



一、设射中为A 选上几级选手为 $B_n$   $n=1,2,3,4$

$$\begin{aligned} P(A) &= P(AB_1) + P(AB_2) + P(AB_3) + P(AB_4) \\ &= P(A|B_1) \cdot P(B_1) + P(A|B_2) \cdot P(B_2) + P(A|B_3) \cdot P(B_3) \\ &\quad + P(A|B_4) \cdot P(B_4) \\ &= 0.9 \cdot 0.2 + 0.8 \cdot 0.3 + 0.5 \times 0.35 + 0.3 \times 0.15 \\ &= 0.64 \end{aligned}$$

二、设“色盲”为A “男”为B

$$\begin{aligned} P(B|A) &= \frac{P(AB)}{P(A)} = \frac{P(A|B) \cdot P(B)}{P(A|B) \cdot P(B) + P(A|\bar{B}) \cdot P(\bar{B})} \\ &= \frac{0.04 \times 0.5}{0.04 \times 0.5 + 0.002 \times 0.5} = 0.952. \end{aligned}$$

三、设“合格n次”为 $A_n$   $n=0,1,2$

c1) “第n次合格”为 $B_n$   $n=1,2$

$$P(A_0) = P(\bar{B}_1 \bar{B}_2) = P(\bar{B}_1) P(\bar{B}_2) = (1-p) \left(1 - \frac{p}{3}\right).$$

$$P(A_1) + P(A_2) = P(\bar{A}_0) = 1 - (1-p) \left(1 - \frac{p}{3}\right) = \frac{4p}{3} - \frac{p^2}{3}$$

$$\begin{aligned} c2) P(B_1|B_2) &= \frac{P(B_1 B_2)}{P(B_2)} = \frac{P(B_2|B_1) \cdot P(B_1)}{P(B_2|B_1) \cdot P(B_1) + P(B_2|\bar{B}_1) \cdot P(\bar{B}_1)} \\ &= \frac{p \cdot p}{p \cdot p + \frac{p}{3} (1-p)} = \frac{3p}{2p+1} \end{aligned}$$

四、  
c1)  $P(Z=k) = \begin{cases} 0.4^{\frac{k-1}{2}} \cdot 0.3^{\frac{k-1}{2}} \cdot 0.6 = 0.12^{\frac{k-1}{2}} \cdot 0.6 & k \text{ 为奇数} \\ 0.4^{\frac{k}{2}} \cdot 0.3^{\frac{k-2}{2}} \cdot 0.7 = 0.12^{\frac{k-2}{2}} \cdot 0.28 & k \text{ 为偶数} \end{cases} \quad k \in \mathbb{Z}^+$

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$$\begin{aligned}
 c2) P(X=k) &= P(Z=2k) + P(Z=2k-1) \quad k \in \mathbb{Z}^+ \\
 &= 0.4^k \cdot 0.3^{k-1} \cdot 0.7 + 0.4^{k-1} \cdot 0.3^{k-1} \cdot 0.6 \\
 &= 0.4^{k-1} \cdot 0.3^{k-1} \cdot 0.88 = 0.12^{k-1} \cdot 0.88
 \end{aligned}$$

$$\begin{aligned}
 c3) P(Y=k) &= P(Z=2k) + P(Z=2k+1) \quad k \in \mathbb{Z}^+ \\
 &= 0.4^k \cdot 0.3^{k-1} \cdot 0.7 + 0.4^k \cdot 0.3^k \cdot 0.6 \\
 &= 0.4^k \cdot 0.3^{k-1} \cdot 0.88 = 0.12^{k-1} \cdot 0.352
 \end{aligned}$$

$$P(Y=0) = 0.6$$

$$\begin{aligned}
 \text{Ex. } c1) \int_{-\infty}^{\infty} A e^{-|x|} dx &= 2 \int_0^{\infty} A e^{-x} dx = -2A e^{-x} \Big|_0^{\infty} \\
 &= 2A = 1
 \end{aligned}$$

$$A = \frac{1}{2}$$

$$c2) F(x) = \int_{-\infty}^x \frac{e^{-|x|}}{2} dx$$

$$\begin{aligned}
 x \geq 0 \quad F(x) &= \frac{1}{2} + \int_0^x \frac{e^{-x}}{2} dx \\
 &= 1 - \frac{e^{-x}}{2}
 \end{aligned}$$

$$x < 0 \quad F(x) = \int_{-\infty}^x \frac{e^x}{2} dx = \frac{e^x}{2}$$

$$\begin{aligned}
 c3) P\{x \in [-1, 2]\} &= F(2) - F(-1) \\
 &= 1 - \frac{1}{2e^2} - \frac{1}{2e}
 \end{aligned}$$

$$\text{v. } P(X=0) = \frac{C_{12}^5}{C_{15}^5} = \frac{24}{91}$$

$$P(X=1) = \frac{C_{12}^4 \cdot C_3^1}{C_{15}^5} = \frac{45}{91}$$

$$P(X=2) = \frac{C_{12}^3 \cdot C_3^2}{C_{15}^5} = \frac{20}{91}$$

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$$P(X=3) = \frac{C_{12}^2 \cdot C_3^3}{C_{15}^5} = \frac{2}{91}$$

$$E(X) = \sum_{k=0}^3 k P(X=k) = 1$$

$$\text{v. } E(X) = \int_{-\infty}^{\infty} x \frac{1}{2} e^{-|x|} dx = 0$$

$$\begin{aligned} D(X) &= E\{[X - E(X)]^2\} = E(X^2) = \int_{-\infty}^{\infty} x^2 \frac{1}{2} e^{-|x|} dx \\ &= \int_0^{\infty} x^2 e^{-x} dx \\ &= -x^2 e^{-x} + 2x e^{-x} - 2e^{-x} \Big|_0^{\infty} \\ &= 2 \end{aligned}$$