

SVM

September 26, 2019

1 Multiclass Support Vector Machine exercise

Complete and hand in this completed worksheet (including its outputs and any supporting code outside of the worksheet) with your assignment submission. For more details see the [assignments page](#) on the course website.

In this exercise you will:

- implement a fully-vectorized **loss function** for the SVM
- implement the fully-vectorized expression for its **analytic gradient**
- **check your implementation** using numerical gradient
- use a validation set to **tune the learning rate and regularization strength**
- **optimize** the loss function with **SGD**
- **visualize** the final learned weights

```
[1]: # Run some setup code for this notebook.
from __future__ import print_function
import random
import numpy as np
from cs231n.data_utils import load_CIFAR10
import matplotlib.pyplot as plt

# This is a bit of magic to make matplotlib figures appear inline in the
# notebook rather than in a new window.
%matplotlib inline
plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
plt.rcParams['image.interpolation'] = 'nearest'
plt.rcParams['image.cmap'] = 'gray'

# Some more magic so that the notebook will reload external python modules;
# see http://stackoverflow.com/questions/1907993/
→ autoreload-of-modules-in-ipython
%load_ext autoreload
%autoreload 2
```

1.1 CIFAR-10 Data Loading and Preprocessing

```
[2]: # Load the raw CIFAR-10 data.
cifar10_dir = 'cs231n/datasets/cifar-10-batches-py'

# Cleaning up variables to prevent loading data multiple times (which may cause
→memory issue)
try:
    del X_train, y_train
    del X_test, y_test
    print('Clear previously loaded data.')
except:
    pass

X_train, y_train, X_test, y_test = load_CIFAR10(cifar10_dir)

# As a sanity check, we print out the size of the training and test data.
print('Training data shape: ', X_train.shape)
print('Training labels shape: ', y_train.shape)
print('Test data shape: ', X_test.shape)
print('Test labels shape: ', y_test.shape)
```

Training data shape: (50000, 32, 32, 3)

Training labels shape: (50000,)

Test data shape: (10000, 32, 32, 3)

Test labels shape: (10000,)

```
[3]: # Visualize some examples from the dataset.
# We show a few examples of training images from each class.
classes = ['plane', 'car', 'bird', 'cat', 'deer', 'dog', 'frog', 'horse',
→'ship', 'truck']
num_classes = len(classes)
samples_per_class = 7
for y, cls in enumerate(classes):
    idxs = np.flatnonzero(y_train == y)
    idxs = np.random.choice(idxs, samples_per_class, replace=False)
    for i, idx in enumerate(idxs):
        plt_idx = i * num_classes + y + 1
        plt.subplot(samples_per_class, num_classes, plt_idx)
        plt.imshow(X_train[idx].astype('uint8'))
        plt.axis('off')
        if i == 0:
            plt.title(cls)
plt.show()
```



```
[4]: # Split the data into train, val, and test sets. In addition we will
# create a small development set as a subset of the training data;
# we can use this for development so our code runs faster.
num_training = 49000
num_validation = 1000
num_test = 1000
num_dev = 500

# Our validation set will be num_validation points from the original
# training set.
mask = range(num_training, num_training + num_validation)
X_val = X_train[mask]
y_val = y_train[mask]

# Our training set will be the first num_train points from the original
# training set.
mask = range(num_training)
X_train = X_train[mask]
y_train = y_train[mask]

# We will also make a development set, which is a small subset of
# the training set.
mask = np.random.choice(num_training, num_dev, replace=False)
X_dev = X_train[mask]
y_dev = y_train[mask]
```

```

# We use the first num_test points of the original test set as our
# test set.
mask = range(num_test)
X_test = X_test[mask]
y_test = y_test[mask]

print('Train data shape: ', X_train.shape)
print('Train labels shape: ', y_train.shape)
print('Validation data shape: ', X_val.shape)
print('Validation labels shape: ', y_val.shape)
print('Test data shape: ', X_test.shape)
print('Test labels shape: ', y_test.shape)

```

```

Train data shape: (49000, 32, 32, 3)
Train labels shape: (49000,)
Validation data shape: (1000, 32, 32, 3)
Validation labels shape: (1000,)
Test data shape: (1000, 32, 32, 3)
Test labels shape: (1000,)

```

```

[5]: # Preprocessing: reshape the image data into rows
X_train = np.reshape(X_train, (X_train.shape[0], -1))
X_val = np.reshape(X_val, (X_val.shape[0], -1))
X_test = np.reshape(X_test, (X_test.shape[0], -1))
X_dev = np.reshape(X_dev, (X_dev.shape[0], -1))

# As a sanity check, print out the shapes of the data
print('Training data shape: ', X_train.shape)
print('Validation data shape: ', X_val.shape)
print('Test data shape: ', X_test.shape)
print('dev data shape: ', X_dev.shape)

```

```

Training data shape: (49000, 3072)
Validation data shape: (1000, 3072)
Test data shape: (1000, 3072)
dev data shape: (500, 3072)

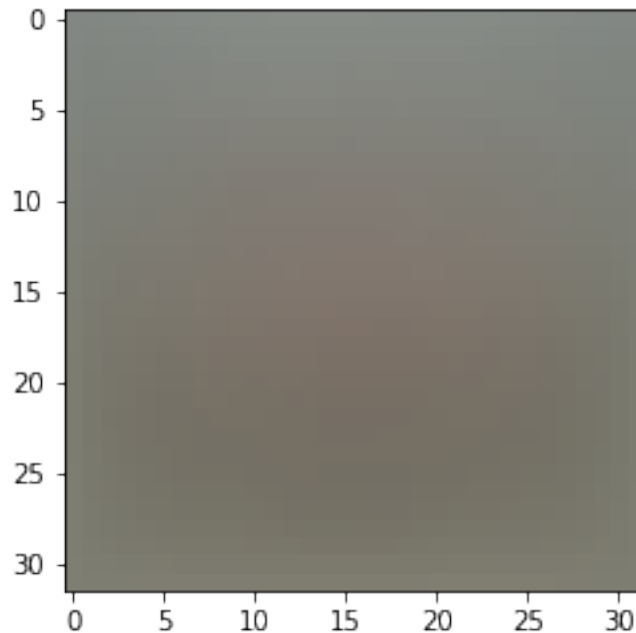
```

```

[6]: # Preprocessing: subtract the mean image
# first: compute the image mean based on the training data
mean_image = np.mean(X_train, axis=0)
print(mean_image[:10]) # print a few of the elements
plt.figure(figsize=(4,4))
plt.imshow(mean_image.reshape((32,32,3)).astype('uint8')) # visualize the mean_
    →image
plt.show()

```

```
[130.64189796 135.98173469 132.47391837 130.05569388 135.34804082
131.75402041 130.96055102 136.14328571 132.47636735 131.48467347]
```



```
[7]: # second: subtract the mean image from train and test data
X_train -= mean_image
X_val -= mean_image
X_test -= mean_image
X_dev -= mean_image

[8]: # third: append the bias dimension of ones (i.e. bias trick) so that our SVM
# only has to worry about optimizing a single weight matrix W.
X_train = np.hstack([X_train, np.ones((X_train.shape[0], 1))])
X_val = np.hstack([X_val, np.ones((X_val.shape[0], 1))])
X_test = np.hstack([X_test, np.ones((X_test.shape[0], 1))])
X_dev = np.hstack([X_dev, np.ones((X_dev.shape[0], 1))])

print(X_train.shape, X_val.shape, X_test.shape, X_dev.shape)
```

```
(49000, 3073) (1000, 3073) (1000, 3073) (500, 3073)
```

SVM Classifier

Your code for this section will all be written inside **cs231n/classifiers/linear_svm.py**.

As you can see, we have prefilled the function `compute_loss_naive` which uses for loops to evaluate the multiclass SVM loss function.

```
[9]: # Evaluate the naive implementation of the loss we provided for you:
from cs231n.classifiers.linear_svm import svm_loss_naive
import time
```

```

# generate a random SVM weight matrix of small numbers
W = np.random.randn(3073, 10) * 0.0001

loss, grad = svm_loss_naive(W, X_dev, y_dev, 0.000005)
print('loss: %f' % (loss, ))

```

loss: 8.626918

```

[10]: # Once you've implemented the gradient, recompute it with the code below
# and gradient check it with the function we provided for you

# Compute the loss and its gradient at W.
loss, grad = svm_loss_naive(W, X_dev, y_dev, 0.0)

# Numerically compute the gradient along several randomly chosen dimensions,
→and
# compare them with your analytically computed gradient. The numbers should
→match
# almost exactly along all dimensions.
from cs231n.gradient_check import grad_check_sparse
f = lambda w: svm_loss_naive(w, X_dev, y_dev, 0.0)[0]
grad_numerical = grad_check_sparse(f, W, grad)

# do the gradient check once again with regularization turned on
# you didn't forget the regularization gradient did you?
loss, grad = svm_loss_naive(W, X_dev, y_dev, 5e1)
f = lambda w: svm_loss_naive(w, X_dev, y_dev, 5e1)[0]
grad_numerical = grad_check_sparse(f, W, grad)

```

```

numerical: -2.466045 analytic: -2.466045, relative error: 2.284785e-11
numerical: 10.575842 analytic: 10.575842, relative error: 2.319544e-11
numerical: -6.360583 analytic: -6.401714, relative error: 3.222871e-03
numerical: 21.351136 analytic: 21.284421, relative error: 1.564769e-03
numerical: 5.297930 analytic: 5.297930, relative error: 5.169709e-11
numerical: 17.994630 analytic: 17.994630, relative error: 1.500532e-11
numerical: -32.992205 analytic: -33.027777, relative error: 5.388037e-04
numerical: 30.315390 analytic: 30.315390, relative error: 7.382201e-12
numerical: -60.022741 analytic: -60.022741, relative error: 4.939124e-12
numerical: -13.588838 analytic: -13.588838, relative error: 9.653802e-12
numerical: 24.819762 analytic: 24.819762, relative error: 1.551701e-11
numerical: -15.917253 analytic: -15.976813, relative error: 1.867415e-03
numerical: 20.092738 analytic: 20.092738, relative error: 1.494005e-12
numerical: 22.969695 analytic: 22.969695, relative error: 2.299550e-11
numerical: -2.734993 analytic: -2.734993, relative error: 3.560354e-11
numerical: 9.010931 analytic: 9.010931, relative error: 3.209719e-11
numerical: -6.168198 analytic: -6.153158, relative error: 1.220618e-03

```

numerical: -13.052581 analytic: -13.052581, relative error: 4.387686e-12
numerical: -2.635361 analytic: -2.635361, relative error: 7.058282e-12
numerical: 3.674104 analytic: 3.674104, relative error: 1.035452e-11

```
[12]: # Next implement the function svm_loss_vectorized; for now only compute the
      ↪ loss;
      # we will implement the gradient in a moment.
      tic = time.time()
      loss_naive, grad_naive = svm_loss_naive(W, X_dev, y_dev, 0.000005)
      toc = time.time()
      print('Naive loss: %e computed in %fs' % (loss_naive, toc - tic))

      from cs231n.classifiers.linear_svm import svm_loss_vectorized
      tic = time.time()
      loss_vectorized, _ = svm_loss_vectorized(W, X_dev, y_dev, 0.000005)
      toc = time.time()
      print('Vectorized loss: %e computed in %fs' % (loss_vectorized, toc - tic))

      # The losses should match but your vectorized implementation should be much
      ↪ faster.
      print('difference: %f' % (loss_naive - loss_vectorized))
```

Naive loss: 8.626918e+00 computed in 0.124000s
Vectorized loss: 8.626918e+00 computed in 0.005000s
difference: -0.000000

```
[13]: # Complete the implementation of svm_loss_vectorized, and compute the gradient
      # of the loss function in a vectorized way.

      # The naive implementation and the vectorized implementation should match, but
      # the vectorized version should still be much faster.
      tic = time.time()
      _, grad_naive = svm_loss_naive(W, X_dev, y_dev, 0.000005)
      toc = time.time()
      print('Naive loss and gradient: computed in %fs' % (toc - tic))

      tic = time.time()
      _, grad_vectorized = svm_loss_vectorized(W, X_dev, y_dev, 0.000005)
      toc = time.time()
      print('Vectorized loss and gradient: computed in %fs' % (toc - tic))

      # The loss is a single number, so it is easy to compare the values computed
      # by the two implementations. The gradient on the other hand is a matrix, so
      # we use the Frobenius norm to compare them.
      difference = np.linalg.norm(grad_naive - grad_vectorized, ord='fro')
      print('difference: %f' % difference)
```

Naive loss and gradient: computed in 0.116000s
Vectorized loss and gradient: computed in 0.008000s
difference: 0.000000

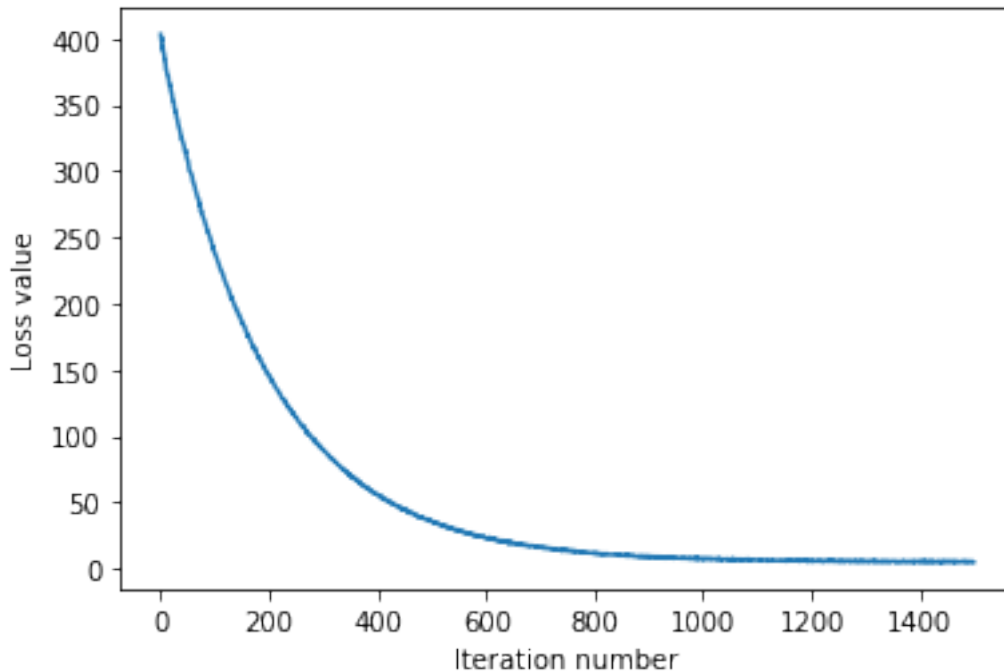
1.1.1 Stochastic Gradient Descent

We now have vectorized and efficient expressions for the loss, the gradient and our gradient matches the numerical gradient. We are therefore ready to do SGD to minimize the loss.

```
[14]: # In the file linear_classifier.py, implement SGD in the function  
# LinearClassifier.train() and then run it with the code below.  
from cs231n.classifiers import LinearSVM  
svm = LinearSVM()  
tic = time.time()  
loss_hist = svm.train(X_train, y_train, learning_rate=1e-7, reg=2.5e4,  
                      num_iters=1500, verbose=True)  
toc = time.time()  
print('That took %fs' % (toc - tic))
```

```
iteration 0 / 1500: loss 403.082491  
iteration 100 / 1500: loss 237.495896  
iteration 200 / 1500: loss 146.260797  
iteration 300 / 1500: loss 89.343949  
iteration 400 / 1500: loss 55.717256  
iteration 500 / 1500: loss 35.624431  
iteration 600 / 1500: loss 22.926838  
iteration 700 / 1500: loss 16.313279  
iteration 800 / 1500: loss 12.210786  
iteration 900 / 1500: loss 9.032064  
iteration 1000 / 1500: loss 7.752169  
iteration 1100 / 1500: loss 6.696593  
iteration 1200 / 1500: loss 6.115931  
iteration 1300 / 1500: loss 5.817259  
iteration 1400 / 1500: loss 5.229668  
That took 9.413000s
```

```
[15]: # A useful debugging strategy is to plot the loss as a function of  
# iteration number:  
plt.plot(loss_hist)  
plt.xlabel('Iteration number')  
plt.ylabel('Loss value')  
plt.show()
```

```
[16]: # Write the LinearSVM.predict function and evaluate the performance on both the
# training and validation set
y_train_pred = svm.predict(X_train)
print('training accuracy: %f' % (np.mean(y_train == y_train_pred), ))
y_val_pred = svm.predict(X_val)
print('validation accuracy: %f' % (np.mean(y_val == y_val_pred), ))
```

```
training accuracy: 0.379857
validation accuracy: 0.404000
```

```
[17]: # Use the validation set to tune hyperparameters (regularization strength and
# learning rate). You should experiment with different ranges for the learning
# rates and regularization strengths; if you are careful you should be able to
# get a classification accuracy of about 0.4 on the validation set.
learning_rates = [1e-7, 5e-5]
regularization_strengths = [2.5e4, 5e4]

# results is dictionary mapping tuples of the form
# (learning_rate, regularization_strength) to tuples of the form
# (training_accuracy, validation_accuracy). The accuracy is simply the fraction
# of data points that are correctly classified.
results = {}
best_val = -1 # The highest validation accuracy that we have seen so far.
best_svm = None # The LinearSVM object that achieved the highest validation
→rate.
```

[illegible]

```
#####

for lr, reg in sorted(results):
    train_accuracy, val_accuracy = results[(lr, reg)]
    print ('lr %e reg %e train accuracy: %f val accuracy: %f' % (
        lr, reg, train_accuracy, val_accuracy))

print ('best validation accuracy achieved during cross-validation: %f' %
    ↪best_val)
```

```
C:\Users\Lavender\Downloads\spring1718_assignment1\assignment1\cs231n\classifier
s\linear_svm.py:90: RuntimeWarning: overflow encountered in double_scalars
    loss += 0.5 * reg * np.sum(W * W)
C:\Users\Lavender\Anaconda3\lib\site-packages\numpy\core\fromnumeric.py:86:
RuntimeWarning: overflow encountered in reduce
    return ufunc.reduce(obj, axis, dtype, out, **passkwargs)
C:\Users\Lavender\Downloads\spring1718_assignment1\assignment1\cs231n\classifier
s\linear_svm.py:90: RuntimeWarning: overflow encountered in multiply
    loss += 0.5 * reg * np.sum(W * W)

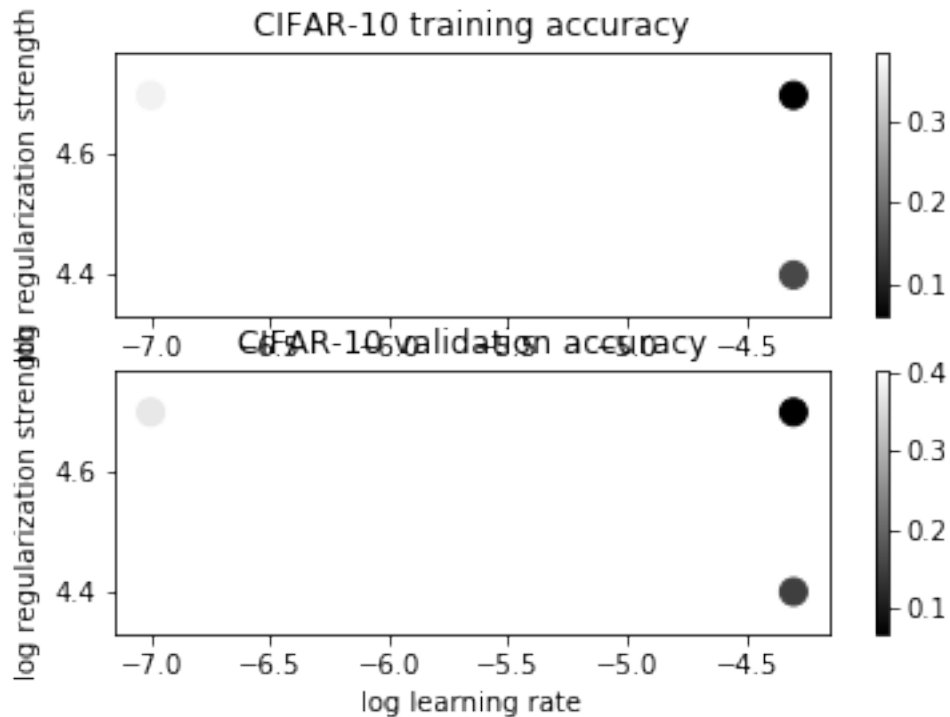
lr 1.000000e-07 reg 2.500000e+04 train accuracy: 0.382449 val accuracy: 0.402000
lr 1.000000e-07 reg 5.000000e+04 train accuracy: 0.365898 val accuracy: 0.371000
lr 5.000000e-05 reg 2.500000e+04 train accuracy: 0.151735 val accuracy: 0.151000
lr 5.000000e-05 reg 5.000000e+04 train accuracy: 0.059959 val accuracy: 0.068000
best validation accuracy achieved during cross-validation: 0.402000
```

```
[19]: # Visualize the cross-validation results
import math
x_scatter = [math.log10(x[0]) for x in results]
y_scatter = [math.log10(x[1]) for x in results]

# plot training accuracy
marker_size = 100
colors = [results[x][0] for x in results]
plt.subplot(2, 1, 1)
plt.scatter(x_scatter, y_scatter, marker_size, c=colors)
plt.colorbar()
plt.xlabel('log learning rate')
plt.ylabel('log regularization strength')
plt.title('CIFAR-10 training accuracy')

# plot validation accuracy
colors = [results[x][1] for x in results] # default size of markers is 20
plt.subplot(2, 1, 2)
plt.scatter(x_scatter, y_scatter, marker_size, c=colors)
plt.colorbar()
plt.xlabel('log learning rate')
```

```
plt.ylabel('log regularization strength')
plt.title('CIFAR-10 validation accuracy')
plt.show()
```



```
[20]: # Evaluate the best svm on test set
y_test_pred = best_svm.predict(X_test)
test_accuracy = np.mean(y_test == y_test_pred)
print('linear SVM on raw pixels final test set accuracy: %f' % test_accuracy)
```

linear SVM on raw pixels final test set accuracy: 0.370000

```
[21]: # Visualize the learned weights for each class.
# Depending on your choice of learning rate and regularization strength, these
→ may
# or may not be nice to look at.
w = best_svm.W[:-1,:] # strip out the bias
w = w.reshape(32, 32, 3, 10)
w_min, w_max = np.min(w), np.max(w)
classes = ['plane', 'car', 'bird', 'cat', 'deer', 'dog', 'frog', 'horse',
→ 'ship', 'truck']
for i in range(10):
    plt.subplot(2, 5, i + 1)
```

```
# Rescale the weights to be between 0 and 255  
wing = 255.0 * (w[:, :, :, i].squeeze() - w_min) / (w_max - w_min)  
plt.imshow(wing.astype('uint8'))  
plt.axis('off')  
plt.title(classes[i])
```

