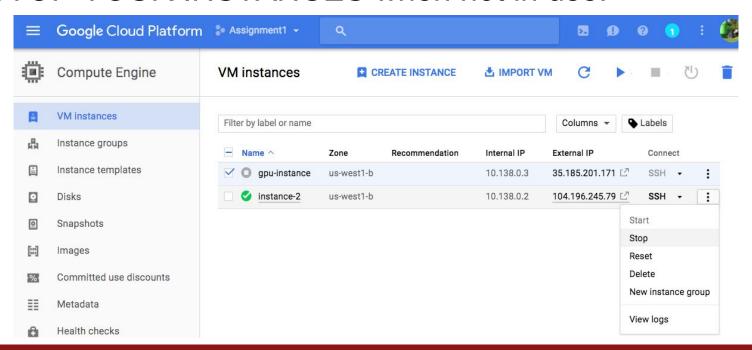
Lecture 7: Training Neural Networks, Part 2

Administrative

- Assignment 1 is being graded, stay tuned
- Project proposals due today by 11:59pm
- Assignment 2 is out, due Thursday May 4 at 11:59pm

Administrative: Google Cloud

STOP YOUR INSTANCES when not in use!



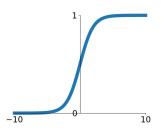
Administrative: Google Cloud

- STOP YOUR INSTANCES when not in use!
- Keep track of your spending!
- GPU instances are much more expensive than CPU instances - only use GPU instance when you need it (e.g. for A2 only on TensorFlow / PyTorch notebooks)

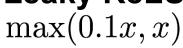
Last time: Activation Functions

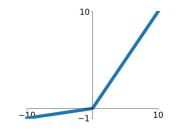
Sigmoid

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$



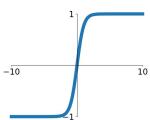
Leaky ReLU





tanh

tanh(x)

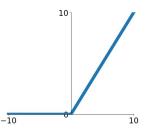


Maxout

 $\max(w_1^T x + b_1, w_2^T x + b_2)$

ReLU

 $\max(0,x)$

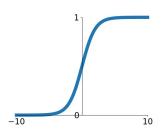


$$\begin{cases} x & x \ge 0 \\ \alpha(e^x - 1) & x < 0 \end{cases}$$

Last time: Activation Functions

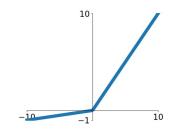
Sigmoid

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$



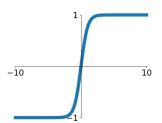
Leaky ReLU

 $\max(0.1x, x)$



tanh

tanh(x)



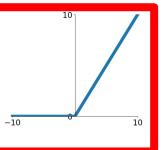
Maxout

 $\max(w_1^T x + b_1, w_2^T x + b_2)$

ReLU

 $\max(0, x)$

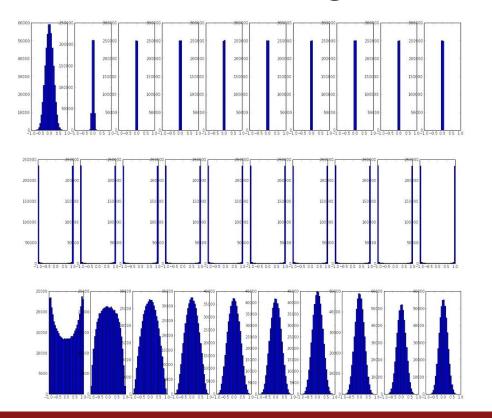
Good default choice



ELU

$$\begin{cases} x & x \ge 0 \\ \alpha(e^x - 1) & x < 0 \end{cases}$$

Last time: Weight Initialization



Initialization too small:

Activations go to zero, gradients also zero, No learning

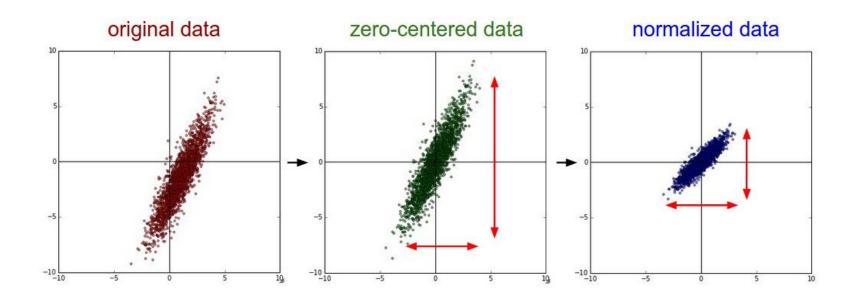
Initialization too big:

Activations saturate (for tanh), Gradients zero, no learning

Initialization just right:

Nice distribution of activations at all layers, Learning proceeds nicely

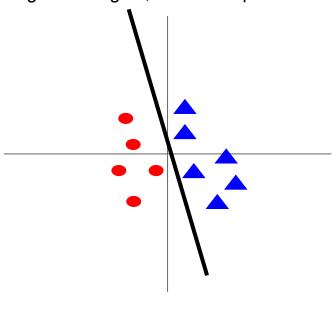
Last time: Data Preprocessing



Last time: Data Preprocessing

Before normalization: classification loss very sensitive to changes in weight matrix; hard to optimize

After normalization: less sensitive to small changes in weights; easier to optimize



Last time: Batch Normalization

Input: $x: N \times D$

 $\mu_j = \frac{1}{N} \sum_{i=1}^{N} x_{i,j}$

Learnable params:

 $\gamma, \beta: D$

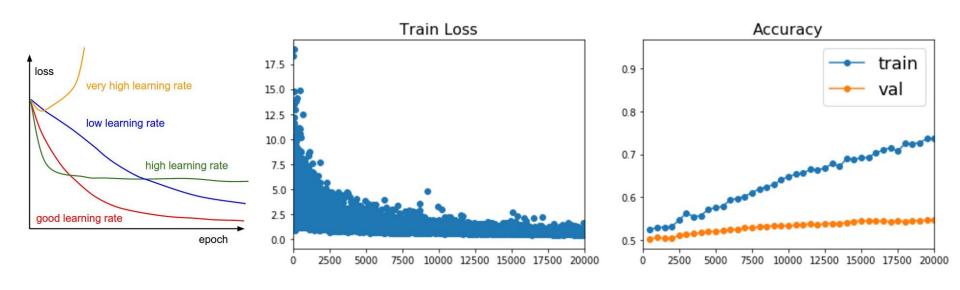
 $\sigma_j^2 = \frac{1}{N} \sum_{i=1}^{N} (x_{i,j} - \mu_j)^2$

Intermediates: $\begin{pmatrix} \mu, \sigma : D \\ \hat{x} \cdot N \times D \end{pmatrix}$

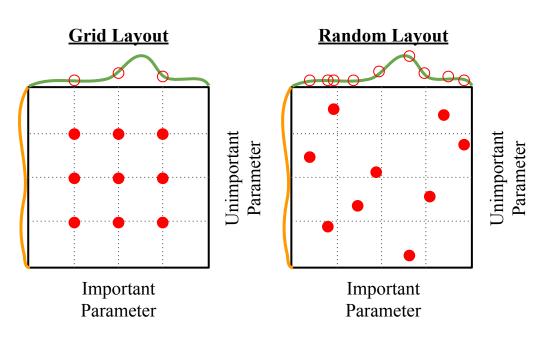
 $\hat{x}_{i,j} = \frac{x_{i,j} - \mu_j}{\sqrt{\sigma_j^2 + \varepsilon}}$ $y_{i,j} = \gamma_j \hat{x}_{i,j} + \beta_j$

Output: $y: N \times D$

Last time: Babysitting Learning



Last time: Hyperparameter Search



Coarse to fine search

```
val acc: 0.412000, lr: 1.405206e-04, reg: 4.793564e-01, (1 / 100)
val acc: 0.214000, lr: 7.231888e-06, reg: 2.321281e-04, (2 / 100)
val acc: 0.208000, lr: 2.119571e-06, reg: 8.011857e+01, (3 / 100)
val acc: 0.196000, lr: 1.551131e-05, req: 4.374936e-05, (4 / 100)
val acc: 0.079000, lr: 1.753300e-05, reg: 1.200424e+03, (5 / 100)
val acc: 0.223000, lr: 4.215128e-05, reg: 4.196174e+01, (6 / 100)
val acc: 0.441000, lr: 1.750259e-04, reg: 2.110807e-04, (7 / 100)
val acc: 0.241000, lr: 6.749231e-05, reg: 4.226413e+01, (8 / 100)
val acc: 0.482000, lr: 4.296863e-04, reg: 6.642555e-01, (9 / 100)
val acc: 0.079000, lr: 5.401602e-06, reg: 1.599828e+04, (10 / 100)
val acc: 0.154000, lr: 1.618508e-06, reg: 4.925252e-01, (11 / 100)
```

```
val acc: 0.527000, lr: 5.340517e-04, reg: 4.097824e-01, (0 / 100)
val acc: 0.492000, lr: 2.279484e-04, req: 9.991345e-04, (1 / 100)
val acc: 0.512000, lr: 8.680827e-04, reg: 1.349727e-02, (2 / 100)
val acc: 0.461000, lr: 1.028377e-04, reg: 1.220193e-02, (3 / 100)
val acc: 0.460000, lr: 1.113730e-04, reg: 5.244309e-02, (4 / 100)
val acc: 0.498000, lr: 9.477776e-04, reg: 2.001293e-03, (5 / 100)
val acc: 0.469000, lr: 1.484369e-04, reg: 4.328313e-01, (6 / 100)
val acc: 0.522000, lr: 5.586261e-04, reg: 2.312685e-04, (7 / 100)
val acc: 0.489000, lr: 1.979168e-04, reg: 1.010889e-04,
val acc: 0.490000, lr: 2.036031e-04, reg: 2.406271e-03, (10 / 100)
val acc: 0.475000, lr: 2.021162e-04, reg: 2.287807e-01, (11 / 100)
val acc: 0.460000, lr: 1.135527e-04, reg: 3.905040e-02, (12 / 100)
val acc: 0.515000, lr: 6.947668e-04, reg: 1.562808e-02, (13 / 100)
val acc: 0.531000, lr: 9.471549e-04, reg: 1.433895e-03,
val acc: 0.514000, lr: 6.438349e-04, reg: 3.033781e-01,
val acc: 0.502000, lr: 3.921784e-04, reg: 2.707126e-04,
val acc: 0.509000, lr: 9.752279e-04, reg: 2.850865e-03,
val acc: 0.500000, lr: 2.412048e-04, reg: 4.997821e-04, (19 / 100)
val acc: 0.466000, lr: 1.319314e-04, reg: 1.189915e-02, (20 / 100)
val acc: 0.516000, lr: 8.039527e-04, reg: 1.528291e-02, (21 / 100)
```

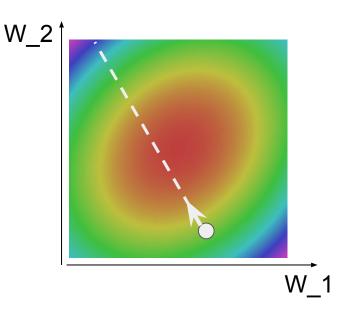
Today

- Fancier optimization
- Regularization
- Transfer Learning

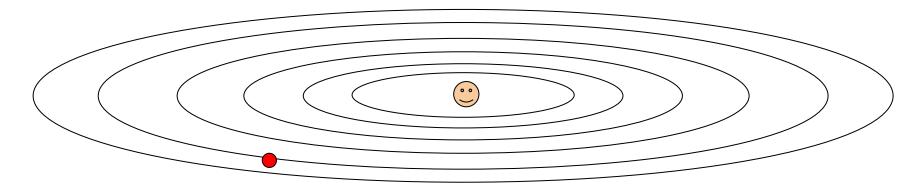
Optimization

```
# Vanilla Gradient Descent

while True:
    weights_grad = evaluate_gradient(loss_fun, data, weights)
    weights += - step_size * weights_grad # perform parameter update
```



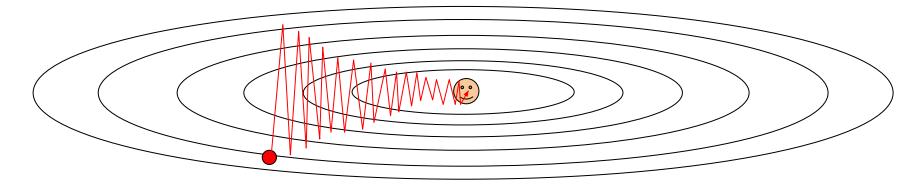
What if loss changes quickly in one direction and slowly in another? What does gradient descent do?



Loss function has high **condition number**: ratio of largest to smallest singular value of the Hessian matrix is large

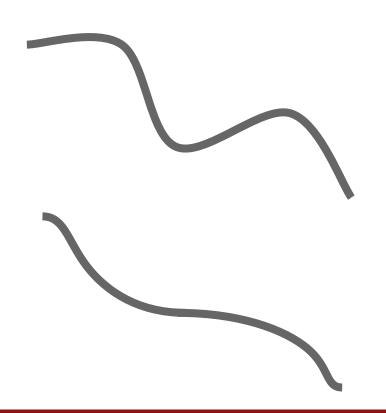
What if loss changes quickly in one direction and slowly in another? What does gradient descent do?

Very slow progress along shallow dimension, jitter along steep direction



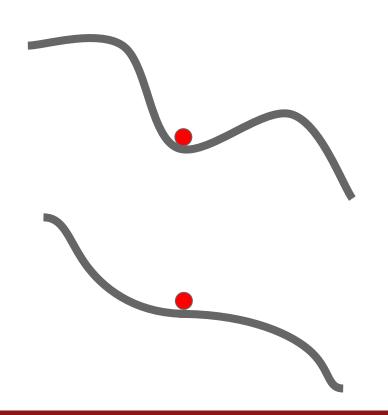
Loss function has high **condition number**: ratio of largest to smallest singular value of the Hessian matrix is large

What if the loss function has a local minima or saddle point?



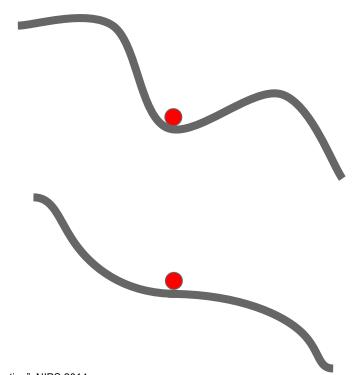
What if the loss function has a local minima or saddle point?

Zero gradient, gradient descent gets stuck



What if the loss function has a local minima or saddle point?

Saddle points much more common in high dimension

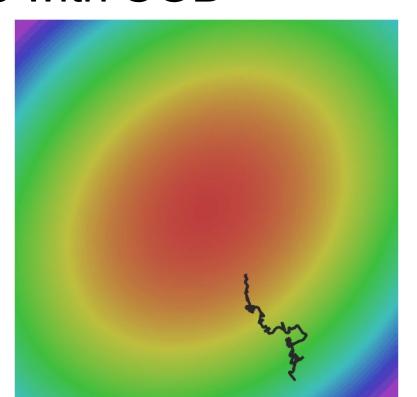


Dauphin et al, "Identifying and attacking the saddle point problem in high-dimensional non-convex optimization", NIPS 2014

Our gradients come from minibatches so they can be noisy!

$$L(W) = \frac{1}{N} \sum_{i=1}^{N} L_i(x_i, y_i, W)$$

$$\nabla_W L(W) = \frac{1}{N} \sum_{i=1}^{N} \nabla_W L_i(x_i, y_i, W)$$



SGD + Momentum

SGD

```
x_{t+1} = x_t - \alpha \nabla f(x_t)
```

```
while True:
    dx = compute_gradient(x)
    x += learning_rate * dx
```

SGD+Momentum

```
v_{t+1} = \rho v_t + \nabla f(x_t) x_{t+1} = x_t - \alpha v_{t+1} vx = \mathbf{0} while True: dx = \text{compute\_gradient(x)} vx = \text{rho * } vx + dx
```

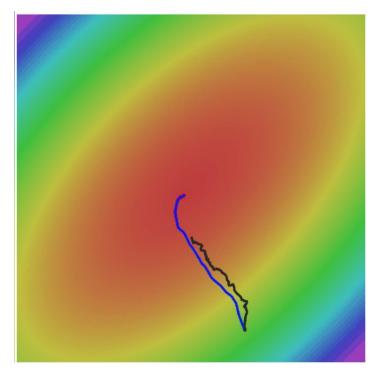
x += learning_rate * vx

- Build up "velocity" as a running mean of gradients
- Rho gives "friction"; typically rho=0.9 or 0.99

SGD + Momentum

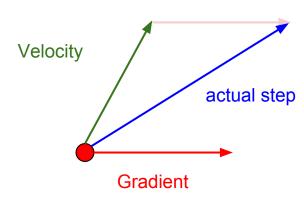
Local Minima Saddle points **Poor Conditioning**

Gradient Noise

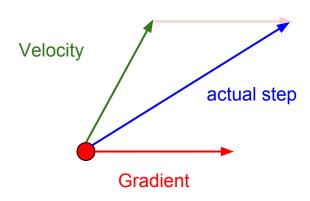


SGD + Momentum

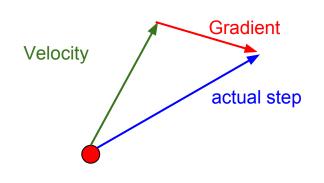
Momentum update:



Momentum update:



Nesterov Momentum



Nesterov, "A method of solving a convex programming problem with convergence rate O(1/k^2)", 1983 Nesterov, "Introductory lectures on convex optimization: a basic course", 2004 Sutskever et al, "On the importance of initialization and momentum in deel learning", ICML 2013

$$v_{t+1} = \rho v_t - \alpha \nabla f(x_t + \rho v_t)$$
$$x_{t+1} = x_t + v_{t+1}$$

$$v_{t+1} = \rho v_t - \alpha \nabla f(x_t + \rho v_t)$$
$$x_{t+1} = x_t + v_{t+1}$$

Annoying, usually we want update in terms of $x_t, \nabla f(x_t)$

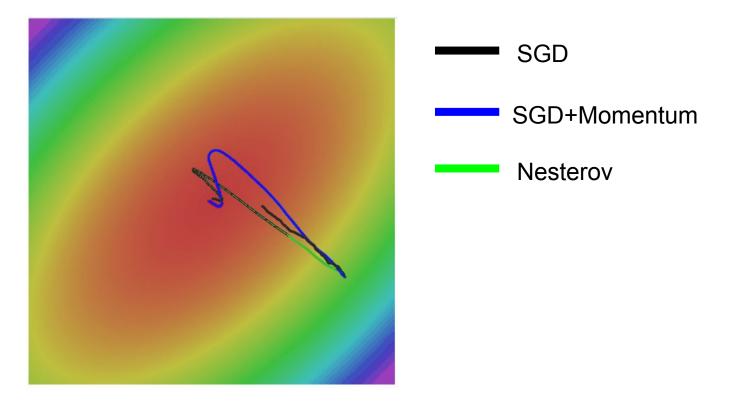
$$v_{t+1} = \rho v_t - \alpha \nabla f(x_t + \rho v_t)$$
$$x_{t+1} = x_t + v_{t+1}$$

Annoying, usually we want update in terms of $x_t, \nabla f(x_t)$

Change of variables $\tilde{x}_t = x_t + \rho v_t$ and rearrange:

```
v_{t+1} = \rho v_t - \alpha \nabla f(\tilde{x}_t)
\tilde{x}_{t+1} = \tilde{x}_t - \rho v_t + (1+\rho)v_{t+1}
         = \tilde{x}_t + v_{t+1} + \rho(v_{t+1} - v_t)
```

```
dx = compute\_gradient(x)
old v = v
v = rho * v - learning_rate * dx
x += -rho * old_v + (1 + rho) * v
```



AdaGrad

```
grad_squared = 0
while True:
    dx = compute_gradient(x)
    grad_squared += dx * dx
x -= learning_rate * dx / (np.sqrt(grad_squared) + 1e-7)
```

Added element-wise scaling of the gradient based on the historical sum of squares in each dimension

Duchi et al, "Adaptive subgradient methods for online learning and stochastic optimization", JMLR 2011

AdaGrad

```
grad_squared = 0
while True:
  dx = compute\_gradient(x)
  grad_squared += dx * dx
 x -= learning_rate * dx / (np.sqrt(grad_squared) + 1e-7)
```

Q: What happens with AdaGrad?

AdaGrad

```
grad_squared = 0
while True:
  dx = compute\_gradient(x)
  grad_squared += dx * dx
 x -= learning_rate * dx / (np.sqrt(grad_squared) + 1e-7)
```

Q2: What happens to the step size over long time?

RMSProp

AdaGrad

```
grad_squared = 0
while True:
  dx = compute\_gradient(x)
  grad_squared += dx * dx
  x -= learning_rate * dx / (np.sqrt(grad_squared) + 1e-7)
```

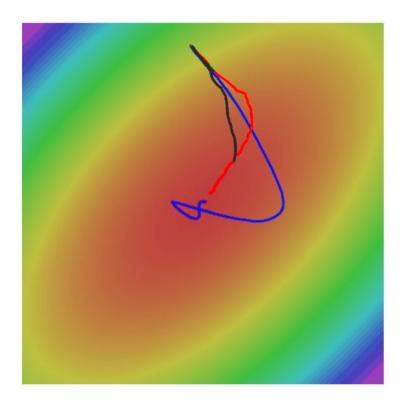


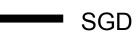
RMSProp

```
grad_squared = 0
while True:
  dx = compute\_gradient(x)
 grad_squared = decay_rate * grad_squared + (1 - decay_rate) * dx * dx
  x -= learning_rate * dx / (np.sqrt(grad_squared) + 1e-7)
```

Tieleman and Hinton, 2012

RMSProp





SGD+Momentum

RMSProp

Adam (almost)

```
first_moment = 0
second_moment = 0
while True:
    dx = compute_gradient(x)
    first_moment = beta1 * first_moment + (1 - beta1) * dx
    second_moment = beta2 * second_moment + (1 - beta2) * dx * dx
    x -= learning_rate * first_moment / (np.sqrt(second_moment) + 1e-7))
```

Kingma and Ba, "Adam: A method for stochastic optimization", ICLR 2015

Adam (almost)

```
first_moment = 0
second_moment = 0
while True:
    dx = compute_gradient(x)
    first_moment = beta1 * first_moment + (1 - beta1) * dx
    second_moment = beta2 * second_moment + (1 - beta2) * dx * dx
    x -= learning_rate * first_moment / (np.sqrt(second_moment) + 1e-7))
Momentum

AdaGrad / RMSProp
```

Sort of like RMSProp with momentum

Q: What happens at first timestep?

Kingma and Ba, "Adam: A method for stochastic optimization", ICLR 2015

Adam (full form)

```
first moment = 0
second moment = 0
for t in range(num_iterations):
                                                                        Momentum
 dx = compute_gradient(x)
 first_moment = beta1 * first_moment
 second_moment = beta2 * second_moment + (1 - beta2)
                                                    * dx * dx
 first_unbias = first_moment / (1 - beta1 ** t)
                                                                        Bias correction
 second unbias = second moment / (1 - beta2 ** t)
 x -= learning_rate * first_unbias / (np.sqrt(second_unbias) + 1e-7))
                                                                      AdaGrad / RMSProp
```

Bias correction for the fact that first and second moment estimates start at zero

Kingma and Ba, "Adam: A method for stochastic optimization", ICLR 2015

Adam (full form)

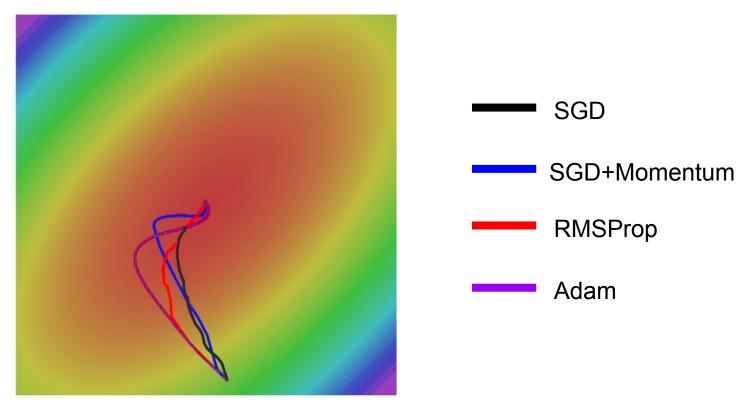
```
first moment = 0
second moment = 0
for t in range(1, num_iterations):
                                                                         Momentum
 dx = compute\_gradient(x)
 first_moment = beta1 * first_moment + (1 - beta1) * dx
  second_moment = beta2 * second_moment + (1 - beta2) * dx * dx
 first_unbias = first_moment / (1 - beta1 ** t)
                                                                         Bias correction
  second_unbias = second_moment / (1 - beta2 ** t)
 x -= learning_rate * first_unbias / (np.sqrt(second_unbias) + 1e-7))
                                                                      AdaGrad / RMSProp
```

Bias correction for the fact that first and second moment estimates start at zero

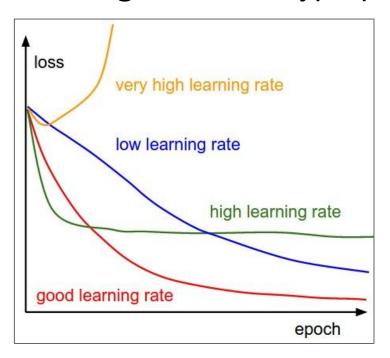
Adam with beta 1 = 0.9. beta2 = 0.999, and learning rate = 1e-3 or 5e-4 is a great starting point for many models!

Kingma and Ba, "Adam: A method for stochastic optimization", ICLR 2015

Adam

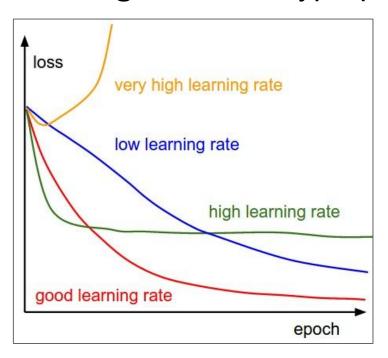


SGD, SGD+Momentum, Adagrad, RMSProp, Adam all have learning rate as a hyperparameter.



Q: Which one of these learning rates is best to use?

SGD, SGD+Momentum, Adagrad, RMSProp, Adam all have learning rate as a hyperparameter.



=> Learning rate decay over time!

step decay:

e.g. decay learning rate by half every few epochs.

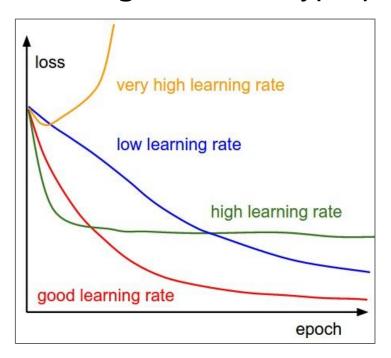
exponential decay:

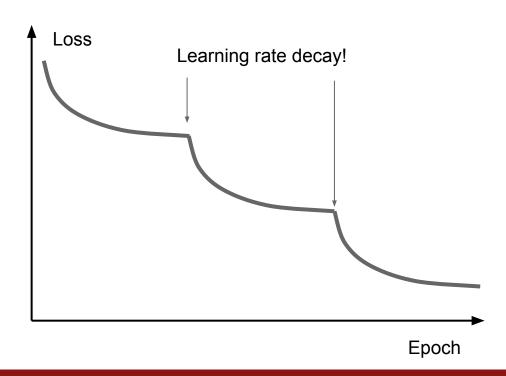
$$\alpha = \alpha_0 e^{-kt}$$

1/t decay:

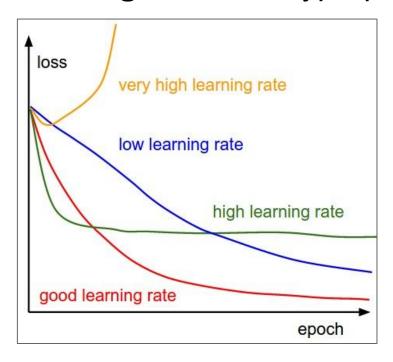
$$\alpha = \alpha_0/(1+kt)$$

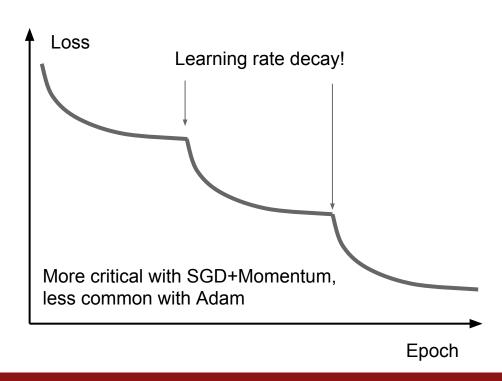
SGD, SGD+Momentum, Adagrad, RMSProp, Adam all have learning rate as a hyperparameter.



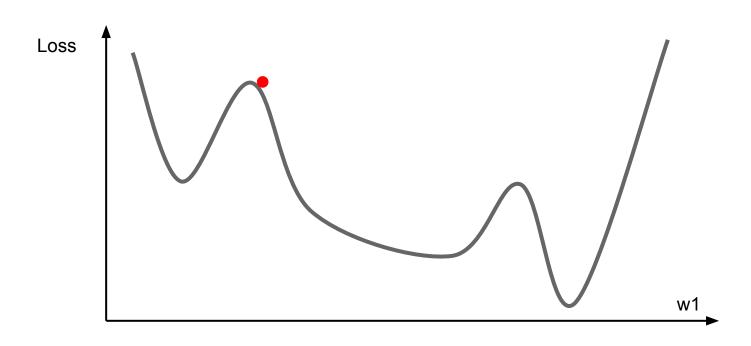


SGD, SGD+Momentum, Adagrad, RMSProp, Adam all have learning rate as a hyperparameter.

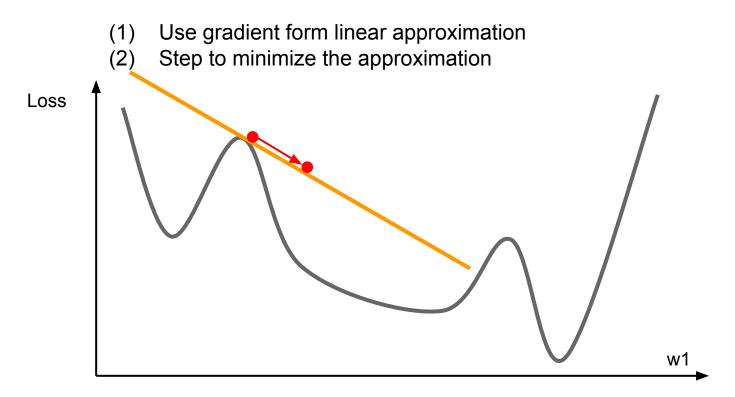




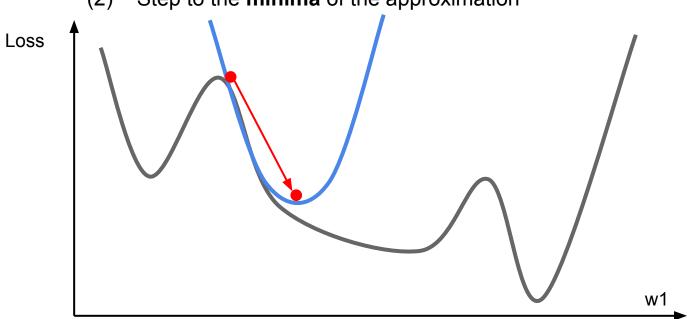
First-Order Optimization



First-Order Optimization



- Use gradient and Hessian to form quadratic approximation
- Step to the **minima** of the approximation



second-order Taylor expansion:

$$J(\boldsymbol{\theta}) \approx J(\boldsymbol{\theta}_0) + (\boldsymbol{\theta} - \boldsymbol{\theta}_0)^{\top} \nabla_{\boldsymbol{\theta}} J(\boldsymbol{\theta}_0) + \frac{1}{2} (\boldsymbol{\theta} - \boldsymbol{\theta}_0)^{\top} \boldsymbol{H} (\boldsymbol{\theta} - \boldsymbol{\theta}_0)$$

Solving for the critical point we obtain the Newton parameter update:

$$\boldsymbol{\theta}^* = \boldsymbol{\theta}_0 - \boldsymbol{H}^{-1} \nabla_{\boldsymbol{\theta}} J(\boldsymbol{\theta}_0)$$

Q: What is nice about this update?

second-order Taylor expansion:

$$J(\boldsymbol{\theta}) \approx J(\boldsymbol{\theta}_0) + (\boldsymbol{\theta} - \boldsymbol{\theta}_0)^{\top} \nabla_{\boldsymbol{\theta}} J(\boldsymbol{\theta}_0) + \frac{1}{2} (\boldsymbol{\theta} - \boldsymbol{\theta}_0)^{\top} \boldsymbol{H} (\boldsymbol{\theta} - \boldsymbol{\theta}_0)$$

Solving for the critical point we obtain the Newton parameter update:

$$\boldsymbol{\theta}^* = \boldsymbol{\theta}_0 - \boldsymbol{H}^{-1} \nabla_{\boldsymbol{\theta}} J(\boldsymbol{\theta}_0)$$

No hyperparameters! No learning rate!

Q: What is nice about this update?

second-order Taylor expansion:

$$J(\boldsymbol{\theta}) pprox J(\boldsymbol{\theta}_0) + (\boldsymbol{\theta} - \boldsymbol{\theta}_0)^{\top} \nabla_{\boldsymbol{\theta}} J(\boldsymbol{\theta}_0) + \frac{1}{2} (\boldsymbol{\theta} - \boldsymbol{\theta}_0)^{\top} \boldsymbol{H} (\boldsymbol{\theta} - \boldsymbol{\theta}_0)$$

Solving for the critical point we obtain the Newton parameter update:

$$\boldsymbol{\theta}^* = \boldsymbol{\theta}_0 - \boldsymbol{H}^{-1} \nabla_{\boldsymbol{\theta}} J(\boldsymbol{\theta}_0)$$

Hessian has O(N²) elements Inverting takes O(N³) N = (Tens or Hundreds of) Millions

Q2: Why is this bad for deep learning?

$$\boldsymbol{\theta}^* = \boldsymbol{\theta}_0 - \boldsymbol{H}^{-1} \nabla_{\boldsymbol{\theta}} J(\boldsymbol{\theta}_0)$$

- Quasi-Newton methods (BGFS most popular): instead of inverting the Hessian (O(n^3)), approximate inverse Hessian with rank 1 updates over time (O(n^2) each).
- **L-BFGS** (Limited memory BFGS): Does not form/store the full inverse Hessian.

$$\boldsymbol{\theta}^* = \boldsymbol{\theta}_0 - \boldsymbol{H}^{-1} \nabla_{\boldsymbol{\theta}} J(\boldsymbol{\theta}_0)$$

- Quasi-Newton methods (BGFS most popular): instead of inverting the Hessian (O(n^3)), approximate inverse Hessian with rank 1 updates over time (O(n^2) each).
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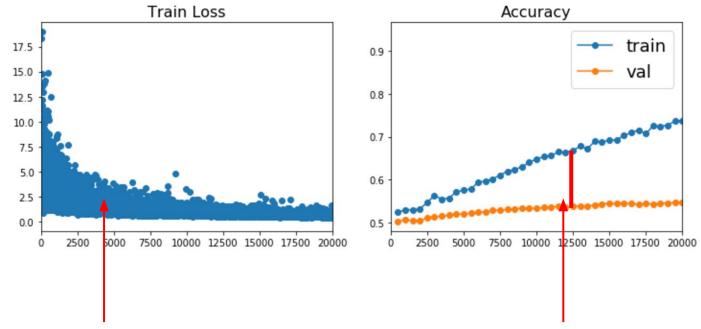
L-BFGS

- Usually works very well in full batch, deterministic mode i.e. if you have a single, deterministic f(x) then L-BFGS will probably work very nicely
- Does not transfer very well to mini-batch setting. Gives bad results. Adapting L-BFGS to large-scale, stochastic setting is an active area of research.

In practice:

- Adam is a good default choice in most cases
- If you can afford to do full batch updates then try out L-BFGS (and don't forget to disable all sources of noise)

Beyond Training Error



Better optimization algorithms help reduce training loss

But we really care about error on new data - how to reduce the gap?

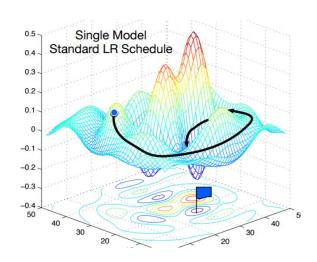
Model Ensembles

- 1. Train multiple independent models
- 2. At test time average their results

Enjoy 2% extra performance

Model Ensembles: Tips and Tricks

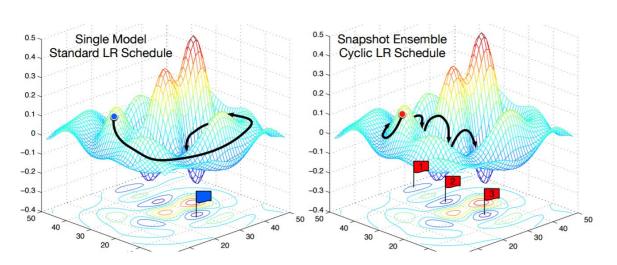
Instead of training independent models, use multiple snapshots of a single model during training!



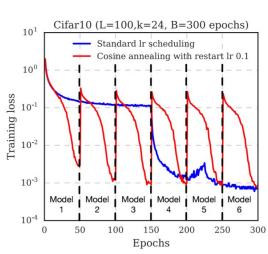
Loshchilov and Hutter, "SGDR: Stochastic gradient descent with restarts", arXiv 2016 Huang et al, "Snapshot ensembles: train 1, get M for free", ICLR 2017 Figures copyright Yixuan Li and Geoff Pleiss, 2017. Reproduced with permission.

Model Ensembles: Tips and Tricks

Instead of training independent models, use multiple snapshots of a single model during training!



Loshchilov and Hutter, "SGDR: Stochastic gradient descent with restarts", arXiv 2016 Huang et al, "Snapshot ensembles: train 1, get M for free", ICLR 2017 Figures copyright Yixuan Li and Geoff Pleiss, 2017. Reproduced with permission.



Cyclic learning rate schedules can make this work even better!

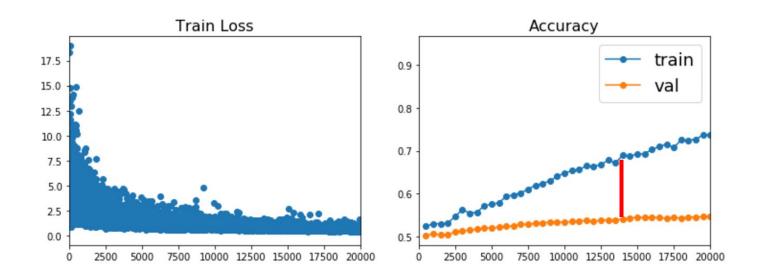
Model Ensembles: Tips and Tricks

Instead of using actual parameter vector, keep a moving average of the parameter vector and use that at test time (Polyak averaging)

```
while True:
   data_batch = dataset.sample_data_batch()
   loss = network.forward(data_batch)
   dx = network.backward()
   x += - learning_rate * dx
   x_test = 0.995*x_test + 0.005*x # use for test set
```

Polyak and Juditsky, "Acceleration of stochastic approximation by averaging", SIAM Journal on Control and Optimization, 1992.

How to improve single-model performance?



Regularization

Regularization: Add term to loss

$$L=rac{1}{N}\sum_{i=1}^{N}\sum_{j
eq y_i}\max(0,f(x_i;W)_j-f(x_i;W)_{y_i}+1)+ \lambda R(W)$$

In common use:

L2 regularization

 $R(W) = \sum_k \sum_l W_{k,l}^2$ (Weight decay)

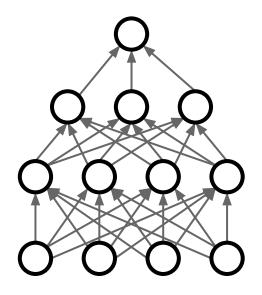
L1 regularization

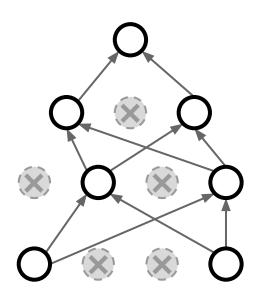
 $R(W) = \sum_k \sum_l |W_{k,l}|$

Elastic net (L1 + L2)

 $R(W) = \sum_k \sum_l eta W_{k,l}^2 + |W_{k,l}|$

In each forward pass, randomly set some neurons to zero Probability of dropping is a hyperparameter; 0.5 is common

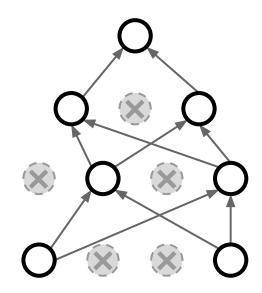




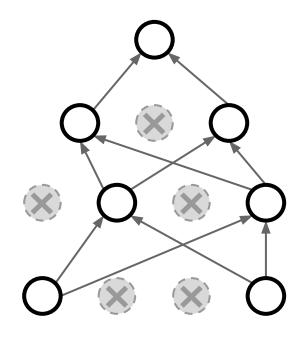
Srivastava et al, "Dropout: A simple way to prevent neural networks from overfitting", JMLR 2014

```
p = 0.5 # probability of keeping a unit active. higher = less dropout
def train_step(X):
  """ X contains the data """
 # forward pass for example 3-layer neural network
 H1 = np.maximum(0, np.dot(W1, X) + b1)
 U1 = np.random.rand(*H1.shape) 
 H1 *= U1 # drop!
 H2 = np.maximum(0, np.dot(W2, H1) + b2)
 U2 = np.random.rand(*H2.shape) < p # second dropout mask
 H2 *= U2 # drop!
 out = np.dot(W3, H2) + b3
 # backward pass: compute gradients... (not shown)
 # perform parameter update... (not shown)
```

Example forward pass with a 3-layer network using dropout



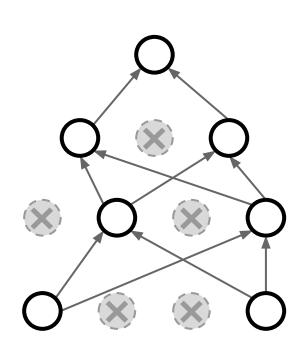
How can this possibly be a good idea?



Forces the network to have a redundant representation; Prevents co-adaptation of features



How can this possibly be a good idea?



Another interpretation:

Dropout is training a large ensemble of models (that share parameters).

Each binary mask is one model

An FC layer with 4096 units has $2^{4096} \sim 10^{1233}$ possible masks! Only $\sim 10^{82}$ atoms in the universe...

Dropout makes our output random!

Output Input (label) (image)
$$y = f_W(x,z) \quad \text{Random} \quad \text{mask}$$

Want to "average out" the randomness at test-time

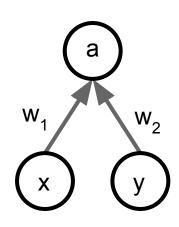
$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$

But this integral seems hard ...

Want to approximate the integral

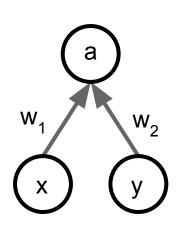
$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$

Consider a single neuron.



Want to approximate the integral

$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$

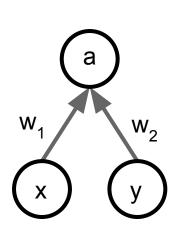


Consider a single neuron.

At test time we have: $E[a] = w_1x + w_2y$

Want to approximate the integral

$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$



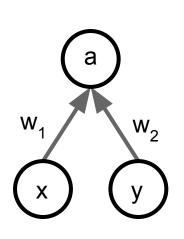
Consider a single neuron.

At test time we have: $E[a] = w_1x + w_2y$

During training we have:
$$E[a] = \frac{1}{4}(w_1x + w_2y) + \frac{1}{4}(w_1x + 0y) + \frac{1}{4}(0x + 0y) + \frac{1}{4}(0x + w_2y) + \frac{1}{4}(0x + w_2y) + \frac{1}{4}(0x + w_2y)$$

Want to approximate the integral

$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$



Consider a single neuron.

At test time we have: $E[a] = w_1x + w_2y$

During training we have: $E[a] = \frac{1}{4}(w_1x + w_2y) + \frac{1}{4}(w_1x + 0y)$

At test time, **multiply** by dropout probability

$$+ \frac{1}{4}(0x + 0y) + \frac{1}{4}(0x + w_2y)$$
$$= \frac{1}{2}(w_1x + w_2y)$$

```
def predict(X):
    # ensembled forward pass
H1 = np.maximum(0, np.dot(W1, X) + b1) * p # NOTE: scale the activations
H2 = np.maximum(0, np.dot(W2, H1) + b2) * p # NOTE: scale the activations
out = np.dot(W3, H2) + b3
```

At test time all neurons are active always => We must scale the activations so that for each neuron: output at test time = expected output at training time

```
Vanilla Dropout: Not recommended implementation (see notes below)
p = 0.5 # probability of keeping a unit active, higher = less dropout
def train step(X):
  """ X contains the data """
 # forward pass for example 3-layer neural network
 H1 = np.maximum(0, np.dot(W1, X) + b1)
 U1 = np.random.rand(*H1.shape) < p # first dropout mask
 H1 *= U1 # drop!
 H2 = np.maximum(0, np.dot(W2, H1) + b2)
 U2 = np.random.rand(*H2.shape) < p # second dropout mask
 H2 *= U2 # drop!
 out = np.dot(W3, H2) + b3
 # backward pass: compute gradients... (not shown)
 # perform parameter update... (not shown)
def predict(X):
 # ensembled forward pass
 H1 = np.maximum(0, np.dot(W1, X) + b1) * p # NOTE: scale the activations
 H2 = np.maximum(0, np.dot(W2, H1) + b2) * p # NOTE: scale the activations
 out = np.dot(W3, H2) + b3
```

Dropout Summary

drop in forward pass

scale at test time

More common: "Inverted dropout"

```
p = 0.5 # probability of keeping a unit active. higher = less dropout
def train step(X):
  # forward pass for example 3-layer neural netw
  H1 = np.maximum(0, np.dot(W1, X) + b1)
 U1 = (np.random.rand(*H1.shape) < p)// p # first dropout mask. Notice /p!
  H1 *= U1 # drop!
 H2 = np.maximum(0, np.dot(W2, H1) + b2)
 U2 = (np.random.rand(*H2.shape) < p) / p # econd dropout mask. Notice /p!
 H2 *= U2 # drop!
  out = np.dot(W3, H2) + b3
 # backward pass: compute gradients... (not shown)
  # perform parameter update... (not shown)
                                                                      test time is unchanged!
def predict(X):
 # ensembled forward pass
 H1 = np.maximum(0, np.dot(W1, X) + b1) # no scaling necessary
 H2 = np.maximum(0, np.dot(W2, H1) + b2)
 out = np.dot(W3, H2) + b3
```

Regularization: A common pattern

Training: Add some kind of randomness

$$y = f_W(x, z)$$

Testing: Average out randomness (sometimes approximate)

$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$

Training: Add some kind of randomness

$$y = f_W(x, z)$$

Testing: Average out randomness (sometimes approximate)

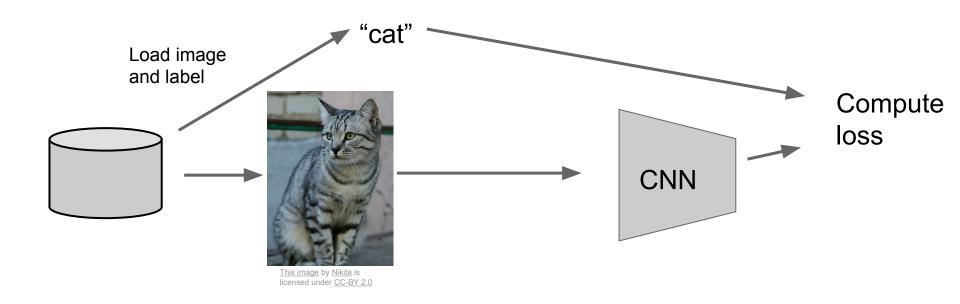
$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$

Example: Batch Normalization

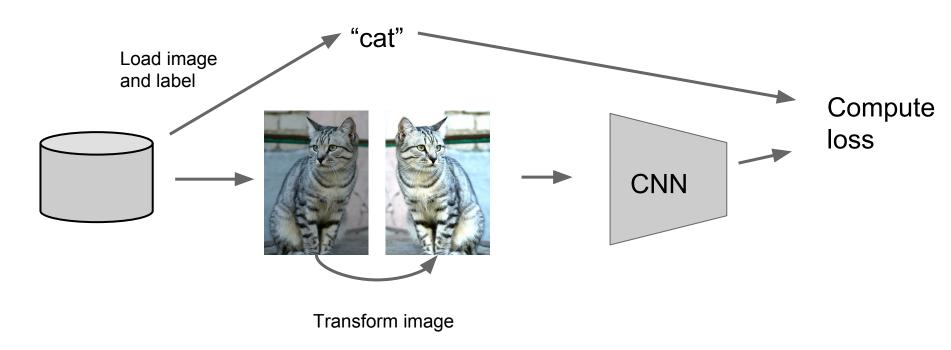
Training:
Normalize using
stats from random
minibatches

Testing: Use fixed stats to normalize

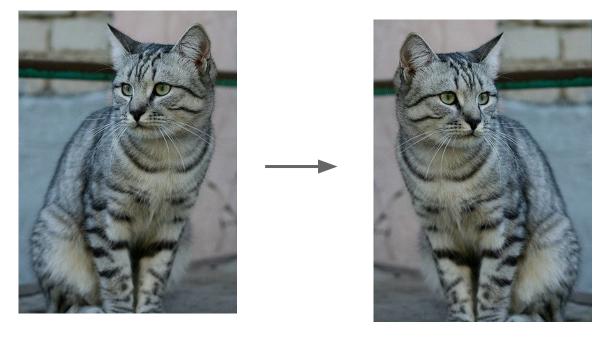
Regularization: Data Augmentation



Regularization: Data Augmentation



Data Augmentation Horizontal Flips



Fei-Fei Li & Justin Johnson & Serena Yeung

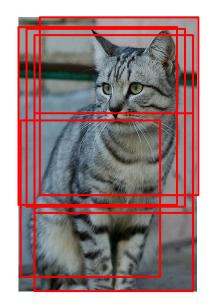
Lecture 7 - 76

April 25, 2017

Data Augmentation Random crops and scales

Training: sample random crops / scales ResNet:

- 1. Pick random L in range [256, 480]
- 2. Resize training image, short side = L
- 3. Sample random 224 x 224 patch

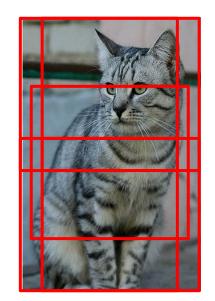


Data Augmentation Random crops and scales

Training: sample random crops / scales

ResNet:

- 1. Pick random L in range [256, 480]
- Resize training image, short side = L
- 3. Sample random 224 x 224 patch



Testing: average a fixed set of crops

ResNet:

- 1. Resize image at 5 scales: {224, 256, 384, 480, 640}
- 2. For each size, use 10 224 x 224 crops: 4 corners + center, + flips

Data Augmentation Color Jitter

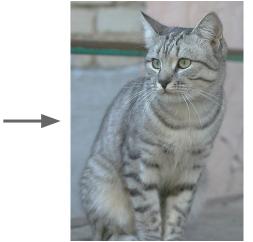
Simple: Randomize contrast and brightness



Data Augmentation Color Jitter

Simple: Randomize contrast and brightness





More Complex:

- 1. Apply PCA to all [R, G, B] pixels in training set
- 2. Sample a "color offset" along principal component directions
- 3. Add offset to all pixels of a training image

(As seen in [Krizhevsky et al. 2012], ResNet, etc)

Data Augmentation Get creative for your problem!

Random mix/combinations of:

- translation
- rotation
- stretching
- shearing,
- lens distortions, ... (go crazy)

Training: Add random noise

Testing: Marginalize over the noise

Examples:

Dropout

Batch Normalization

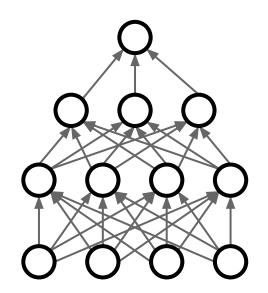
Data Augmentation

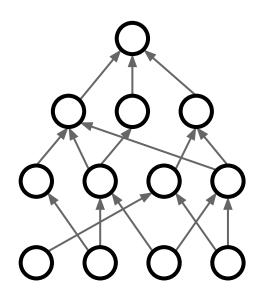
Training: Add random noise

Testing: Marginalize over the noise

Examples:

Dropout Batch Normalization Data Augmentation DropConnect





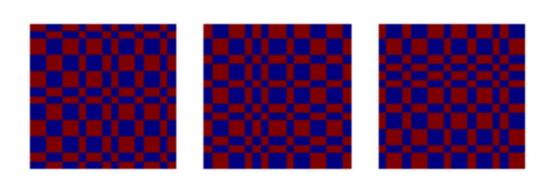
Wan et al, "Regularization of Neural Networks using DropConnect", ICML 2013

Training: Add random noise

Testing: Marginalize over the noise

Examples:

Dropout
Batch Normalization
Data Augmentation
DropConnect
Fractional Max Pooling



Graham, "Fractional Max Pooling", arXiv 2014

Training: Add random noise

Testing: Marginalize over the noise

Examples:

Dropout

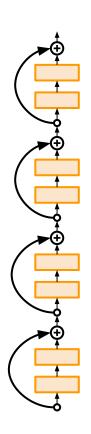
Batch Normalization

Data Augmentation

DropConnect

Fractional Max Pooling

Stochastic Depth



Huang et al, "Deep Networks with Stochastic Depth", ECCV 2016

Transfer Learning

"You need a lot of a data if you want to train/use CNNs"

Transfer Learning

"You need a lot of a data if you want to train/(se CNNs"

Transfer Learning with CNNs

1. Train on Imagenet

FC-1000 FC-4096 FC-4096 MaxPool Conv-512 Conv-512 MaxPool Conv-512 Conv-512 MaxPool Conv-256 Conv-256 MaxPool Conv-128 Conv-128 MaxPool Conv-64 Conv-64 **Image**

Donahue et al, "DeCAF: A Deep Convolutional Activation Feature for Generic Visual Recognition", ICML 2014 Razavian et al, "CNN Features Off-the-Shelf: An Astounding Baseline for Recognition", CVPR Workshops 2014

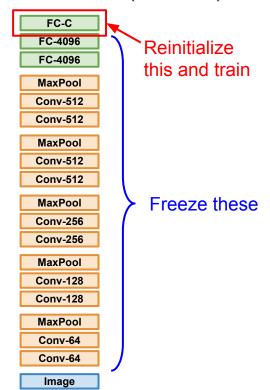
Transfer Learning with CNNs

1. Train on Imagenet

FC-1000 FC-4096 FC-4096 MaxPool Conv-512 Conv-512 MaxPool Conv-512 Conv-512 MaxPool Conv-256 Conv-256 MaxPool Conv-128 Conv-128 MaxPool Conv-64 Conv-64

Image

2. Small Dataset (C classes)



Donahue et al, "DeCAF: A Deep Convolutional Activation Feature for Generic Visual Recognition", ICML 2014 Razavian et al, "CNN Features Off-the-Shelf: An Astounding Baseline for Recognition", CVPR Workshops 2014

Transfer Learning with CNNs

1. Train on Imagenet

FC-1000 FC-4096 FC-4096 MaxPool Conv-512 Conv-512 MaxPool Conv-512 Conv-512 MaxPool Conv-256 Conv-256 MaxPool Conv-128 Conv-128 MaxPool Conv-64 Conv-64

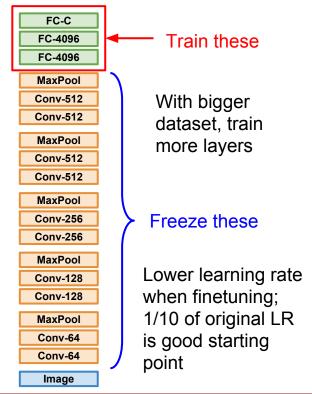
Image

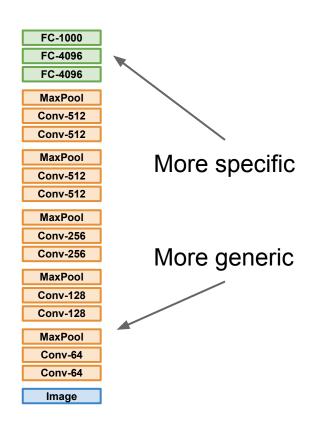
2. Small Dataset (C classes)



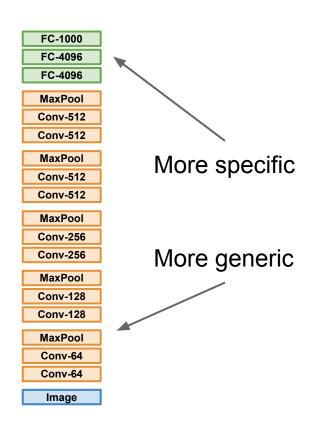
Donahue et al, "DeCAF: A Deep Convolutional Activation Feature for Generic Visual Recognition", ICML 2014 Razavian et al, "CNN Features Off-the-Shelf: An Astounding Baseline for Recognition", CVPR Workshops 2014

3. Bigger dataset

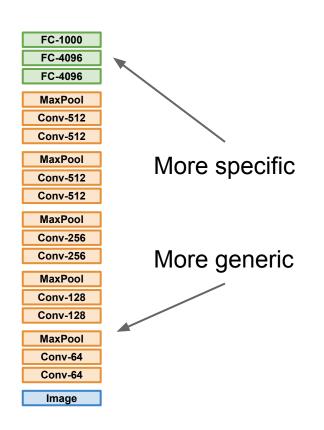




	very similar dataset	very different dataset
very little data	?	?
quite a lot of data	?	?



	very similar dataset	very different dataset
very little data	Use Linear Classifier on top layer	?
quite a lot of data	Finetune a few layers	?



	very similar dataset	very different dataset
very little data	Use Linear Classifier on top layer	You're in trouble Try linear classifier from different stages
quite a lot of data	Finetune a few layers	Finetune a larger number of layers

Transfer learning with CNNs is pervasive... (it's the norm, not an exception)

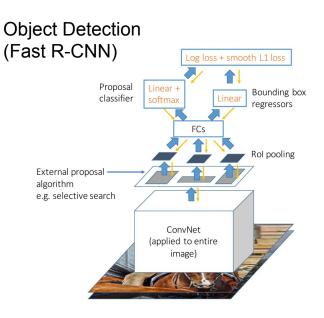
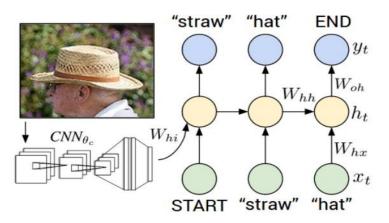
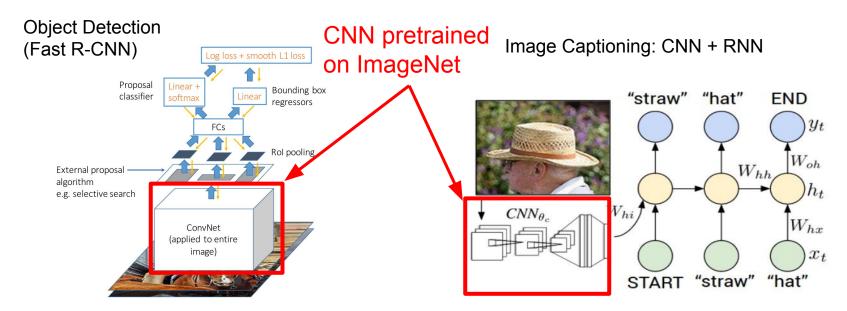


Image Captioning: CNN + RNN



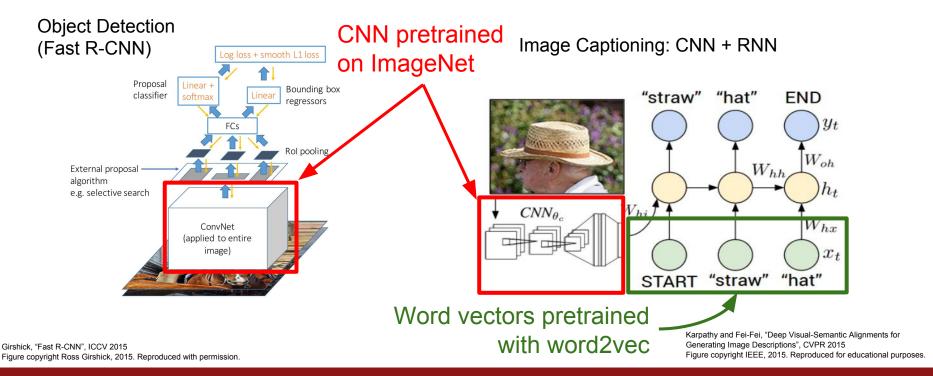
Girshick, "Fast R-CNN", ICCV 2015 Figure copyright Ross Girshick, 2015. Reproduced with permission Karpathy and Fei-Fei, "Deep Visual-Semantic Alignments for Generating Image Descriptions", CVPR 2015 Figure copyright IEEE, 2015. Reproduced for educational purposes.

Transfer learning with CNNs is pervasive... (it's the norm, not an exception)



Girshick, "Fast R-CNN", ICCV 2015 Figure copyright Ross Girshick, 2015. Reproduced with permission Karpathy and Fei-Fei, "Deep Visual-Semantic Alignments for Generating Image Descriptions", CVPR 2015 Figure copyright IEEE, 2015. Reproduced for educational purposes.

Transfer learning with CNNs is pervasive... (it's the norm, not an exception)



Takeaway for your projects and beyond:

Have some dataset of interest but it has < ~1M images?

- 1. Find a very large dataset that has similar data, train a big ConvNet there
- 2. Transfer learn to your dataset

Deep learning frameworks provide a "Model Zoo" of pretrained models so you don't need to train your own

Caffe: https://github.com/BVLC/caffe/wiki/Model-Zoo

TensorFlow: https://github.com/tensorflow/models

PyTorch: https://github.com/pytorch/vision

Summary

- Optimization
 - Momentum, RMSProp, Adam, etc
- Regularization
 - Dropout, etc
- Transfer learning
 - Use this for your projects!

Next time: Deep Learning Software!