

# Decoding for SMT

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Monotone word replacement models

Reordering

- Unconstrained

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# Task

Translate a source text (e.g. sentence)

Examples:

<i>um conto de duas cidades</i>	→	a tale of two cities
<i>nosso amigo comum</i>	→	our mutual friend
<i>a loja de antiguidades</i>	→	the old curiosity shop
<i>o grill da lareira</i>	→	the cricket on the hearth

# Model of translational equivalences

Defines the space of possible translations

- ▶ think of it as a recipe to generate translations  
[Lopez, 2008]

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- ▶ with no insertions or deletions

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[Lopez, 2008]

Example:

- ▶ a word replacement model
- ▶ operates in monotone left-to-right order
- ▶ with no insertions or deletions
- ▶ constrained to known word-to-word bilingual mappings  
(rule set)



# Monotone word-by-word translation: solutions

Source: *um conto de duas cidades*

Translation rules<sup>1</sup>

<i>um</i>	{a, some, one}
<i>conto</i>	{tale, story, narrative, novella}
<i>de</i>	{of, from, 's}
<i>duas</i>	{two, couple}
<i>cidades</i>	{cities, towns, villages}

---

<sup>1</sup>Unrealistically simple

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*um conto de duas cidades*

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*um conto de duas cidades*  
a tale of two cities

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*um conto de duas cidades*

a tale of two cities

a tale of two **towns**

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a tale of two **towns**

a tale of two **villages**

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*um conto de duas cidades*

a tale of two cities

a tale of two **towns**

a tale of two **villages**

a tale of **couple cities**

# Monotone word-by-word translation: solutions

*um conto de duas cidades*

a tale of two cities

a tale of two **towns**

a tale of two **villages**

a tale of **couple cities**

a tale of couple **towns**

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# Monotone word-by-word translation: solutions

*um conto de duas cidades*

a tale of two cities

a tale of two **towns**

a tale of two **villages**

a tale of **couple cities**

a tale of couple **towns**

...

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<i>de</i>	{of, from, 's}
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This can go very far :(



# Monotone word-by-word translation: complexity

Say

- ▶ the input has  $I$  words
- ▶ we know at most  $t$  translation options per source word

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This makes  $O(t^I)$  solutions

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This makes  $O(t^I)$  solutions

Note

- ▶ WMT14's shared task:  $I = 40$  on average
- ▶ last I checked Moses default was  $t = 100$   
(for a more complex model)
- ▶ silly monotone word replacement model:  $10^{80}$  solutions

# Space of solutions as intersection/composition



*um*:a  
*um*:some  
*um*:one  
*conto*:tale  
*conto*:story  
*conto*:narrative  
*conto*:novella  
*de*:of  
*de*:from  
*de*: 's  
*duas*:two  
*duas*:couple  
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*idades*:towns  
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*idades*:towns  
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# Space of solutions as intersection/composition



$um:a \leftarrow$   
 $um:some$   
 $um:one$   
 $conto:tale$   
 $conto:story$   
 $conto:narrative$   
 $conto:novella$   
 $de:of$   
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 $de:'s$   
 $duas:two$   
 $duas:couple$   
 $cidades:cities$   
 $cidades:towns$   
 $cidades:villages$



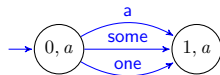
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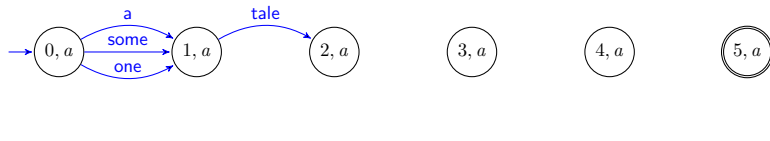




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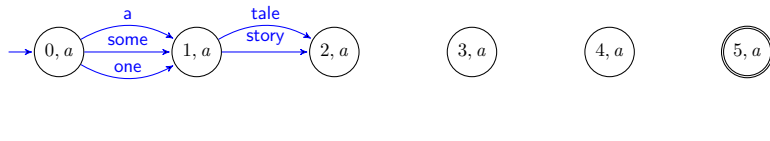
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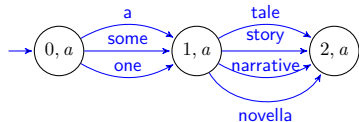
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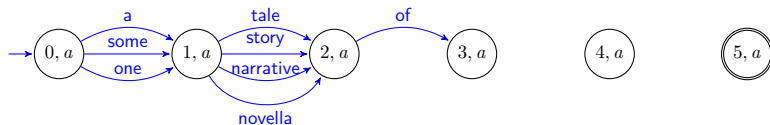
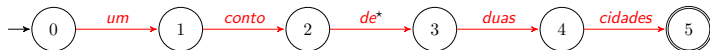
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 cidades:cities  
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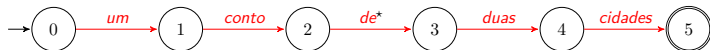
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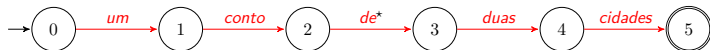
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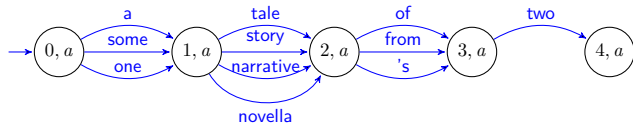
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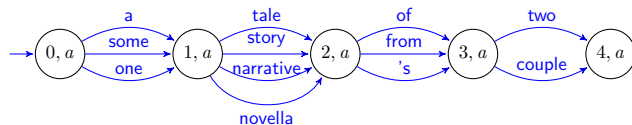


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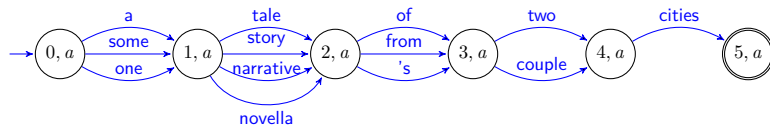
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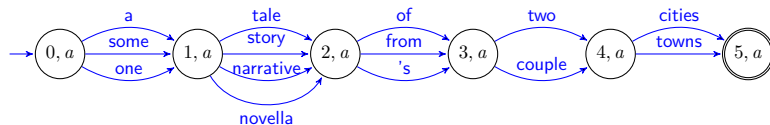
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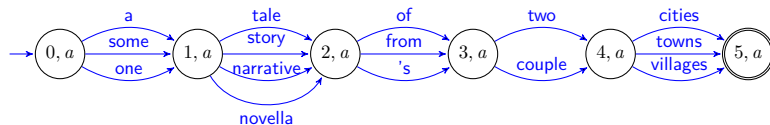
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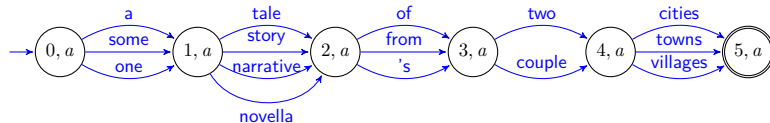
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$$3 \times 4 \times 3 \times 2 \times 3 = 216 \text{ solutions}$$

► 6 states

►  $3 + 4 + 3 + 2 + 3 = 15$  transitions

# Packing solutions with finite-state automata

Same  $O(t^I)$  solutions using

- ▶  $O(I)$  states
- ▶  $O(tI)$  transitions

# Recap 1

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- ▶ exponential number of solutions in linear space

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## Monotone word replacement model

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- ▶ set of translations given by composition
- ▶ exponential number of solutions in linear space
- ▶ translates infinitely many sentences

**but not nearly enough interesting cases!**

# Monotone word-by-word translation: fail!

*nosso* {our, ours}

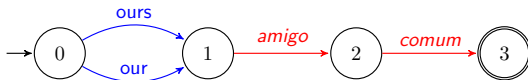
*amigo* {friend, mate}

*comum* {ordinary, common, usual, mutual}



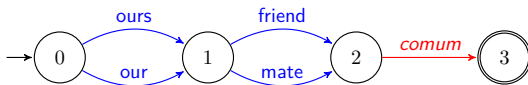
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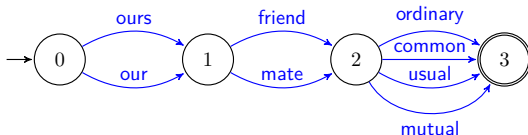
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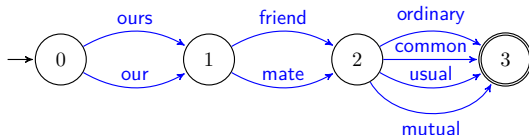
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# Monotone word-by-word translation: fail!

*nosso*     {our, ours}  
*amigo*    {friend, mate}  
*comum*    {ordinary, common, usual, mutual}



We simply cannot obtain a correct translation

our mutual friend

# Reordering

Our model of translational equivalences assumes monotonicity

- ▶ a word replacement model
- ▶ operates in **monotone** left-to-right order
- ▶ with no insertions or deletions
- ▶ constrained to known word-to-word bilingual mappings (rule set)

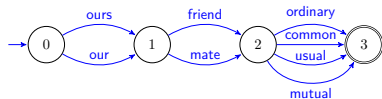
# Reordering

Not anymore!

- ▶ a word replacement model
- ▶ operates in **arbitrary** order
- ▶ with no insertions or deletions
- ▶ constrained to known word-to-word bilingual mappings (rule set)

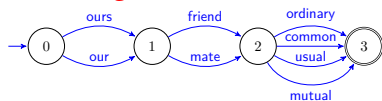
# Translating arbitrary permutations

*nosso amigo comum*

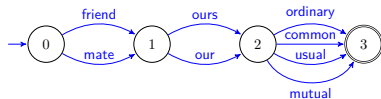


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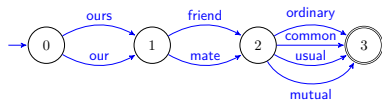


*amigo nosso comum*

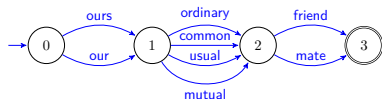


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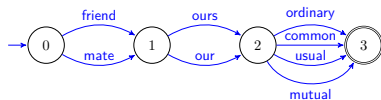
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*nosso comum amigo*

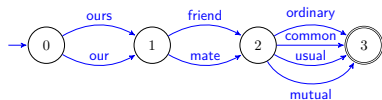


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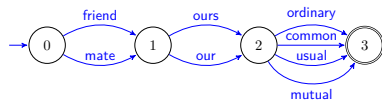


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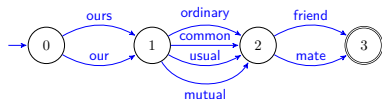
*nosso amigo comum*



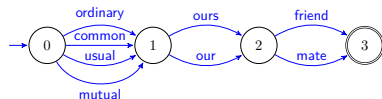
*amigo nosso comum*



*nosso comum amigo*



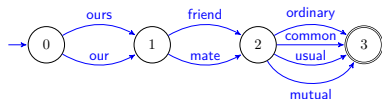
*comum nosso amigo*



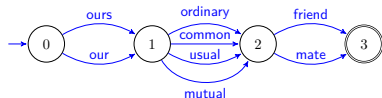


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*nosso amigo comum*



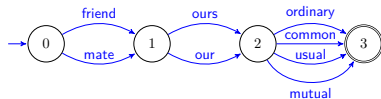
*nosso comum amigo*



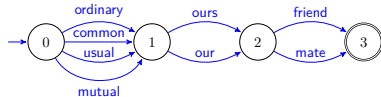
*amigo comum nosso*



*amigo nosso comum*

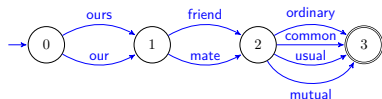


*comum nosso amigo*

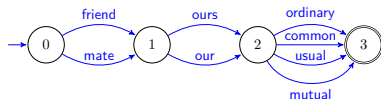


# Translating arbitrary permutations

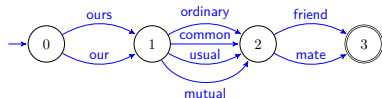
*nosso amigo comum*



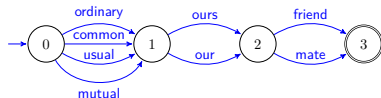
*amigo nosso comum*



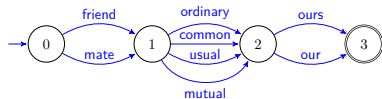
*nosso comum amigo*



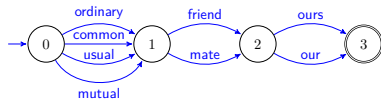
*comum nosso amigo*



*amigo comum nosso*

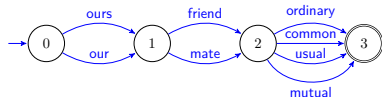


*comum amigo nosso*

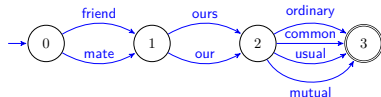


# Translating arbitrary permutations

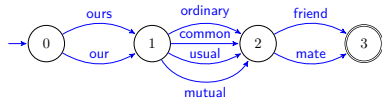
*nosso amigo comum*



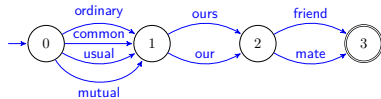
*amigo nosso comum*



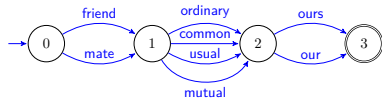
*nosso comum amigo*



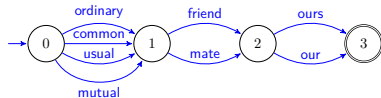
*comum nosso amigo*



*amigo comum nosso*



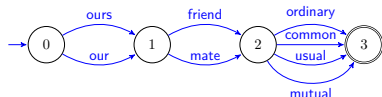
*comum amigo nosso*



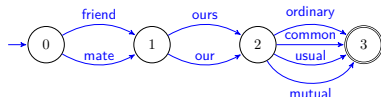
$3! = 3 \times 2 \times 1 = 6$  permutations

# Translating arbitrary permutations

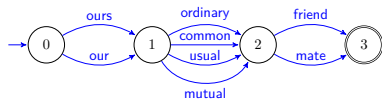
*nosso amigo comum*



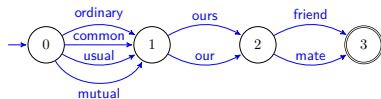
*amigo nosso comum*



*nosso comum amigo*



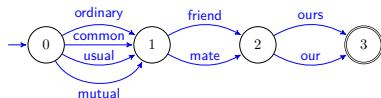
*comum nosso amigo*



*amigo comum nosso*



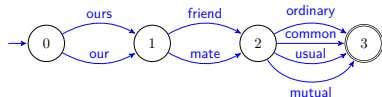
*comum amigo nosso*



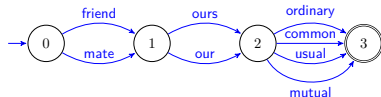
each has  $2 \times 2 \times 4 = 16$  translations

# Translating arbitrary permutations

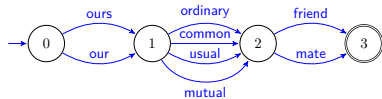
*nosso amigo comum*



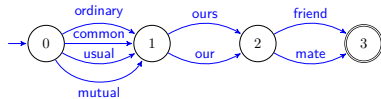
*amigo nosso comum*



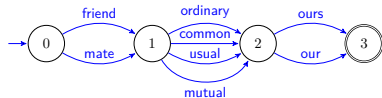
*nosso comum amigo*



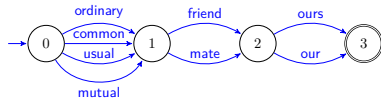
*comum nosso amigo*



*amigo comum nosso*



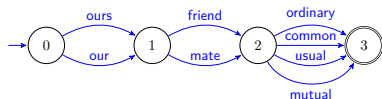
*comum amigo nosso*



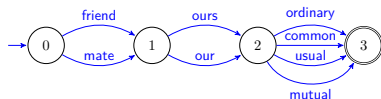
amounting to  $6 \times 16 = 96$  solutions

# Translating arbitrary permutations

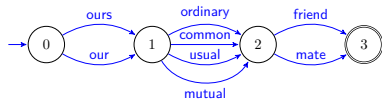
*nosso amigo comum*



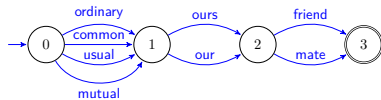
*amigo nosso comum*



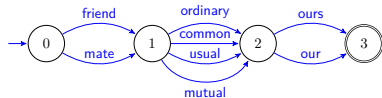
*nosso comum amigo*



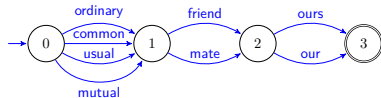
*comum nosso amigo*



*amigo comum nosso*

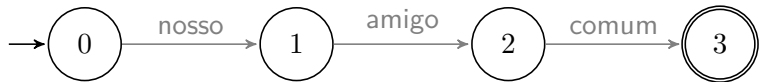


*comum amigo nosso*



$I!$  permutations  $\times t^I$  translations

## Packing permutations



# Packing permutations





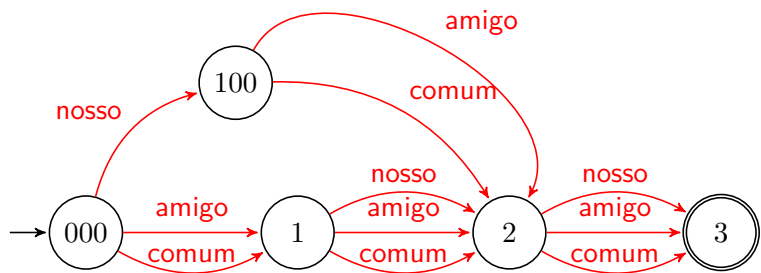
# Packing permutations



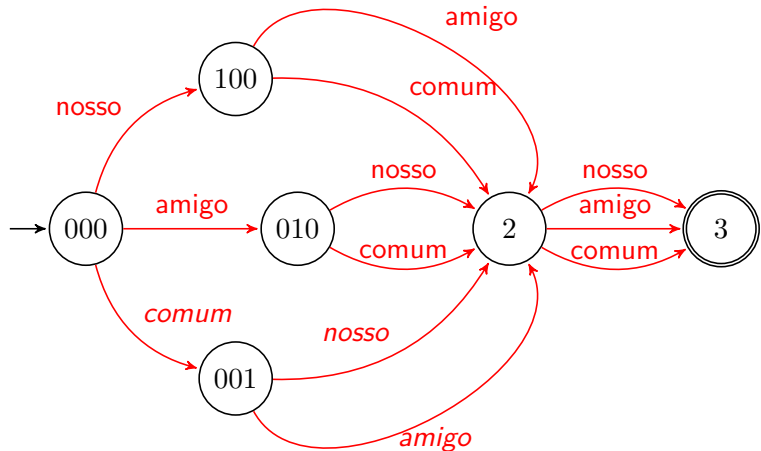
# Packing permutations



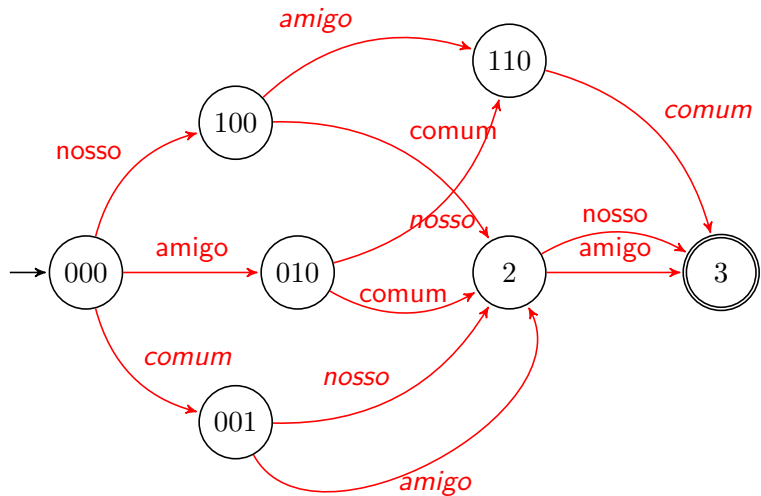
# Packing permutations



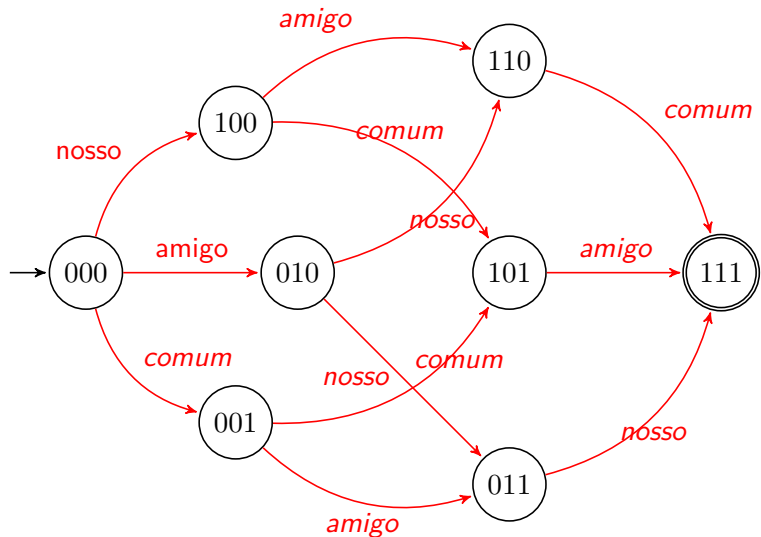
# Packing permutations



# Packing permutations



## Packing permutations



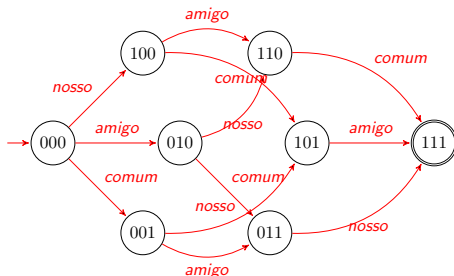
# Packing permutations

Powerset (*all subsets*) of  $\{1, 2, \dots, I\}$

- ▶  $2^I$  subsets  
think of a vector of  $I$  bits ;)

Lattice

- ▶  $O(2^I)$  states
- ▶  $O(I \times 2^I)$  transitions



# Deductive logic

ITEM  $\left[ \{0, 1\}^I \right]$

GOAL  $\left[ 1^I \right]$

AXIOM

$\overline{[0^I]}$

EXPAND

$\frac{[C]}{[\alpha_i(C)]} \quad 1 \leq i \leq I$   
 $c_i = \bar{0}$

where  $\alpha_i(C)$  is a copy of  $C$  with  $c_i = \bar{1}$

Template

- ▶ items  $\rightarrow$  states
- ▶ deduction rules  $\rightarrow$  transitions



# Deductive logic

ITEM  $\left[ \{0, 1\}^I \right]$

GOAL  $\left[ 1^I \right]$

AXIOM

$\overline{[0^I]}$

EXPAND

$\frac{[C]}{[\alpha_i(C)]} \quad 1 \leq i \leq I$   
 $c_i = \bar{0}$

where  $\alpha_i(C)$  is a copy of  $C$  with  $c_i = \bar{1}$

- ▶ a subset of  $\{1, \dots, I\}$   
encoded as a bit vector of length  $I$

# Deductive logic

ITEM  $\left[ \{0, 1\}^I \right]$   
GOAL  $\left[ 1^I \right]$

AXIOM

$\overline{[0^I]}$

EXPAND

$$\frac{[C]}{[\alpha_i(C)]} \quad 1 \leq i \leq I$$

where  $\alpha_i(C)$  is a copy of  $C$  with  $c_i = \bar{1}$

- ▶ we start with an empty sentence  
e.g.  $I = 3 \rightarrow 0^3 = 000$

# Deductive logic

ITEM  $\left[ \{0, 1\}^I \right]$

GOAL  $\left[ 1^I \right]$

AXIOM

$\overline{[0^I]}$

EXPAND

$\frac{[C]}{[\alpha_i(C)]} \quad 1 \leq i \leq I$   
 $c_i = \bar{0}$

where  $\alpha_i(C)$  is a copy of  $C$  with  $c_i = \bar{1}$

► and continue one word at a time

e.g.  $[000](i = 1) \rightarrow [100]$

# Deductive logic

ITEM  $\left[ \{0, 1\}^I \right]$

GOAL  $\left[ 1^I \right]$

AXIOM

$\overline{[0^I]}$

EXPAND

$\frac{[C]}{[\alpha_i(C)]} \quad 1 \leq i \leq I$   
 $c_i = \bar{0}$

where  $\alpha_i(C)$  is a copy of  $C$  with  $c_i = \bar{1}$

- until we have a complete sentence  
e.g.  $[111]$

# Instantiated deductive logic program

ITEM  $\left[ \{0, 1\}^I \right]$   
GOAL  $\left[ 1^I \right]$

AXIOM

$\overline{[0^I]}$

EXPAND

$$\frac{[C]}{[\alpha_i(C)]} \quad \begin{array}{l} 1 \leq i \leq I \\ c_i = \bar{0} \end{array}$$

Source: *nosso*<sub>1</sub> *amigo*<sub>2</sub> *comum*<sub>3</sub>

# Instantiated deductive logic program

Source: *nosso*<sub>1</sub> *amigo*<sub>2</sub> *comum*<sub>3</sub>

Axiom

[000]



ITEM  $\left[ \{0, 1\}^I \right]$   
GOAL  $\left[ 1^I \right]$

AXIOM

$\overline{[0^I]}$

EXPAND

$$\frac{[C]}{[\alpha_i(C)]} \quad \begin{array}{l} 1 \leq i \leq I \\ c_i = \bar{0} \end{array}$$

# Instantiated deductive logic program

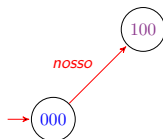
Source: *nosso*<sub>1</sub> *amigo*<sub>2</sub> *comum*<sub>3</sub>

Axiom

[000]

Expand

[000]( $i = 1$ )  $\rightarrow$  [100]



ITEM  $\left[ \{0, 1\}^I \right]$

GOAL  $\left[ 1^I \right]$

AXIOM

$\overline{[0^I]}$

EXPAND

$$\frac{[C]}{[\alpha_i(C)]} \quad \begin{array}{l} 1 \leq i \leq I \\ c_i = \bar{0} \end{array}$$

# Instantiated deductive logic program

Source: *nosso*<sub>1</sub> *amigo*<sub>2</sub> *comum*<sub>3</sub>

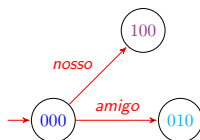
Axiom

[000]

Expand

[000]( $i = 1$ )  $\rightarrow$  [100]

[000]( $i = 2$ )  $\rightarrow$  [010]



ITEM  $\left[ \{0, 1\}^I \right]$

GOAL  $\left[ 1^I \right]$

AXIOM

$\overline{[0^I]}$

EXPAND

$\frac{[C]}{[\alpha_i(C)]} \quad 1 \leq i \leq I$   
 $c_i = \bar{0}$



# Instantiated deductive logic program

Source: *nosso*<sub>1</sub> *amigo*<sub>2</sub> *comum*<sub>3</sub>

Axiom

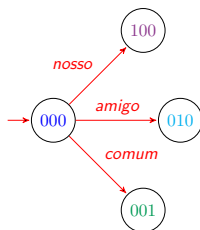
[000]

Expand

[000](*i* = 1) → [100]

[000](*i* = 2) → [010]

[000](*i* = 3) → [001]



ITEM  $\left[ \{0, 1\}^I \right]$

GOAL  $\left[ 1^I \right]$

AXIOM

$\overline{[0^I]}$

EXPAND

$\frac{[C]}{[\alpha_i(C)]} \quad 1 \leq i \leq I$   
 $c_i = \bar{0}$

# Instantiated deductive logic program

Source: *nosso*<sub>1</sub> *amigo*<sub>2</sub> *comum*<sub>3</sub>

Axiom

[000]

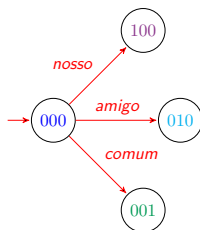
Expand

[000](*i* = 1) → [100]

[000](*i* = 2) → [010]

[000](*i* = 3) → [001]

[100](*i* = 1) ✗



ITEM  $\left[ \{0, 1\}^I \right]$

GOAL  $\left[ 1^I \right]$

AXIOM

$\overline{[0^I]}$

EXPAND

$\frac{[C]}{[\alpha_i(C)]} \quad 1 \leq i \leq I$   
 $c_i = \bar{0}$

# Instantiated deductive logic program

Source: *nosso*<sub>1</sub> *amigo*<sub>2</sub> *comum*<sub>3</sub>

Axiom

[000]

Expand

[000]( $i = 1$ )  $\rightarrow$  [100]

[000]( $i = 2$ )  $\rightarrow$  [010]

[000]( $i = 3$ )  $\rightarrow$  [001]

[100]( $i = 1$ ) ✗

[100]( $i = 2$ )  $\rightarrow$  [110]

ITEM  $\left[ \{0, 1\}^I \right]$

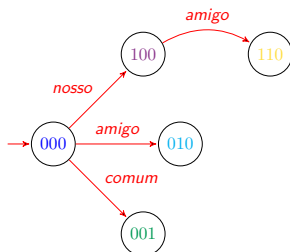
GOAL  $\left[ 1^I \right]$

AXIOM

$\overline{[0^I]}$

EXPAND

$\frac{[C]}{[\alpha_i(C)]} \quad 1 \leq i \leq I$   
 $c_i = \bar{0}$



# Instantiated deductive logic program

Source: *nosso*<sub>1</sub> *amigo*<sub>2</sub> *comum*<sub>3</sub>

Axiom

[000]

Expand

[000] ( $i = 1$ )  $\rightarrow$  [100]

[000] ( $i = 2$ )  $\rightarrow$  [010]

[000] ( $i = 3$ )  $\rightarrow$  [001]

[100] ( $i = 1$ ) ✗

[100] ( $i = 2$ )  $\rightarrow$  [110]

[100] ( $i = 3$ )  $\rightarrow$  [101]

ITEM  $\left[ \{0, 1\}^I \right]$

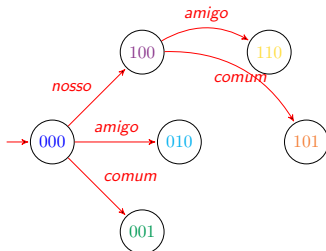
GOAL  $\left[ 1^I \right]$

AXIOM

$\overline{[0^I]}$

EXPAND

$\frac{[C]}{[\alpha_i(C)]} \quad 1 \leq i \leq I$   
 $c_i = \bar{0}$



# Instantiated deductive logic program

Source: *nosso*<sub>1</sub> *amigo*<sub>2</sub> *comum*<sub>3</sub>

Axiom

[000]

Expand

[000] ( $i = 1$ )  $\rightarrow$  [100]

[000] ( $i = 2$ )  $\rightarrow$  [010]

[000] ( $i = 3$ )  $\rightarrow$  [001]

[100] ( $i = 1$ ) ✗

[100] ( $i = 2$ )  $\rightarrow$  [110]

[100] ( $i = 3$ )  $\rightarrow$  [101]

[010] ( $i = 1$ )  $\rightarrow$  [110]

ITEM  $\left[ \{0, 1\}^I \right]$

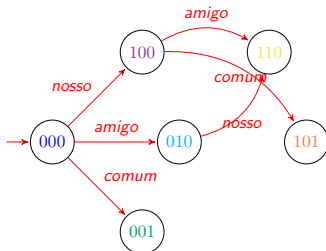
GOAL  $\left[ 1^I \right]$

AXIOM

$\overline{[0^I]}$

EXPAND

$\frac{[C]}{[\alpha_i(C)]} \quad 1 \leq i \leq I$   
 $c_i = \bar{0}$



# Instantiated deductive logic program

Source: *nosso*<sub>1</sub> *amigo*<sub>2</sub> *comum*<sub>3</sub>

Axiom

[000]

Expand

[000] ( $i = 1$ )  $\rightarrow$  [100]

[000] ( $i = 2$ )  $\rightarrow$  [010]

[000] ( $i = 3$ )  $\rightarrow$  [001]

[100] ( $i = 1$ ) ✗

[100] ( $i = 2$ )  $\rightarrow$  [110]

[100] ( $i = 3$ )  $\rightarrow$  [101]

[010] ( $i = 1$ )  $\rightarrow$  [110]

[010] ( $i = 2$ ) ✗

ITEM  $\left[ \{0, 1\}^I \right]$

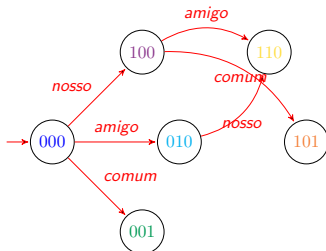
GOAL  $\left[ 1^I \right]$

AXIOM

$\overline{[0^I]}$

EXPAND

$\frac{[C]}{[\alpha_i(C)]} \quad 1 \leq i \leq I$   
 $c_i = \bar{0}$



# Instantiated deductive logic program

Source: *nosso*<sub>1</sub> *amigo*<sub>2</sub> *comum*<sub>3</sub>

Axiom

[000]

Expand

[000]( $i = 1$ )  $\rightarrow$  [100]

[000]( $i = 2$ )  $\rightarrow$  [010]

[000]( $i = 3$ )  $\rightarrow$  [001]

[100]( $i = 1$ ) ✗

[100]( $i = 2$ )  $\rightarrow$  [110]

[100]( $i = 3$ )  $\rightarrow$  [101]

[010]( $i = 1$ )  $\rightarrow$  [110]

[010]( $i = 2$ ) ✗

[010]( $i = 3$ )  $\rightarrow$  [011]

ITEM  $\left[ \{0, 1\}^I \right]$

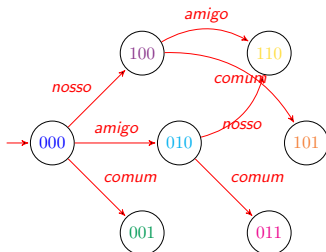
GOAL  $\left[ 1^I \right]$

AXIOM

$\overline{[0^I]}$

EXPAND

$\frac{[C]}{[\alpha_i(C)]} \quad 1 \leq i \leq I$   
 $c_i = \bar{0}$



# Instantiated deductive logic program

Source: *nosso*<sub>1</sub> *amigo*<sub>2</sub> *comum*<sub>3</sub>

Axiom

[000]

Expand

[000](*i* = 1) → [100]

[000](*i* = 2) → [010]

[000](*i* = 3) → [001]

[100](*i* = 1) ✗

[100](*i* = 2) → [110]

[100](*i* = 3) → [101]

[010](*i* = 1) → [110]

[010](*i* = 2) ✗

[010](*i* = 3) → [011]

[001](*i* = 1) → [101]

ITEM  $\left[ \{0, 1\}^I \right]$

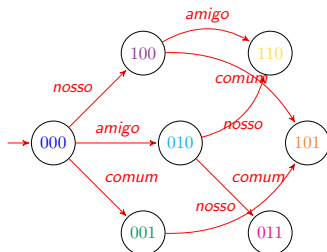
GOAL  $\left[ 1^I \right]$

AXIOM

$\overline{[0^I]}$

EXPAND

$\frac{[C]}{[\alpha_i(C)]} \quad 1 \leq i \leq I$   
 $c_i = \bar{0}$





# Instantiated deductive logic program

Source: *nosso*<sub>1</sub> *amigo*<sub>2</sub> *comum*<sub>3</sub>

Axiom

[000]

Expand

[000](*i* = 1) → [100]

[000](*i* = 2) → [010]

[000](*i* = 3) → [001]

[100](*i* = 1) ✗

[100](*i* = 2) → [110]

[100](*i* = 3) → [101]

[010](*i* = 1) → [110]

[010](*i* = 2) ✗

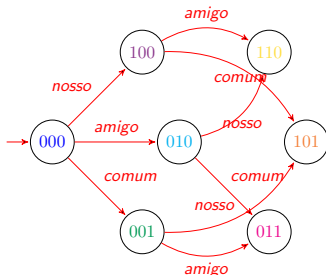
[010](*i* = 3) → [011]

[001](*i* = 1) → [101]

[001](*i* = 2) → [011]

ITEM  $\left[ \{0, 1\}^I \right]$   
GOAL  $\left[ 1^I \right]$   
AXIOM

$\overline{[0^I]}$   
EXPAND  
 $\frac{[C]}{[\alpha_i(C)]} \quad 1 \leq i \leq I$   
 $c_i = \bar{0}$



# Instantiated deductive logic program

Source: *nosso*<sub>1</sub> *amigo*<sub>2</sub> *comum*<sub>3</sub>

Axiom

[000]

Expand

[000]( $i = 1$ )  $\rightarrow$  [100]

[000]( $i = 2$ )  $\rightarrow$  [010]

[000]( $i = 3$ )  $\rightarrow$  [001]

[100]( $i = 1$ ) ✗

[100]( $i = 2$ )  $\rightarrow$  [110]

[100]( $i = 3$ )  $\rightarrow$  [101]

[010]( $i = 1$ )  $\rightarrow$  [110]

[010]( $i = 2$ ) ✗

[010]( $i = 3$ )  $\rightarrow$  [011]

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[001]( $i = 2$ )  $\rightarrow$  [011]

[001]( $i = 3$ ) ✗

ITEM  $\left[ \{0, 1\}^I \right]$

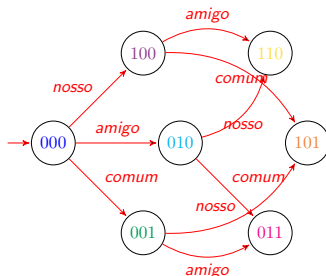
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ITEM  $\left[ \{0, 1\}^I \right]$

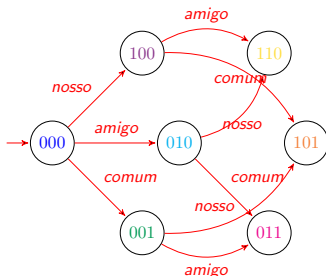
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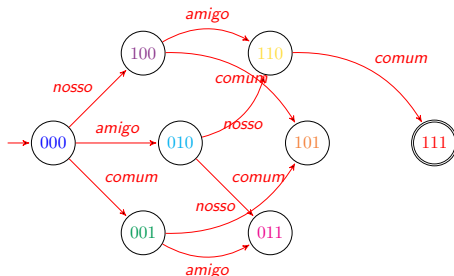
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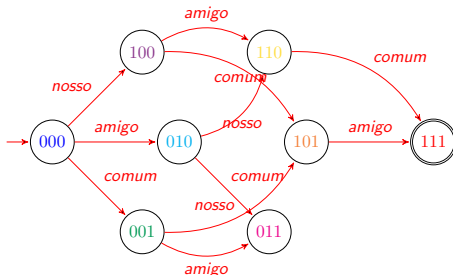
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ITEM  $\left[ \{0, 1\}^I \right]$

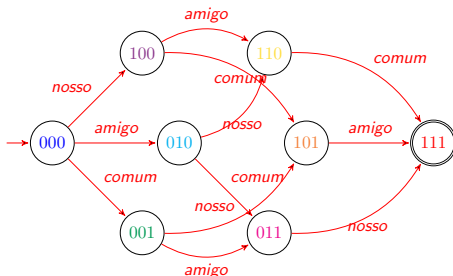
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Goal

[111]

ITEM  $\left[ \{0, 1\}^I \right]$

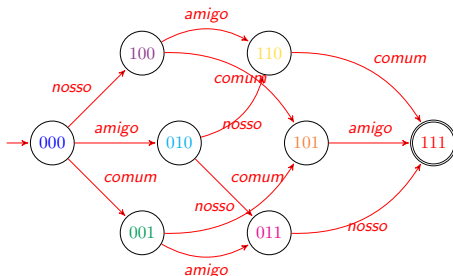
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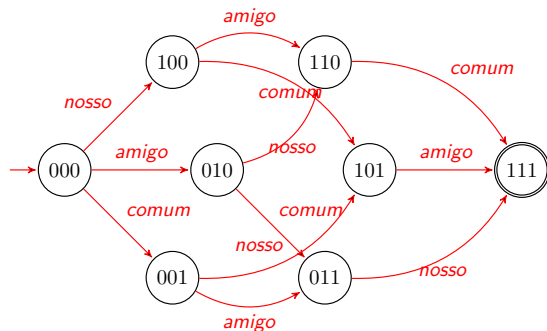


# Word replacement with unconstrained reordering

Source: *nosso amigo comum*



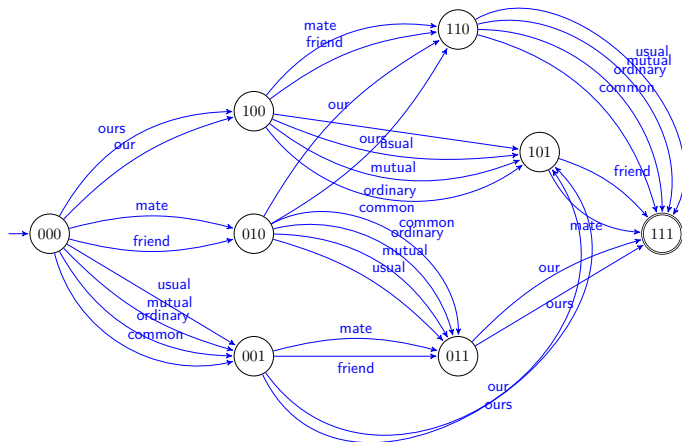
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1. arbitrary permutations:  $O(2^I)$  states

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Source: *nosso amigo comum*

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2. intersection with the rule set:  $O(tI2^I)$  transitions

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- ▶ **0.o** but how?



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Moses allows reordering within a window of length  $d$

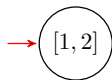
- ▶ starting from the leftmost uncovered word

## WL $d$ (example)

Suppose  $d = 2$  and  $I = 3$

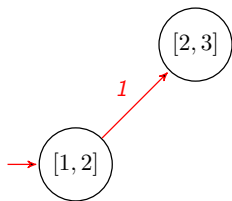
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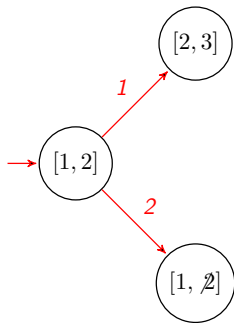
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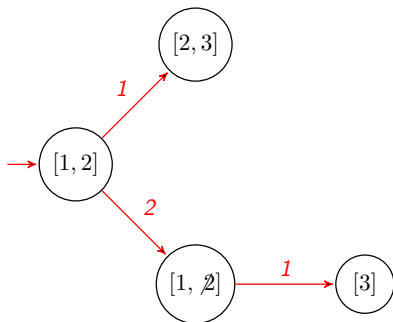
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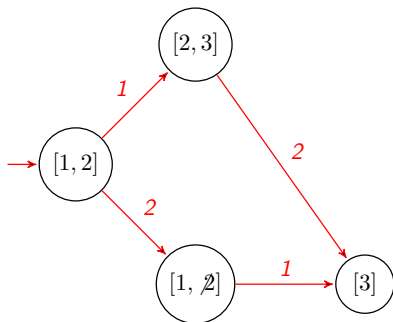
Suppose  $d = 2$  and  $I = 3$





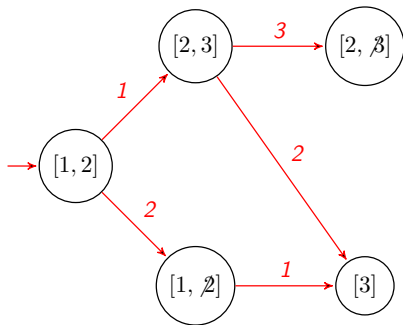
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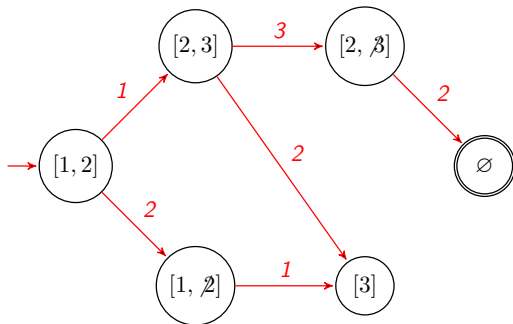
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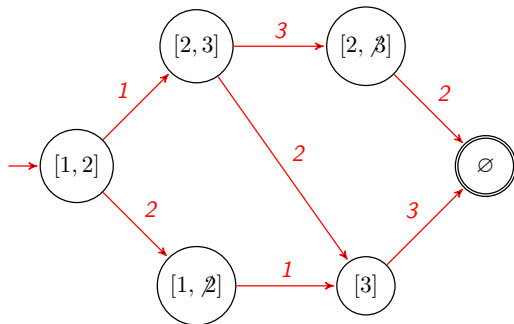
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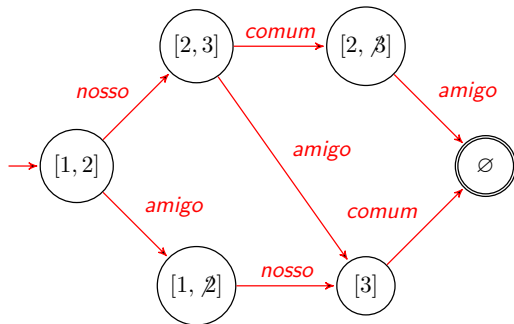
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## WL<sub>d</sub> (example)

Suppose  $d = 2$  and  $I = 3$  (e.g. *nosso amigo comum*)



# WLd (logic)

ITEM  $\left[ [1..I + 1], \{0, 1\}^{d-1} \right]$

GOAL  $[I + 1, C]$

AXIOM

$\overline{[1, 0^{d-1}]}$

ADJACENT

$\frac{[l, C]}{[l + n, C \ll n]} \quad i = l$

where  $n = \#_1(C) + 1$

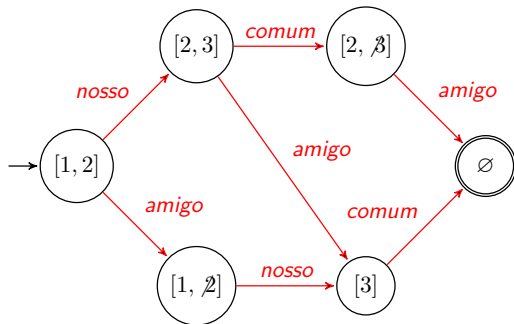
NON-ADJACENT

$\frac{[l, C]}{[l, \alpha_l^i(C)]} \quad \begin{array}{l} l < i \leq I \\ \delta(i, l) \leq d \\ c_{i-l} = \bar{0} \end{array}$

- ▶  $O(Id2^{d-1})$  states
- ▶  $O(Id2^{d-1})$  transitions

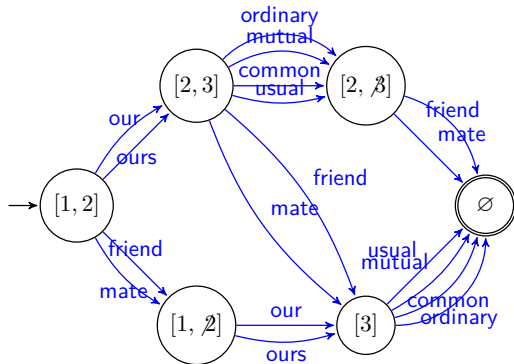
# Word replacement with reordering constrained by WL2

Complexity:  $O(I2^{d-1})$  states



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e.g. OV vs VO, head-initial vs head-final
- ▶ can we do better?

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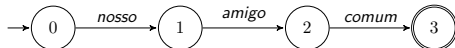
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inverted order
- ▶  $X \rightarrow f/e$ , where  $(f, e) \in R$   
bilingual mappings



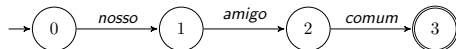
# Parsing, intersection and hypergraphs

Source



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Source



Grammar

$X \rightarrow XX$

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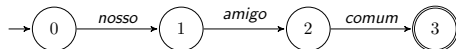
$X \rightarrow \textit{nosso}$

$X \rightarrow \textit{amigo}$

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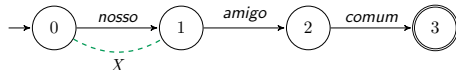
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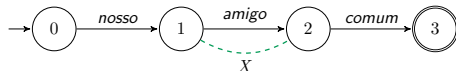
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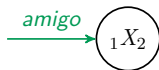
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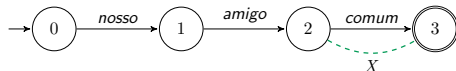
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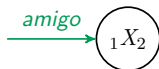
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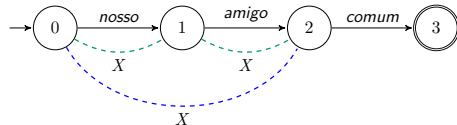
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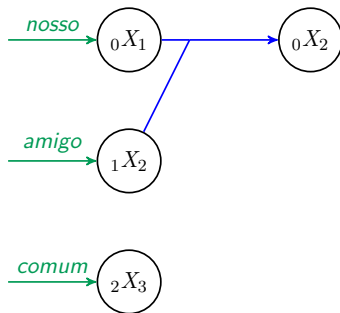
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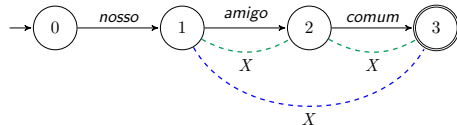
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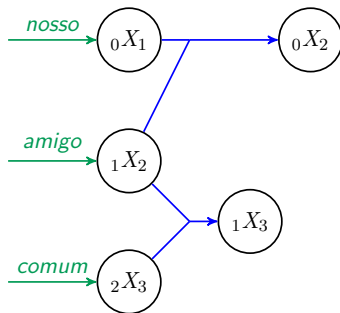
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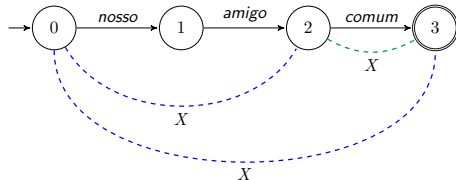
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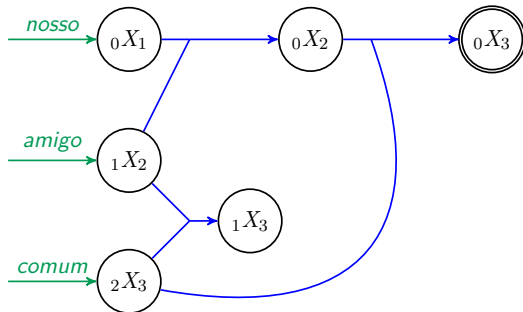
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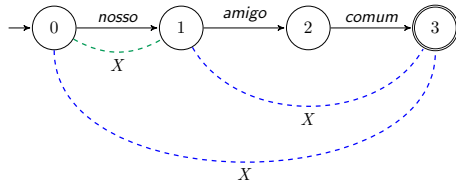
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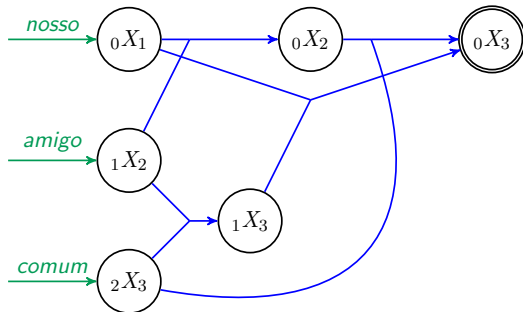
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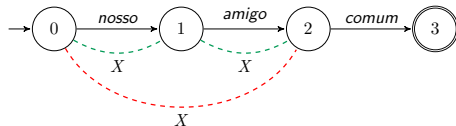
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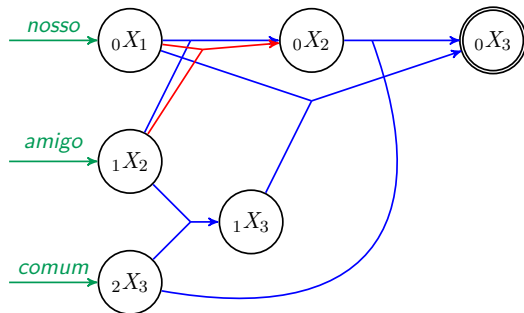
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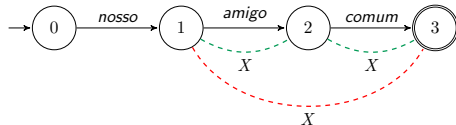
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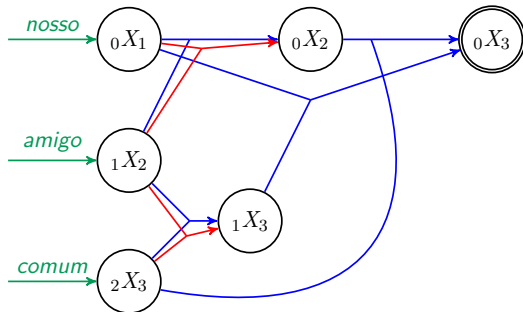
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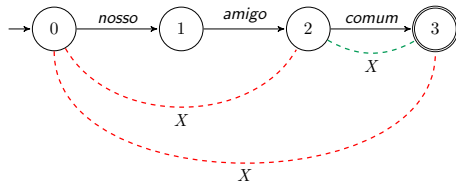
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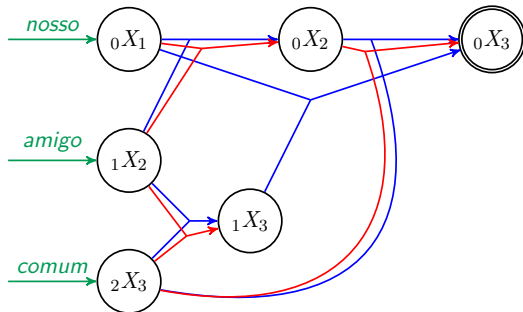
# Parsing, intersection and hypergraphs

Source



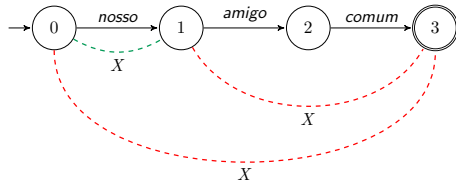
Grammar

$X \rightarrow XX$   
 $X \rightarrow \langle XX \rangle$   
 $X \rightarrow \textit{nosso}$   
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 $X \rightarrow \textit{comum}$



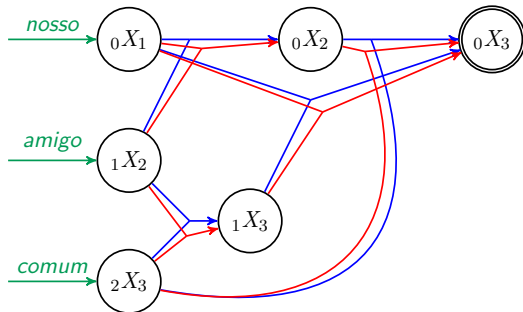
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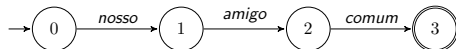
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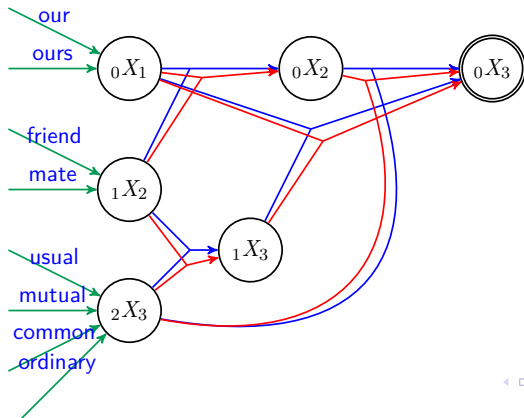
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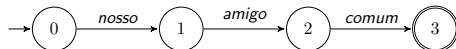
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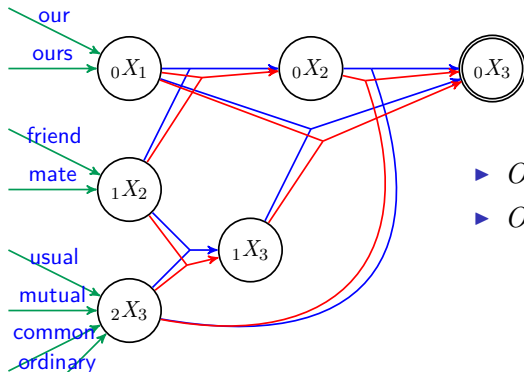
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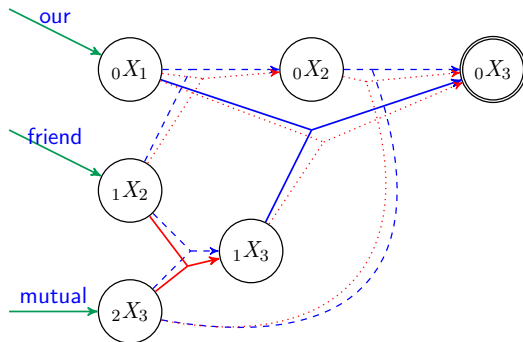


- ▶  $O(I^3)$  nodes
- ▶  $O(tI^3)$  edges



# Example

(nosso  $\langle$ amigo comum $\rangle$ )  $\rightarrow$  **our mutual friend**



## Recap 2

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But we still perform translation word-by-word with no insertion or deletion!

# 1-1 mappings: fail!

Source: o<sub>1</sub> grilo<sub>2</sub> *da*<sub>3</sub> lareira<sub>4</sub>

Target: the<sub>1</sub> cricket<sub>2</sub> [on the]<sub>3</sub> hearth<sub>4</sub>

# Insertion and deletion

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Implicitly modelled by moving from words to phrases

- ▶ a phrase replacement model
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- ▶ constrained to known phrase-to-phrase bilingual mappings (rule set)

# Phrase mappings

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e.g. *a **loja de antiguidades**/old curiosity shop*

# Generalising the rule set (FST)

## Rules

<i>o</i>	{the, a}
<i>grilo</i>	{cricket, annoyance}
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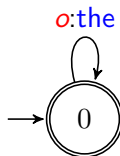
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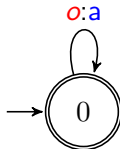
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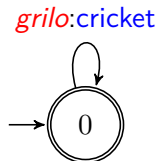
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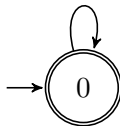


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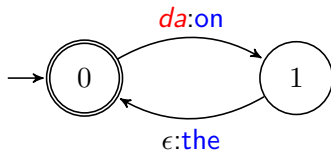
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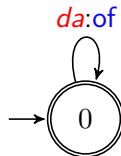
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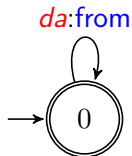
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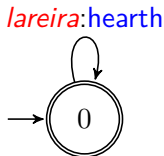
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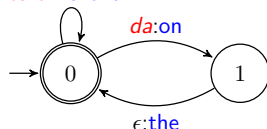
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*o*:the  
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- ▶ each rule can be seen as a transducer
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- ▶ standard intersection mechanisms do the rest



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We can translate a lattice encoding the  $WL_d$  permutations

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- ▶ complexity remains
  - ▶ linear with sentence length
  - ▶ exponential with distortion limit

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Examples

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The intersection mechanisms do the rest

- ▶  $O(I^3)$  nodes (phrases are limited in length)
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  - ▶ trivially expressed in terms of intersection/composition
  - ▶ a logic program can do the same  
(sometimes more convenient, e.g.  $WLD$  constraints)

# Remarks

Phrase-based SMT [Koehn et al., 2003]

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- ▶ the space of solutions is cubic in length
- ▶ better motivated constraints on reordering

# Remarks (hiero)

Hierarchical phrase-based models [Chiang, 2005]

---

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We are missing a parameterisation of the model

- ▶ the scoring function which will guide the decision making process

# Linear models

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It assigns a real-valued score to each and every derivation

Think of it as a surrogate for translation quality at decoding time

[Berger et al., 1996]

[Och and Ney, 2002]

# Feature functions

Independently capture different aspects of the translation, such as

- ▶ adequacy
  - ▶ translation probabilities
  - ▶ confidence on lexical choices
- ▶ fluency
  - ▶ LM probabilities
  - ▶ confidence on reordering

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Certain aspects of translation quality comply with such assumptions

- ▶ how likely a certain translation rule is  
e.g. relative frequency in a bilingual corpus

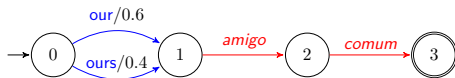
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Scoring rules independently



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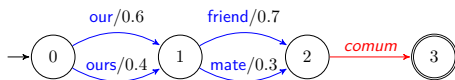
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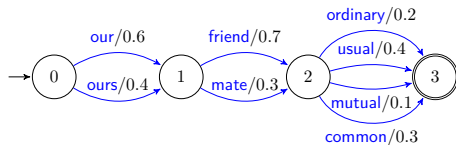
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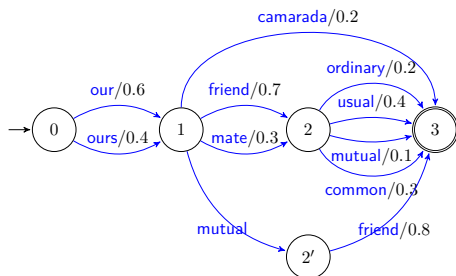
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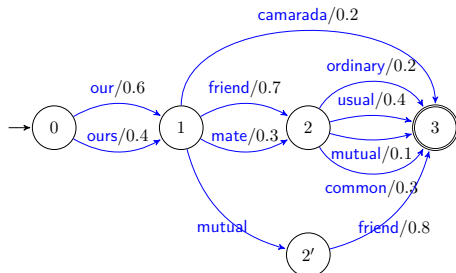
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inference runs in time linear with the size of the automaton

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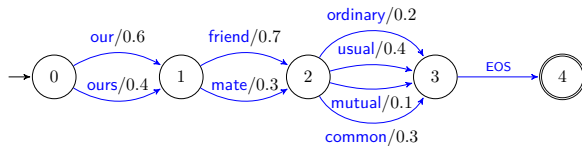
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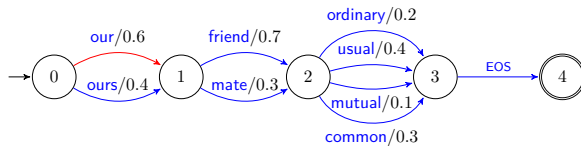
- ▶ fluency as captured by an  $n$ -gram LM component

## Scoring strings with a 2-gram LM



requires unpacking the representation

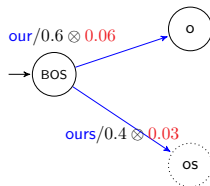
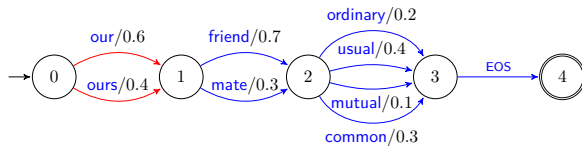
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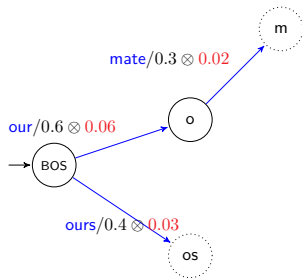
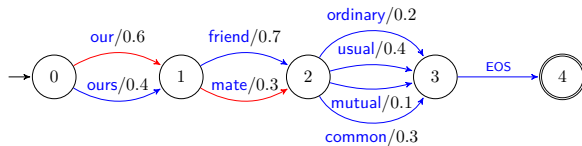


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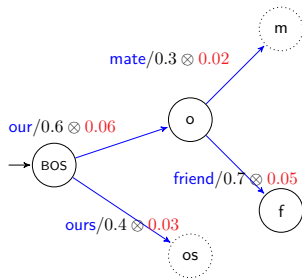
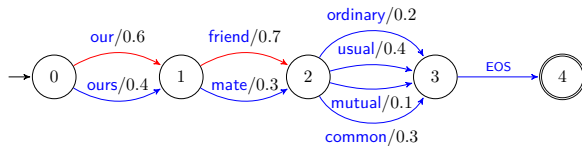
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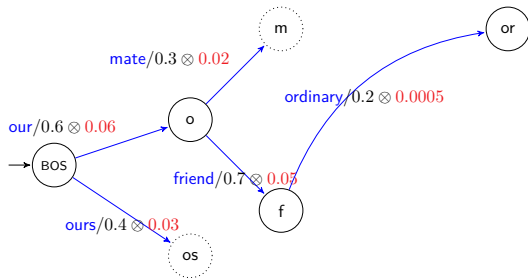
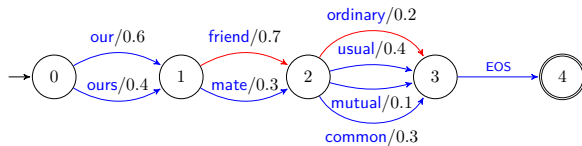
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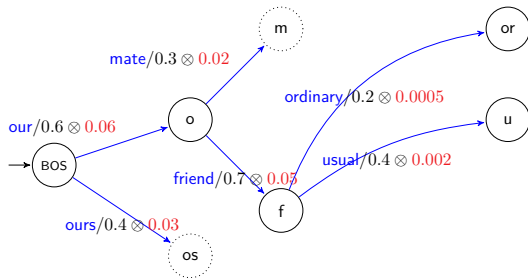
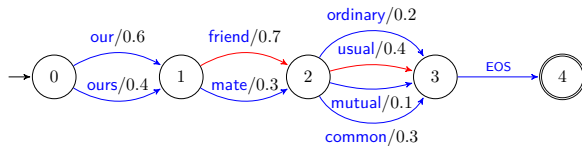
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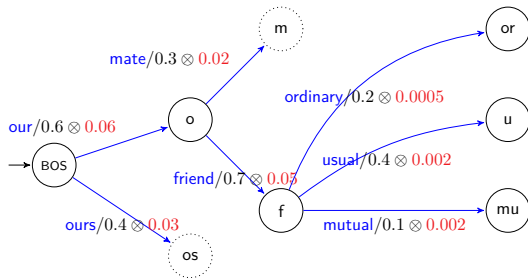
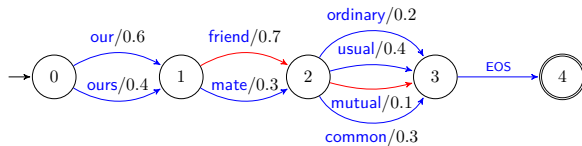
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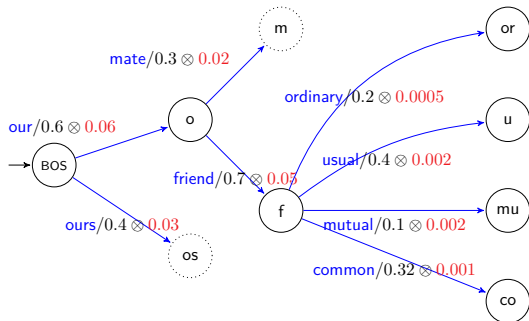
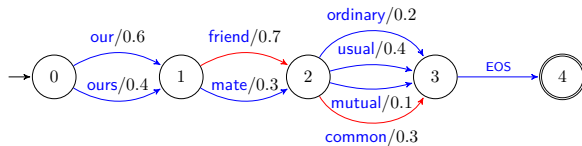
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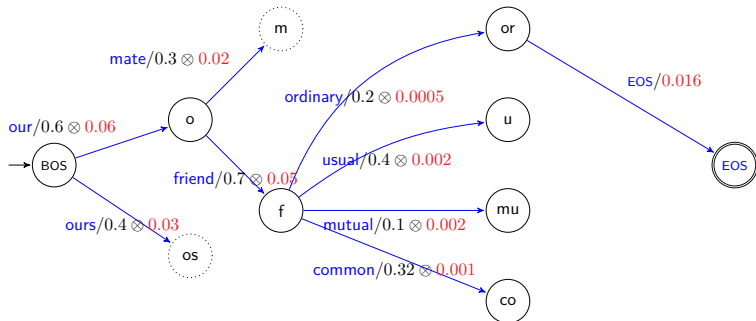
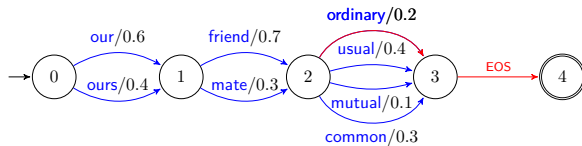
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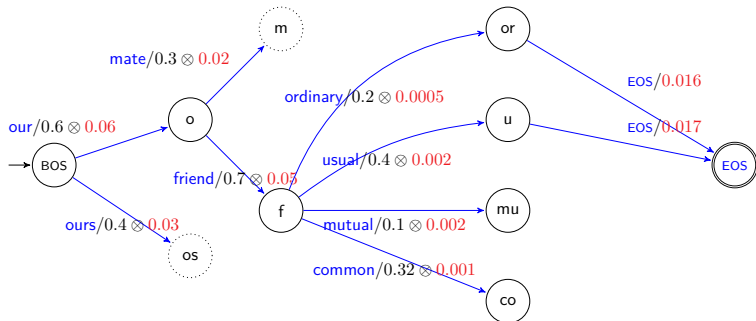
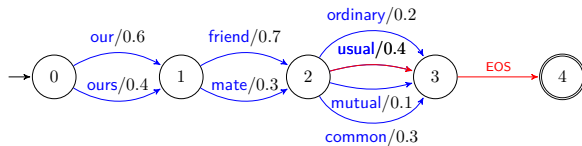
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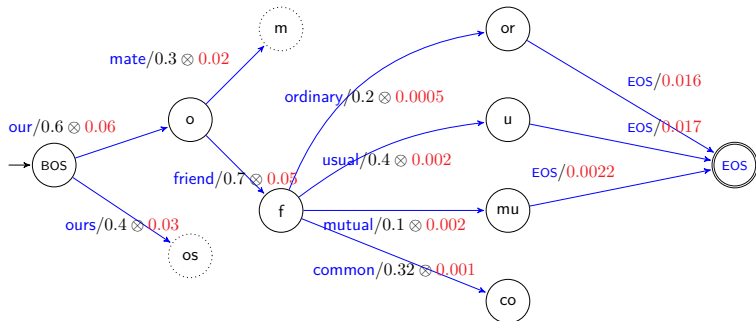
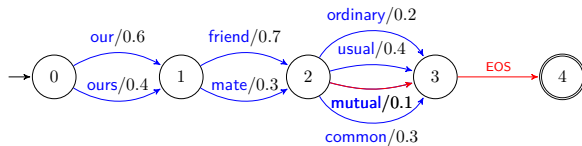


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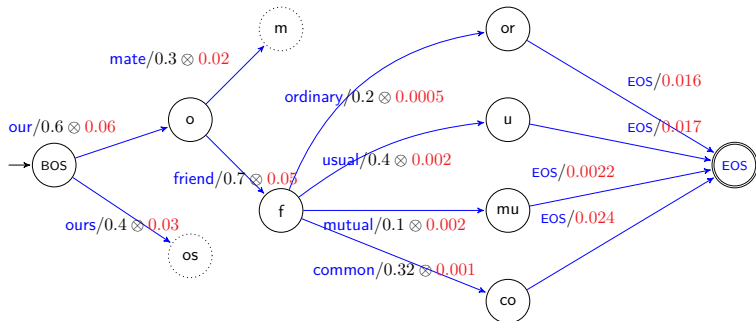
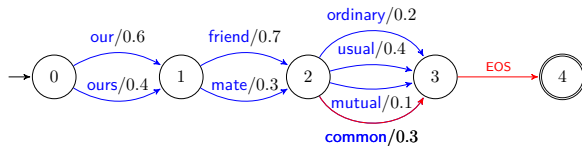
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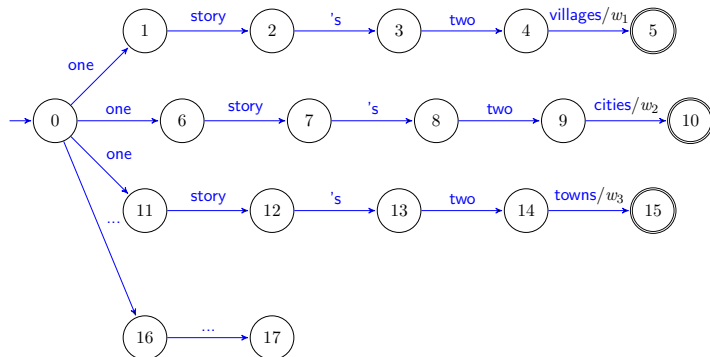
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- ▶ making dependencies explicit through the graphical structure



# Scoring whole sentences: example



Exhaustive enumeration

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- ▶ there are up to  $|\Delta|^{n-1}$  contexts that must be made explicit
- ▶ nodes must group derivations sharing the same context
- ▶ polynomial, though often prohibitive (**impracticable**)

## Recap 4

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  - ▶ lexicalised models
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- ▶ techniques to make inference feasible for interesting models

# Picking one solution

What do we pick out of the (whole) weighted space of solutions?

- ▶ best translation
- ▶ “minimum-loss” translation

# Best translation

MAP

$$\mathbf{y}^* = \operatorname{argmax}_{\mathbf{y}} \sum_{\mathbf{y}[\mathbf{d}]=\mathbf{y}} f(\mathbf{d}|\mathbf{x})$$

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## Viterbi (approximation to MAP)

$$\mathbf{d}^* = \operatorname{argmax}_{\mathbf{d}} f(\mathbf{d}|\mathbf{x})$$

- ▶ assumes the most likely derivation is enough

# Minimum Bayes Risk translation

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$$\mathbf{y} = \operatorname{argmin}_{\mathbf{y}} \langle \operatorname{loss}(\mathbf{y}, \mathbf{y}') \rangle_{p(\mathbf{y}'|\mathbf{x})}$$

# Minimum Bayes Risk translation

MBR

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[Koehn et al., 2003]

[Chiang, 2007]

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[Kumar and Byrne, 2004]

[Tromble et al., 2008]

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5. repeat 2-3 until acceptance rate is reasonable (e.g. 5-10%)

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5. typically stupid simple to parallelise

# Thanks!

Questions?

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