# Working our way through your requests for folks to interview:

(We did request Oski and have not yet gotten a reply)

Any requests for people to interview from 1:0small-1:10 in the future? e.g., (listed in order of how likely it is that we can convince them to come) cs61a TAs, other CS faculty, other Berkeley faculty, anyone

A random student from the crowd



# Submit questions: pollev.com/cs61a

#### Rules of engagement:

Can say "pass" at any time!

# Tree Recursion





#### How to Know That a Recursive Case is Implemented Correctly

**Tracing:** Diagram the whole computational process (only feasible for very small examples) **Induction:** Check that f(n) is correct as long as f(n-1) ... f(0) are. (*This the recursive leap of faith.*) (**Abstraction!**)

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#### Discussion Review: Hailstone

```
• If n is even, divide it by 2
 • If n is odd, multiply it by 3
  and add 1

    Repeat until n is 1.

    Print out the values and return

  the number of steps
>>> a = hailstone(10)
10
16
8
4
2
1
```

```
def hailstone(n):
    """Print out the hailstone sequence
    starting at n, and return the number of
    elements in the sequence."""
    print(n)
    if n % 2 == 0:
        return even(n)
    else:
        return odd(n)
def even(n):
    return hailstone(n // 2) + 1
def odd(n):
    if n == 1:
        return 1
    return hailstone(n * 3 + 1) + 1
```

### Spring 2024 Midterm 1 Question 4(e)

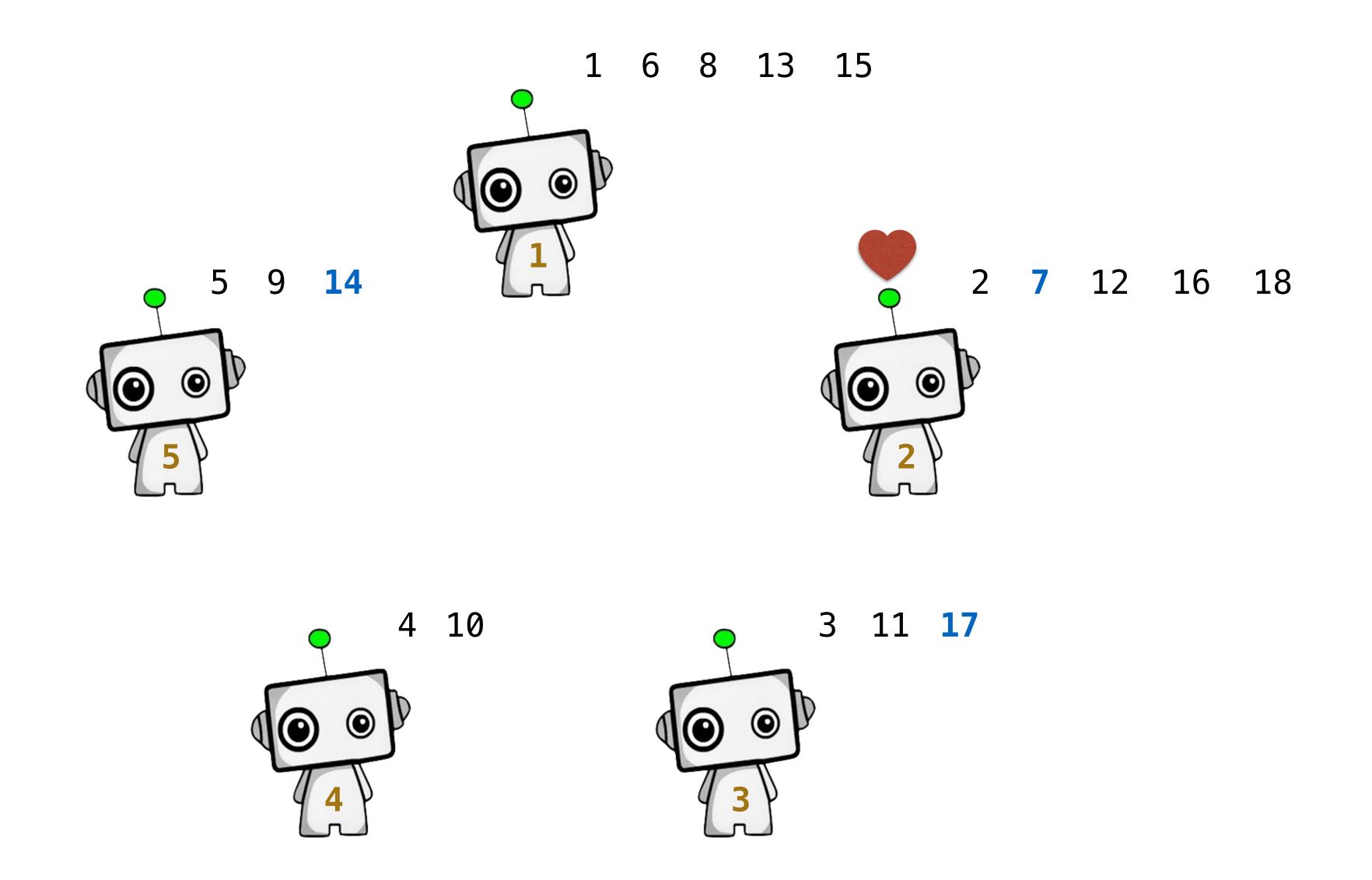
**Definition.** A dice integer is a positive integer whose digits are all from 1 to 6. def streak(n): """Return whether positive n is a dice integer in which all the digits are the same. >>> streak(22222) True >>> streak(4) True >>> streak(22322) # 2 and 3 are different digits. False >>> streak(99999) # 9 is not allowed in a dice integer. False 111111 return (n >= 1 and n <= 6) or (n > 9 and n % 10 == n // 10 % 10 and streak(n // 10)

Idea: In a streak, every digit except the last is a streak, and the last matches

Idea (iterative): In a streak, all pairs of adjacent digits are equal.

Discussion Review: Sevens

Players in a circle count up from 1 in the clockwise direction. If a number is divisible by 7 or contains a 7 (or both), switch directions. With 5 players, who says 18?



#### The Game of Sevens

Players in a circle count up from 1 in the clockwise direction. If a number is divisible by 7 or contains a 7 (or both), switch directions. If someone says a number when it's not their turn or someone misses the beat on their turn, the game ends.

Implement sevens(n, k) which returns the position of who says n among k players.

- 1. Pick an example input and corresponding output.
- 2. Describe a process (in English) that computes the output from the input using simple steps.
- 3. Figure out what additional names you'll need to carry out this process.
- 4. Implement the process in code using those additional names.

```
n: the final number
k: how many players
i: the current number
who: the current player
direction: who's next
```

(Demo)



#### Mutually Recursive Functions

```
Two functions f and g are mutually recursive if f calls g and g calls f.
def unique_prime_factors(n):
                                                           def smallest_factor(n):
    """Return the number of unique prime factors of n.
                                                               "The smallest divisor of n above 1."
    >>> unique_prime_factors(51) # 3 * 17
    >>> unique_prime_factors(9) # 3 * 3
    >>> unique_prime_factors(576) # 2 * 2 * 2 * 2 * 2 * 2 * 3 * 3
    111111
                                      Find the smallest
                                                              Keep removing that factor until
    k = smallest_factor(n)
                                        (prime) factor
                                                                only other factors are left
    def no_k(n):
        "Return the number of unique prime factors of n other than k."
                                                                             And then count the
        if n == 1:
                                                                           prime factors of that
           return 0
        elif n % k != 0:
                                                                     what remains
                                                          count
                   unique_prime_factors(n)
                                                                          576
        else:
                                                              (k = 2)
           return no_k(n // k)
                                                            2 (k = 3)
    return 1 + no_k(n)
```



### **Counting Partitions**

The number of partitions of a positive integer n, using parts up to size m, is the number of ways in which n can be expressed as the sum of positive integer parts up to m in increasing order.

$$1 + 5 = 6$$
 5 > m (4)

$$4 + 2 = 6$$
 Decreasing order

$$2 + 4 = 6$$

$$1 + 1 + 4 = 6$$

$$3 + 3 = 6$$

$$1 + 2 + 3 = 6$$

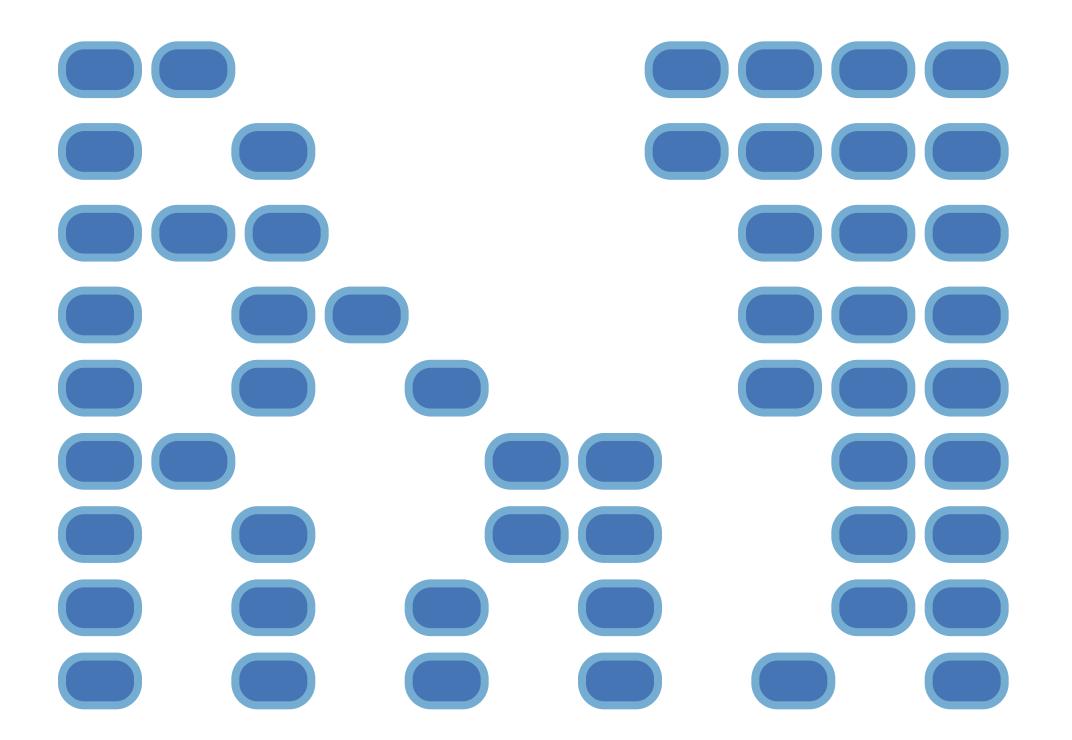
$$1 + 1 + 1 + 3 = 6$$

$$2 + 2 + 2 = 6$$

$$1 + 1 + 2 + 2 = 6$$

$$1 + 1 + 1 + 1 + 2 = 6$$

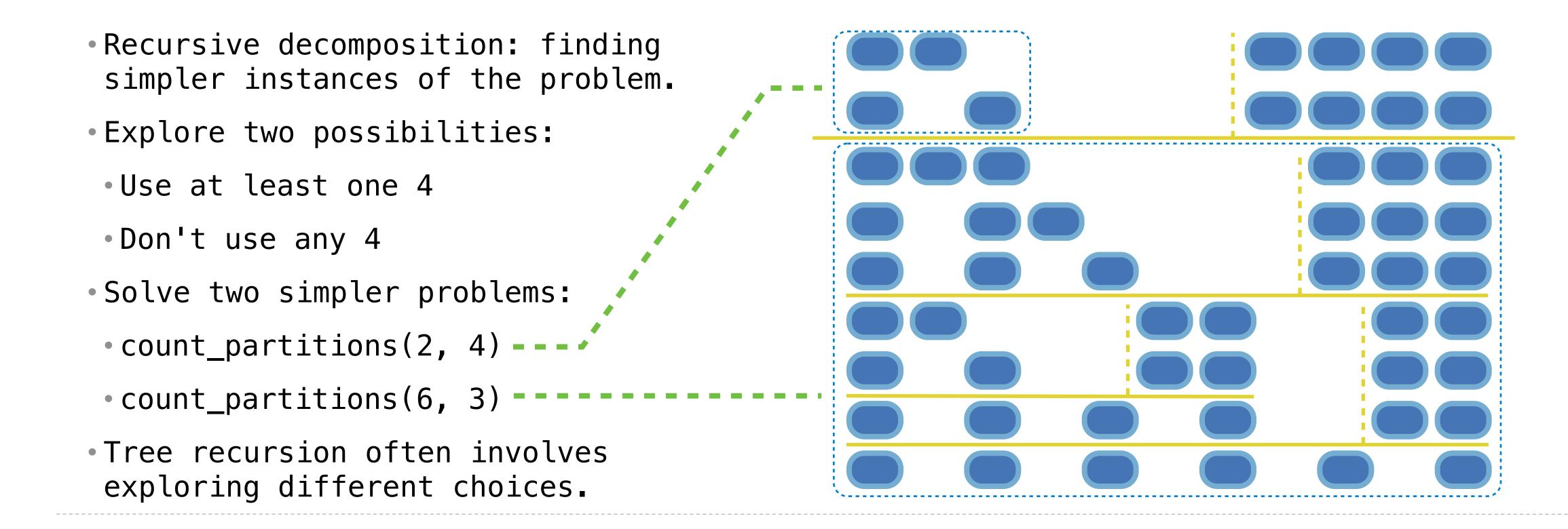
$$1 + 1 + 1 + 1 + 1 + 1 = 6$$



### **Counting Partitions**

The number of partitions of a positive integer n, using parts up to size m, is the number of ways in which n can be expressed as the sum of positive integer parts up to m in non-decreasing order.

count\_partitions(6, 4)



## **Counting Partitions**

Tree recursion often involves

exploring different choices.

The number of partitions of a positive integer n, using parts up to size m, is the number of ways in which n can be expressed as the sum of positive integer parts up to m in increasing order.

```
def count partitions(n, m):
                                             if n == 0:

    Recursive decomposition: finding

simpler instances of the problem.
                                                 return 1 # We found a way
                                             elif n < 0:
Explore two possibilities:
                                                 return 0 # We counted too many

    Use at least one 4

                                             elif m == 0:
                                                 return 0 # We didn't count enough
Don't use any 4

    Solve two simpler problems:

                                             else:
                                             with_m = count_partitions(n-m, m)
count_partitions(2, 4) ---
                                                 without m = count partitions(n, m-1)
count_partitions(6, 3) -----
                                                 return with m + without m
```

(Demo)