# features

October 25, 2019

# 1 Image features exercise

Complete and hand in this completed worksheet (including its outputs and any supporting code outside of the worksheet) with your assignment submission. For more details see the assignments page on the course website.

We have seen that we can achieve reasonable performance on an image classification task by training a linear classifier on the pixels of the input image. In this exercise we will show that we can improve our classification performance by training linear classifiers not on raw pixels but on features that are computed from the raw pixels.

All of your work for this exercise will be done in this notebook.

#### 1.1 Load data

Similar to previous exercises, we will load CIFAR-10 data from disk.

```
[5]: from cs231n.features import color_histogram_hsv, hog_feature

def get_CIFAR10_data(num_training=49000, num_validation=1000, num_test=1000):
    # Load the raw CIFAR-10 data
    cifar10_dir = 'cs231n/datasets/cifar-10-batches-py'
```

```
X_train, y_train, X_test, y_test = load_CIFAR10(cifar10_dir)
    # Subsample the data
    mask = list(range(num_training, num_training + num_validation))
    X_val = X_train[mask]
    y_val = y_train[mask]
    mask = list(range(num_training))
    X_train = X_train[mask]
    y_train = y_train[mask]
    mask = list(range(num test))
    X_{test} = X_{test}[mask]
    y_test = y_test[mask]
    return X_train, y_train, X_val, y_val, X_test, y_test
# Cleaning up variables to prevent loading data multiple times (which may cause,
→memory issue)
try:
  del X_train, y_train
  del X test, y test
  print('Clear previously loaded data.')
except:
  pass
X_train, y_train, X_val, y_val, X_test, y_test = get_CIFAR10_data()
```

# 1.2 Extract Features

For each image we will compute a Histogram of Oriented Gradients (HOG) as well as a color histogram using the hue channel in HSV color space. We form our final feature vector for each image by concatenating the HOG and color histogram feature vectors.

Roughly speaking, HOG should capture the texture of the image while ignoring color information, and the color histogram represents the color of the input image while ignoring texture. As a result, we expect that using both together ought to work better than using either alone. Verifying this assumption would be a good thing to try for your interests.

The hog\_feature and color\_histogram\_hsv functions both operate on a single image and return a feature vector for that image. The extract\_features function takes a set of images and a list of feature functions and evaluates each feature function on each image, storing the results in a matrix where each column is the concatenation of all feature vectors for a single image.

```
X_train_feats = extract_features(X_train, feature_fns, verbose=True)
X_val_feats = extract_features(X_val, feature_fns)
X_test_feats = extract_features(X_test, feature_fns)
# Preprocessing: Subtract the mean feature
mean_feat = np.mean(X_train_feats, axis=0, keepdims=True)
X_train_feats -= mean_feat
X_val_feats -= mean_feat
X_test_feats -= mean_feat
# Preprocessing: Divide by standard deviation. This ensures that each feature
# has roughly the same scale.
std_feat = np.std(X_train_feats, axis=0, keepdims=True)
X_train_feats /= std_feat
X_val_feats /= std_feat
X_test_feats /= std_feat
# Preprocessing: Add a bias dimension
X_train_feats = np.hstack([X_train_feats, np.ones((X_train_feats.shape[0], 1))])
X_val_feats = np.hstack([X_val_feats, np.ones((X_val_feats.shape[0], 1))])
X_test_feats = np.hstack([X_test_feats, np.ones((X_test_feats.shape[0], 1))])
```

```
Done extracting features for 1000 / 49000 images
Done extracting features for 2000 / 49000 images
Done extracting features for 3000 / 49000 images
Done extracting features for 4000 / 49000 images
Done extracting features for 5000 / 49000 images
Done extracting features for 6000 / 49000 images
Done extracting features for 7000 / 49000 images
Done extracting features for 8000 / 49000 images
Done extracting features for 9000 / 49000 images
Done extracting features for 10000 / 49000 images
Done extracting features for 11000 / 49000 images
Done extracting features for 12000 / 49000 images
Done extracting features for 13000 / 49000 images
Done extracting features for 14000 / 49000 images
Done extracting features for 15000 / 49000 images
Done extracting features for 16000 / 49000 images
Done extracting features for 17000 / 49000 images
Done extracting features for 18000 / 49000 images
Done extracting features for 19000 / 49000 images
Done extracting features for 20000 / 49000 images
Done extracting features for 21000 / 49000 images
Done extracting features for 22000 / 49000 images
Done extracting features for 23000 / 49000 images
Done extracting features for 24000 / 49000 images
Done extracting features for 25000 / 49000 images
```

```
Done extracting features for 26000 / 49000 images
Done extracting features for 27000 / 49000 images
Done extracting features for 28000 / 49000 images
Done extracting features for 29000 / 49000 images
Done extracting features for 30000 / 49000 images
Done extracting features for 31000 / 49000 images
Done extracting features for 32000 / 49000 images
Done extracting features for 33000 / 49000 images
Done extracting features for 34000 / 49000 images
Done extracting features for 35000 / 49000 images
Done extracting features for 36000 / 49000 images
Done extracting features for 37000 / 49000 images
Done extracting features for 38000 / 49000 images
Done extracting features for 39000 / 49000 images
Done extracting features for 40000 / 49000 images
Done extracting features for 41000 / 49000 images
Done extracting features for 42000 / 49000 images
Done extracting features for 43000 / 49000 images
Done extracting features for 44000 / 49000 images
Done extracting features for 45000 / 49000 images
Done extracting features for 46000 / 49000 images
Done extracting features for 47000 / 49000 images
Done extracting features for 48000 / 49000 images
```

#### 1.3 Train SVM on features

Using the multiclass SVM code developed earlier in the assignment, train SVMs on top of the features extracted above; this should achieve better results than training SVMs directly on top of raw pixels.

```
[12]: # Use the validation set to tune the learning rate and regularization strength
     from cs231n.classifiers.linear_classifier import LinearSVM
     learning_rates = [1e-8, 1e-7]
     regularization_strengths = [3e4, 5e5, 5e6]
     results = {}
     best_val = -1
     best_svm = None
     # TODO:
     # Use the validation set to set the learning rate and regularization strength.
     # This should be identical to the validation that you did for the SVM; save
     # the best trained classifer in best_sum. You might also want to play
                                                                            #
     # with different numbers of bins in the color histogram. If you are careful
                                                                            #
     # you should be able to get accuracy of near 0.44 on the validation set.
                                                                            #
```

```
print("X_train shape: {}".format(X_train.shape))
print("X_train_feats shape: {}\n".format(X_train_feats.shape))
num_iters = 2000
num_combs = len(learning_rates) * len(regularization_strengths)
progress = 0
print("Training:")
for lr in learning rates:
   for reg in regularization_strengths:
      print("Progress: {}/{} (LR: {:.3e}, reg: {})".format(progress,
→num_combs, lr, int(reg)))
      # Train
      svm = LinearSVM()
      loss_hist = svm.train(X_train_feats, y_train, learning_rate=lr, reg=reg,
                         num_iters=num_iters, verbose=False)
      # Predict
      y_train_pred = svm.predict(X_train_feats)
      y_val_pred = svm.predict(X_val_feats)
      # Evaluate
      acc train = np.mean(y train == y train pred)
      acc val = np.mean(y val == y val pred)
      # Best value and SVM
      if acc_val > best_val:
          best_val = acc_val
          best_svm = svm
      # Save results
      results[(lr, reg)] = (acc_train, acc_val)
      progress += 1
print("Done training.")
END OF YOUR CODE
# Print out results.
for lr, reg in sorted(results):
   train_accuracy, val_accuracy = results[(lr, reg)]
   print('lr %e reg %e train accuracy: %f val accuracy: %f' % (
             lr, reg, train_accuracy, val_accuracy))
print('best validation accuracy achieved during cross-validation: %f' %u
→best_val)
```

X\_train shape: (49000, 32, 32, 3)
X\_train feats shape: (49000, 155)

Training:

```
Progress: 0/6 (LR: 1.000e-08, reg: 30000)
Progress: 1/6 (LR: 1.000e-08, reg: 500000)
Progress: 2/6 (LR: 1.000e-08, reg: 5000000)
Progress: 3/6 (LR: 1.000e-07, reg: 30000)
Progress: 4/6 (LR: 1.000e-07, reg: 500000)
Progress: 5/6 (LR: 1.000e-07, reg: 500000)
Done training.
lr 1.000000e-08 reg 3.000000e+04 train accuracy: 0.097980 val accuracy: 0.088000 lr 1.000000e-08 reg 5.000000e+05 train accuracy: 0.415653 val accuracy: 0.423000 lr 1.000000e-07 reg 3.000000e+06 train accuracy: 0.404551 val accuracy: 0.399000 lr 1.000000e-07 reg 5.000000e+04 train accuracy: 0.406143 val accuracy: 0.402000 lr 1.000000e-07 reg 5.000000e+05 train accuracy: 0.409265 val accuracy: 0.413000 lr 1.000000e-07 reg 5.000000e+06 train accuracy: 0.370980 val accuracy: 0.345000 best validation accuracy achieved during cross-validation: 0.423000
```

```
[13]: # Evaluate your trained SVM on the test set
y_test_pred = best_svm.predict(X_test_feats)
test_accuracy = np.mean(y_test == y_test_pred)
print(test_accuracy)
```

#### 0.414

```
[14]: # An important way to gain intuition about how an algorithm works is to
      # visualize the mistakes that it makes. In this visualization, we show examples
      # of images that are misclassified by our current system. The first column
      # shows images that our system labeled as "plane" but whose true label is
      # something other than "plane".
     examples_per_class = 8
     classes = ['plane', 'car', 'bird', 'cat', 'deer', 'dog', 'frog', 'horse', _
      for cls, cls_name in enumerate(classes):
         idxs = np.where((y_test != cls) & (y_test_pred == cls))[0]
         idxs = np.random.choice(idxs, examples_per_class, replace=False)
         for i, idx in enumerate(idxs):
             plt.subplot(examples_per_class, len(classes), i * len(classes) + cls + u
      →1)
             plt.imshow(X_test[idx].astype('uint8'))
             plt.axis('off')
             if i == 0:
                 plt.title(cls_name)
     plt.show()
```

## 1.3.1 Inline question 1:

Describe the misclassification results that you see. Do they make sense?

## 1.4 Neural Network on image features

Earlier in this assignment we saw that training a two-layer neural network on raw pixels achieved better classification performance than linear classifiers on raw pixels. In this notebook we have seen that linear classifiers on image features outperform linear classifiers on raw pixels.

For completeness, we should also try training a neural network on image features. This approach should outperform all previous approaches: you should easily be able to achieve over 55% classification accuracy on the test set; our best model achieves about 60% classification accuracy.

```
[15]: # Preprocessing: Remove the bias dimension
    # Make sure to run this cell only ONCE
    print(X_train_feats.shape)
    X_train_feats = X_train_feats[:, :-1]
    X_val_feats = X_val_feats[:, :-1]
    X_test_feats = X_test_feats[:, :-1]
    print(X_train_feats.shape)
```

```
(49000, 155)
(49000, 154)
```

```
[18]: from cs231n.classifiers.neural_net import TwoLayerNet
    input_dim = X_train_feats.shape[1]
    hidden_dim = 500
    num classes = 10
    #net = TwoLayerNet(input_dim, hidden_dim, num_classes) # Not needed
    best_net = None
    # TODO: Train a two-layer neural network on image features. You may want to
    # cross-validate various parameters as in previous sections. Store your best
    # model in the best net variable.
    batch_size = 200
    num_epochs = 7
    num_iters = batch_size * num_epochs
    best_val = -1
    best_hyps = {}
    results
            = {}
    progress = 1
    # Hyperparameters generation function
    def hyperparameters(gen_fns, fn_args, num):
        """Hyperparameter generator.
        Args:
           gen_fns: Generator functions
           fn_args: Arguments of gen_fns
           num: Number of iterations
        Returns:
           Tuple of hyperparameters
        for _ in range(num):
           yield tuple(fn(*params) for (fn, params) in zip(gen_fns, fn_args))
    lr dec = 0.95
                     # This one is set
    hsize = hidden_dim # This one is set
    # Coarse search
    print("Coarse search")
    print("----")
    learn_rates = np.logspace(-3, 0, 3)
    reg_strengths = np.logspace(-3, 0, 3)
```

```
num = len(learn_rates) * len(reg_strengths)
import itertools
for lr, reg in itertools.product(learn_rates, reg_strengths):
   # Info
   print("Progress: {}/{} (lr: {:.3e}, lr_dec: {:.2f}, reg: {:.3e}, hsize: {})"
             .format(progress, num, lr, lr_dec, reg, int(hsize)))
    # Train
   net = TwoLayerNet(input_dim, hsize, num_classes)
   train_hist = net.train(X_train_feats, y_train, X_val_feats, y_val,
                         learning rate=lr, learning rate decay=lr dec,
→reg=reg, num_iters=num_iters,
                         batch_size=batch_size, verbose=False)
   # Predict
   acc_val = (net.predict(X_val_feats) == y_val).mean()
   acc_train = (net.predict(X_train_feats) == y_train).mean()
   print("prediction accuracy - train: {:.3f} | val: {:.3f}".format(acc_train, __
→acc_val))
   # Choose best network
   if acc_val > best_val:
       best_val = acc_val
       best_hyps = {'lr': lr, 'lr_dec': lr_dec, 'reg': reg, 'hsize': hsize}
       best_net = net
   results[(lr, lr_dec, reg, hsize)] = (acc_train, acc_val)
   progress += 1
print("Done training.\n")
# Best validation results
print("Best validation accuracy: {} ".format(best_val))
print("Hyperparameters: {}\n".format(best_hyps))
# Fine search (random instead of grid search, random values in focused ranges)
print("Fine search")
print("----")
lr\_range = (-0.1, -1.0) # Best seems to be around 10^0
reg_range = (-3.5, -1.75) # Best seems to be around 10^-3 towards 10^-1.5
# random generation functions
lr_fn = reg_fn = lambda x,y: 10**np.random.uniform(x,y)
# number of combinations
num = 20
progress = 1
results = {}
for lr, reg in hyperparameters((lr_fn, reg_fn), (lr_range, reg_range), num):
    # Info
   print("Progress: {}/{} (lr: {:.3e}, lr_dec: {:.2f}, reg: {:.3e}, hsize: {})"
```

```
.format(progress, num, lr, lr_dec, reg, int(hsize)))
    # Train
    net = TwoLayerNet(input_dim, hsize, num_classes)
    train_hist = net.train(X_train_feats, y_train, X_val_feats, y_val,
                         learning_rate=lr, learning_rate_decay=lr_dec,__
 →reg=reg, num_iters=num_iters,
                         batch size=batch size, verbose=False)
    # Predict
    acc_val = (net.predict(X_val_feats) == y_val).mean()
    acc_train = (net.predict(X_train_feats) == y_train).mean()
    print("prediction accuracy - train: {:.3f} | val: {:.3f}".format(acc_train,
 →acc_val))
    # Choose best network
    if acc_val > best_val:
       best_val = acc_val
       best_hyps = {'lr': lr, 'lr_dec': lr_dec, 'reg': reg, 'hsize': hsize}
       best net = net
    results[(lr, lr_dec, reg, hsize)] = (acc_train, acc_val)
    progress += 1
print("Done training.\n")
# Best validation results
print("Best validation accuracy: {} ".format(best_val))
print("Hyperparameters: {}\n".format(best_hyps))
END OF YOUR CODE
[autoreload of cs231n.classifiers.neural_net failed: Traceback (most recent call
last):
 File "D:\Anaconda\lib\site-packages\IPython\extensions\autoreload.py", line
245, in check
   superreload(m, reload, self.old_objects)
 File "D:\Anaconda\lib\site-packages\IPython\extensions\autoreload.py", line
450, in superreload
   update_generic(old_obj, new_obj)
 File "D:\Anaconda\lib\site-packages\IPython\extensions\autoreload.py", line
387, in update_generic
   update(a, b)
 File "D:\Anaconda\lib\site-packages\IPython\extensions\autoreload.py", line
357, in update_class
   update_instances(old, new)
 File "D:\Anaconda\lib\site-packages\IPython\extensions\autoreload.py", line
317, in update_instances
   update_instances(old, new, obj, visited)
 File "D:\Anaconda\lib\site-packages\IPython\extensions\autoreload.py", line
```

```
317, in update_instances
    update_instances(old, new, obj, visited)
 File "D:\Anaconda\lib\site-packages\IPython\extensions\autoreload.py", line
317, in update_instances
    update instances(old, new, obj, visited)
 File "D:\Anaconda\lib\site-packages\IPython\extensions\autoreload.py", line
302, in update instances
   visited.update({id(obj):obj})
MemoryError
1
Coarse search
_____
Progress: 1/9 (lr: 1.000e-03, lr_dec: 0.95, reg: 1.000e-03, hsize: 500)
prediction accuracy - train: 0.100 | val: 0.079
Progress: 2/9 (lr: 1.000e-03, lr_dec: 0.95, reg: 3.162e-02, hsize: 500)
prediction accuracy - train: 0.100 | val: 0.098
Progress: 3/9 (lr: 1.000e-03, lr_dec: 0.95, reg: 1.000e+00, hsize: 500)
prediction accuracy - train: 0.100 | val: 0.087
Progress: 4/9 (lr: 3.162e-02, lr_dec: 0.95, reg: 1.000e-03, hsize: 500)
prediction accuracy - train: 0.412 | val: 0.401
Progress: 5/9 (lr: 3.162e-02, lr_dec: 0.95, reg: 3.162e-02, hsize: 500)
prediction accuracy - train: 0.370 | val: 0.363
Progress: 6/9 (lr: 3.162e-02, lr_dec: 0.95, reg: 1.000e+00, hsize: 500)
prediction accuracy - train: 0.100 | val: 0.098
Progress: 7/9 (lr: 1.000e+00, lr_dec: 0.95, reg: 1.000e-03, hsize: 500)
prediction accuracy - train: 0.683 | val: 0.573
Progress: 8/9 (lr: 1.000e+00, lr_dec: 0.95, reg: 3.162e-02, hsize: 500)
prediction accuracy - train: 0.447 | val: 0.445
Progress: 9/9 (lr: 1.000e+00, lr_dec: 0.95, reg: 1.000e+00, hsize: 500)
prediction accuracy - train: 0.100 | val: 0.119
Done training.
Best validation accuracy: 0.573
Hyperparameters: {'lr': 1.0, 'lr_dec': 0.95, 'reg': 0.001, 'hsize': 500}
Fine search
Progress: 1/20 (lr: 5.068e-01, lr_dec: 0.95, reg: 5.925e-03, hsize: 500)
prediction accuracy - train: 0.585 | val: 0.557
Progress: 2/20 (lr: 6.518e-01, lr_dec: 0.95, reg: 7.258e-04, hsize: 500)
prediction accuracy - train: 0.671 | val: 0.557
Progress: 3/20 (lr: 1.926e-01, lr_dec: 0.95, reg: 5.386e-04, hsize: 500)
prediction accuracy - train: 0.582 | val: 0.548
Progress: 4/20 (lr: 1.226e-01, lr_dec: 0.95, reg: 4.313e-03, hsize: 500)
prediction accuracy - train: 0.541 | val: 0.526
Progress: 5/20 (lr: 4.050e-01, lr_dec: 0.95, reg: 1.228e-03, hsize: 500)
prediction accuracy - train: 0.644 | val: 0.577
```

```
prediction accuracy - train: 0.536 | val: 0.529
     Progress: 7/20 (lr: 3.397e-01, lr_dec: 0.95, reg: 7.051e-03, hsize: 500)
     prediction accuracy - train: 0.579 | val: 0.542
     Progress: 8/20 (lr: 2.282e-01, lr dec: 0.95, reg: 6.855e-03, hsize: 500)
     prediction accuracy - train: 0.561 | val: 0.545
     Progress: 9/20 (lr: 3.092e-01, lr dec: 0.95, reg: 6.264e-03, hsize: 500)
     prediction accuracy - train: 0.581 | val: 0.555
     Progress: 10/20 (lr: 1.040e-01, lr_dec: 0.95, reg: 4.943e-04, hsize: 500)
     prediction accuracy - train: 0.541 | val: 0.528
     Progress: 11/20 (lr: 1.605e-01, lr dec: 0.95, reg: 1.396e-02, hsize: 500)
     prediction accuracy - train: 0.529 | val: 0.516
     Progress: 12/20 (lr: 7.129e-01, lr_dec: 0.95, reg: 5.311e-03, hsize: 500)
     prediction accuracy - train: 0.602 | val: 0.547
     Progress: 13/20 (lr: 6.385e-01, lr_dec: 0.95, reg: 9.641e-03, hsize: 500)
     prediction accuracy - train: 0.546 | val: 0.527
     Progress: 14/20 (lr: 2.190e-01, lr_dec: 0.95, reg: 8.741e-03, hsize: 500)
     prediction accuracy - train: 0.554 | val: 0.531
     Progress: 15/20 (lr: 3.802e-01, lr_dec: 0.95, reg: 4.950e-03, hsize: 500)
     prediction accuracy - train: 0.597 | val: 0.562
     Progress: 16/20 (lr: 2.094e-01, lr dec: 0.95, reg: 8.947e-03, hsize: 500)
     prediction accuracy - train: 0.547 | val: 0.525
     Progress: 17/20 (lr: 1.504e-01, lr_dec: 0.95, reg: 1.177e-02, hsize: 500)
     prediction accuracy - train: 0.532 | val: 0.513
     Progress: 18/20 (lr: 5.367e-01, lr_dec: 0.95, reg: 1.714e-03, hsize: 500)
     prediction accuracy - train: 0.653 | val: 0.574
     Progress: 19/20 (lr: 1.963e-01, lr_dec: 0.95, reg: 4.238e-04, hsize: 500)
     prediction accuracy - train: 0.585 | val: 0.562
     Progress: 20/20 (lr: 4.620e-01, lr dec: 0.95, reg: 1.298e-03, hsize: 500)
     prediction accuracy - train: 0.651 | val: 0.579
     Done training.
     Best validation accuracy: 0.579
     Hyperparameters: {'lr': 0.4620462990017729, 'lr_dec': 0.95, 'reg':
     0.001297871203094331, 'hsize': 500}
[19]: # Run your best neural net classifier on the test set. You should be able
      # to get more than 55% accuracy.
      test_acc = (best_net.predict(X_test_feats) == y_test).mean()
      print(test_acc)
     0.579
 []:
```

Progress: 6/20 (lr: 1.037e-01, lr\_dec: 0.95, reg: 2.261e-03, hsize: 500)