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Faculty of Natural and Mathematical Sciences
January 2021



4CCS1DBS – Database Systems

Week 9 – Functional Dependencies and Normalisation

Topic: Informal Rules to Assess Database Design

# **List of Topics**

Term week	Topic	Lecturer
22	Introduction to Database Systems	Dr Tsoka
23	Data Modeling Using the Entity-Relationship Model	Dr Tsoka
24	Relational Data Model	Dr Curcin
25	SQL 1	Dr Curcin
26	SQL 2	Dr Curcin
27	CATCH UP WEEK	
28	Relational Algebra 1	Dr Curcin
29	Relational Algebra 2	Dr Curcin
30	Normalisation 1	Dr Tsoka
31	Normalisation 2	Dr Tsoka
32	Advanced Topics and Security Issues	Dr Tsoka

### Overview of this week's topics

- Informal Design Guidelines for Relational Databases
  - Semantics of the Relation Attributes
  - Redundant Information in Tuples and Update Anomalies
  - Null Values in Tuples
  - Spurious Tuples
- Functional Dependencies (FDs)
  - Definition of FD
  - Inference Rules for FDs

### Next week: Functional Dependencies and Normalisation

- Normal Forms Based on Primary Keys
  - Normalisation of Relations
  - Practical Use of Normal Forms
  - Definitions of Keys and Attributes Participating in Keys
  - First Normal Form
  - Second Normal Form
  - Third Normal Form
- BCNF (Boyce-Codd Normal Form)

## In this Recording

- Informal Design Guidelines for Relational Databases
  - Semantics of the Relation Attributes
  - Redundant Information in Tuples and Update Anomalies
  - Null Values in Tuples
  - Spurious Tuples

### Purpose

- Develop measures for quality in database design
  - why is one grouping of attributes better than another?
- Two levels at which to discuss 'goodness' of design:
  - Logical or conceptual level
    - How users interpret the relation schemas and meaning of attributes?
  - Implementation or storage level
    - How are the tuples in a database stored and updated ?

### Informal Design Guidelines for Relational Databases

- What is relational database design?
  - The grouping of attributes to form "good" relation schemas
- Two levels of relation schemas
  - The logical "user view" level
  - The storage "base relation" level
- Design is concerned mainly with base relations
- What are the criteria for "good" base relations?

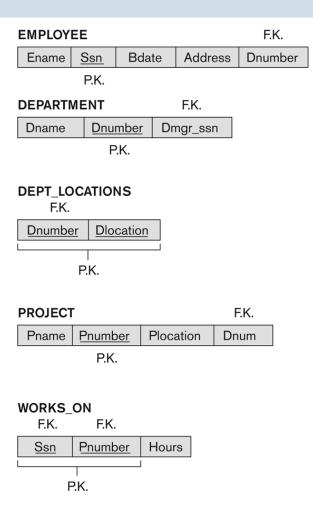
### Informal Design Guidelines for Relational Databases (contd)

- We first discuss informal guidelines for good relational design
- Then we discuss formal concepts of functional dependencies and normal forms
  - 1NF (First Normal Form)
  - 2NF (Second Normal Form)
  - 3NF (Third Normal Form)
  - BCNF (Boyce-Codd Normal Form)

### Semantics of Relation Attributes

- **Semantics:** how to interpret the attribute values stored in a tuple of the relation, i.e. how the attribute values in a tuple relate to one another.
- Generally, the easier to explain the semantics of a relation, the better the relation schema design.
  - The *ease* with which the meaning of relation attributes can be explained, is an *informal* measure of relation design quality.

### Semantics of Relation Attributes: Examples



# Semantics of Relation Attributes: Examples

(a)

EMP\_DEPT

Ename Ssn Bdate Address Dnumber Dname Dmgr\_ssn

(b)

#### EMP\_PROJ

<u>Ssn</u>	<u>Pnumber</u>	Hours	Ename	Pname	Plocation
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### Semantics of Relation Attributes: Overall

- GUIDELINE 1: Informally, each tuple in a relation should represent one entity or relationship instance. (Applies to individual relations and their attributes).
  - Attributes of different entities (EMPLOYEEs, DEPARTMENTs, PROJECTs) should not be mixed in the same relation
  - Only foreign keys should be used to refer to other entities
  - Entity and relationship attributes should be kept apart as much as possible.
- Note: Design a schema that can be explained easily relation by relation. The semantics of attributes should be easy to interpret.

### Redundant Information in Tuples and Update Anomalies

- When information is stored redundantly:
  - Wastes storage
  - Causes problems with update anomalies
    - Insertion anomalies
    - Deletion anomalies
    - Modification anomalies

# Redundant Information in Tuples: example EMP\_DEPT

EMPLOYEE				
Ename	<u>Ssn</u>	Bdate	Address	Dnumber
Smith, John B.	123456789	1965-01-09	731 Fondren, Houston, TX	5
Wong, Franklin T.	333445555	1955-12-08	638 Voss, Houston, TX	5
Zelaya, Alicia J.	999887777	1968-07-19	3321 Castle, Spring, TX	4
Wallace, Jennifer S.	987654321	1941-06-20	291Berry, Bellaire, TX	4
Narayan, Ramesh K.	666884444	1962-09-15	975 Fire Oak, Humble, TX	5
English, Joyce A.	453453453	1972-07-31	5631 Rice, Houston, TX	5
Jabbar, Ahmad V.	987987987	1969-03-29	980 Dallas, Houston, TX	4
Borg, James E.	888665555	1937-11-10	450 Stone, Houston, TX	1

Base Relation EMP\_DEPT formed after a Natural Join with redundant information

Redundancy

#### **DEPARTMENT**

Dname	<u>Dnumber</u>	Dmgr_ssn
Research	5	333445555
Administration	4	987654321
Headquarters	1	888665555

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EMP_DEPT				1		
Ename	<u>Ssn</u>	Bdate	Address	Dnumber	Dname	Dmgr_ssn
Smith, John B.	123456789	1965-01-09	731 Fondren, Houston, TX	5	Research	333445555
Wong, Franklin T.	333445555	1955-12-08	638 Voss, Houston, TX	5	Research	333445555
Zelaya, Alicia J.	999887777	1968-07-19	3321 Castle, Spring, TX	4	Administration	987654321
Wallace, Jennifer S.	987654321	1941-06-20	291 Berry, Bellaire, TX	4	Administration	987654321
Narayan, Ramesh K.	666884444	1962-09-15	975 FireOak, Humble, TX	5	Research	333445555
English, Joyce A.	453453453	1972-07-31	5631 Rice, Houston, TX	5	Research	333445555
Jabbar, Ahmad V.	987987987	1969-03-29	980 Dallas, Houston, TX	4	Administration	987654321
Borg, James E.	888665555	1937-11-10	450 Stone, Houston, TX	1	Headquarters	888665555

## Redundant Information in Tuples: example EMP\_PROJ

EMPLOYEE				
Ename	<u>Ssn</u>	Bdate	Address	Dnumber
Smith, John B.	123456789	1965-01-09	731 Fondren, Houston, TX	5
Wong, Franklin T.	333445555	1955-12-08	638 Voss, Houston, TX	5
Zelaya, Alicia J.	999887777	1968-07-19	3321 Castle, Spring, TX	4
Wallace, Jennifer S.	987654321	1941-06-20	291Berry, Bellaire, TX	4
Narayan, Ramesh K.	666884444	1962-09-15	975 Fire Oak, Humble, TX	5
English, Joyce A.	453453453	1972-07-31	5631 Rice, Houston, TX	5
Jabbar, Ahmad V.	987987987	1969-03-29	980 Dallas, Houston, TX	4
Borg, James E.	888665555	1937-11-10	450 Stone, Houston, TX	1

Pname	<u>Pnumber</u>	Plocation	Dnum
ProductX	1	Bellaire	5
ProductY	2	Sugarland	5
ProductZ	3	Houston	5
Computerization	10	Stafford	4
Reorganization	20	Houston	1
Newbenefits	30	Stafford	4

# Base Relation EMP\_PROJ formed after a Natural Join with redundant information

			Redundancy	Redunda	incy
EMP_PROJ			, i	·	
<u>Ssn</u>	<u>Pnumber</u>	Hours	Ename	Pname	Plocation
123456789	1	32.5	Smith, John B.	ProductX	Bellaire
123456789	2	7.5	Smith, John B.	ProductY	Sugarland
666884444	3	40.0	Narayan, Ramesh K.	ProductZ	Houston
453453453	1	20.0	English, Joyce A.	ProductX	Bellaire
453453453	2	20.0	English, Joyce A.	ProductY	Sugarland
333445555	2	10.0	Wong, Franklin T.	ProductY	Sugarland
333445555	3	10.0	Wong, Franklin T.	ProductZ	Houston
333445555	10	10.0	Wong, Franklin T.	Computerization	Stafford
333445555	20	10.0	Wong, Franklin T.	Reorganization	Houston
999887777	30	30.0	Zelaya, Alicia J.	Newbenefits	Stafford
999887777	10	10.0	Zelaya, Alicia J.	Computerization	Stafford
987987987	10	35.0	Jabbar, Ahmad V.	Computerization	Stafford
987987987	30	5.0	Jabbar, Ahmad V.	Newbenefits	Stafford
987654321	30	20.0	Wallace, Jennifer S.	Newbenefits	Stafford
987654321	20	15.0	Wallace, Jennifer S.	Reorganization	Houston
888665555	20	Null	Borg, James E.	Reorganization	Houston

### Insertion Anomalies: example

- Consider the relation:
  - EMP\_PROJ (Emp#, Proj#, Hours Ename, Pname, Plocation)
- Insert Anomaly:
  - Cannot insert a *new* project unless an employee is assigned to it.
- Conversely
  - Cannot insert an employee unless a he/she is assigned to a project.
- Also: consistency problems when assigning projects to every employee

			Redundancy	Podundo	anov.
			Redundancy	Redunda 	шсу
EMP_PROJ			·		
<u>Ssn</u>	<u>Pnumber</u>	Hours	Ename	Pname	Plocation
123456789	1	32.5	Smith, John B.	ProductX	Bellaire
123456789	2	7.5	Smith, John B.	ProductY	Sugarland
666884444	3	40.0	Narayan, Ramesh K.	ProductZ	Houston
453453453	1	20.0	English, Joyce A.	ProductX	Bellaire
453453453	2	20.0	English, Joyce A.	ProductY	Sugarland
333445555	2	10.0	Wong, Franklin T.	ProductY	Sugarland
333445555	3	10.0	Wong, Franklin T.	ProductZ	Houston
333445555	10	10.0	Wong, Franklin T.	Computerization	Stafford
333445555	20	10.0	Wong, Franklin T.	Reorganization	Houston
999887777	30	30.0	Zelaya, Alicia J.	Newbenefits	Stafford
999887777	10	10.0	Zelaya, Alicia J.	Computerization	Stafford
987987987	10	35.0	Jabbar, Ahmad V.	Computerization	Stafford
987987987	30	5.0	Jabbar, Ahmad V.	Newbenefits	Stafford
987654321	30	20.0	Wallace, Jennifer S.	Newbenefits	Stafford
987654321	20	15.0	Wallace, Jennifer S.	Reorganization	Houston
888665555	20	Null	Borg, James E.	Reorganization	Houston

### Deletion Anomalies: example

- Consider the relation:
  - EMP\_PROJ (Emp#, Proj#, Hours Ename, Pname, Plocation)
- Deletion Anomaly:
  - When a project is deleted, it will result in deleting all the employees who work on that project.
  - Alternatively, if an employee is the sole employee on a project, deleting that employee would result in deleting the corresponding project.

			Redundancy	Redunda	ıncy
EMP_PROJ					
Ssn	Pnumber	Hours	Ename	Pname	Plocation
123456789	1	32.5	Smith, John B.	ProductX	Bellaire
123456789	2	7.5	Smith, John B.	ProductY	Sugarland
666884444	3	40.0	Narayan, Ramesh K.	ProductZ	Houston
453453453	1	20.0	English, Joyce A.	ProductX	Bellaire
453453453	2	20.0	English, Joyce A.	ProductY	Sugarland
333445555	2	10.0	Wong, Franklin T.	ProductY	Sugarland
333445555	3	10.0	Wong, Franklin T.	ProductZ	Houston
333445555	10	10.0	Wong, Franklin T.	Computerization	Stafford
333445555	20	10.0	Wong, Franklin T.	Reorganization	Houston
999887777	30	30.0	Zelaya, Alicia J.	Newbenefits	Stafford
999887777	10	10.0	Zelaya, Alicia J.	Computerization	Stafford
987987987	10	35.0	Jabbar, Ahmad V.	Computerization	Stafford
987987987	30	5.0	Jabbar, Ahmad V.	Newbenefits	Stafford
987654321	30	20.0	Wallace, Jennifer S.	Newbenefits	Stafford
987654321	20	15.0	Wallace, Jennifer S.	Reorganization	Houston
888665555	20	Null	Borg, James E.	Reorganization	Houston

### **Update Anomalies: example**

- Consider the relation:
  - EMP\_PROJ (Emp#, Proj#, Hours Ename, Pname, Plocation)
- Update Anomaly:
  - Changing the name of project number P1 (e.g from "Billing" to "Customer-Accounting") may cause this update to be made for all 100 employees working on project P1.
  - If we fail to update some tuples, inconsistencies are introduced.

			Redundancy	Redunda I	ıncy
EMP_PROJ					
<u>Ssn</u>	Pnumber	Hours	Ename	Pname	Plocation
123456789	1	32.5	Smith, John B.	ProductX	Bellaire
123456789	2	7.5	Smith, John B.	ProductY	Sugarland
666884444	3	40.0	Narayan, Ramesh K.	ProductZ	Houston
453453453	1	20.0	English, Joyce A.	ProductX	Bellaire
453453453	2	20.0	English, Joyce A.	ProductY	Sugarland
333445555	2	10.0	Wong, Franklin T.	ProductY	Sugarland
333445555	3	10.0	Wong, Franklin T.	ProductZ	Houston
333445555	10	10.0	Wong, Franklin T.	Computerization	Stafford
333445555	20	10.0	Wong, Franklin T.	Reorganization	Houston
999887777	30	30.0	Zelaya, Alicia J.	Newbenefits	Stafford
999887777	10	10.0	Zelaya, Alicia J.	Computerization	Stafford
987987987	10	35.0	Jabbar, Ahmad V.	Computerization	Stafford
987987987	30	5.0	Jabbar, Ahmad V.	Newbenefits	Stafford
987654321	30	20.0	Wallace, Jennifer S.	Newbenefits	Stafford
987654321	20	15.0	Wallace, Jennifer S.	Reorganization	Houston
888665555	20	Null	Borg, James E.	Reorganization	Houston

### Guideline to Redundant Information in Tuples and Update Anomalies

### ■ GUIDELINE 2:

- Design a schema that does not suffer from the insertion, deletion and update anomalies.
- If there are any anomalies present, then note them so that applications can be made to take them into account.

### **Null Values in Tuples**

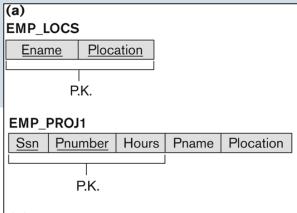
- When grouping attributes in an enlarged relation:
  - End up with many nulls
  - Waste of storage
  - Problems in understanding meanings of attributes
  - Problems with aggregate functions (SUM etc)
- Reasons for nulls:
  - Attribute not applicable or invalid
  - Attribute value unknown (may exist)
  - Value known to exist, but unavailable

### Null Values in Tuples (contd)

### GUIDELINE 3:

- Relations should be designed such that their tuples will have as few NULL values as possible
- Attributes that are NULL frequently could be placed in separate relations (with the primary key)
- Example: if 10% of employees have individual offices, attribute should not be included in EMPLOYEE relation. Instead, use separate relation: EMP\_OFFICES (ESSN, OFFICE-NUMBER).

An example of schema comprising relations EMP\_LOCS EMP\_PROJ1



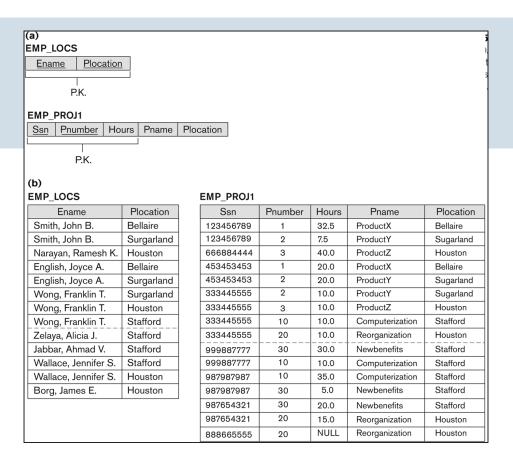
### (b)

#### EMP\_LOCS

Ename	Plocation
Smith, John B.	Bellaire
Smith, John B.	Surgarland
Narayan, Ramesh K.	Houston
English, Joyce A.	Bellaire
English, Joyce A.	Surgarland
Wong, Franklin T.	Surgarland
Wong, Franklin T.	Houston
Wong, Franklin T.	Stafford
Zelaya, Alicia J.	Stafford
Jabbar, Ahmad V.	Stafford
Wallace, Jennifer S.	Stafford
Wallace, Jennifer S.	Houston
Borg, James E.	Houston

#### EMP\_PROJ1

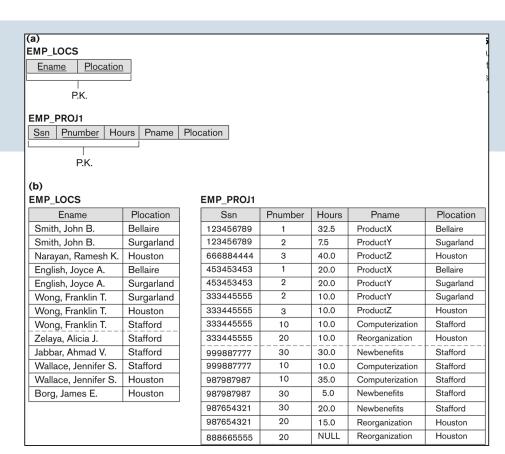
Ssn	Pnumber	Hours	Pname	Plocation
123456789	1	32.5	ProductX	Bellaire
123456789	2	7.5	ProductY	Sugarland
666884444	3	40.0	ProductZ	Houston
453453453	1	20.0	ProductX	Bellaire
453453453	2	20.0	ProductY	Sugarland
333445555	2	10.0	ProductY	Sugarland
333445555	3	10.0	ProductZ	Houston
333445555	10	10.0	Computerization	Stafford
333445555	20	10.0	Reorganization	Houston
999887777	30	30.0	Newbenefits	Stafford
999887777	10	10.0	Computerization	Stafford
987987987	10	35.0	Computerization	Stafford
987987987	30	5.0	Newbenefits	Stafford
987654321	30	20.0	Newbenefits	Stafford
987654321	20	15.0	Reorganization	Houston
888665555	20	NULL	Reorganization	Houston



How can EMP\_PROJ (right) be generated from EMP\_PROJ1 and EMP\_LOCS (above)?

Can we use a JOIN operation?

EMP_PROJ					
<u>Ssn</u>	<u>Pnumber</u>	Hours	Ename	Pname	Plocation
123456789	1	32.5	Smith, John B.	ProductX	Bellaire
123456789	2	7.5	Smith, John B.	ProductY	Sugarland
666884444	3	40.0	Narayan, Ramesh K.	ProductZ	Houston
453453453	1	20.0	English, Joyce A.	ProductX	Bellaire
453453453	2	20.0	English, Joyce A.	ProductY	Sugarland
333445555	2	10.0	Wong, Franklin T.	ProductY	Sugarland
333445555	3	10.0	Wong, Franklin T.	ProductZ	Houston
333445555	10	10.0	Wong, Franklin T.	Computerization	Stafford
333445555	20	10.0	Wong, Franklin T.	Reorganization	Houston
999887777	30	30.0	Zelaya, Alicia J.	Newbenefits	Stafford
999887777	10	10.0	Zelaya, Alicia J.	Computerization	Stafford
987987987	10	35.0	Jabbar, Ahmad V.	Computerization	Stafford
987987987	30	5.0	Jabbar, Ahmad V.	Newbenefits	Stafford
987654321	30	20.0	Wallace, Jennifer S.	Newbenefits	Stafford
987654321	20	15.0	Wallace, Jennifer S.	Reorganization	Houston
888665555	20	Null	Borg, James E.	Reorganization	Houston



The result of JOIN is shown on the right.

	Ssn	Pnumber	Hours	Pname	Plocation	Ename
	123456789	1	32.5	ProductX	Bellaire	Smith, John B.
*	123456789	1	32.5	ProductX	Bellaire	English, Joyce A.
	123456789	2	7.5	ProductY	Sugarland	Smith, John B.
*	123456789	2	7.5	ProductY	Sugarland	English, Joyce A.
*	123456789	2	7.5	ProductY	Sugarland	Wong, Franklin T.
	666884444	3	40.0	ProductZ	Houston	Narayan, Ramesh K.
*	666884444	3	40.0	ProductZ	Houston	Wong, Franklin T.
*	453453453	1	20.0	ProductX	Bellaire	Smith, John B.
	453453453	1	20.0	ProductX	Bellaire	English, Joyce A.
*	453453453	2	20.0	ProductY	Sugarland	Smith, John B.
	453453453	2	20.0	ProductY	Sugarland	English, Joyce A.
*	453453453	2	20.0	ProductY	Sugarland	Wong, Franklin T.
*	333445555	2	10.0	ProductY	Sugarland	Smith, John B.
*	333445555	2	10.0	ProductY	Sugarland	English, Joyce A.
	333445555	2	10.0	ProductY	Sugarland	Wong, Franklin T.
*	333445555	3	10.0	ProductZ	Houston	Narayan, Ramesh K.
	333445555	3	10.0	ProductZ	Houston	Wong, Franklin T.
	333445555	10	10.0	Computerization	Stafford	Wong, Franklin T.
*	333445555	20	10.0	Reorganization	Houston	Narayan, Ramesh K.
	333445555	20	10.0	Reorganization	Houston	Wong, Franklin T.

When comparing with our original EMP\_RPOJ relation, we conclude that the JOIN operation has created spurious (erroneous) tuples, marked with an asterisk.

EMP_PROJ					
<u>Ssn</u>	<u>Pnumber</u>	Hours	Ename	Pname	Plocation
123456789	1	32.5	Smith, John B.	ProductX	Bellaire
123456789	2	7.5	Smith, John B.	ProductY	Sugarland
666884444	3	40.0	Narayan, Ramesh K.	ProductZ	Houston
453453453	1	20.0	English, Joyce A.	ProductX	Bellaire
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333445555	2	10.0	Wong, Franklin T.	ProductY	Sugarland
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987987987	30	5.0	Jabbar, Ahmad V.	Newbenefits	Stafford
987654321	30	20.0	Wallace, Jennifer S.	Newbenefits	Stafford
987654321	20	15.0	Wallace, Jennifer S.	Reorganization	Houston
888665555	20	Null	Borg, James E.	Reorganization	Houston

	Ssn	Pnumber	Hours	Pname	Plocation	Ename
	123456789	1	32.5	ProductX	Bellaire	Smith, John B.
*	123456789	1	32.5	ProductX	Bellaire	English, Joyce A.
	123456789	2	7.5	ProductY	Sugarland	Smith, John B.
*	123456789	2	7.5	ProductY	Sugarland	English, Joyce A.
*	123456789	2	7.5	ProductY	Sugarland	Wong, Franklin T.
	666884444	3	40.0	ProductZ	Houston	Narayan, Ramesh K.
*	666884444	3	40.0	ProductZ	Houston	Wong, Franklin T.
*	453453453	1	20.0	ProductX	Bellaire	Smith, John B.
	453453453	1	20.0	ProductX	Bellaire	English, Joyce A.
*	453453453	2	20.0	ProductY	Sugarland	Smith, John B.
	453453453	2	20.0	ProductY	Sugarland	English, Joyce A.
*	453453453	2	20.0	ProductY	Sugarland	Wong, Franklin T.
*	333445555	2	10.0	ProductY	Sugarland	Smith, John B.
*	333445555	2	10.0	ProductY	Sugarland	English, Joyce A.
	333445555	2	10.0	ProductY	Sugarland	Wong, Franklin T.
*	333445555	3	10.0	ProductZ	Houston	Narayan, Ramesh K.
	333445555	3	10.0	ProductZ	Houston	Wong, Franklin T.
	333445555	10	10.0	Computerization	Stafford	Wong, Franklin T.
*	333445555	20	10.0	Reorganization	Houston	Narayan, Ramesh K.
	333445555	20	10.0	Reorganization	Houston	Wong, Franklin T.

### **Spurious Tuples**

 Bad designs for a relational database may result in erroneous results for certain JOIN operations.

#### GUIDELINE 4:

- Design relation schemas that can be joined with equality conditions on attributes that are either primary keys or foreign keys in a way that guarantees that no spurious tuples will be generated.
- Avoid relations that contain matching attributes that are not (foreign key, primary key) combinations, as joining on such attributes will produce spurious tuples.

### Summary of Design Guidelines

- Problems pointed out stemming from sub-optimal database design:
  - Anomalies that cause redundant work during insertion or modification, as well as accidental loss of information during deletion.
  - Waste of storage space due to nulls, difficulty in join or aggregation functions due to null values.
  - Generation of invalid or spurious data during joins or improperly related base relations.



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Faculty of Natural and Mathematical Sciences
January 2021



4CCS1DBS – Database Systems

Week 9 – Functional Dependencies and Normalisation

**Topic: Functional Dependencies** 

### Overview of this week's topics

- Informal Design Guidelines for Relational Databases
  - Semantics of the Relation Attributes
  - Redundant Information in Tuples and Update Anomalies
  - Null Values in Tuples
  - Spurious Tuples
- Functional Dependencies (FDs)
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## In this Recording

- Functional Dependencies (FDs)
  - Definition of FD
  - Inference Rules for FDs

### **Functional Dependencies**

- Functional dependencies (FDs)
  - Used to specify formal measures of how good a relational database design is
  - Keys are used to define normal forms for relations
  - Constraints are derived from the meaning and interrelationships of the data attributes
- A set of attributes X functionally determines a set of attributes Y if the value of X determines a unique value for Y

### Functional Dependencies (contd)

- Functional dependency (FD) between attributes X and Y of relation R:
  - X → Y, if whenever two tuples have the same value for X, they must have the same value for Y
  - for any two tuples t1 and t2 in any relation instance r(R): if t1[X]=t2[X], then t1[Y]=t2[Y]
- $\rightarrow$  Y in R specifies a *constraint* on all relation instances r(R)
- Written as X → Y; can be displayed graphically on a relation schema as in Figures (denoted by an arrow).
- FDs are derived from the real-world constraints on the attributes
- X: left-hand side, Y: right-hand side

### **Functional Dependency Example**

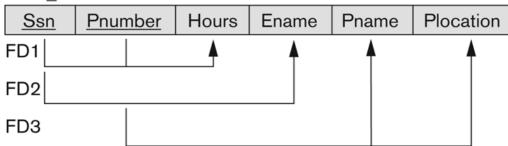
What are the functional dependencies in this relation?

### EMP\_PROJ

<u>sn</u>	<u>Pnumber</u>		Hours	Ename	Pname	Plocation			
			-			-			
[	EMP_PROJ				I				
	<u>Ssn</u>	Pnumber	Hours	Ename	Pname	Plocation			
	123456789	1	32.5	Smith, John B.	ProductX	Bellaire			
	123456789	2	7.5	Smith, John B.	ProductY	Sugarland			
	666884444	3	40.0	Narayan, Ramesh K.	ProductZ	Houston			
	453453453	1	20.0	English, Joyce A.	ProductX	Bellaire			
	453453453	2	20.0	English, Joyce A.	ProductY	Sugarland			
	333445555	2	10.0	Wong, Franklin T.	ProductY	Sugarland			
	333445555	3	10.0	Wong, Franklin T.	ProductZ	Houston			
	333445555	10	10.0	Wong, Franklin T.	Computerization	Stafford			
	333445555	20	10.0	Wong, Franklin T.	Reorganization	Houston			
	999887777	30	30.0	Zelaya, Alicia J.	Newbenefits	Stafford			
	999887777	10	10.0	Zelaya, Alicia J.	Computerization	Stafford			
	987987987	10	35.0	Jabbar, Ahmad V.	Computerization	Stafford			
	987987987	30	5.0	Jabbar, Ahmad V.	Newbenefits	Stafford			
	987654321	30	20.0	Wallace, Jennifer S.	Newbenefits	Stafford			
	987654321	20	15.0	Wallace, Jennifer S.	Reorganization	Houston			
	888665555	20	Null	Borg, James E.	Reorganization	Houston			

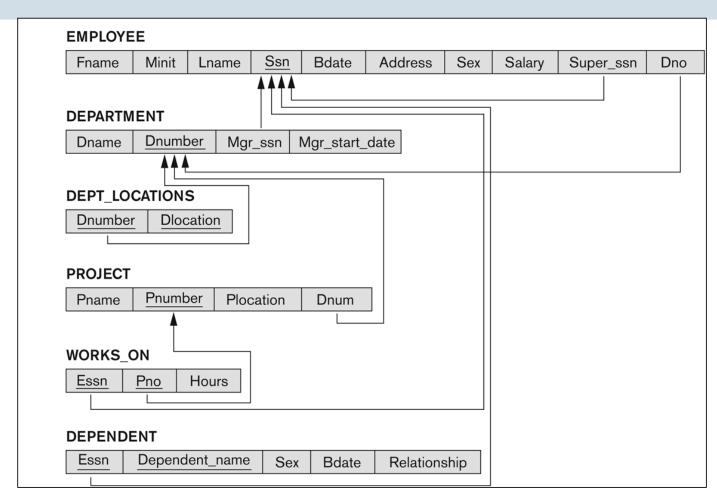
# **Functional Dependency Example**





EMP_PROJ					I
<u>Ssn</u>	<u>Pnumber</u>	Hours	Ename	Pname	Plocation
123456789	1	32.5	Smith, John B.	ProductX	Bellaire
123456789	2	7.5	Smith, John B.	ProductY	Sugarland
666884444	3	40.0	Narayan, Ramesh K.	ProductZ	Houston
453453453	1	20.0	English, Joyce A.	ProductX	Bellaire
453453453	2	20.0	English, Joyce A.	ProductY	Sugarland
333445555	2	10.0	Wong, Franklin T.	ProductY	Sugarland
333445555	3	10.0	Wong, Franklin T.	ProductZ	Houston
333445555	10	10.0	Wong, Franklin T.	Computerization	Stafford
333445555	20	10.0	Wong, Franklin T.	Reorganization	Houston
999887777	30	30.0	Zelaya, Alicia J.	Newbenefits	Stafford
999887777	10	10.0	Zelaya, Alicia J.	Computerization	Stafford
987987987	10	35.0	Jabbar, Ahmad V.	Computerization	Stafford
987987987	30	5.0	Jabbar, Ahmad V.	Newbenefits	Stafford
987654321	30	20.0	Wallace, Jennifer S.	Newbenefits	Stafford
987654321	20	15.0	Wallace, Jennifer S.	Reorganization	Houston
888665555	20	Null	Borg, James E.	Reorganization	Houston

# Schema Showing Foreign Keys



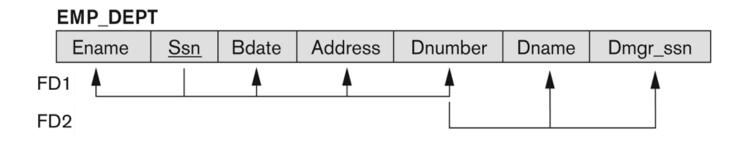
## **Functional Dependency Example**

### **EMP\_DEPT**

Ename	Ssn	Bdate	Address	Dnumber	Dname	Dmgr_ssn
	<u> </u>	0.0.00	7 10.0			g

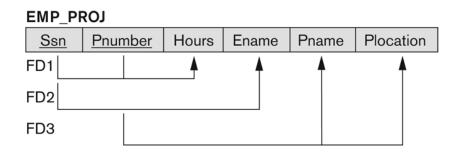
What are the functional dependencies in this relation?

# **Functional Dependency Example**



EMP_DEPT						
Ename	<u>Ssn</u>	Bdate	Address	Dnumber	Dname	Dmgr_ssn
Smith, John B.	123456789	1965-01-09	731 Fondren, Houston, TX	5	Research	333445555
Wong, Franklin T.	333445555	1955-12-08	638 Voss, Houston, TX	5	Research	333445555
Zelaya, Alicia J.	999887777	1968-07-19	3321 Castle, Spring, TX	4	Administration	987654321
Wallace, Jennifer S.	987654321	1941-06-20	291 Berry, Bellaire, TX	4	Administration	987654321
Narayan, Ramesh K.	666884444	1962-09-15	975 FireOak, Humble, TX	5	Research	333445555
English, Joyce A.	453453453	1972-07-31	5631 Rice, Houston, TX	5	Research	333445555
Jabbar, Ahmad V.	987987987	1969-03-29	980 Dallas, Houston, TX	4	Administration	987654321
Borg, James E.	888665555	1937-11-10	450 Stone, Houston, TX	1	Headquarters	888665555

### **Examples of FD Constraints**



- Social security number determines employee name
  - SSN  $\rightarrow$  ENAME
- Project number determines project name and location
  - PNUMBER → {PNAME, PLOCATION}
- Employee ssn and project number determine the hours per week that the employee works on the project
  - {SSN, PNUMBER} → HOURS

### **Examples of FD Constraints**

- An FD is a property of the attributes in the schema R
- The constraint must hold on *every* relation instance r(R)
- If K is a key of R, then K functionally determines all attributes in R
  - as we never have two distinct tuples with t1[K]=t2[K]

### What is the Functional Dependency in this example?

#### **TEACH**

Teacher	Course	Text
Smith	Data Structures	Bartram
Smith	Data Management	Martin
Hall	Compilers	Hoffman
Brown	Data Structures	Horowitz

FDs are a property of the meaning of data and hold at all times

Certain FD's can be ruled out based on a given state of the database

### Functional Dependencies in TEACH Database

#### **TEACH**

Course	Text
Data Structures	Bartram
Data Management	Martin
Compilers	Hoffman
Data Structures	Horowitz
	Data Structures  Data Management  Compilers

A relation state of TEACH with a possible functional dependency TEXT → COURSE. However, TEACHER → COURSE is ruled out.

### Inference Rules for FDs (1)

- Given a set of FDs F, we can infer additional FDs that hold whenever the FDs in F hold
- Armstrong's inference rules:
  - IR1. (**Reflexive**) If Y subset-of X, then  $X \rightarrow Y$
  - IR2. (Augmentation) If  $X \rightarrow Y$ , then  $XZ \rightarrow YZ$ 
    - (Notation: XZ stands for X U Z)
  - IR3. (**Transitive**) If  $X \rightarrow Y$  and  $Y \rightarrow Z$ , then  $X \rightarrow Z$
- IR1, IR2, IR3 form a **sound** and **complete** set of inference rules
  - These rules hold and all other rules that hold can be deduced from these

### **Summary**

- Informal Design Guidelines for Relational Databases
- Functional Dependencies (FDs)
  - Definition, Inference Rules
- Next week we discuss:
- Formal rules for normalisation
  - First Normal Form
  - Second Normal Form
  - Third Normal Form
  - BCNF (Boyce-Codd Normal Form)