ASSIGNMENT 10: Linear and Circular Convolution

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1 Brief Up:

The tasks of this assignment is the following:

- Realising linear and circular convolutions
- Using circular convolution to implement linear convolution
- Autocorrelation of Zadoff-Chu Sequence

2 plotting function:

```
def plot_fun(x,y,x1='w',y1='Magnitude',t1='xyz'):
    plot(x,y)
    xlabel(x1)
    ylabel(y1)
    title(t1)
    grid(True)
    show()
```

3 Interpreting the filter:

We use freqz to convert the given filter from the time domain to the frequency domain.

```
details =np.zeros(12)
i = 0
with open("h.csv", 'r') as file:
    for line in file:
        details[i] = float(line)
        i+=1
w,h = sig.freqz(details)
```

 $\begin{array}{l} plot_fun\left(w,abs\left(h\right),\,'w'\,,\,'Magnitude'\,,\,'Low_pass_filter'\right)\\ plot_fun\left(w,angle\left(h\right),\,'w'\,,\,'Phase'\,,\,'Low_pass_filter'\right) \end{array}$ The plots obtained represent an LPF

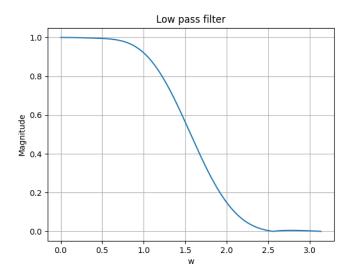


Figure 1: Magnitude plot of transfer function of filter

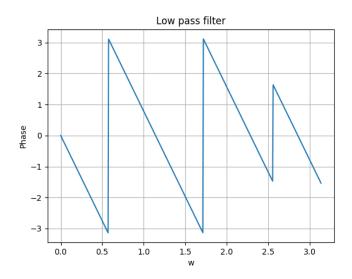


Figure 2: Phase plot of transfer function of filter

4 Generating given signal:

We generate the input signal given.

```
\begin{array}{ll} n = \operatorname{arange}\left(2**10\right) \\ x = \cos\left(0.2*\operatorname{pi}*n\right) + \cos\left(0.85*\operatorname{pi}*n\right) \\ \operatorname{plot}_{-}\operatorname{fun}\left(n,x,'n','\operatorname{Amplitude}','\operatorname{Input\_signal}'\right) \end{array}
```

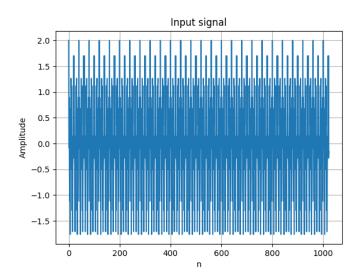


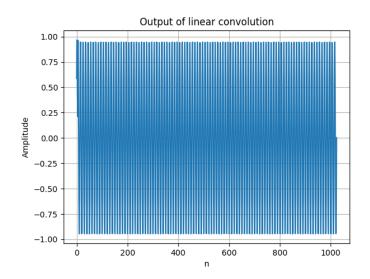
Figure 3: Fourier transform

5 Linear convolution:

We do linear convolution using the formula

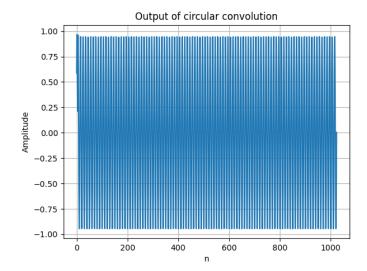
$$y[n] = \sum_{k=0}^{n-1} x[n-k]h[k]$$
 (1)

```
 \begin{array}{lll} y = & np.\,zeros\left(\textbf{len}\left(x\right)\right) \\ \textbf{for } i & \textbf{in } arange\left(\textbf{len}\left(x\right)\right); \\ & \textbf{for } k & \textbf{in } arange\left(\textbf{len}\left(\text{details}\right)\right); \\ & y\left[i\right] + = & x\left[i - k\right] * \det ails\left[k\right] \\ plot_fun\left(n,y,'n','Amplitude','Output\_of\_linear\_convolution') \end{array}
```



6 Circular Convolution:

To solve this more efficiently we shift to circular convolutions, where we convert to the frequency domain, multiply and go back to the time domain.

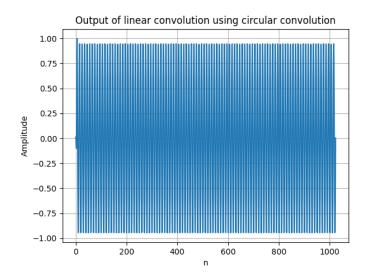


7 Linear convolution using circular convolution:

- We observe that this efficient solution is non causal and requires the entire signal to perform a convolution.
- So, We implement a linear method of circular convolution so that we need not depend on the next infinite values in the input but only a finite number of values(this is still non causal but the delay in the response is lower)

```
def circular_conv(x,h):
    P = len(h)
    n_ = int(ceil(log2(P)))
    h_ = np.concatenate((h,np.zeros(int(2**n_)-P)))
    P = len(h_)
    n1 = int(ceil(len(x)/2**n_))
    x_ = np.concatenate((x,np.zeros(n1*(int(2**n_))-len(x))))
    y = np.zeros(len(x_)+len(h_)-1)
    for i in range(n1):
        temp = np.concatenate((x_[i*P:(i+1)*P],np.zeros(P-1)))
        y[i*P:(i+1)*P+P-1] += np.fft.ifft(np.fft.fft(temp) * np.fft.fft(return y)
```

plot_fun(n, real(y[:1024]), 'n', 'Amplitude', 'Output_of_linear_convolution_u



8 Correlation of Zadoff Chu Sequence:

We analyse the Zadoff Chu Sequence which has the following properties:

- complex sequence,
- constant amplitude sequence,
- The auto correlation of a Zadoff–Chu sequence with a cyclically shifted version of itself is zero,
- Correlation of Zadoff–Chu sequence with the delayed version of itself will give a peak at that delay.t

The output obtained for correlation with a shifted version of itself was completely in line with these properties Given above. This is what we should graphically show.

```
lines = []
with open("x1.csv", 'r') as file 2:
    csvreader = csv.reader(file2)
    for row in csvreader:
        lines.append(row)
lines2 = []
for line in lines:
    line = list(line[0])
        line [line.index('i')]='j'
        lines2.append(line)
    except ValueError:
        lines 2. append (line)
        continue
x = [complex(''.join(line)) for line in lines2]
x2 = np.roll(x,5)
cor = np.fft.ifftshift(np.correlate(x2,x,'full'))
x \lim (0, 25)
plot_fun(linspace(0,len(cor)-1,len(cor)),abs(cor),'t','Correlation','auto
```

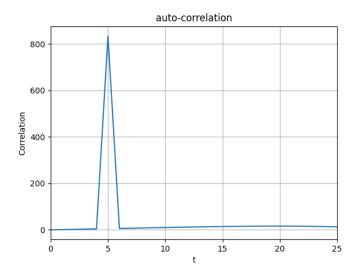


Figure 4: Correlation between Zadoff Chu Sequence and its 5samples shifted version

9 Conclusion:

- We implemented different algorithms for convolution.
- We see that using circular convolution to figure out linear convolution is more efficient.
- We see that the peak is obtained at the nth sample is the zadoff sequence is correlated with its nth sample shifted version.