

Homework 9 - Physics 240

Gauss and Kirchhoff

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1 Introduction

The purpose of this exercise is to practice the Gaussian elimination method to solve a system of linear equations. In this case, the system of equations is constructed by applying Kirchhoff's laws of current to the circuit given in the homework. The system equation I came up with is :

$$\begin{aligned}E_1 - I_1 R_1 - I_2 R_3 - E_2 - I_1 R_2 &= 0 \\-I_3 R_4 - E_3 - I_3 R_5 + E_2 + I_2 R_3 &= 0 \\I_1 - I_2 - I_3 &= 0\end{aligned}$$

Applying the values for $R_1 = R_2 = 1$, $R_3 = R_4 = 2$, $R_5 = 5$, $E_1 = 2$, $E_3 = 5$, and $E_2 = 20$ I get the following equations

$$\begin{aligned}I_1 + I_2 + 0 &= -9 \\7I_3 - 2I_2 &= 15 \\I_1 - I_2 - I_3 &= 0\end{aligned}$$

Putting the matrix form of this system of equations into my program and I get

$$\begin{aligned}I_1 &= -4.125 \\I_2 &= -4.875 \\I_3 &= 0.75\end{aligned}$$

The answers are verified with `numpy.linalg`, direct substitution, and reduced row echelon form methods, all of which gave the same answers.