

# 1 Table of Some Anti-derivatives

- $\int x^n dx = \begin{cases} \frac{x^{n+1}}{n+1}, & n \neq -1 \\ \ln|x|, & n = -1 \end{cases}$ .
- $\int \frac{dx}{a^2+x^2} = \frac{1}{a} \operatorname{arctg} \frac{x}{a}$ .
- $\int \frac{dx}{a^2-x^2} = \frac{1}{2a} \ln \left| \frac{a+x}{a-x} \right|$ .
- $\int \ln x dx = x \ln x - x$ .
- $\int \frac{dx}{x \ln x} = \ln |\ln x|$ .
- $\int \log_b x dx = x \frac{\ln x - 1}{\ln b}$ .
- $\int e^x dx = e^x$ .
- $\int a^x dx = \frac{a^x}{\ln a}$ .
- $\int \frac{x dx}{a^2 \pm x^2} = \pm \frac{1}{2} \ln |a^2 \pm x^2|$ .
- $\int \frac{dx}{\sqrt{a^2-x^2}} = \arcsin \frac{x}{a} \ (a > 0)$ .
- $\int \frac{-dx}{\sqrt{a^2-x^2}} = \arccos \frac{x}{a} \ (a > 0)$ .
- $\int \frac{dx}{\sqrt{x^2 \pm a^2}} = \ln |x + \sqrt{x^2 \pm a^2}| \ (a > 0)$ .
- $\int \frac{x dx}{\sqrt{a^2 \pm x^2}} = \pm \sqrt{a^2 \pm x^2} \ (a > 0)$ .
- $\int \sqrt{a^2 - x^2} dx = \frac{x}{2} \sqrt{a^2 - x^2} + \frac{a^2}{2} \arcsin \frac{x}{a} \ (a > 0)$ .
- $\int \sqrt{x^2 \pm a^2} dx = \frac{x}{2} \sqrt{x^2 \pm a^2} \pm \frac{a^2}{2} \ln |x + \sqrt{x^2 \pm a^2}| \ (a > 0)$ .
- $\int \sin x dx = -\cos x$ .
- $\int \cos x dx = \sin x$ .
- $\int \operatorname{tg} x dx = -\ln |\cos x|$ .
- $\int \operatorname{ctg} x dx = \ln |\sin x|$ .
- $\int \sin^2 x dx = \frac{1}{2}(x - \sin x \cos x)$ .
- $\int \cos^2 x dx = \frac{1}{2}(x + \sin x \cos x)$ .
- $\int \arcsin x dx = x \arcsin x + \sqrt{1-x^2}$ .
- $\int \arccos x dx = x \arccos x - \sqrt{1-x^2}$ .
- $\int \operatorname{arctg} x dx = x \operatorname{arctg} x - \frac{1}{2} \ln(1+x^2)$ .
- $\int \operatorname{arcctg} x dx = x \operatorname{arcctg} x + \frac{1}{2} \ln(1+x^2)$ .
- $\int \operatorname{sh} x dx = \operatorname{ch} x$ .
- $\int \operatorname{ch} x dx = \operatorname{sh} x$ .
- $\int \operatorname{th} x dx = \ln |\operatorname{ch} x|$ .
- $\int \operatorname{cth} x dx = \ln |\operatorname{sh} x|$ .
- $\int \operatorname{arsh} x dx = x \operatorname{arsh} x - \sqrt{x^2+1}$ .
- $\int \operatorname{arch} x dx = x \operatorname{arch} x - \sqrt{x^2-1}$ .
- $\int \operatorname{arth} x dx = x \operatorname{arth} x + \frac{1}{2} \ln |1-x^2|$ .
- $\int \operatorname{arcth} x dx = x \operatorname{arcth} x + \frac{1}{2} \ln |x^2-1|$ .
- $\int |x| dx = \frac{|x|x}{2}$ .
- $\int \operatorname{sgn} x dx = |x|$ .
- $\int \operatorname{sgn} x \cdot f(x) dx = \operatorname{sgn} x \int f(x) dx$ .