



# **Modeling ER Features with Functional Dependencies**

## **Functional Dependency Exercises**



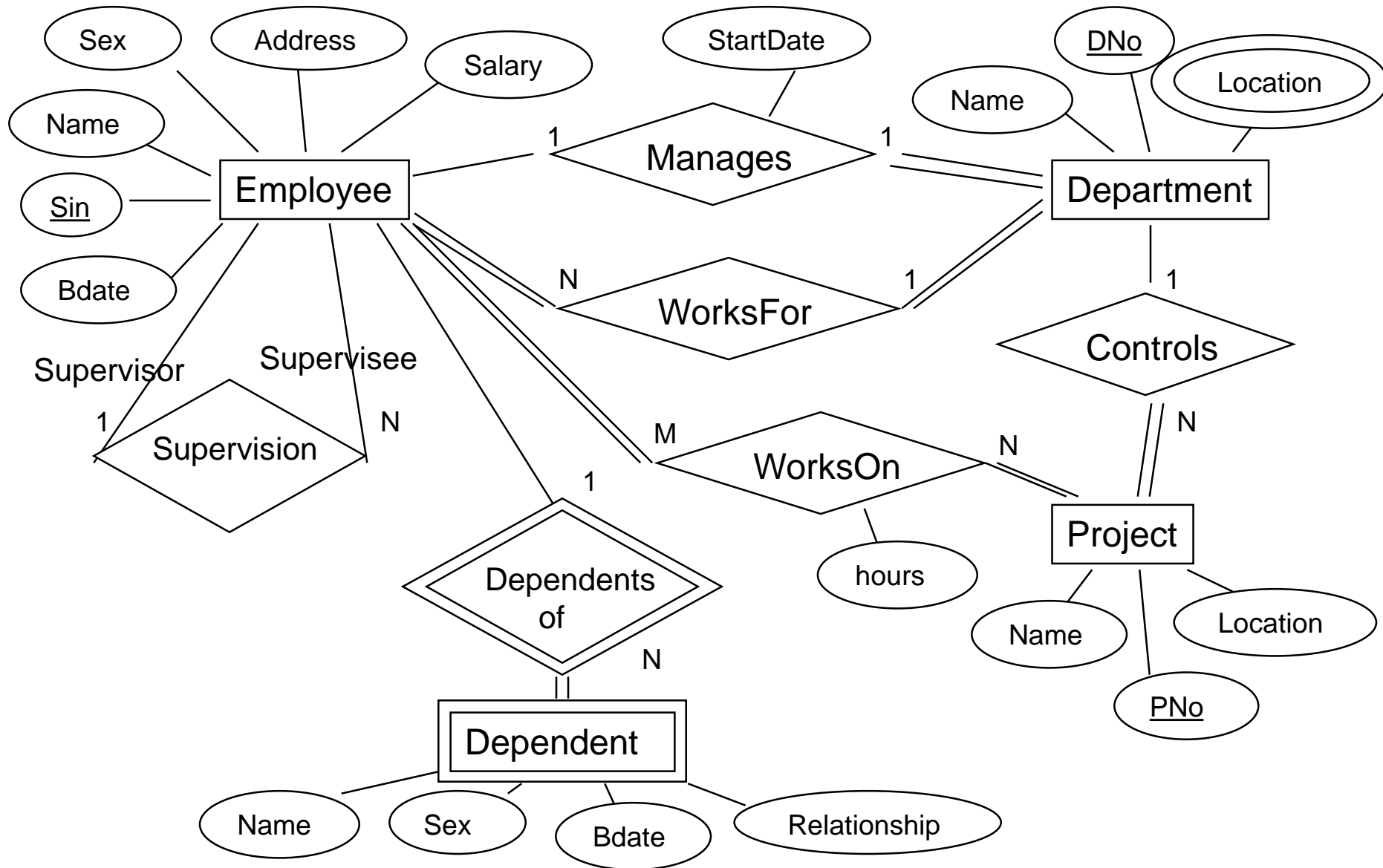
## Objectives

- **Learn how Entity-Relationship features can be modeled with Functional Dependencies**
- **Some practice exercises involving functional dependencies**

## Topics

- **Entities and Weak Entities**
- **1:1, 1:N and N:N Relationships**
- **Multi-valued Attributes**
- **Inheritance**

# E-R diagram for Company Data (fig 3.2)



# Elmasri Data Set

**//Elmasri and Navathe Employee Dataset example**

**//As per 3005 Notes: Modeling ER with FD.**

**SIN -> Bdate,Name,Sex,Address,Salary**

**DNo->DName**

**PNo->Pname,Plocation**

**SIN,DepName -> DepSex,DepBdate,Relationship**

**DNo->Manages\_SIN,Manages\_StartDate**

**SIN->WorksFor\_DNo**

**SIN->Supervisor\_SIN**

**PNo->Control\_DNo**

**SIN,PNo->WorksOn\_Hours**

**DNo,Location->temp //remove column temp from final design**

## Minimal Cover

**//Elmasri and Navathe Employee Dataset example**

**//As per 3005 Notes: Modeling ER with FD.**

**SIN ->**

**Bdate,Name,Sex,Address,Salary,WorksFor\_DNo,Supervisor\_SIN**

**DNo -> DName,Manages\_SIN,Manages\_StartDate**

**PNo -> Pname,Plocation,Control\_DNo**

**SIN,DepName -> DepSex,DepBdate,Relationship**

**SIN,PNo -> WorksOn\_Hours**

**DNo,Location -> temp**

# 3NF Tables

## Dependency Preserving, 3NF tables

[SIN | Bdate,Name,Sex,Address,Salary,WorksFor\_DNo,Supervisor\_SIN]

[DNo | DName,Manages\_SIN,Manages\_StartDate]

[PNo | Pname,Plocation,Control\_DNo]

[SIN,DepName | DepSex,DepBdate,Relationship]

[SIN,PNo | WorksOn\_Hours]

[DNo,Location | temp]

# 3NF Tables

Dependency Preserving, 3NF tables that can be joined into a single table (though not what you likely need)

[SIN | Bdate,Name,Sex,Address,Salary,WorksFor\_DNo,Supervisor\_SIN]

[DNo | DName,Manages\_SIN,Manages\_StartDate]

[PNo | Pname,Plocation,Control\_DNo]

[SIN,DepName | DepSex,DepBdate,Relationship]

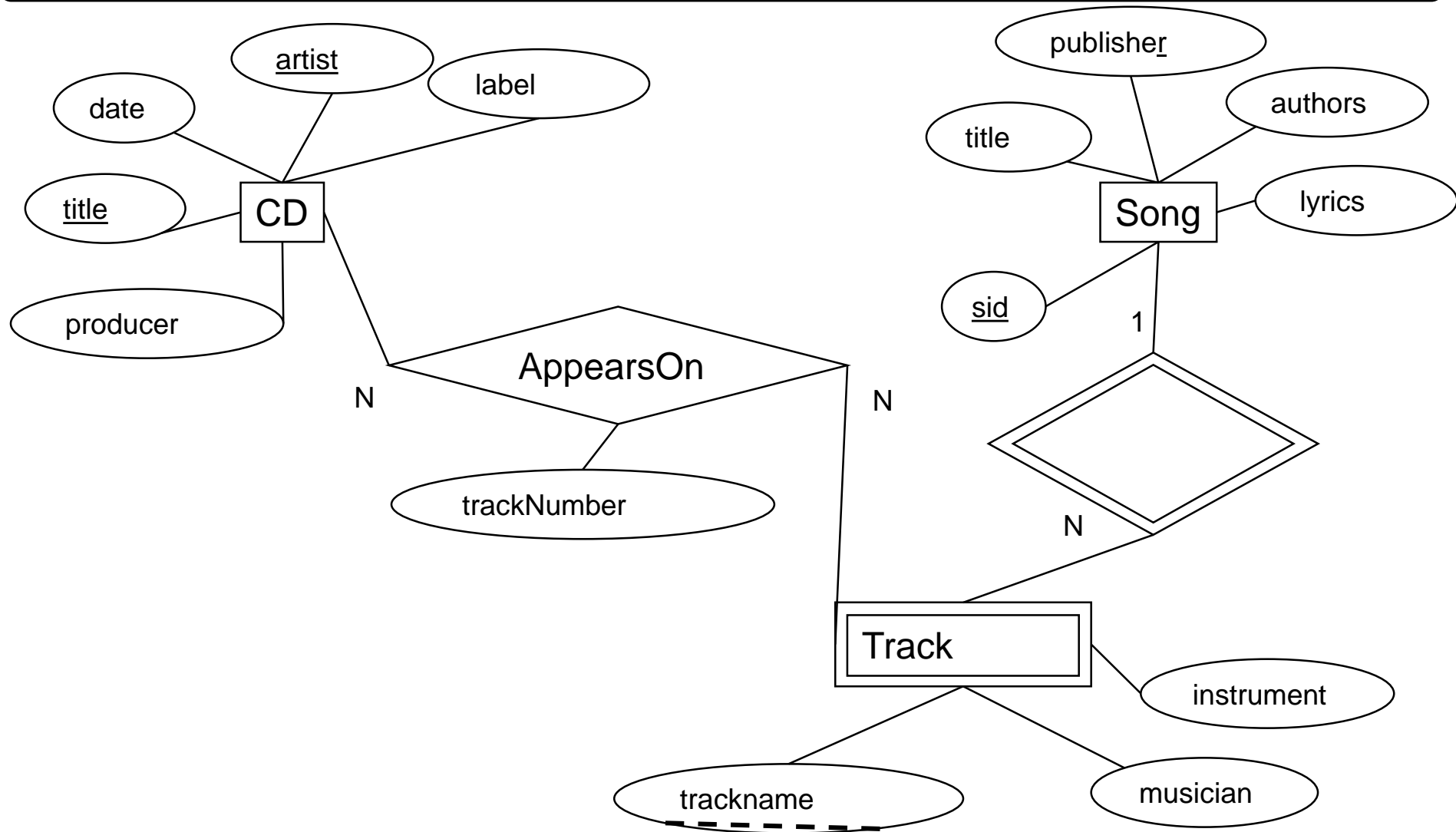
[SIN,PNo | WorksOn\_Hours]

[DNo,Location | temp]

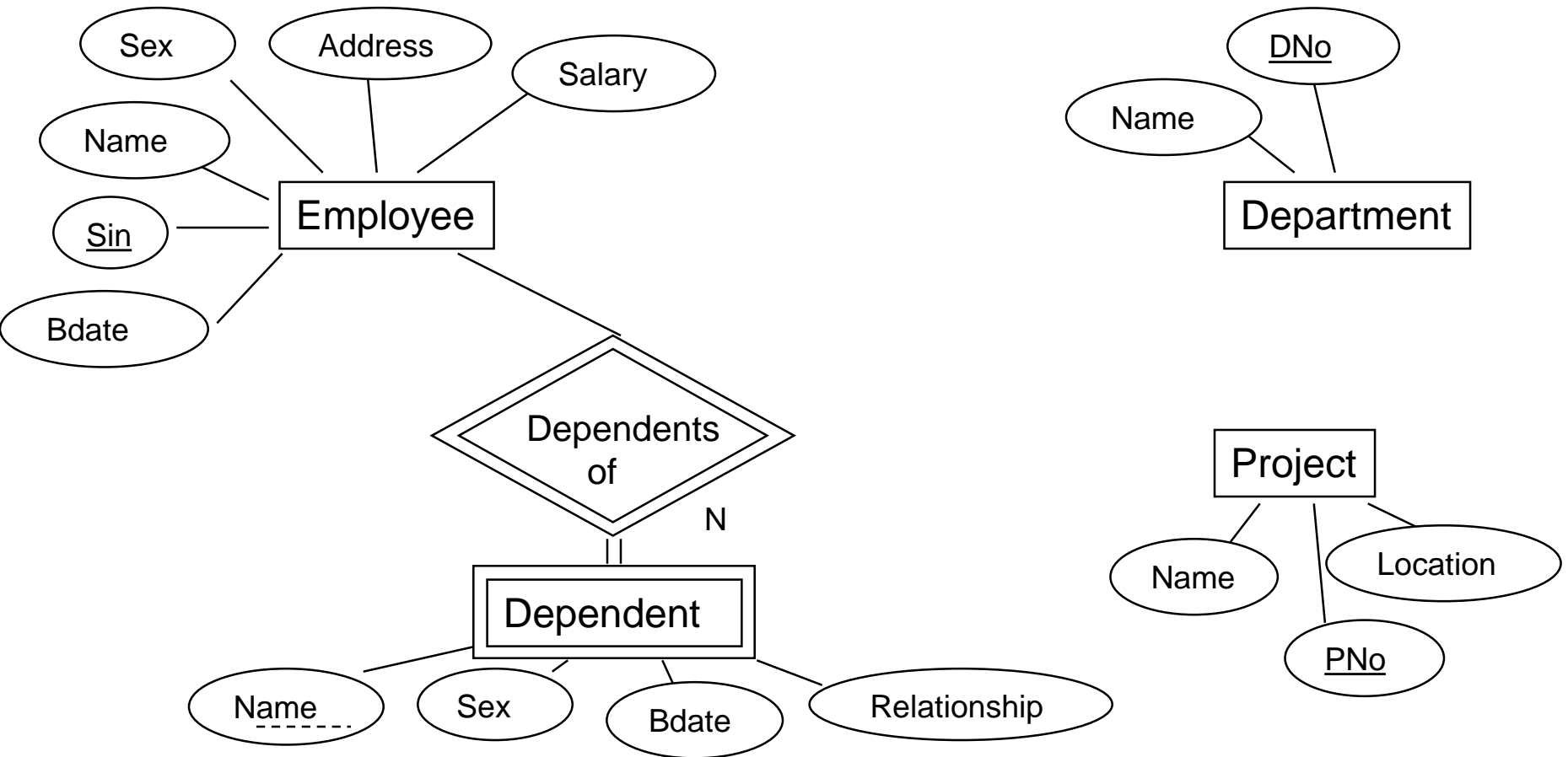
[DNo,DepName,Location,PNo,SIN |]



# A2, Q1 Possible Solution (others are possible as well)



# Entities and Weak Entities



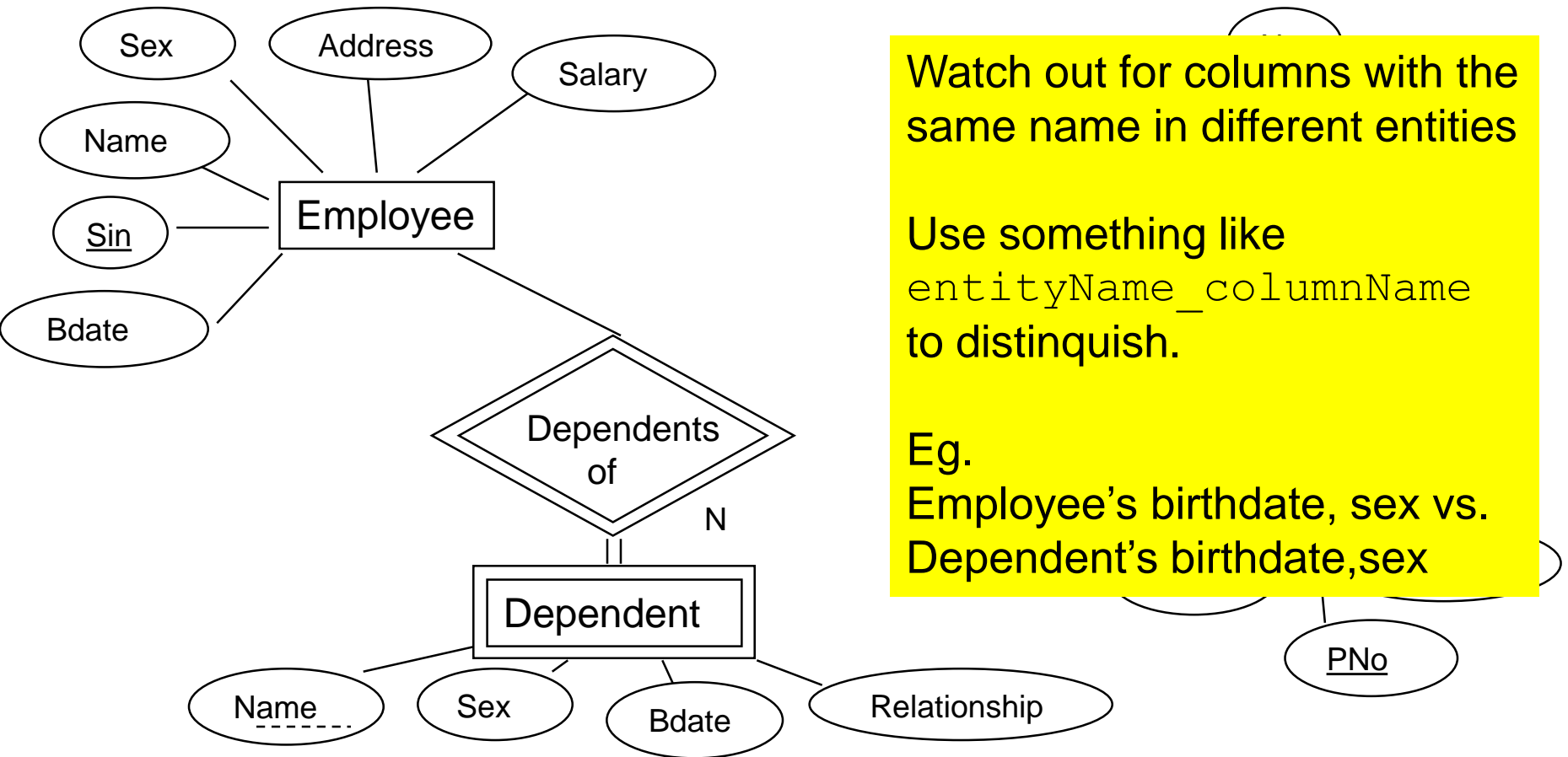
**SIN -> Bdate, Name, Sex, Address, Salary**

**DNo -> DName**

**PNo -> Pname, Plocation**

**SIN, DepName -> Dep\_Sex, Dep\_Bdate, Relationship**

# Entities and Weak Entities



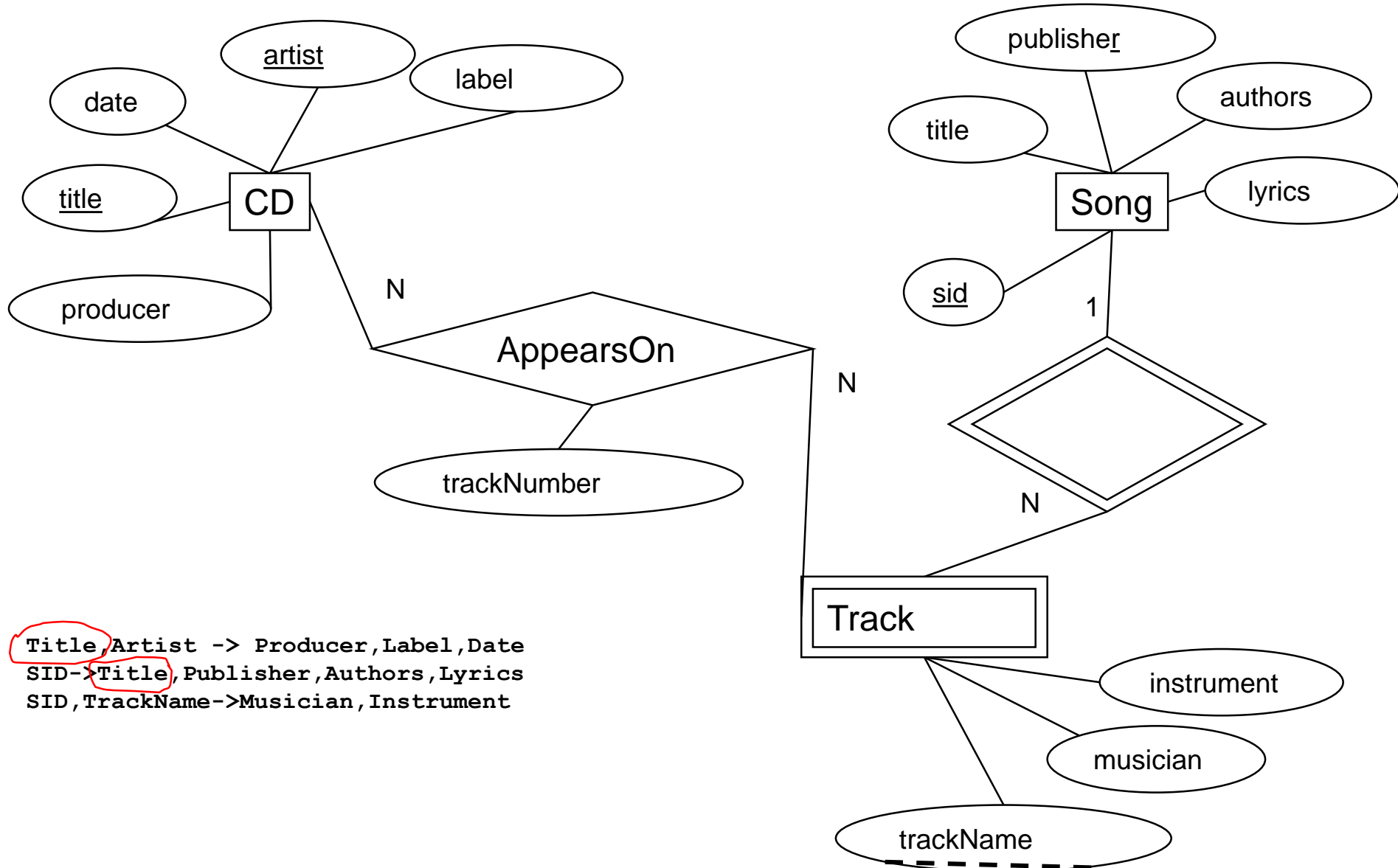
**SIN -> Bdate, Name, Sex, Address, Salary**

**DNo->DName**

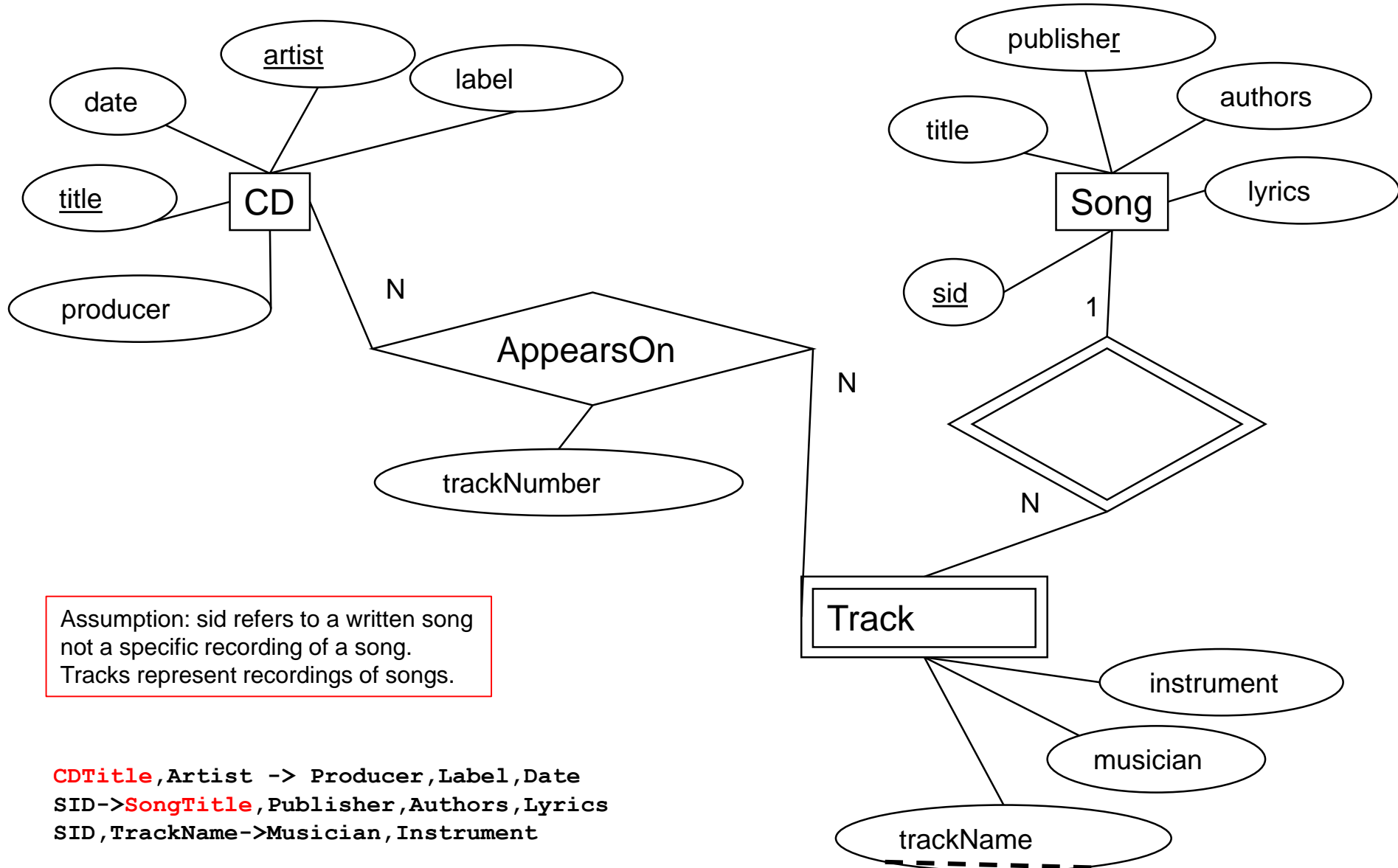
**PNo->Pname, Plocation**

**SIN, DepName -> Dep\_Sex, Dep\_Bdate, Relationship**

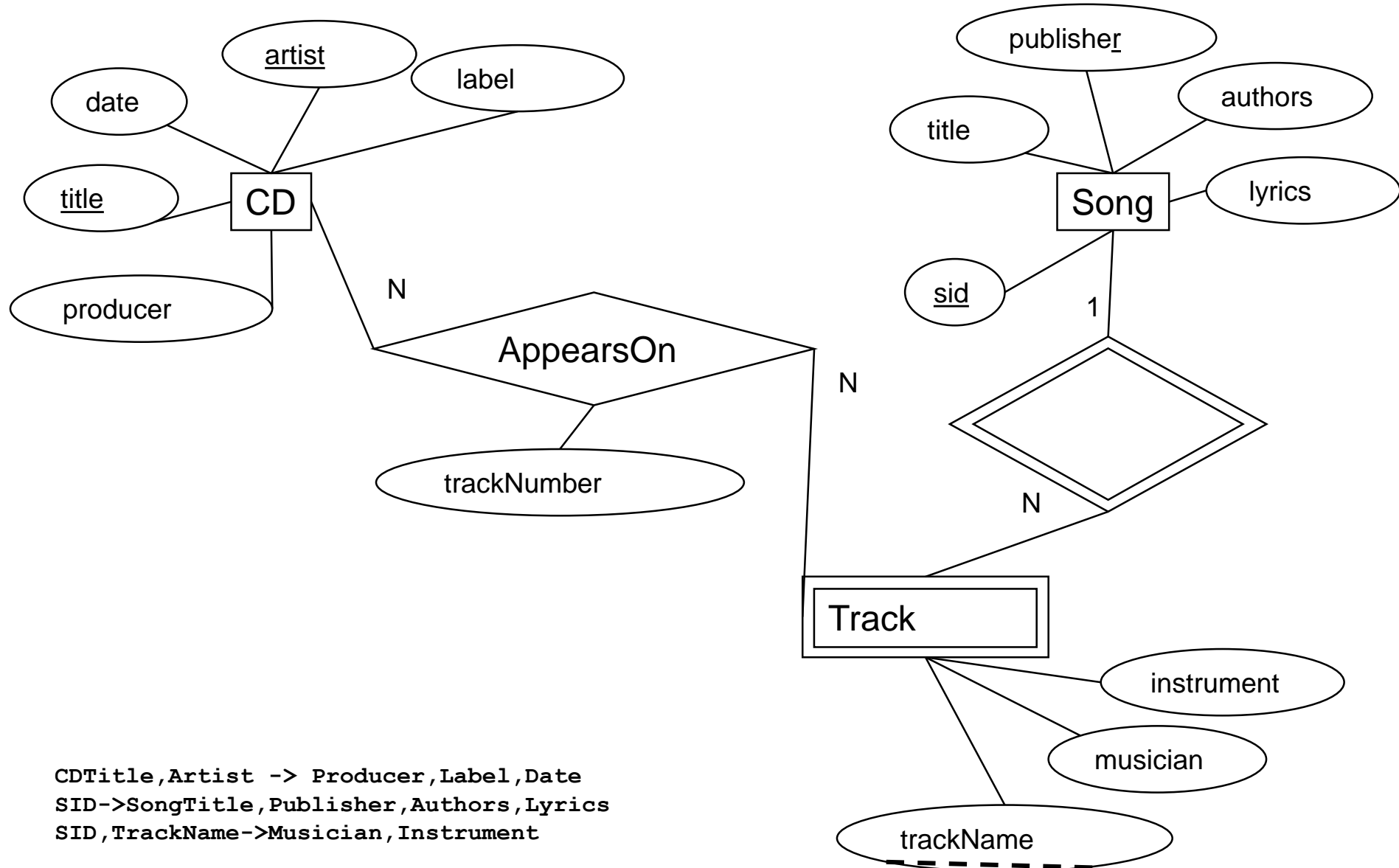
# A2,Q1: Entities and Weak Entities



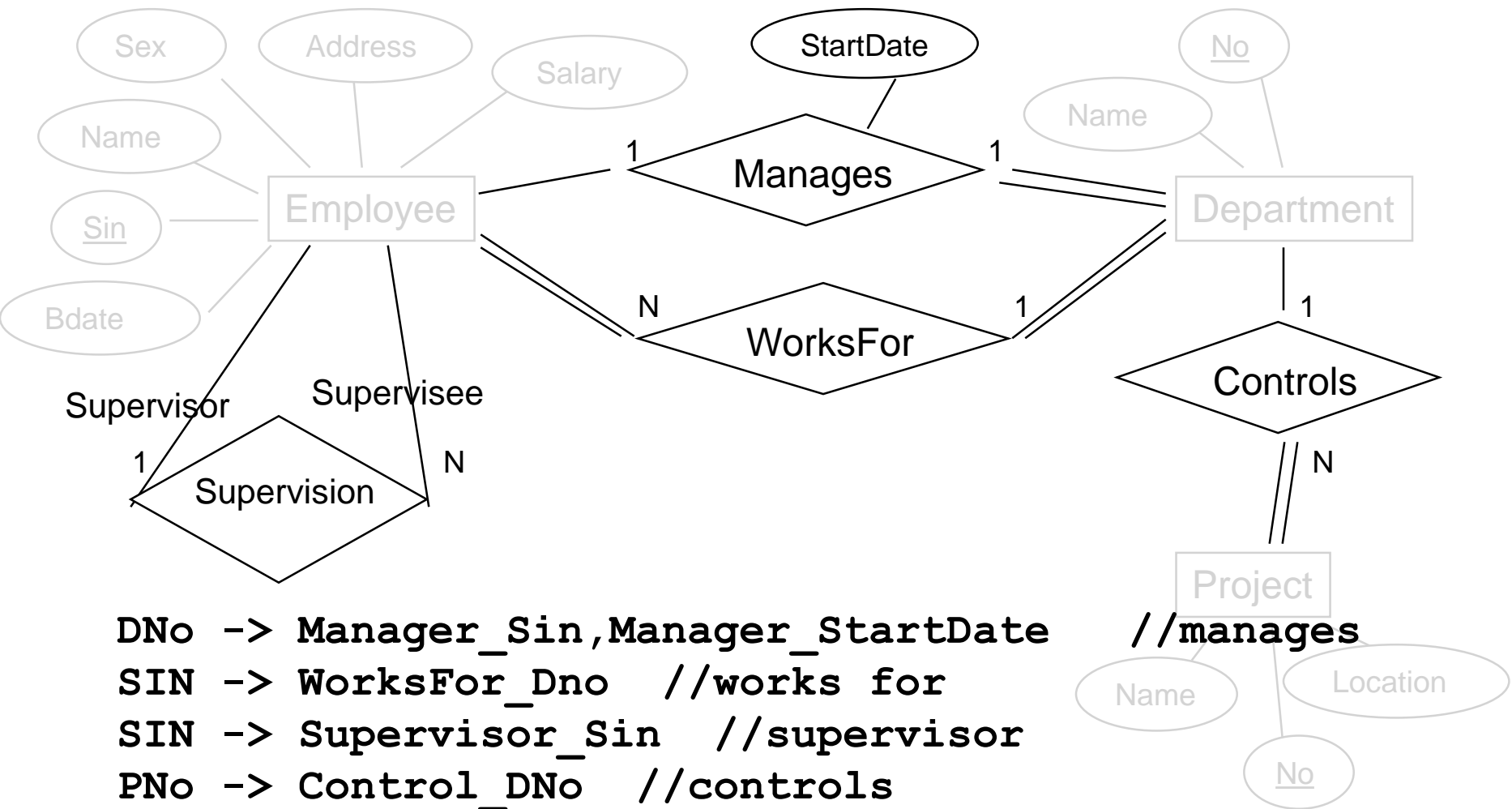
# A2,Q1: Entities and Weak Entities



# A2,Q1: Entities and Weak Entities

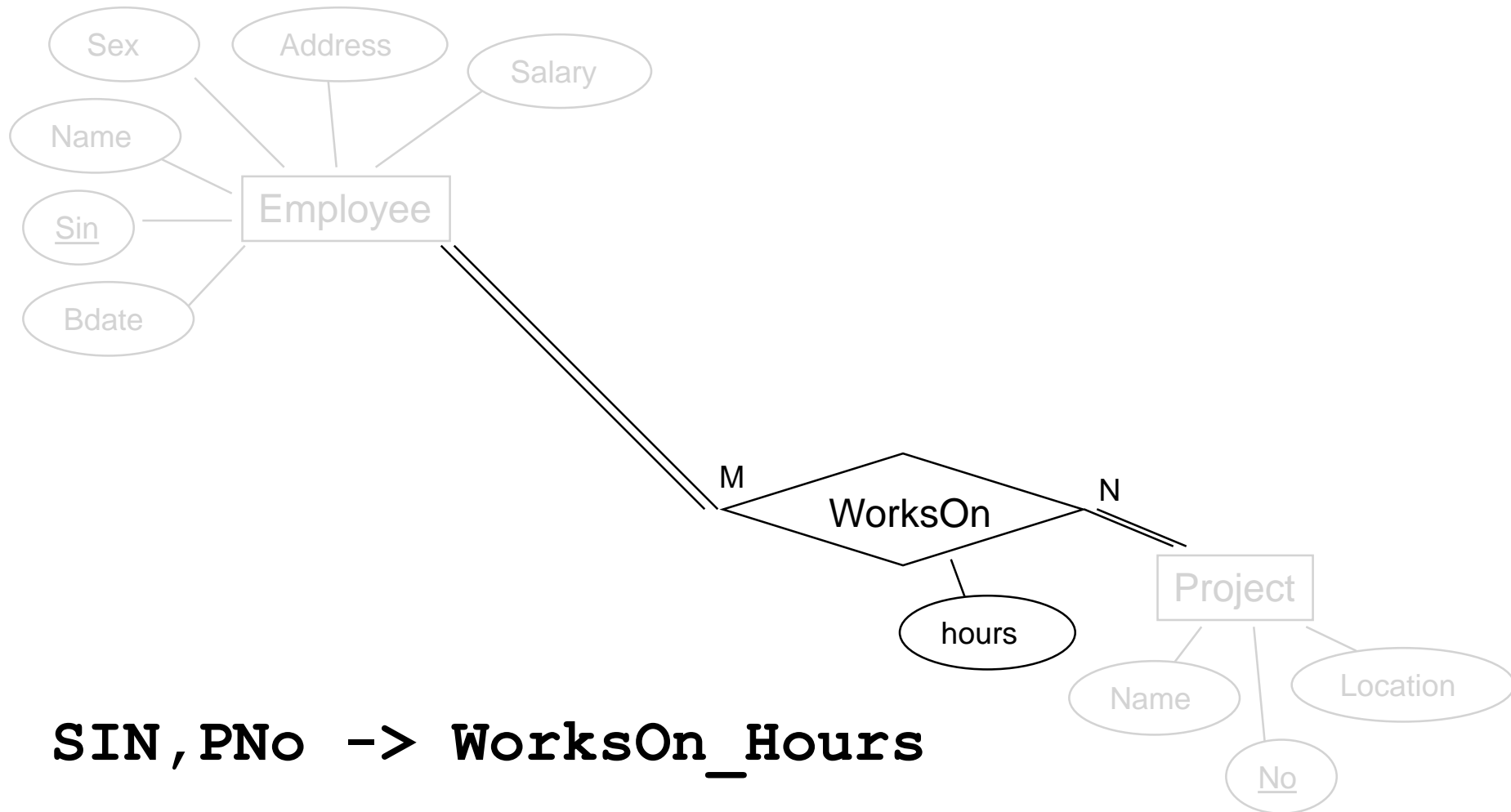


# 1:1 and 1:N Relationships



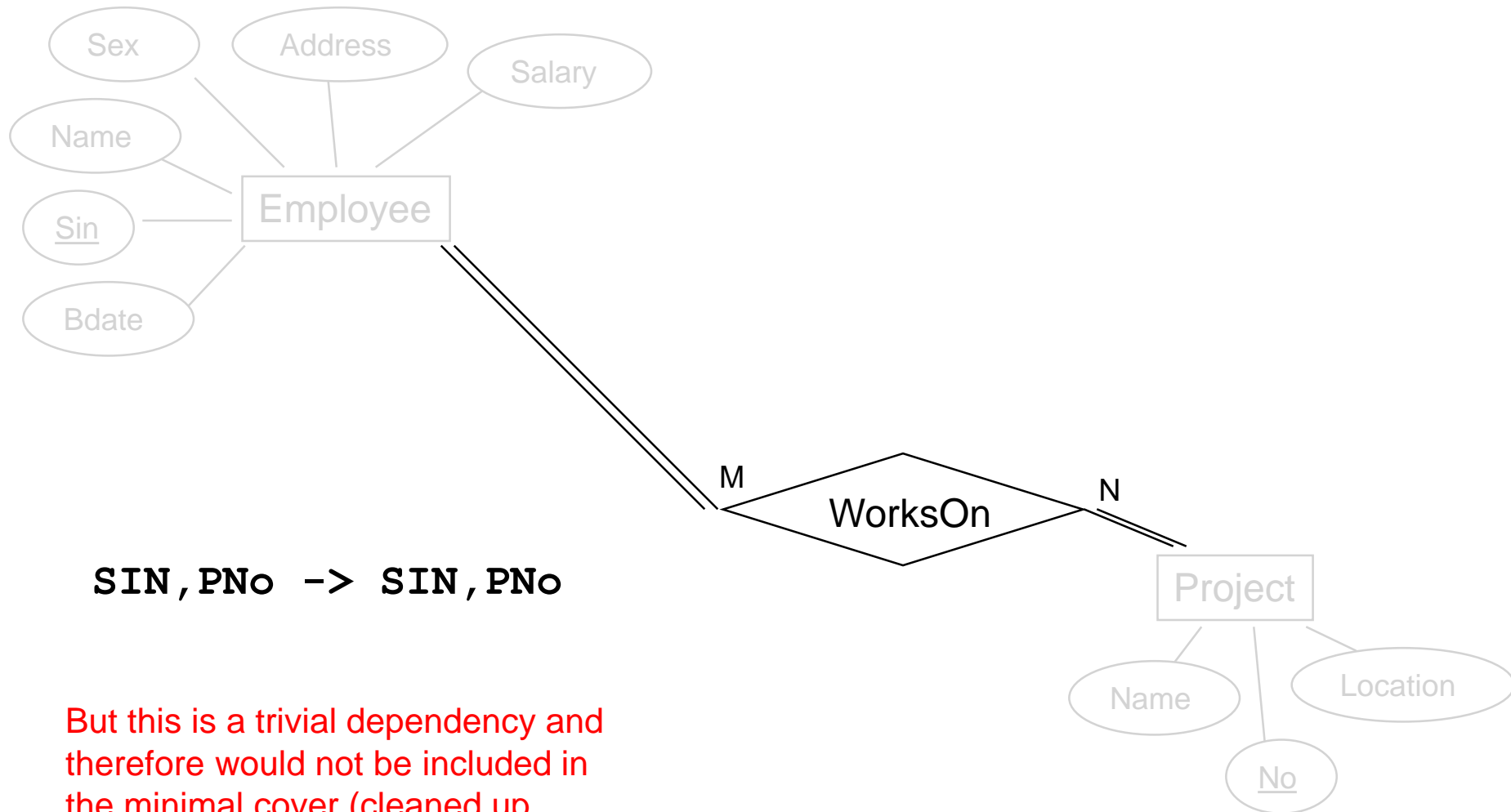
Here Underscore attributes to distinguish from previous Entity attributes

# N:N Relationships –with relationship attributes





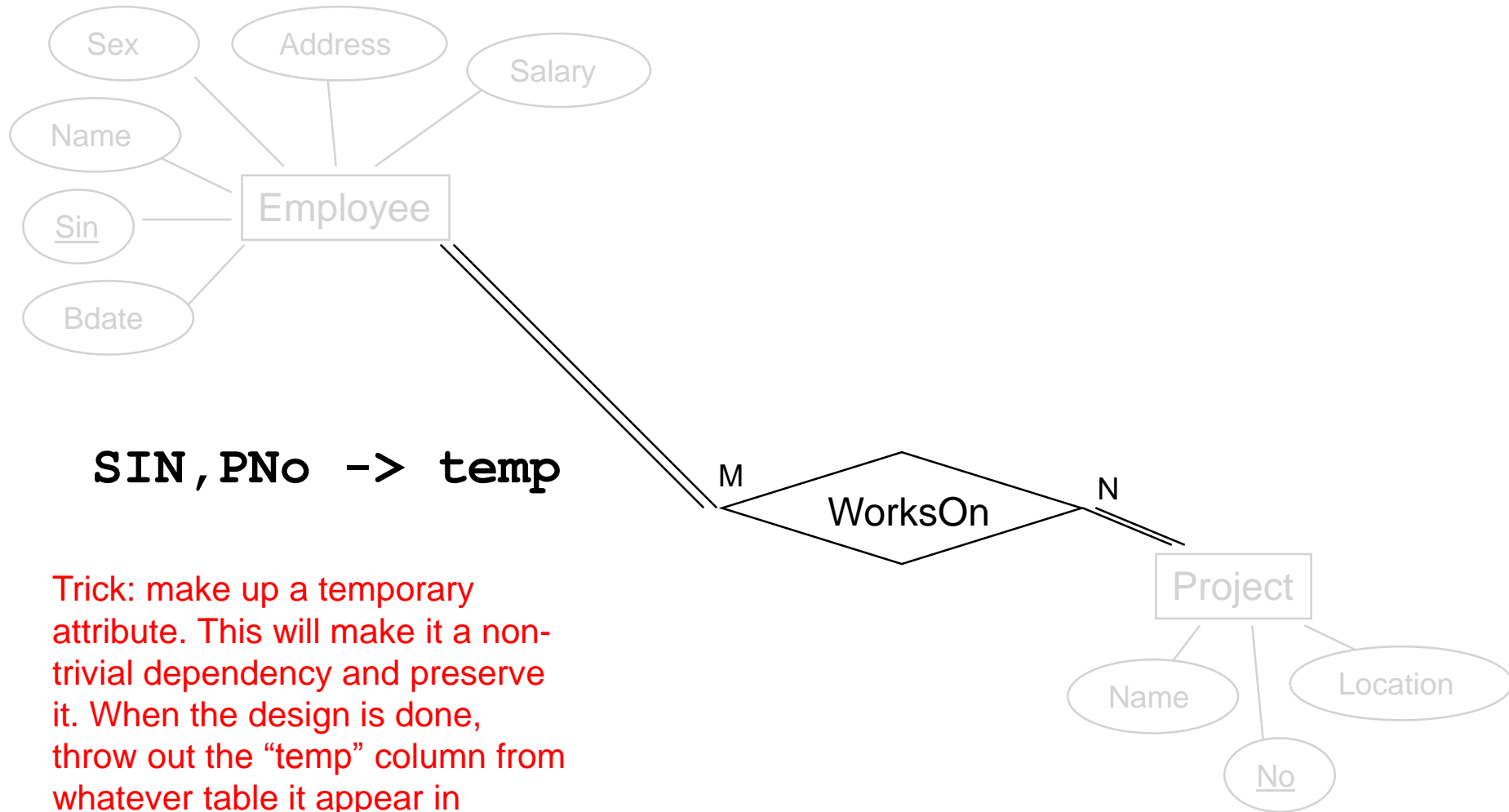
# N:N Relationships –without relationship attributes



**SIN, PNo → SIN, PNo**

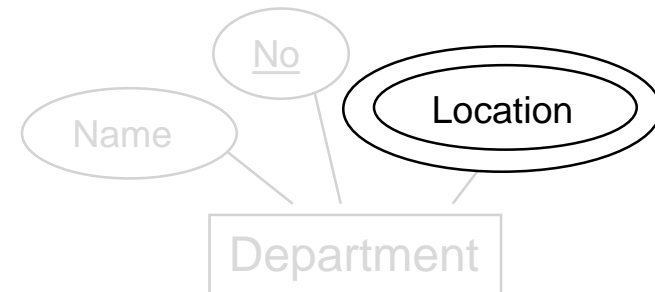
But this is a trivial dependency and therefore would not be included in the minimal cover (cleaned up version) of F

# N:N Relationships –without relationship attributes



## E-R diagram for Company Data (fig 3.2)

On the surface this is a 1:N relationship between department and locations (a department can have many locations)



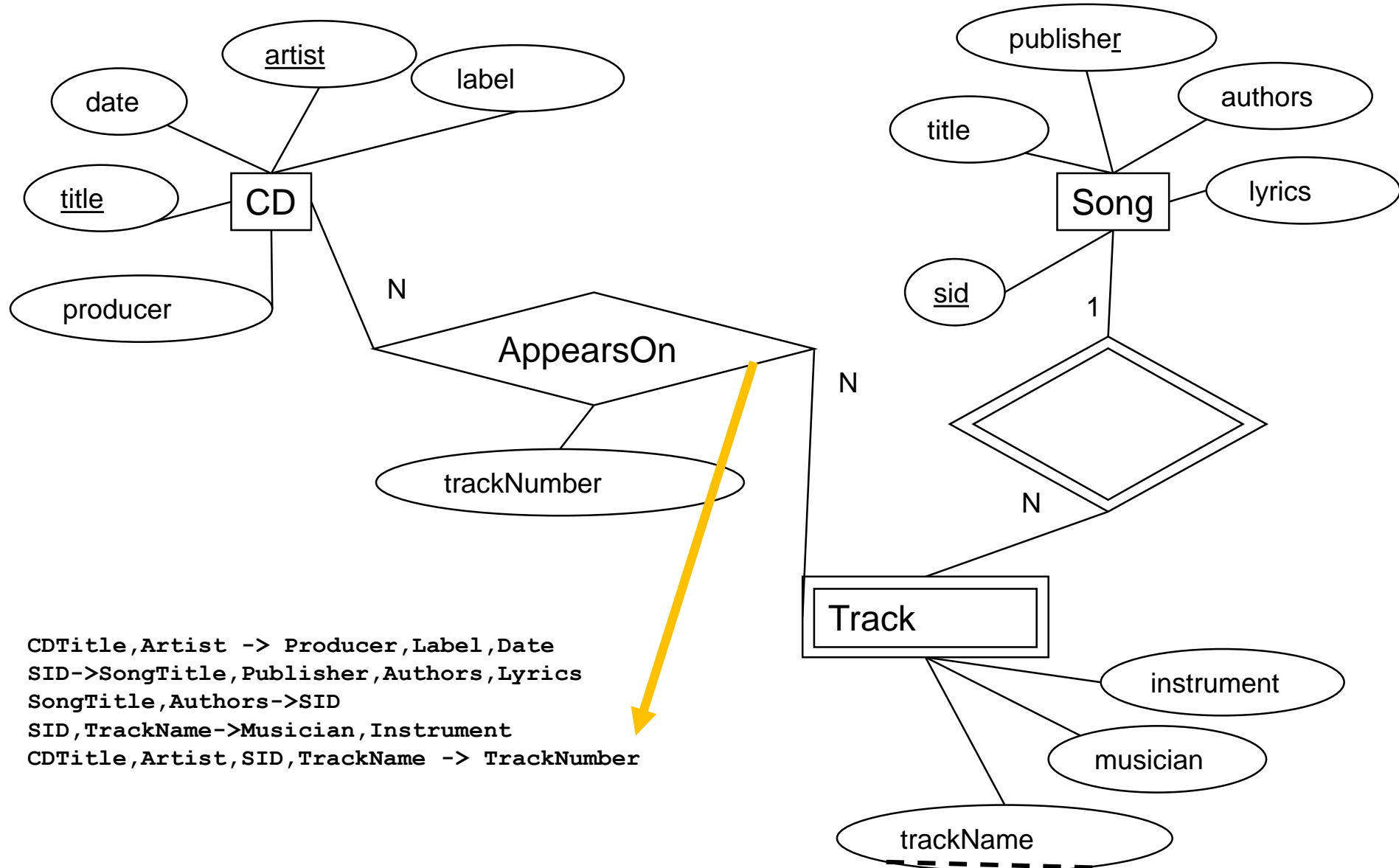
But if more than one department can have the same location, then this is really a N:N relationship between departments and locations

`DNo,Location -> Dno,Location //trivial dependency`

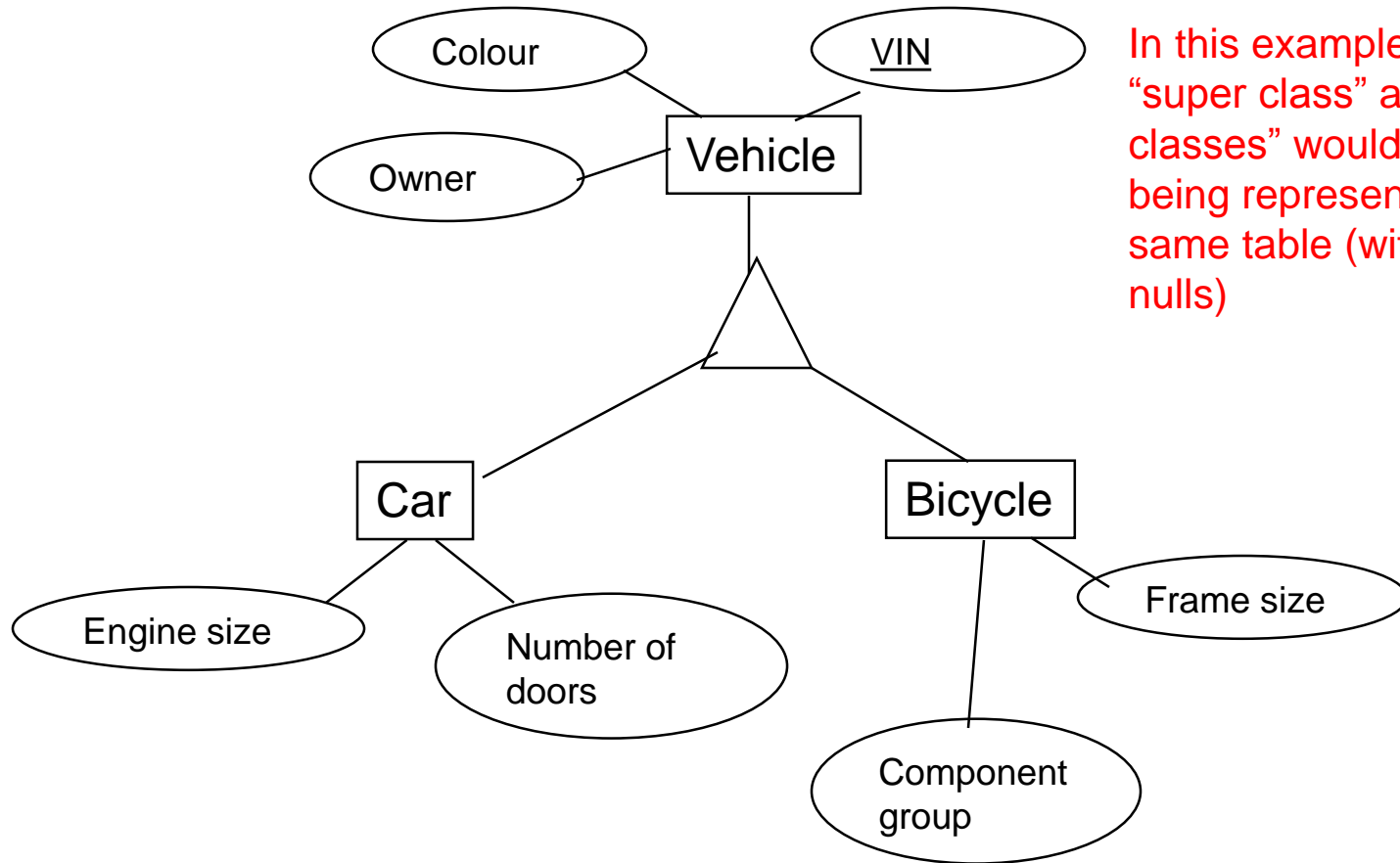
Or

`Dno,Location -> temp2 //non trivial`

# A2,Q1: Entities and Weak Entities



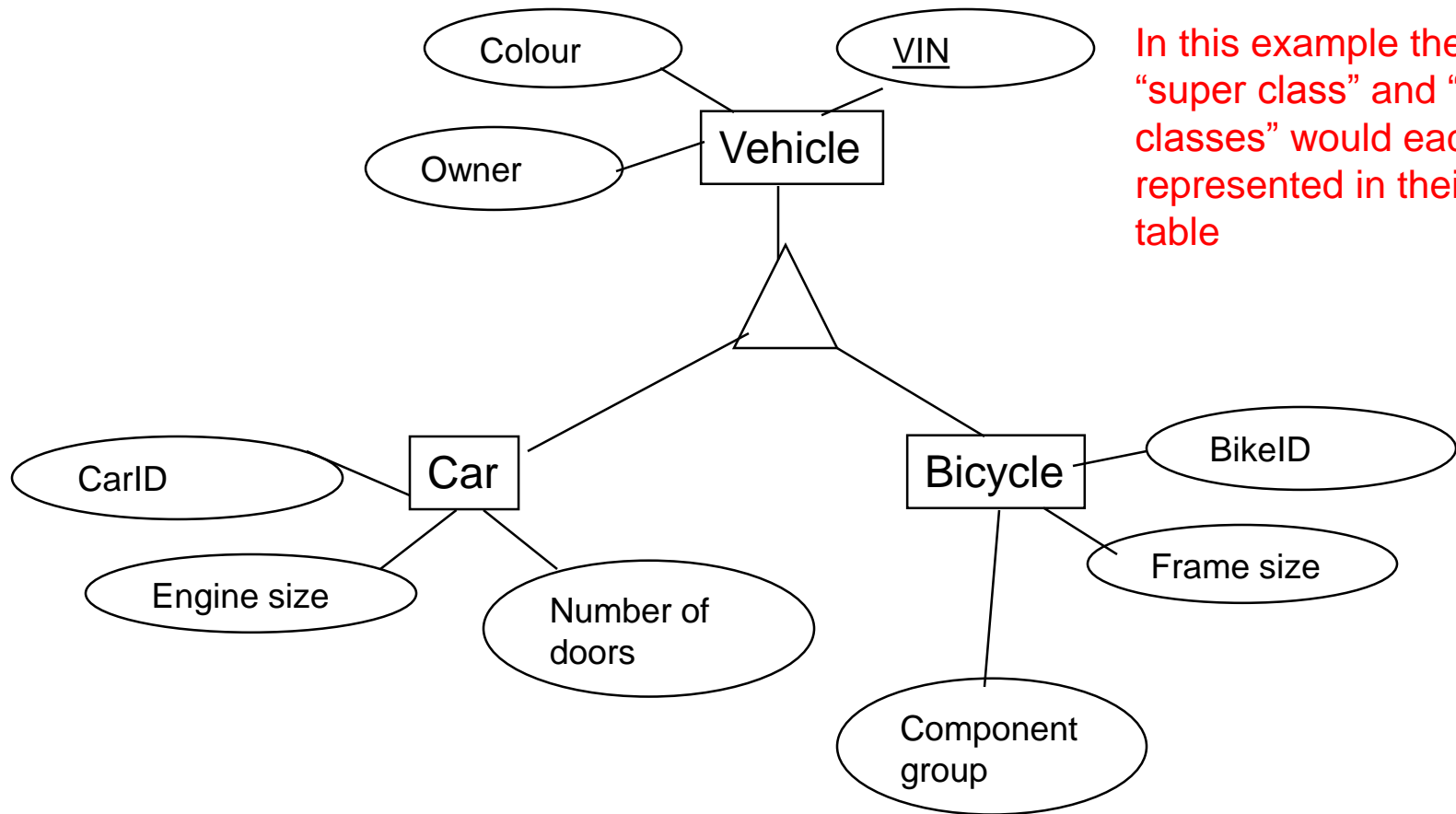
# Inheritance



In this example the “super class” and “sub-classes” would end up being represented in the same table (with lots of nulls)

**VIN -> Colour, Owner, EngineSize, Ndoors, Group, FrameSize**

# Inheritance



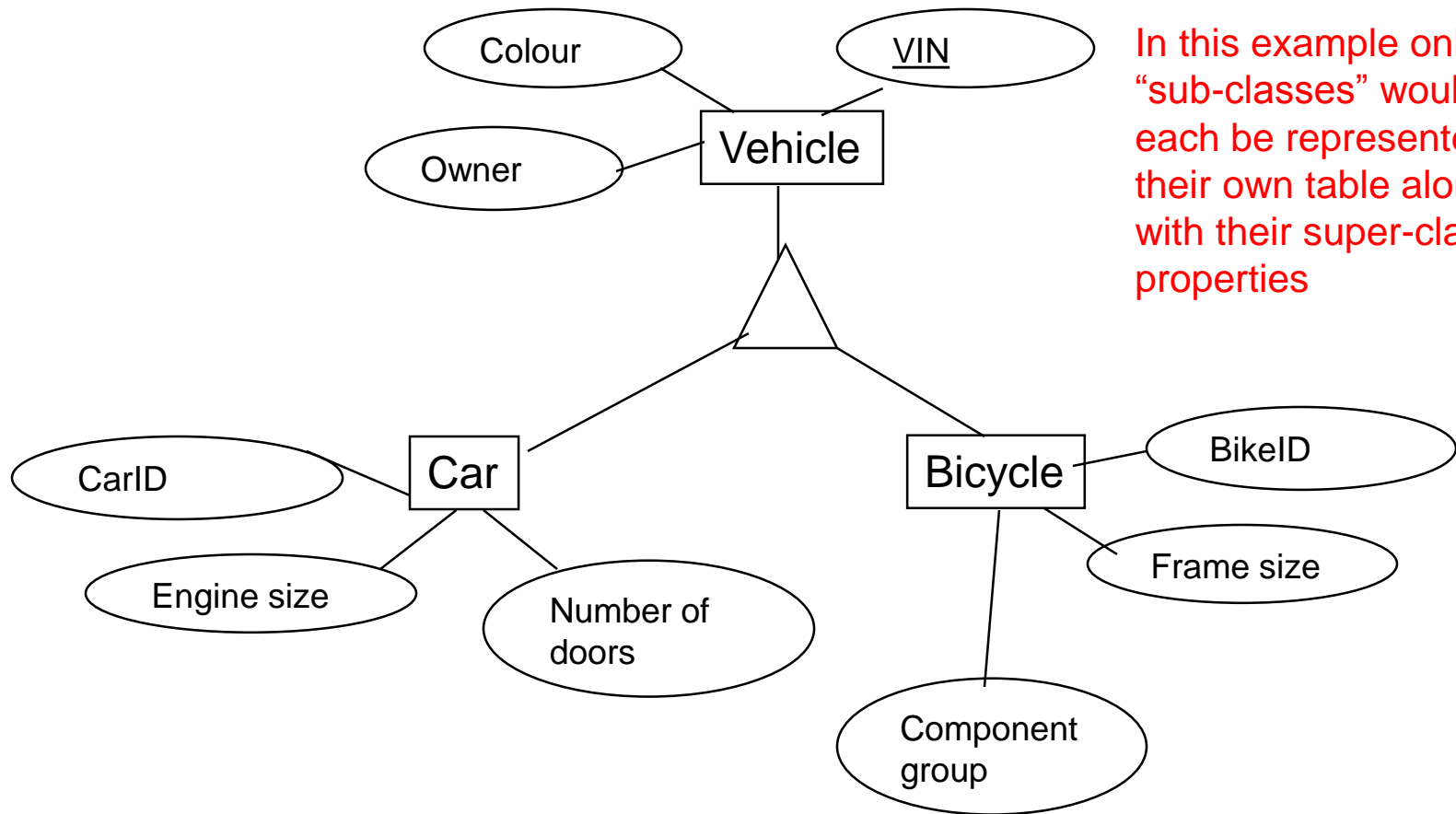
In this example the “super class” and “sub-classes” would each be represented in their own table

VIN -> Colour, Owner, CarID, BikeID

CarID -> EngineSize, Ndoors

BikeID -> Group, FrameSize

# Inheritance



**CarID -> VIN, CarColour, CarOwner, EngineSize, Ndoors**

**BikeID -> VIN, BikeColour, BikeOwner, Group, FrameSize**

## Exercise 1

**Consider the set of attributes  $R=\{A,B,C,D,E,F\}$  and the following set of functional dependencies proposed by the table designer.**

**$F_1 = \{ABD \rightarrow AC, B \rightarrow E, BA \rightarrow E, C \rightarrow BE, AD \rightarrow FB, C \rightarrow E\}$**

**A colleague suggests that they use the following dependency set instead**

**$F_2 = \{AD \rightarrow CF, C \rightarrow B, B \rightarrow E\}$**

**Determine if this is a reasonable suggestion**



## Approach 1

**If we can show the sets are equivalent then F2 can be used instead of F1**

**F1 and F2 are equivalent if  $F1^+ = F2^+$**

**To show this we must show that each functional dependency in F1 is implied by the set F2 and vice versa each functional dependency in F2 is implied by the set F1**

## Approach 1

As illustration we will show that:

**ABD- $\rightarrow$ AC from F1 is implied by set F2**  
**and**

**AD- $\rightarrow$ CF from F2 is implied by set F1**

**The same would have to be done for each functional dependency in each set, but for illustration here we only show the above two.**

## Approach 1

**AD->CF from F2 is implied by set F1**

### Proof

**AD->CF implied because :**

**AD->BF, given in F1**

**AD->F decomposition rule**

**ABD->AC given in F1**

**ABD->C decomposition rule**

**AD->B given in F1**

**AD->ABD augmentation rule**

**AD->C transitive rule : AD->ABD, ABD->C**

**AD->CF union rule, AD->C, AD->F**

**$F_1 = \{$   
**ABD->AC,**  
**B->E,**  
**BA->E,**  
**C->BE,**  
**AD->BF,**  
**C->E  $\}$****

**$F_2 = \{$   
**AD->CF,**  
**C->B,**  
**B->E $\}$****

## Approach 1

**ABD-→AC from F1 is implied by set F2**

### **Proof**

**ABD-→AC implied because :**

**AD-→CF, given in F2**

**AD- →ACF augmentation rule (add A to both sides)**

**ABD-→ABCF augmentation rule (add B to both sides)**

**ABD- →AC decomposition rules (ABD-→AC, ABD-→BF)**

**$F_1 = \{$   
**ABD-→AC,**  
**B-→E,**  
**BA-→E,**  
**C-→BE,**  
**AD-→FB,**  
**C-→E  $\}$****

**$F_2 = \{$   
**AD-→CF,**  
**C-→B,**  
**B-→E $\}$****

## Approach 2

We can find a **minimal cover**  $F_{m1}$  of  $F_1$  and a minimal cover  $F_{m2}$  of  $F_2$  and show that these minimal covers are equivalent

Again we would have to show that  $F_{m1}^+ = F_{m2}^+$  but the hope is that this would be trivial by inspection, or an easier problem than working with the “raw” dependency sets.

## Approach 2

Find a minimal cover of F1

$F_1 = \{$

$F_1 = \{$

ABD  $\rightarrow$  AC,

B  $\rightarrow$  E,

BA  $\rightarrow$  E,

C  $\rightarrow$  BE,

AD  $\rightarrow$  FB,

C  $\rightarrow$  E

$\}$

=

ABD  $\rightarrow$  A //decomposition

ABD  $\rightarrow$  C //decomposition

B  $\rightarrow$  E,

BA  $\rightarrow$  E,

C  $\rightarrow$  B, //decomposition

C  $\rightarrow$  E, //decomposition

AD  $\rightarrow$  F, //decomposition

AD  $\rightarrow$  B, //decomposition

C  $\rightarrow$  E

$\}$

## Approach 2

$F_1 = \{$		$F_1 = \{$
<del>ABD</del> $\rightarrow$ A	//reflexive	ABD $\rightarrow$ C
ABD $\rightarrow$ C		B $\rightarrow$ E,
B $\rightarrow$ E,		C $\rightarrow$ B,
<del>BA</del> $\rightarrow$ <del>E</del> ,	//implied by	C $\rightarrow$ E,
	//previous rule	AD $\rightarrow$ F,
C $\rightarrow$ B,	=	AD $\rightarrow$ B,
C $\rightarrow$ E,		
AD $\rightarrow$ F,		}
AD $\rightarrow$ B,		
<del>C</del> $\rightarrow$ <del>E</del>	//duplicate	
}		

## Approach 2

$$\begin{aligned} F_1 = \{ & \quad ABD \rightarrow C \quad // \text{since } AD \rightarrow B \\ & B \rightarrow E, \\ & C \rightarrow B, \\ & \cancel{C \rightarrow E}, \quad // \text{transitive} \\ & AD \rightarrow F, \\ & AD \rightarrow B, \\ & \} \end{aligned} = \begin{aligned} F_1 = \{ & AD \rightarrow C \\ & B \rightarrow E, \\ & C \rightarrow B, \\ & AD \rightarrow F, \\ & AD \rightarrow B, \\ & \} \end{aligned}$$



## Approach 2

$$\begin{aligned} F_1 = \{ & \text{AD} \rightarrow \text{C} \\ & \text{B} \rightarrow \text{E}, \\ & \text{C} \rightarrow \text{B}, \\ & \text{AD} \rightarrow \text{F}, \\ & \text{AD} \rightarrow \text{B}, \text{ //transitive} \\ & \} \end{aligned} = \begin{aligned} F_1 = \{ & \text{AD} \rightarrow \text{C} \\ & \text{B} \rightarrow \text{E}, \\ & \text{C} \rightarrow \text{B}, \\ & \text{AD} \rightarrow \text{F}, \\ & \} \end{aligned}$$

$$F_{m1} = \{\text{AD} \rightarrow \text{C}, \text{AD} \rightarrow \text{F}, \text{B} \rightarrow \text{E}, \text{C} \rightarrow \text{B}\}$$

## Approach 2

Find a minimal cover of F2

$$\begin{array}{lcl} F_2 = \{ & & F_2 = \{ \\ & AD \rightarrow CF, & AD \rightarrow C, \text{ //decomposition} \\ & C \rightarrow B, & AD \rightarrow F, \text{ //decomposition} \\ & B \rightarrow E & C \rightarrow B, \\ \} & = & B \rightarrow E \\ & & \} \end{array}$$

$$F_{m2} = \{ AD \rightarrow C, AD \rightarrow F, C \rightarrow B, B \rightarrow E \}$$

## Approach 2

$$F_{m1} = \{AD \rightarrow C, AD \rightarrow F, B \rightarrow E, C \rightarrow B\}$$

$$F_{m2} = \{AD \rightarrow C, AD \rightarrow F, C \rightarrow B, B \rightarrow E\}$$

By inspection  $F_{m1} = F_{m2}$  so the sets  $F_1$  and  $F_2$  are equivalent

## Exercise 2

- For each of the following cases a relation R has been defined over attributes A,B,C,D,E,F along with a set of functional dependencies that apply to them.
- Find all the candidate keys for the relation
- State the highest normal form the table R=ABCDEF would currently satisfy
- Decompose the table until all resulting tables are in BCNF form

## Exercise 2

**$F = \{ AB \rightarrow CDEF, EF \rightarrow C \}$**

## Exercise 2

$F = \{ AB \rightarrow CDEF, EF \rightarrow C \}$

Candidate keys: AB

Current Normal Form: = 2<sup>nd</sup> NF since  $EF \rightarrow C$  violates 3<sup>rd</sup> NF.

Decomposition:

ABDEF

EFC

## Exercise 2

**$F = \{ AB \rightarrow CDEF, EF \rightarrow B, D \rightarrow B \}$**

## Exercise 2

$F = \{ AB \rightarrow CDEF, EF \rightarrow B, D \rightarrow B \}$

Candidate keys: AB, AD, AEF

Current Normal Form: = 3<sup>rd</sup> NF since  $D \rightarrow B$  violates BCNF.

Decomposition:

ADEF

DB



## Exercise 2

**$F = \{ AB \rightarrow CDEF, BC \rightarrow D, \}$**

## Exercise 2

$F = \{ AB \rightarrow CDEF, BC \rightarrow D, \}$

Candidate keys: AB

Current Normal Form: = 2<sup>nd</sup> NF since  $BC \rightarrow D$  violates 3<sup>rd</sup> NF.

(Recall:  $Y \rightarrow A$  is a transitive dependency if Y is neither a superkey of R nor a proper subset of a key of R)

Decomposition:

ABCEF

BCD

## Exercise 2

**$F = \{ AB \rightarrow CDEF, B \rightarrow C, D \rightarrow C \}$**

## Exercise 2

$F = \{ AB \rightarrow CDEF, B \rightarrow C, D \rightarrow C \}$

Candidate keys: AB

Current Normal Form: = 1<sup>st</sup> NF since  $B \rightarrow C$  violates 2<sup>nd</sup> NF.

Decomposition:

ABDEF

BC

DC