 4, 4. , 4.5, 3.668, 1, 0.85),
 (238, 329, 114, 5, 4.5, 5. , 3.676, 1, 0.86),
 (246, 328, 110, 4, 4. , 2.5, 3.608, 1, 0.81),
 (254, 335, 115, 4, 4.5, 4.5, 3.872, 1, 0.93),
 (255, 321, 114, 4, 4. , 5. , 3.648, 0, 0.85),
 (260, 331, 119, 4, 5. , 4.5, 3.736, 1, 0.9),
 (261, 327, 108, 5, 5. , 3.5, 3.652, 1, 0.87),
 (269, 327, 113, 4, 4.5, 5. , 3.656, 0, 0.83),

```

(277, 329, 113, 5, 5. , 4.5, 3.78 , 1, 0.89),
(283, 312, 106, 3, 4. , 3.5, 3.516, 1, 0.81),
(285, 340, 112, 4, 5. , 4.5, 3.864, 1, 0.94),
(286, 331, 116, 5, 4. , 4. , 3.704, 1, 0.93),
(287, 336, 118, 5, 4.5, 4. , 3.676, 1, 0.92),
(288, 324, 114, 5, 5. , 4.5, 3.632, 1, 0.89),
(289, 314, 104, 4, 5. , 5. , 3.608, 0, 0.82),
(298, 320, 120, 3, 4. , 4.5, 3.644, 0, 0.86),
(299, 330, 114, 3, 4.5, 4.5, 3.696, 1, 0.9 ),
(312, 328, 108, 4, 4.5, 4. , 3.672, 1, 0.84),
(326, 326, 116, 3, 3.5, 4. , 3.656, 1, 0.81),
(336, 325, 111, 4, 4. , 4.5, 3.644, 1, 0.83),
(338, 332, 118, 5, 5. , 5. , 3.788, 1, 0.94),
(339, 323, 108, 5, 4. , 4. , 3.496, 1, 0.81),
(340, 324, 107, 5, 3.5, 4. , 3.464, 1, 0.81),
(360, 321, 107, 2, 2. , 1.5, 3.376, 0, 0.81),
(361, 322, 110, 3, 4. , 5. , 3.456, 1, 0.85),
(362, 334, 116, 4, 4. , 3.5, 3.816, 1, 0.93),
(363, 338, 115, 5, 4.5, 5. , 3.692, 1, 0.91),
(366, 330, 114, 4, 4.5, 3. , 3.668, 1, 0.86),
(372, 324, 110, 3, 3.5, 3. , 3.688, 1, 0.89),
(373, 336, 119, 4, 4.5, 4. , 3.848, 1, 0.95),
(383, 324, 110, 4, 4.5, 4. , 3.66 , 1, 0.82),
(385, 340, 113, 4, 5. , 5. , 3.896, 1, 0.96),
(386, 335, 117, 5, 5. , 5. , 3.928, 1, 0.96),
(393, 326, 112, 4, 4. , 3.5, 3.648, 1, 0.84),
(395, 329, 111, 4, 4.5, 4. , 3.692, 1, 0.89),
(396, 324, 110, 3, 3.5, 3.5, 3.616, 1, 0.82),
(397, 325, 107, 3, 3. , 3.5, 3.644, 1, 0.84),
(398, 330, 116, 4, 5. , 4.5, 3.78 , 1, 0.91),
(400, 333, 117, 4, 5. , 4. , 3.864, 1, 0.95)],
dtype=[('Serial_No', '<i8'), ('GRE_Score', '<i8'), ('TOEFL_Score', '<i8'),
('University_Rating', '<i8'), ('SOP', '<f8'), ('LOR', '<f8'), ('CGPA', '<f8'),
('Research', '<i8'), ('Chance_of_Admit', '<f8')])

```

```

[63]: # Let's also do this with GPA
print(graduate_admission[graduate_admission['Chance_of_Admit'] > 0.8]['CGPA'].
      ↪mean())
print(graduate_admission[graduate_admission['Chance_of_Admit'] < 0.4]['CGPA'].
      ↪mean())

```

```

3.7106666666666666
3.0222857142857142

```

```

[64]: # Hrm, well, I guess one could have expected this. The GPA and GRE for students
      ↪who have a higher chance of
      # being admitted, at least based on our cursory look here, seems to be higher.

```

So that's a bit of a whirlwing tour of numpy, the core scientific computing library in python. Now, you're going to see a lot more of this kind of discussion, as the library we'll be focusing on in this course is pandas, which is built on top of numpy. Don't worry if it didn't all sink in the first time, we're going to dig in to most of these topics again with pandas. However, it's useful to know that many of the functions and capabilities of numpy are available to you within pandas.