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<https://arxiv.org/pdf/1904.00360>

Deep learning inter-atomic potential model for accurate irradiation damage simulations

Ziegler-Biersack-Littmark-modified deep learning scheme

System energy:

$$E^{\text{ZBL-DP}} = \sum_i E_i^{\text{ZBL-DP}}$$

The atomic contribution of atom i is fully determined by the coordinates of atom i and its near neighbors:

$$E_i^{\text{ZBL-DP}} = E_{s(i)}^{\text{ZBL-DP}}(\mathbf{R}_i, \{\mathbf{R}_j | j \in \mathcal{N}_{R_c}(i)\})$$

Ziegler-Biersack-Littmark-modified deep learning scheme

The atom contribution of DP-ZBL is the interpolation of the ZBL screened nuclear repulsion potential E_i^{ZBL} and the standard deep potential E_i^{DP}

$$E_i^{\text{ZBL-DP}} = w_i E_i^{\text{ZBL}} + (1 - w_i) E_i^{\text{DP}}$$

$$w_i = \begin{cases} 1 & \sigma_i < R_a, \\ -6u_i^5 + 15u_i^4 - 10u_i^3 + 1 & R_a \leq \sigma_i < R_b \\ 0 & \sigma_i \geq R_b, \end{cases}$$



Ziegler-Biersack-Littmark-modified deep learning scheme

$$u_i = \frac{\sigma_i - R_a}{R_b - R_a}$$

Smooth-minimal distance of atom i 's near neighbors:

$$\sigma_i = \frac{\sum_{j \in \mathcal{N}_{R_c}(i)} R_{ij} e^{-R_{ij}/\alpha}}{\sum_{j \in \mathcal{N}_{R_c}(i)} e^{-R_{ij}/\alpha}},$$

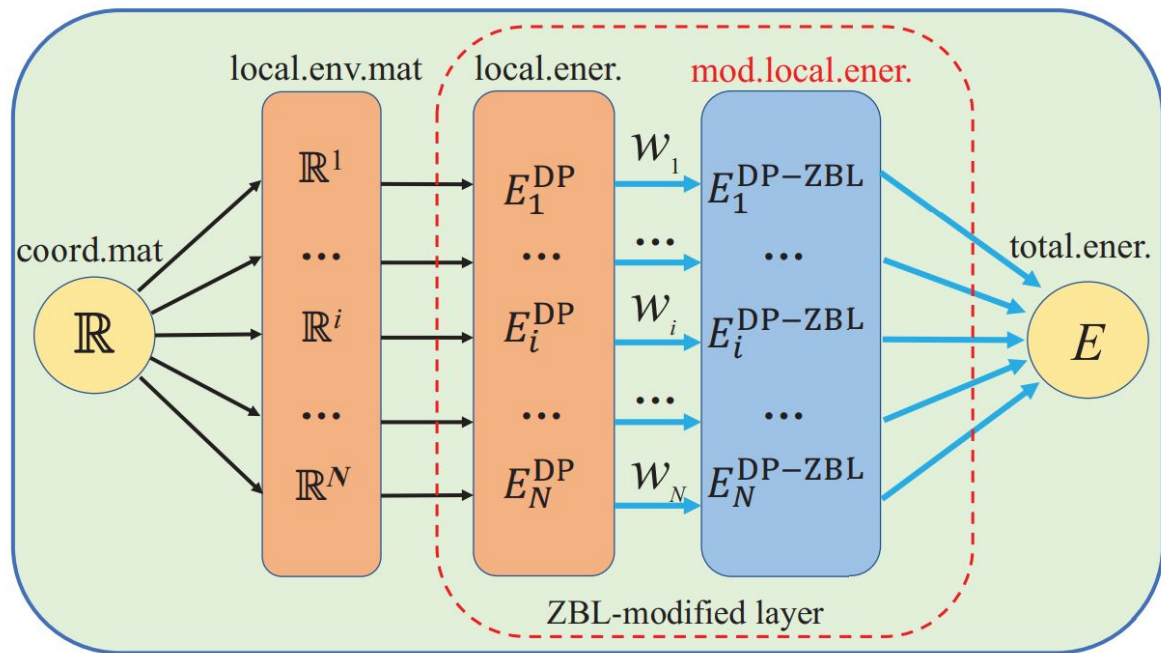


Equilibrium properties of Al

Al ^a	EXP.	DFT	DP-ZBL	DP ²⁴	MEAM-ZBL	EAM-ZBL ^b
E_{am} [eV/atom]	-3.49 ²⁵	-3.75	-3.74	-3.65	-3.36	-3.39
a_0 [Å]	4.04 ²⁶	4.04	4.04	4.04	4.05	4.01
E_{vf} [eV]	0.66 ^{27,28}	0.67 ²⁹	0.73	0.79	0.67	1.14
$E_{if}(oh)$ [eV]	-	2.91 ²⁹	2.57	2.45	3.12	-
$E_{if}(th)$ [eV]	-	3.23 ²⁹	3.23	3.12	3.83	-
C_{11} [GPa]	114.3 ³⁰	111.2	112.8	120.9	113.5	106.9
C_{12} [GPa]	61.9 ³⁰	61.4	57.6	59.6	61.6	81.5
C_{44} [GPa]	31.6 ³⁰	36.8	41.2	40.4	45.4	44.2
B_V [GPa]	79.4 ³⁰	78.0	76.0	80.1	78.9	90.0
G_V [GPa]	29.4 ³⁰	32.1	35.8	36.5	37.6	31.6
γ_{sf} [J/m ²]	0.11-0.21 ³¹⁻³⁴	0.142 ³⁵	0.070	0.132	0.184	-
γ_{tsf} [J/m ²]	-	0.135 ³⁵	0.075	0.130	0.184	-
T_m [K]	935 ³⁶	950(±50) ³⁷	885	918	950	1050
ΔH_f [KJ/mol]	10.7(± 0.2) ³⁸	-	9.3	10.2	11.5	8.8
D [10 ⁻⁹ m ² /s]	7.2-7.9 ³⁹	-	6.8	7.1	4.9	6.8

Atomization energy E_{am} , equilibrium lattice constant a_0 , vacancy formation energy E_{vf} , interstitial formation energy E_{if} for octahedral interstitial (oh) and tetrahedral interstitial (th), independent elastic constant C_{11} , C_{12} , and C_{44} , Bulk modulus B_V (Voigt), shear modulus G_V (Voigt), stacking fault energy γ_{sf} , twin stacking fault energy γ_{tsf} , melt point T_m , enthalpy of fusion ΔH_f and diffusion coefficient D at $T = 1000$ K.

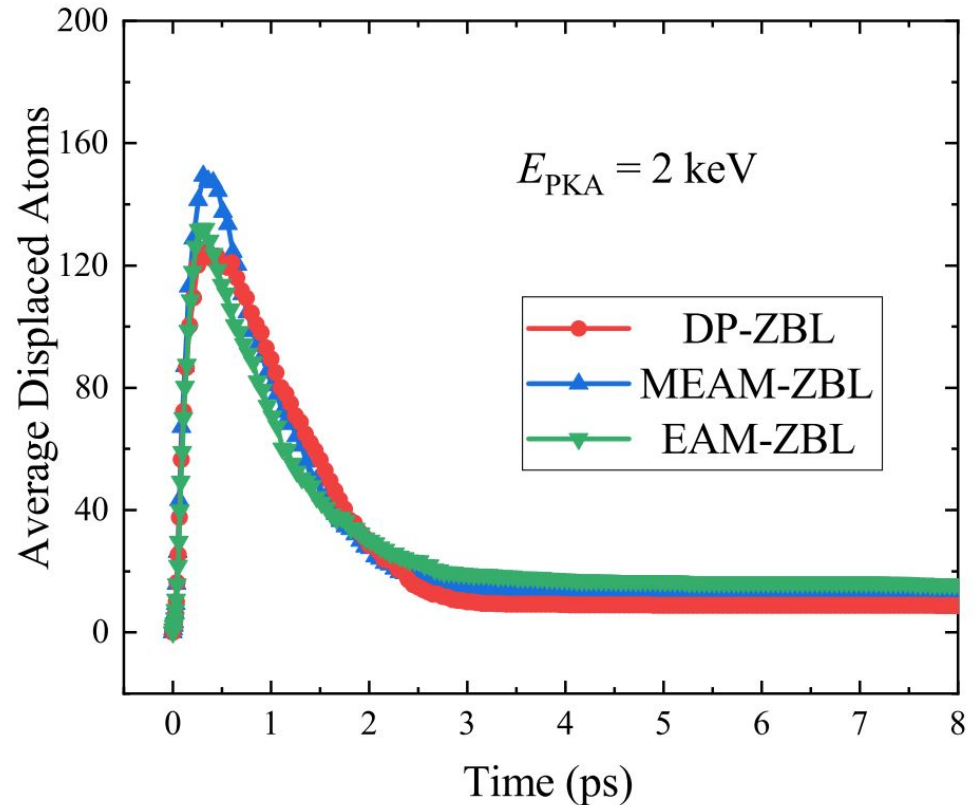
Schematic plot of the DP-ZBL model



Coordinate matrix R to the potential energy E , R is firstly transformed to local environment matrices. Then each R^i is mapped and ZBL-modified layer is added

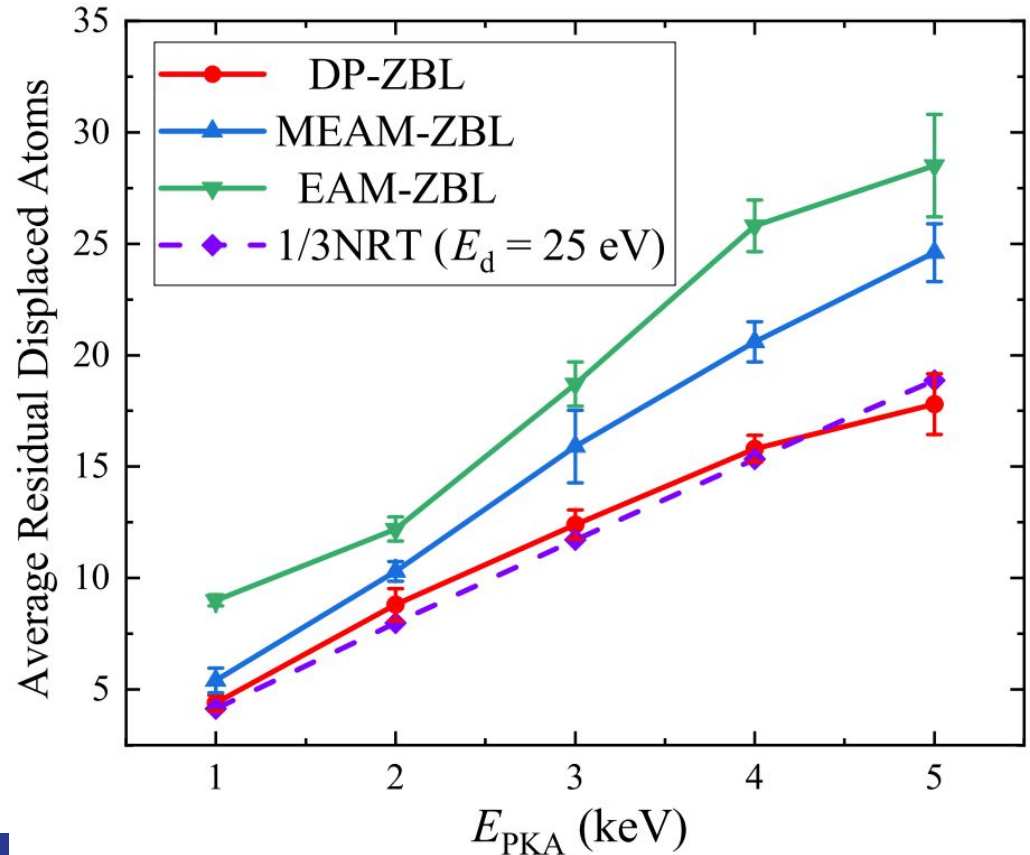
Average displaced atoms

The number of average displaced atoms N_d during the evolution of the collision cascade caused by a 2 keV PKA. Each point is the average of 10 independent 2 keV cascade simulations.



Point defects after 50 ps relaxation

The residual point defects after 50 ps relaxation and the corresponding 1/3 NRT model results. Each point is the average of 10 independent cascade simulations, and the errors are given in the standard error of the mean



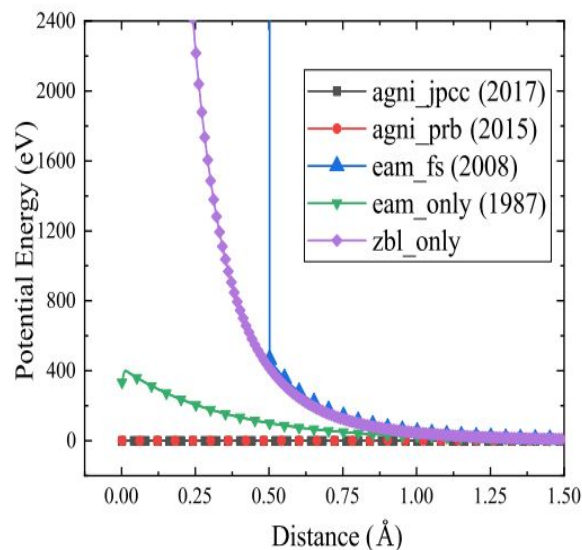
Conclusions

The average displacement threshold energy (E_d) of fcc Al

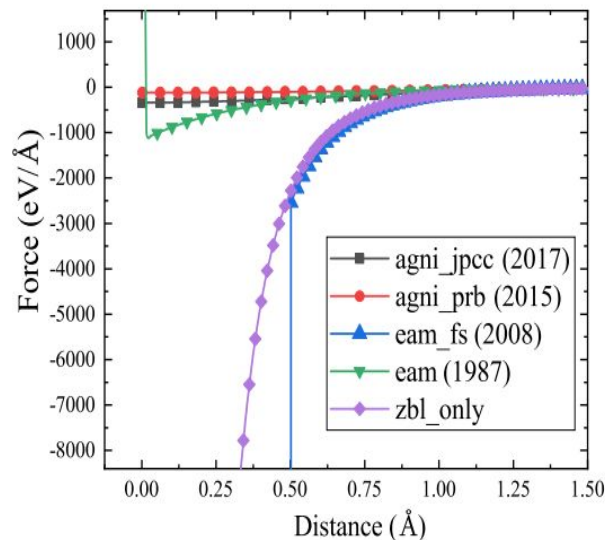
fcc Al	Recommended ⁶⁶	DP-ZBL	MEAM-ZBL	EAM-ZBL
E_d (eV)	25.0	26.54	22.67	16.73

- Proposed DP-ZBL scheme by smoothly interpolating the accurate repulsive pair potential (ZBL) into the DP model
- Not only give accurate results regarding the material properties near equilibrium states but also sufficient to describe the atomic collision cascades during the irradiation damage processes
- Minimize the impact of subjective factors on potentials during their establishments
- May be used in the irradiation effect studies of new advanced materials, such as high entropy alloys, layered transition metal ternary nitrides and carbides, and 2D materials, for whom suitable classical potentials are still lacking

The pair potential (a) and force (b) calculated using two classical potentials (eam and eam.fs) and two machine learning potentials (agni_jpcc and agni_prb). Compared the ZBL repulsive pair potential, all the four potentials cannot give an accurate description about the interatomic interactions below 1 Å.

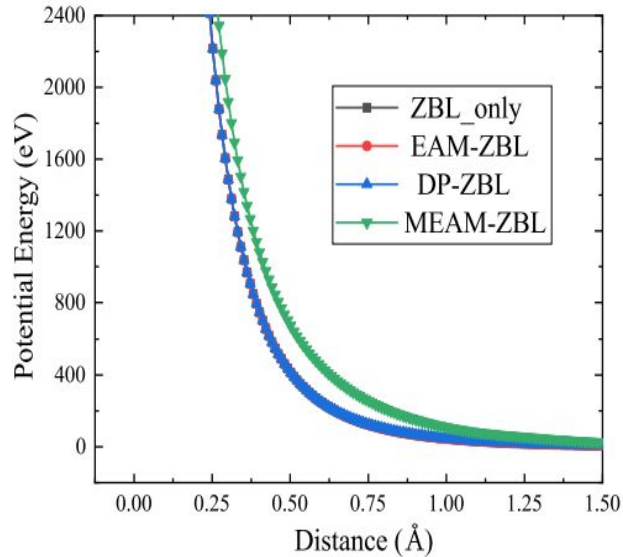


(a)

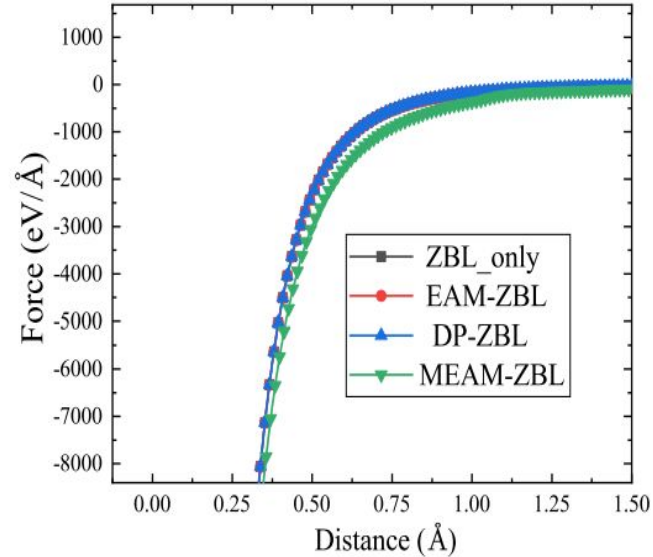


(b)

The pair potential (a) and force (b) calculated using the DP-ZBL, EAM-ZBL and one state-of-art classical potentials MEAM-ZBL. As all these potentials are smoothly transformed into the ZBL repulsive potential at short distance, they are sufficient to describe the interatomic interactions during the cascade simulations.

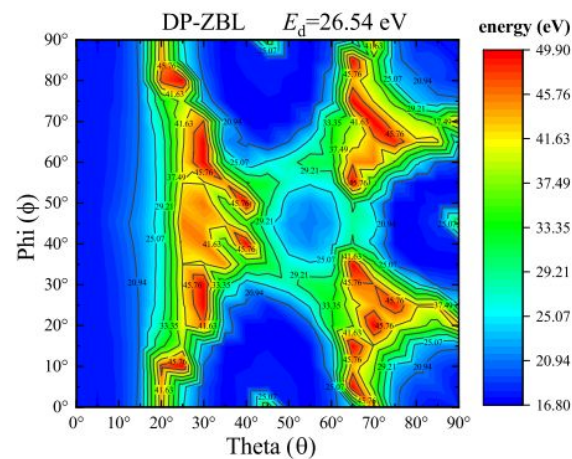


(a)

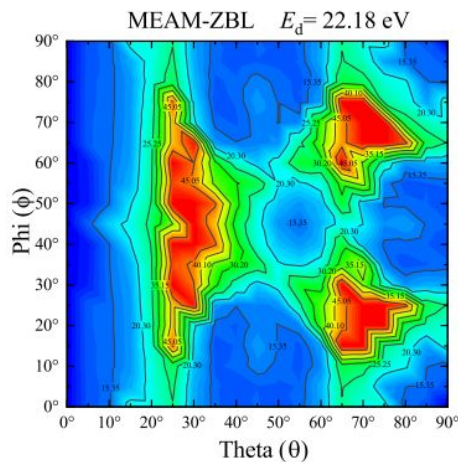


(b)

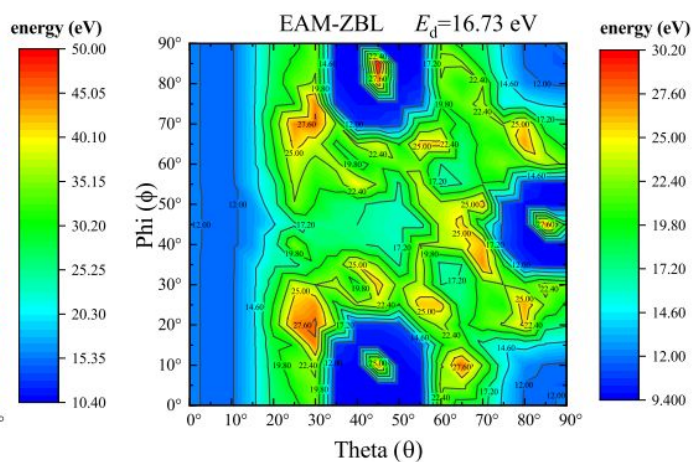
The corresponding $E_d(\theta, \phi)$ calculated using the (a) DP-ZBL, (b) MEAM-ZBL, and (c) MEAM-ZBL potentials. All the three potentials show similar dependence of E_d on the PKA initial direction (θ, ϕ)



(a)

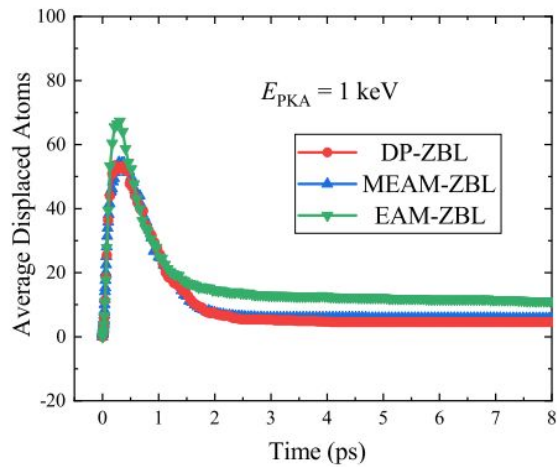


(b)

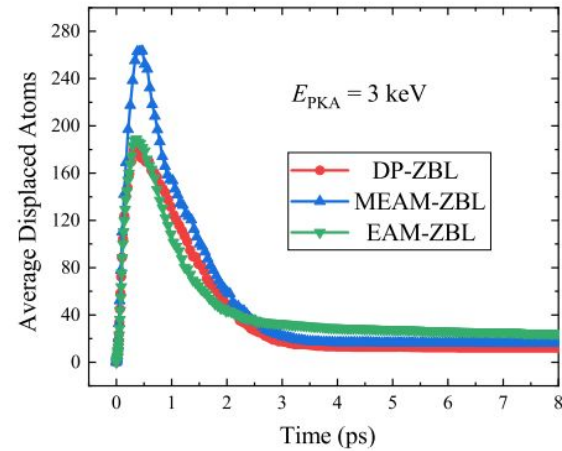


(c)

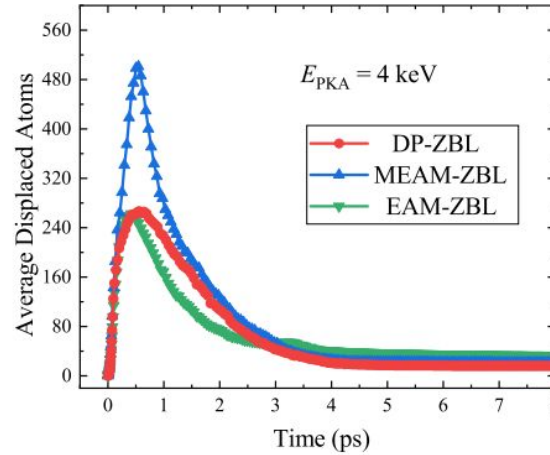
The evolution of average displaced atoms number (N_d) during the cascades events induced by 1 keV(a), 3 keV (b), 4 keV (c) and 5 keV (d) PKAs. Each point is the average of 10 independent simulations.



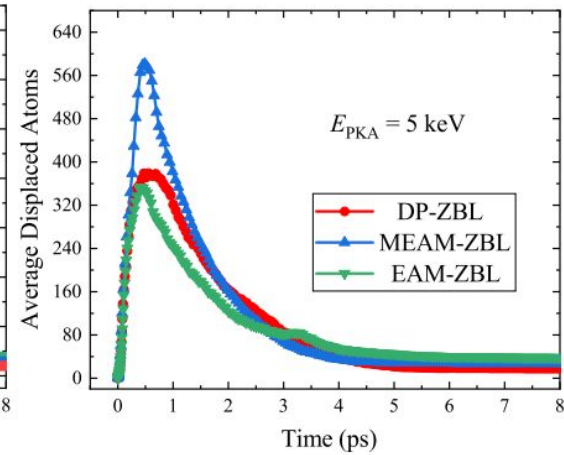
(a)



(b)



(c)



(d)