

Simple example

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1 Hello

This is a simple example using the $\text{H}\text{A}\text{T}\text{E}\text{X}$ library and some math stuff.

1.1 Arithmetics with infix operators

$4^{(2^3)^2} - 10000 \cdot 10000 \cdot (10000 \cdot 10000) \cdot (10000 \cdot 10000 \cdot 10000)$
is $3.40282 \cdot 10^{38}$. For $x = 19$ and $\tau = 2 \cdot \pi$,

$$2 + 7 \cdot (6 - \tau) - e^{5 - \sqrt{x^2 + \frac{4}{\pi}}} \approx 1.7702 \cdot 10^{-2}.$$

1.2 Simple finite sums

$$\sum_{n \in \{0, 1, 4, 5\}} \frac{5}{2} - n = 0$$

$$\sum_{n=1}^4 \frac{5}{2} - n = 0$$

$$\sum_{j=1}^{40} \cos\left(\frac{2 \cdot \pi}{40} \cdot j\right) \approx -2.6645 \cdot 10^{-15}$$

$$2 \cdot \sum_{i=1}^6 i^2 + i = 224$$

$$\left(\sum_{i=1}^6 i^2 + i\right) \cdot 2 = 224$$

$$\left(\sum_{i=1}^6 i^2 + i\right) + 2 = 114$$

1.3 Checking some simple identities

$$\arcsin(\sin(\arccos(\cos(\arctan(\tan 0)))))$$

is 0,

$$\operatorname{arcsinh}\left(\sinh\left(\operatorname{arccosh}\left(\frac{\cosh(\operatorname{arctanh}(\tanh 0))}{2}\right)\right)\right)$$

is not. (Test passed.)

A simple equations chain:

$$\begin{aligned}10^{18} &= 10^9 \cdot 10^9 \\ &= 10^{3^2} \cdot 10^5 \cdot 10^4 \\ &= 1000000000000000000.\end{aligned}$$

(Test passed.)

Another equations chain, this time using floats:

$$\begin{aligned}10^{-18} &= 10^{-9} \cdot 10^{-9} \\ &= 10^{-(3^2)} \cdot 10^{-5} \cdot 10^{-4} \\ &= \frac{1}{1000000000000000000}.\end{aligned}$$

Test failed. Even true mathematical identities may not show to hold when using floating-point arithmetics.

Equation-chains can also be approximate (“rough”):

$$\begin{aligned}10^{-18} &\approx 10^{-9} \cdot 10^{-9} \\ &\approx 10^{-(3^2)} \cdot 10^{-5} \cdot 10^{-4} \\ &\approx \frac{1}{999236372934876337}.\end{aligned}$$

(Test passed.)