

# CODE3

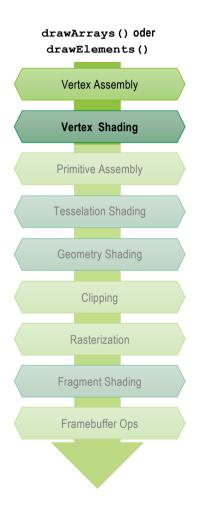
SoSe 2025

Prof. Dr.-Ing. Uwe Hahne

# **Appendix on transformations**

### **Vertex Assembly and Vertex Shader**





#### **Vertex Assembly**

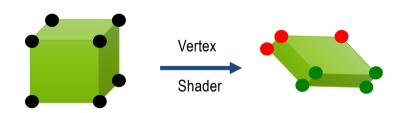
Search for all attributes of a single vertex from potentially multiple vertex buffers

#### **Vertex Shader**

Transformation of the vertex into clip coordinates (e.g. depending on the current camera / scene transformation)

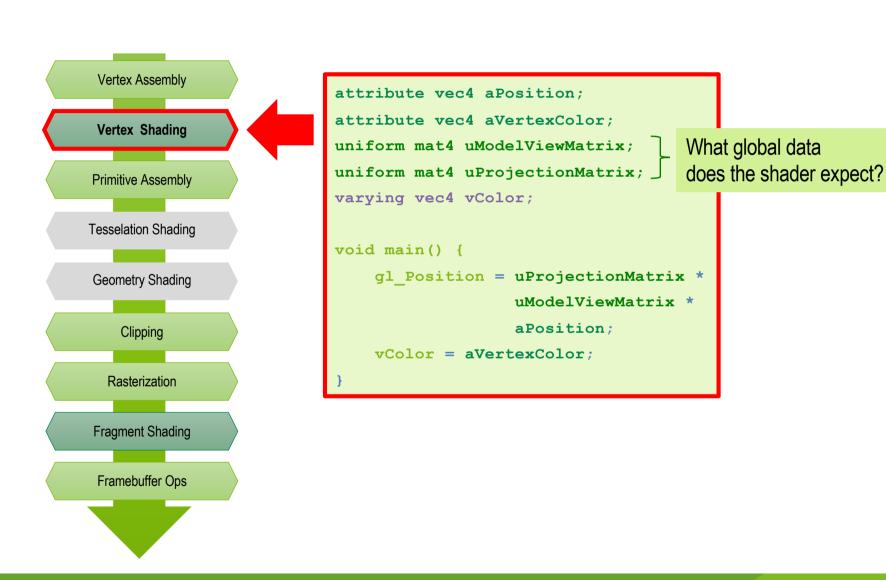
Generation or transformation of further vertex attributes (e.g. normals, texture coordinates, colors)

Lighting calculation per vertex (unusual nowadays)



### Configuration of the pipeline: install vertex shader





#### Transformation in vertex shader



```
attribute: Vertex attribute, receives data from an attribute buffer (VBO)
The position is potentially different for each vertex.

Two matrices are passed as global variables (uniform); they are constant for all vertices during a gl.draw*() command.

Vertex

Yertex

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Yertex

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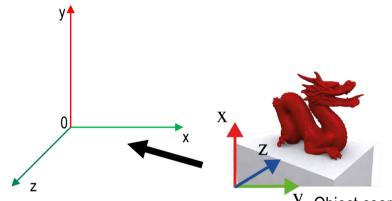
Goal: **gl\_Position** must contain the vertex position in clip coordinates after the shader has been executed.

Matrix multiplications are read from right to left: first apply uModelViewMatrix, then uProjectionMatrix.

## **Modeling transformation**



#### World coordinate system



$$x_w = F \cdot x_o$$
  
$$x_w = F_3 \cdot F_2 \cdot F_1 \cdot x_o$$

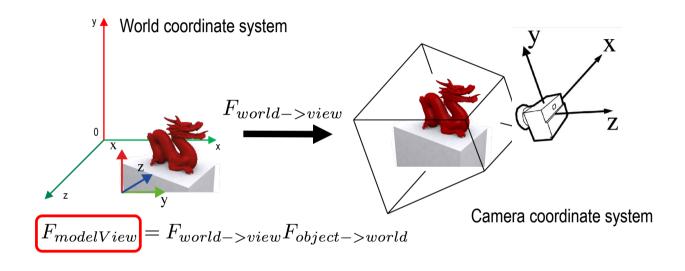
composite transformations

y Object coordinate system

$$F(x, y, z, w) = \begin{bmatrix} a_{11} & a_{12} & a_{13} & t_x \\ a_{21} & a_{22} & a_{23} & t_y \\ a_{31} & a_{32} & a_{33} & t_z \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix}$$

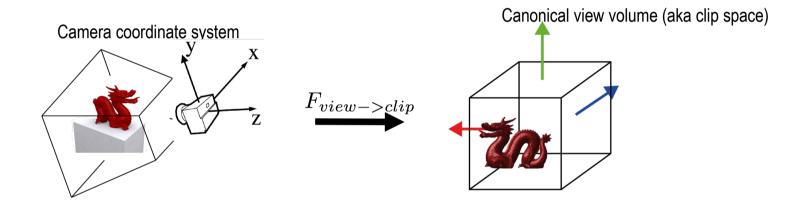
### **View transformation**





# **Projection transformation**

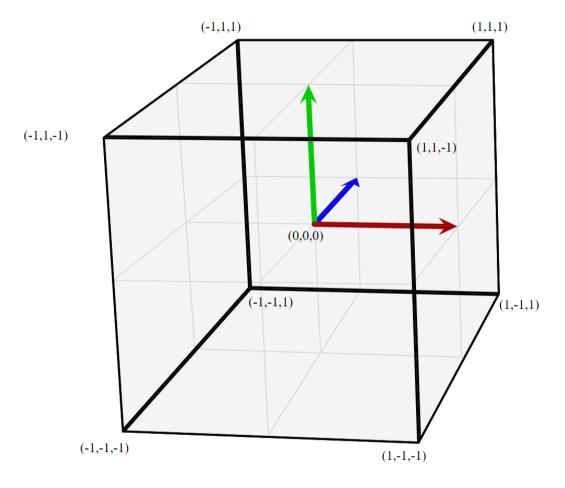




Prof Ilwe Hahne

# Clip space

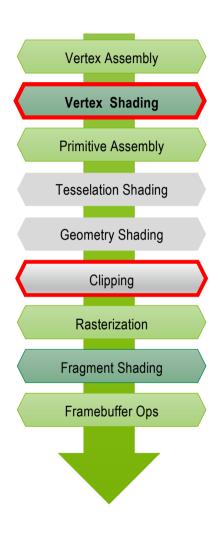




Clipspace

# **Viewport - Transformation**

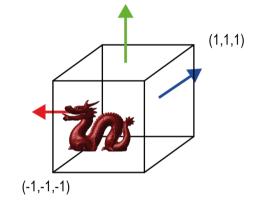




Vertex shader returns position in canonical volume before perspective division

- Clipping
- Perspective division

$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \frac{1}{w_c} \begin{bmatrix} x_c \\ y_c \\ z_c \\ w_c \end{bmatrix}$$

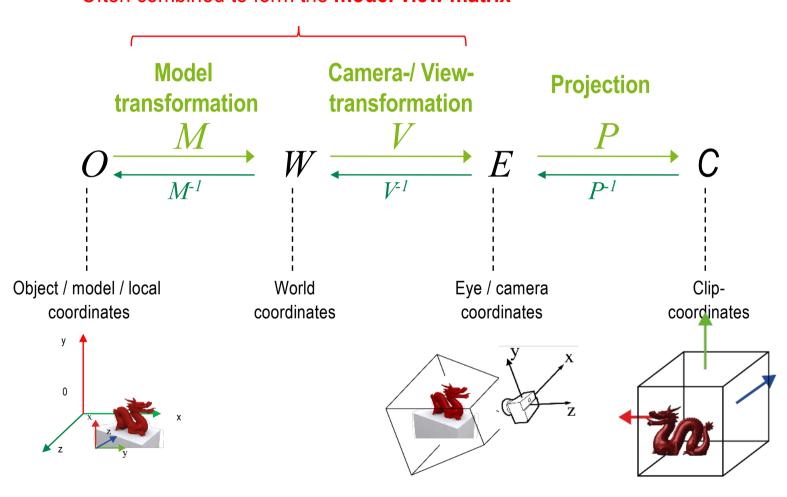


Viewport transformation (window coordinates)

### Transformation chain from model to clip coordinates

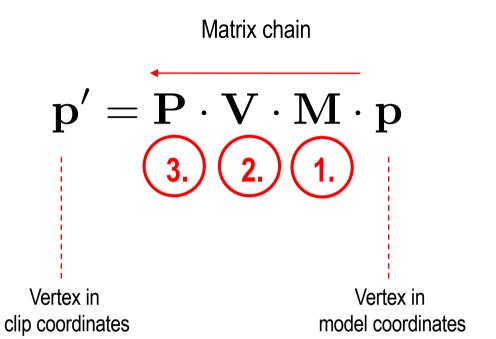


### Often combined to form the model view matrix



### Die Transformationskette von Modell- in Clipkoordinaten



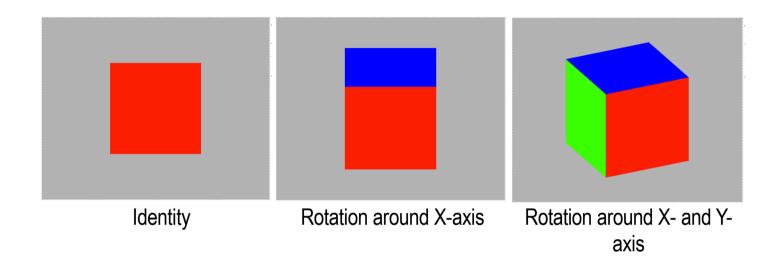


#### Attention order!

- The vertex to be transformed is on the right
- The transformations are multiplied in sequence from the left
- Read from right to left

#### Effect of the model-view-transformation matrix



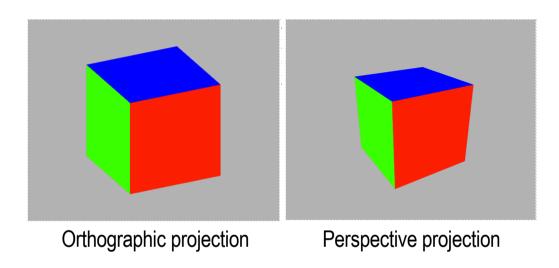


### Who is actually rotating here, the camera or the scene?

- The model view matrix is a relative transformation between two coordinate systems
- Rotation of the scene corresponds to opposite rotation of the camera, one transformation is the inverse of the other

### **Effect of the projection matrix**





### **Orthographic projection ("telephoto lens")**

Parallel lines remain parallel

## Perspective projection ("wide-angle lens")

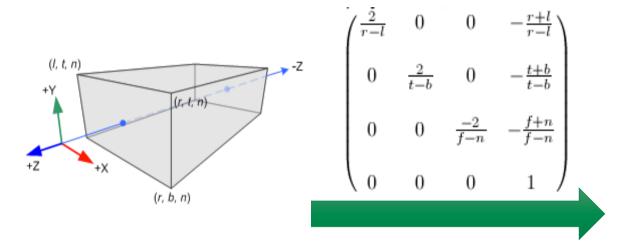
- "Oblique" projection with a selectable aperture angle
- Falling lines, distant objects appear smaller

# **Orthographic projection**



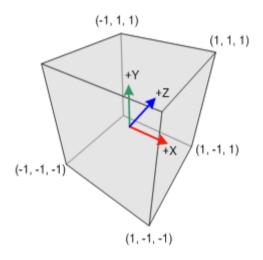
Illustration by Song Ho Ahn, www.songho.ca

# Camera coordinates



projection matrix

#### **Clip coordinates**

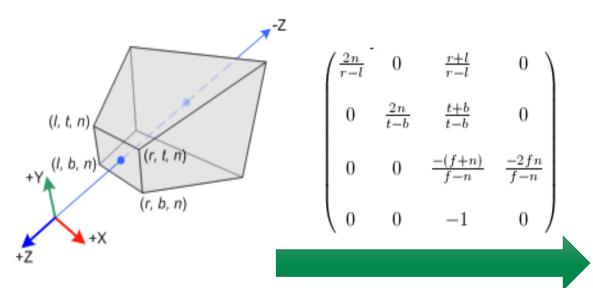


# **Perspective projection**



Illustration by Song Ho Ahn, www.songho.ca

#### camera coordinates



### projection matrix

#### clip coordinates

