

M_1 , $\theta = \epsilon_1 - \alpha \rightarrow \beta - \theta - M$ chart \rightarrow betad function to get β .

$$M_{n,1u} = M_1 \sin(\beta) \quad M_{n,1L} = M_1 \sin(\beta)$$

$$\left[M_{n,2}, \frac{P_2}{P_1} \right] = \text{flownormalshock}(\gamma, M_{n,1u})$$

$$\left[M_{n,4}, \frac{P_4}{P_1} \right] = \text{,,}$$

$$\text{from PM table at } [M_2, M_4] = \frac{1}{\sin(\beta - \theta)} \left[\frac{M_{n,2}}{M_{n,4}} \right] \quad \theta_1 = \epsilon_1 - \alpha$$

$$[V_{13}, V_{15}] = \text{flowprandtlmeyer}(\gamma, [M_2, M_4])$$

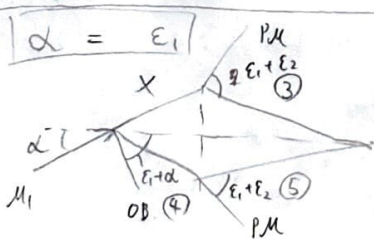
$$[V_{23}, V_{25}] = \theta_1 + [V_{13}, V_{15}] \rightarrow [M_3, M_5] = \text{flowprandtlmeyer}(\gamma, [V_{23}, V_{25}], 'mu')$$

from isentropic table, goal: $\frac{P_3}{P_1}, \frac{P_5}{P_1}$

$$\frac{P_3}{P_1} = \frac{P_3}{P_{03}} \cdot \underbrace{\frac{P_{03}}{P_{02}}}_{=1} \cdot \frac{P_{02}}{P_2} \cdot \frac{P_2}{P_1} \quad \left[\frac{P_{02}}{P_2}, \frac{P_{03}}{P_3}, \frac{P_{04}}{P_4}, \frac{P_{05}}{P_5} \right] = \text{flowisentropic}(\gamma, [M_2, M_3, M_4, M_5])$$

$$\frac{P_5}{P_1} = \frac{P_5}{P_{05}} \cdot \underbrace{\frac{P_{05}}{P_{04}}}_{=1} \cdot \frac{P_{04}}{P_4} \cdot \frac{P_4}{P_1}$$

$$C_N = \frac{1}{\gamma M_1^2} \left[\frac{P_4}{P_1} - \frac{P_2}{P_1} + \frac{P_5}{P_1} - \frac{P_3}{P_1} \right] \quad C_A = \frac{1}{\gamma M_1^2} \left[\left(\frac{P_2}{P_1} + \frac{P_4}{P_1} \right) \tan(\epsilon_1) + \left(\frac{P_3}{P_1} + \frac{P_5}{P_1} \right) \tan(\epsilon_2) \right]$$



$$M_1, \theta = \alpha + \epsilon_1 \rightarrow \beta - \theta - M \quad [\beta] = \text{betad}(\quad)$$

$$M_{n,1L} = M_1 \sin(\beta)$$

$$\left[M_{n,4}, \frac{P_4}{P_1} \right] = \text{flownormalshock}(\gamma, M_{n,1L})$$

$$\text{from PM table at } [M_1, M_4] = \left[M_1, \frac{M_{n,4}}{\sin(\beta - \theta)} \right]$$

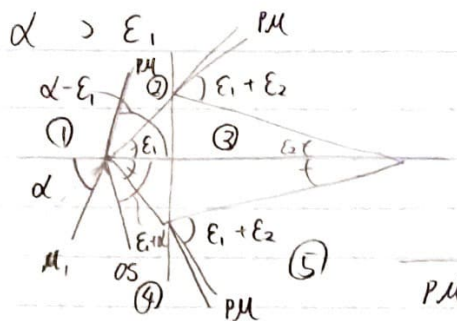
$$[V_{13}, V_{15}] = \text{flowpm}(\gamma, [M_1, M_4])$$

$$[V_{23}, V_{25}] = [\theta_1] + [V_{13}, V_{15}] \rightarrow [M_3, M_5] = \text{flowpm}(\gamma, [V_{23}, V_{25}], 'mu')$$

from isentropic table, goal $\frac{P_3}{P_1}, \frac{P_5}{P_1}$

$$\alpha > 0 \quad \frac{P_5}{P_1} = \frac{P_5}{P_{05}} \cdot \frac{P_{05}}{P_{04}} \cdot \frac{P_{04}}{P_4} \cdot \frac{P_4}{P_1} \quad \frac{P_3}{P_1} = \frac{P_3}{P_{03}} \cdot \frac{P_{03}}{P_{01}} \cdot \frac{P_{01}}{P_1} \quad \left[\frac{P_{01}}{P_1}, \frac{P_{03}}{P_3}, \frac{P_{04}}{P_4}, \frac{P_{05}}{P_5} \right] = \text{flowisentropic}(\gamma, [M_1, M_3, M_4, M_5])$$

$$\alpha < 0 \quad \frac{P_5}{P_1} = \frac{P_5}{P_{05}} \cdot \frac{P_{05}}{P_{01}} \cdot \frac{P_{01}}{P_1} \quad \frac{P_3}{P_1} = \frac{P_3}{P_{03}} \cdot \frac{P_{03}}{P_{02}} \cdot \frac{P_{02}}{P_2} \cdot \frac{P_2}{P_1} = 1$$



$$M_1, \theta = \epsilon_1 + \alpha \rightarrow [\beta] = \text{betad}()$$

$$M_{n,1L} = M_1 \sin(\beta)$$

$$[M_{n,4}, \frac{P_4}{P_1}] = \text{flowns}(\gamma, M_{n,1L})$$

$$M_4 = M_{n,4} / \sin(\beta - \theta)$$

PM Exp. (1)-(2).

$$V_{11} = \text{flowpm}(\gamma, M_1)$$

$$V_{12} = \theta_{2,4} + V_{11} \rightarrow M_2 = \text{flowpm}(\gamma, V_{12}, 'mu')$$

now I got M_2 , & M_4 , get M_3 & M_5 to find necessary pressure ratios

from PM table at $[M_2, M_4]$

$$[V_{13}, V_{15}] = \text{flowpm}(\gamma, [M_2, M_4])$$

$$[V_{23}, V_{25}] = \theta + [V_{13}, V_{15}]$$

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$$[M_3, M_5] = \text{flowpm}(\gamma, [V_{23}, V_{25}], 'mu')$$

$$\left[\frac{P_{01}}{P_1}, \frac{P_{02}}{P_2}, \frac{P_{03}}{P_3}, \frac{P_{04}}{P_4}, \frac{P_{05}}{P_5} \right] = \text{flowisentropic}(\gamma, [M_1, M_2, M_3, M_4, M_5])$$

when $\alpha > 0$

$$\frac{P_2}{P_1} = \frac{P_2}{P_{02}} \cdot \underbrace{\frac{P_{02}}{P_{01}}}_{=1} \cdot \frac{P_{01}}{P_1}$$

$$\frac{P_3}{P_1} = \frac{P_3}{P_{03}} \cdot \underbrace{\frac{P_{03}}{P_{02}}}_{=1} \cdot \underbrace{\frac{P_{02}}{P_{01}}}_{=1} \cdot \frac{P_{01}}{P_1}$$

$$\frac{P_4}{P_1} \text{ from NS relations}$$

$$\frac{P_5}{P_1} = \frac{P_5}{P_{05}} \cdot \underbrace{\frac{P_{05}}{P_{04}}}_{=1} \cdot \frac{P_{04}}{P_4} \cdot \frac{P_4}{P_1}$$

when $\alpha < 0$

$$\frac{P_2}{P_1} \text{ from NS relations}$$

$$\frac{P_4}{P_1} = \frac{P_4}{P_{04}} \cdot \frac{P_{04}}{P_{01}} \cdot \frac{P_{01}}{P_1}$$

$$\frac{P_3}{P_1} = \frac{P_3}{P_{03}} \cdot \frac{P_{03}}{P_{02}} \cdot \frac{P_{02}}{P_2} \cdot \frac{P_2}{P_1}$$

$$\frac{P_5}{P_1} = \frac{P_5}{P_{05}} \cdot \frac{P_{05}}{P_{01}} \cdot \frac{P_{01}}{P_1}$$

$$y_1 = \frac{v}{c_1} x$$

$$= \frac{\tan(\epsilon_1) \tan(\epsilon_2)}{\tan(\epsilon_2)} x$$

$$v(x) = \begin{cases} \tan(\epsilon_1) x & 0 \leq x < c_1 \\ v - \tan(\epsilon_2)(x - c_1) & c_1 \leq x \leq c \end{cases}$$

$$\frac{dv(x)}{dx} = \begin{cases} \tan(\epsilon_1) & 0 \leq x < c_1 \\ -\tan(\epsilon_2) & c_1 \leq x \leq c \end{cases}$$

$$\int_0^c \frac{1}{c} \left[\int_0^{c_1} \tan(\epsilon_1)^2 dx + \int_{c_1}^c -\tan(\epsilon_2)^2 dx \right] dx$$

$$= \frac{1}{c} \left[\tan(\epsilon_1)^2 x \Big|_0^{c_1} - \tan(\epsilon_2)^2 x \Big|_{c_1}^c \right]$$

$$= \frac{c_1}{c} \tan^2(\epsilon_1) - \tan^2(\epsilon_2) + \frac{c_1}{c} \tan^2(\epsilon_2)$$



$$\frac{dv(x)}{dx} = \tan(x) - \frac{v(x)}{x}$$