

1. 应用冲激信号的抽样特性 筛选特性),求下列表示式的<u>函数值</u>。

(1) 
$$\int_{-\infty}^{\infty} f(t-t_0)\delta(t)dt = \int (t-t_0) \Big|_{t=0} = \int [-t_0]$$

(2) 
$$\int_{-\infty}^{\infty} f(t_0 - t)\delta(t)dt = \int (t_0 - t)\Big|_{t=0} = \int (t_0)$$

(3) 
$$\int_{-\infty}^{\infty} \delta(t - t_0) u(t - 2t_0) dt = u(t - 2t_0) \Big|_{t=t_0} = u(t - t_0) = \begin{cases} 0 & t > 0 \\ 1 & t \leq 0 \end{cases}$$

$$(4) \int_{-\infty}^{\infty} (t+\sin t)\delta(t-\frac{\pi}{6})dt = (t+\sin t)\left|_{t=\frac{\pi}{6}} = \frac{1}{2} + \frac{\pi}{6}\right|$$

(5) 
$$\int_{-\infty}^{\infty} e^{-j\omega t} [\delta(t) - \delta(t - t_0)] dt$$

$$= \int_{-\infty}^{\infty} e^{-iwt} S(t) dt - \int_{-\infty}^{\infty} e^{-iwt} S(t-t_0) dt = e^{0} - e^{-iwt_0} = |-e^{-iwt_0}|$$

2. 判断信号  $f(t) = 2\cos(10t + 5) - \sin(6t - 3)$  是否为周期信号(要求写出步骤)? 如是周期信号,计算f(t)的基波周期。

用 2605 (10tt5) 
$$T_1 = \frac{26}{6} = \frac{5}{5}$$
  $\frac{T_1}{T_2} = \frac{3}{5}$  为有理数,  $-\sin(6t-3)$  ·  $T_2 = \frac{26}{5} = \frac{5}{3}$  故 ftt) 是周期信号

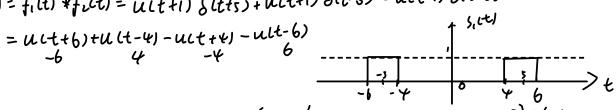
fu的基波周期为 T. T. 的最大公的数十二元

3. 已知信号 $f_1(t) = u(t+1) - u(t-1)$ ,  $f_2(t) = \delta(t+5) + \delta(t-5)$ , 画出下列各卷积 计算表积积分 波形。

(1) 
$$s_1(t) = f_1(t) * f_2(t)$$

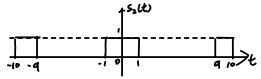
$$(2) \ s_2(t) = \{ [f_1(t) * f_2(t)] [u(t+5) - u(t-5)] \} * f_2(t)$$
 fit - ti) \*  $\{ (t-t_1) * (t-t_2) = f(t-t_1-t_2) \}$ 

発. 相談いい siti=fiti\*fiti= ult+1) bltts)+ ult+1) blt-5> - ult-1) blt+5)- ult-1) blt+5)



(2) Sitt) = / Sitt)[u(t+5)-u(t-5)] \* filt)= {[ Sitt u(t+5)]-[sitt) u(t-5)] } \*filt) =[[u(++5)+u(t-+) - u(t++) - u(t-6)]-[u(t-5)-u(t-6)]\*fict)

- = Utto) + ultt1) ulttq) ult) + ult+ ult-9)-ult-1) ult-10)
- = ultto)-u(t+9) +ult+1) -u(t-1)+ult-9)-u(t-10)



- 4. 证明: sin(t), sin(2t), ..., sin(nt) (n为正整数)是在区间(0, $2\pi$ )的正交函数集。
- 然后回答: (1) 该函数集在区间 $(0,2\pi)$ 是否为完备的正交函数集,为什么?

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(2) 该函数集在区间 $\left(0,\frac{\pi}{2}\right)$ 是否为正交函数集,为什么?

(所有证明和计算都要求写出具体步骤)

VEOR 只需证 「Sin (dt) sin(ft)dt = O bd、β 6 Zt, dt sin (kt) sin (kt) dt +0 和用 sin AsinB= 之[ws(A-B)-ws(A+B)]原式= = = ( ws/d-B)tdt-= 1 ( ws/d-B)tdt 其中, ld-月, dt 的正整数数 b>b-月t T=20 , vos(dtp)t·T=200 积分区间 (0,2人)为 下、下的整数任而经函数在单个周期上的积分零(对种性) ⇒原式=ロ

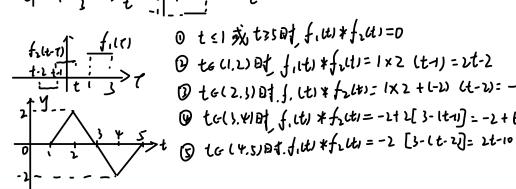
 $\int_{0}^{2\pi} \sin(kt) \sin(kt) dt = \frac{1}{2} \int_{0}^{2\pi} (1 - \omega_{5} 2kt) dt = \pi - \frac{1}{2} \int_{0}^{2\pi} \omega_{5} 2kt dt = \pi + 0$ 人人而, 多正数集在10,1人)为正交函数集

U) 不是 ( Sint wit dt = = 1 ( w sin2t dt = = 4 ws2t | = -4 ( ws4x-ws0) = D

说明在区间(0,2元)内, sint与Gst正交效(sint. sinnt)在(0,以)内很完备的正交函数集

UL) 程,  $\int_0^{\frac{\pi}{2}} \sin t \sin \lambda t dt = \frac{1}{2} \int_0^{\frac{\pi}{2}} \cos(t) dt - \frac{1}{2} \int_0^{\frac{\pi}{2}} \cos(t) dt - \frac{1}{2} \int_0^{\frac{\pi}{2}} \sin t \sin \lambda t dt = \frac{1}{2} - \frac{1}{6} \int_0^{\frac{\pi}{2}} \cos(t) dt - \frac{1}{2} \int_0^{\frac{\pi}{2}} \sin t \sin \lambda t dt = \frac{1}{2} - \frac{1}{6} \int_0^{\frac{\pi}{2}} \cos(t) dt - \frac{1}{2} \int_0^{\frac{\pi}{2}} \sin t \sin \lambda t dt = \frac{1}{2} - \frac{1}{6} \int_0^{\frac{\pi}{2}} \cos(t) dt - \frac{1}{2} \int_0^{\frac{\pi}{2}} \sin t \sin \lambda t dt = \frac{1}{2} - \frac{1}{6} \int_0^{\frac{\pi}{2}} \cos(t) dt - \frac{1}{2} \int_0^{\frac{\pi}{2}} \cos(t) dt - \frac{1}{2} \int_0^{\frac{\pi}{2}} \sin(t) dt - \frac{1}{2} \int_0^{\frac{\pi}{2}} \sin(t)$ 说明区间(0.至)中. sint与sinzt不正交 故该函数集在10,至,不是正交函数集

5. 已知连续信号
$$f_1(t) = \begin{cases} 2, & 1 < t < 3 \\ 0, & \text{其他} \end{cases}$$
,  $f_2(t) = \begin{cases} 1, & 0 < t < 1 \\ -1, & 1 < t < 2 \\ 0, & \text{其他} \end{cases}$  (1) 求卷积函数 $y(t) = f_1(t) * f_2(t)$ ,并画出其概略图。



- 1 to(2.5) 01 1, (t) \* f2(+)= 1x2+(-1) (t-2)=-2+6
- @ to().418 f. it) \*frui=-2+2[3-141]=-2+6-2++2=6-2+

法=・fit)=2[u(t-1)-u(t-3)] fi(t)=u(t)-2u(t-1)+u(t-2) filti \* fz(t)= atfilt) \* [+ f(t) to f(t) dT=2[8(t-1)-8(t-1)] \* [r(t)-2r(t-1)+r(t-2)] =2/81t-1)r(t)-28(t-1)r(t-1)+8(t-1)r(t-2)-8(t-3)r(t)+28(t-3)r(t)-8(t-3)r(t-2)) = 2[r(t-1)-2r(t-2)+r(t-3)-r(t-3)+2r(t-4)-r(t-5)] =2[r(t-1)-2r(t-2)+2r(t-4)-r(t-5)] 图同上