The total fun = a'x st = a for x'a st = a 16. Pual cones of the total. this set is convex. x+5255, if 知证从的对隔部的 k* 2.美人ご本志師: minfo(XO=IIAX-bll; x+y 65, for all y 65. Therefore 1x1x+52 65, |= n. 5x | x y y 65, |= n (5, -y) 14:11x113=x7x =>114x-6113=(Ax-6)*(Ax-6) 126+1; K=R+; K=R+, K=S+, K=S+ the intersection of convex sets Si-y. =x1A1Ax-2x1A16+66 3fe=2A1Ax-2A16=0 K= (x, t) | ||x1/1, st | : K+= (x, t) | ||x1/1, st | =>x = (ATA) ATB. 340 = 2ATA. (ATA70) k= {(x,t) | 11x41 5t] : k*= {(x,t) | 4x1 00 5t} 05051 The set is convex, in fact a 阿此是中的水水 相美地画:の用はははいいのでは、例のの見 ball. 「xl ||x-a||x-b||x-b||x] * LONG TATO: FUE X'ATAX & TONG CIR (By induction Albinia) XTATAX = |AXII, TO STATE HAX , WATATO illustrate the idea for kes (\$151). illustrate the idea for k=3 (\$154). If $\theta=1$, this is a half-space. If $\theta<1$, it is If f(x,y) is convex in x for each $y \in A$, then $\theta_1, \theta_2, x_3 \in A$. ($\theta_1, \theta_2, \theta_3 \in A$) as a left $\theta_1, \theta_2, \theta_3 \in A$. So at least one of the θ_1 with center x_0 and radius $x_0 \in A$ given by $x_0 \in A$ for $x_1 \in A$ for $x_1 \in A$ for $x_2 \in A$ for $x_1 \in A$ for $x_2 \in A$ for $x_1 \in A$ for $x_1 \in A$ for $x_2 \in A$ for $x_2 \in A$ for $x_1 \in A$ for $x_2 \in A$ for $x_2 \in A$ for $x_1 \in A$ for $x_2 \in A$ for $x_2 \in A$ for $x_1 \in A$ for $x_2 \in$ 4. Affine see 1万朋本 · 原理过去,x1、x2、数量成份x至x分下达形别: x=0x+(1-0)x, (OCR) 这处、两点的有线也老在此部分,即为方面茶 (3) [x|AX=b] 小山地域 dom f is convex set 江水城北山 x,ycdomf, 050ミ Mr=62/(1-8,) and M3=83/(1-8.) NA, M3>0 方别从却可以用代偿在租赁的的产业表示。 we know 10+112=01+03=1. C is convex 6. 凸k:Convex set 取行的全型两点连起的现在现在这个块层内。 [x|11x-a11/5|1x-b1]> 11x-a11; 511x-b1] 2. 14 577 Restriction of a Convex function =>(x-a) (x-a) = (x-b) (x-b) x1, x, 6€, 05851 => 8x1+(1-8)x, 6€ a line の当地は、x=も、x+も、x+・・・・+もたな ⇒xx-22x+2+2+2×xx-26x+6+6 f: R">R is convex if and only if the => 2(b-a) x < b b-ata the see is indeed の出る:日子東に参い的と集合 〇 〇 a helfspace. and when ||x-a||_ = ||x-b||_y the point that are equidistant to a and in t for any x Edomf is convex to a year of your by a hilber lane where a holfspace and when 11x-211x = 11x-611x 7. 53 Convex cone. base given by a hyperplane whose normal is in the direction b-a 和祖子:x=8,x+8,x,(6,70,8,70) 也即即为所在三時前後子18左其中 3. First-order condition-17,349 S. Hyperphies and holf-paces. Sing #210

Otto () (a/o)

Otto () (a/o) f is differentiable if domf is open ③ WACH 的多一种方式。 C=1XER* X AX HJX + C SO! A65". is William A>O. 那以C是当集解: A see is convex if and only if its intersection with an arbitrary line and the gradient vf(x) exists spen of f(y) > f(x) + v f(x) (y-x) for all x, y edop O丰沙河·河×加×sbj(a+0) ②李宇间可以ATX至的(a≠0) 高级的 即山村的集下、当钱于是西马钱 atx=6, atx=6, atx-atx=0=0=) at(x-x=)=0 r=c+bx+xAx. Then the intersection is strictly convex. to ellipsoid 科為國籍 of a wish the line defined by & and v JELIX-XC) TP (X-XC) SI) with PEST # : = + + = = [y] [0' 6] [y] ≤ I 另一种新为流和了:[Xc+Au[IIII]以 がたいますないでは、Norm ball and cones &=9Tは、E=9Tをお、Assume 名とは、E=0convex for any A. のでは、「スールーンでは、アールーンでは、「スールーンでは、「スールーンでは、「スールーンでは、「スールーンでは、「スールーンでは、「スールーンでは、「スールーンでは、「スールーンでは、「スールーンでは、アールーンでは、「スールーンでは、アールーンでは、「スールーンでは、アールーンでは 范数码和范数领荷是巴的 92++V | dt + pt+ r <0, 8t=0| convex for you 12.多面接 Polyhedra Axxb, Cx=d 8=9"18 =0. the intersection is the singleton 5. Lipigraph and sublevel set. 还完本空间来吧前:AX≤b⇒aitx≤bi SE So it is a convex set If &= gTix =0 d-sublevel set of f:R"→R 13. \$ 22 to Positive semidefinise cone the set reduces to (2+tv lat+pt+150) Osymmetric metrices estracts which is convex if grue =0 => vTAVE70

Shirt is is true if there exists > such

This is true if there exists > such Cx=[x&domf|f(x)&d] sublevel sets which is convex if d >0. Therefore Cn H of convex functions are convex 成过来是不成之后。 论明如下: f(0x1+(1-0)x,) < d \x1, x, <-Ca
f(0x1+(1-0)x,) < 0 f(x1)+(1-0)f(x,) epif that A+299T >0. then VAV=U (A+299TV St is a convex come citil. >0 for all v satisfying gro=0 epigraph of f: R" -> R.

epigraph of f: R" -> R.

epigraph of f: R" -> R. e.x. [x y] 65 0 x2-y'70 Show set [XERF |XIXI>] is convex consider a convex combination & of two points (X1, Xn) and (Y1, Yr) in the set. **冰冰粉茶3品体的塔顶×** の後には、ストモし、ロミのミーシのスト(1-日)なったと f is convex if and only if epifix a convex set ① 技》: intersection laffine functions perspective function linear fractional F 支肤 作射效。查纳表数、低级的比较级 20 张作儿好多。 ifxzy, then t=0x+(1-0)yzy and 6. Jensen's inequality basic inequality if fix convex, then for 050≤1. f(0xx1-0)y)≤0 f(x)+1-0)f(y) obviously Eitr > 41421. Similar proof of yxx (Show that [XER+ Tin xiz] is convex (TAKES FOX)=AX+b with AER My: f: R-R is convex, and a, bedomf with a b. Will f(x) = b-x f(a) + x-a f(b) USSE convex ラ f(s)= f(x) | x es | convex 主対 (以来) | x es | convex を対していまった。 | x es | x e Hint It a, byo and 05051, then a 6 b 1-8 ≤ Ba + (1-8)b. for all x6[a,b] Solution: Assume that TI, XiZI and Solution: This is Jensen's inequality with Tiyi >1. Uting the inequality in the a=(b-x)/(ba) hint, we have f(x)=f(xa+(1-x)b) = b-x f(a)+ x-a f(b) TIE (BX;+(1-0)/1)>TIXE 4; = (TIXE) (TYE) >1 署書的一个小川村子写本ldist(x,S)≤dist(x,T) is an intersection of two helfspaces.

Assignments of law this section of law foods @ fxGR" | deatx= B] [x|xTpx < (CTx)2, CTx70] (with PES+) ①透松悠悠:P(x,t)=x/t. 值城 这样,他们是我们是我们的,Ax+b。 domf={x|c*x+d>0} 主文均和作成的是当的。(如解出版) is an intersection of two helfspaces, which dearly is not convex. 7.0 pentrons thet preserve convexity 南美的巴普兹拉达铁特马比的绿油的 1.15世纪之马克敦 Anonnepatrie weighted sum 2. com position; will affine function so it is convex set. It is also a Pof(x)=P(Ax+b, (Tx+d) = Ax+b polyhedian. It is a cone if bi=o and bi=o 因为是珍尔比较未造的生物的复数这 Tellix-xollx=11x-yllr for all yts]. SER"
it is conver because it can be expected は. minimum element 多利量 3. pointwise maximum and supremum as psx/11x-xol/25 11x-y1/2 an XES美子人K花是了局最小 4. composition t. minimization 6. perspective allegantager. 154725511 intersection of holfspaces.
The set | x|x+Sv Ssi, where Si, Sv E.R. YES ⇒ X K y PP Y-ZEK minimal element 15年年) XES 美子 K 本是10年至41 组合、成立取最大和取上不确告、会成 动和投影和侧似保持凸比. wich S, convex. yes, yex=>y=x opx-yex =

f(Axitb) is convex if f is convex (any) norm of affine function fue)=11AxHb11 is convex Iffi,..., fm are convex, then fix)=max (fice), ..., fm(x) is convex. Tats: piecewise-linear function: fix = mex (Aix+bi) is convex In Compassion with salar functions

In Compassion with salar functions

A the Bold of the salar functions

A the Bold of the salar functions

In Compassion of 9: R' > R and h: R > R: if

I is convex if 9 a, h.C., hability the

Proof for no. 1. Affective the J.h.)

Free powers convex if 1 is convex

Vyou is convex if 9 is concave and positive.

Vector composition:

I "(x)=9'(x) The flowing (x) + The (12x) I g'(x)

II Minimization I the (that he) fix)=g'(x)=g'(x)Th(g(x))g'(x)

If f(x,y) is convex in(x,y) and (is a convex set, then g(x)=inff(x,y) is convex

set, then g(x)=inff(x,y) is convex

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set, then g(x)=inff(x,y)

set, then g(x)=inff(x,y)

=x(A-bc-16T)x, g is convex, hence

schur complement A-Bc-16T>0.

The g-28 schuze -> y=-c-16Tx

=>g(x)=x(A-Bc-16T)x

12. Perspective of a function f: R->R is the domg=[(x,t)] x f edomf, trol
g is convex if t is convex

13. The conjugate function (x)

13. The conjugate function (x)

13. The conjugate function (x)

13. The conjugate function (x) BORE FOX = U/D) X'QX with QES f(0x+84)=df(x)+8f(y) f(x)=xz f(0x+84)=(0x+84)==dx2+84z=df(x)+8f(4) EXT = ||Xz||; is convex (由地版的等为) Z'(0x+(1-0)))'z 50z'x'z+(1-0)z'y'z forx.yes", 000 1 .=> (0x+(1-0))'<0x'+(1-0)Y' Mo(x)=logx (with domus=R++).

8, composition with affine function

Lp and equivalent SDP min CTX
Lp: min CTX
St. AXSb SDP: st. diag(AX-b) SO isty is not possibly occi fati 神文趣度(a) min 是 p(a; x-bi) (94)的海顶的多块:给此打华色0 はいいは(x) = lim (d/b()(x)³-1) = lim x^d logx (x)² (d/dx) d = lim x^d logx (d/dx) d = Φ(ω)= (u² · 1ωξη | M(2 | ω) · 1ωξη (b) min = (α; κ-τυ)/(νυτ1) + μ° 1 ω . s.t ω > ο (c) min = (ω; κ-τυ)/(νυτ1) . s.t ω - υ-υσαχ- δ ε ω τυ Eigenvalue minimisetion: min Amar (Acci) Spp:mint. s.t. A(x) sti AMAXIAIST COASTI. DSUSMI. V >0.

AT (a) (b) fixe. mly with the is given by w=glu/m+, 141/2m the optimal value.

ontuine my (with + m'w) = facility-m, 141/2m

who of the wise. => uacx x0 => ua is strictly concave (i) f(x)=t+(x') is convex on donf=Shi if: Refine g(t)=f(z+tv), where z roand Vesn g(t)=tr((z+tv)')=tr(z'(I+tz')vz')) のlagrangian ままける。 対けが知い prin fo(c)、 s.c. fi(x)(c) トシ(x) =0 L(x, れ, v)=fo(x)+ これがな(x)+ これら(x) = the Q(1+th) QT) = th(QTE Q(1+th))

= \(\begin{align*} \left(\ =tr(z'a(1+tn)'a")=tr(a"z'a(1+tn)") the optimit we = flat x-bil/M-1, lat x-bil>M The opening we = (ax+v) = |av x - bi|

Vi= |av x-bi|-uv = min = (ui-xmu; + ma; xm)

Sit. 0 = (ui < min(M, |av x - bi|) I flav x - bi| < M Diagrange dust function 13th English of 12th Concerns on the confiction of the confi then function reduces to laix-bil
If laix-bil-M. then function reduces to
IMALY whilm. Finally (c) is given by Ξi=ι φ (aix-bi) MAXIO, min Etc., s.t. Ax=b D

Aprilled min Etc., s.t. Ax=b D Calculus of variations. 查的语义, 性格的特殊, J=hlx(+f),+f)+f=g(x(+),u(+),+fdt 7×1(x,v)=2x+A"2=0=>x=-(1/2)A"19 tag(v)=L((-15)ATV, v)=-+v*AATV-bTV Lower bound projectly 2px > (1/4) VAA'U-15U
13/11 Minr CZ SSE AX=b . X > 0
16/11(L(A) VA) = CX+V*(AX-b)-A*X=-b*V+((+A) VA)*X x(t)=a(x(t), w(t), t). X(E)= a(X(E)) (100, 10) p-to unbounder this pt pts - to it Aret to it with a state of it is in the last of it. Aret to otherwise.

(xy=0, i=1,..., p | This in the last | S.t. Aret to to it. It with a state of it. It with a state of it. is feasible, and cis not in the range of A((20)) the problem is unbounded (pt=-00) make x=x0-t2, t>0.

TSHE'S, pt= (+0, b & R(A))

TO STEEL STEEL AND SOME X

L-00, otherwise. 应需等件: he(tf)+H(tf)=0 计算 tf的形式表演是: x=a(X,u,t)=(等), p=-(3H) 如果从(tf)是自由的还是话是上楼就争叫: P;(tf)= 32;(tf) 下面经出了到是: Tillik=supjudje ut is dual norm of III.

Tobal: " Tilliy=0 if IIII = 1, -0 otherwise

Nylk=1=> Nxll-y'x>0 for all x equality if x=0

Nylk=1, choose x=th. Mull=1, u'y=1ylk=1 min ctx s.t. atx= where a =0 D

Apr this problem is a luming feasible make
cante with a c=0. If >0. those x=-ta
lett >0. Ctx=-tca=-traca>-o and
atx-b=-tara-b=0 for large t, so x is
feasible for large t | 1 f = 2+0, the problem is
introdunded below. choose x=ba-te and lee
t go to 60 | If c=ax for some x=0, the optimal
value is ctal=2x In summan, the optimal
value is ctal=2x In summan, the optimal value is crab=26. In summery, the optimel 受けまればない SX(S)-x(0)=-X(S)-入(S) SX(S)-X(0)=-X(S)+X(S)= X(S)= X(S)-X(S) S+1 value is px = 526, c=ax for some x 50 min C'X. St. LSXSU. Where LSU 3 酶识称的物类更多多种的 The objective is 行是可以解出入(s)和X(s),然后通过扩放设备 独可以得出入(o),散后和出(b(t)=-入(t) asum of terms Cixi. xi-liszisui If Ciro, then xi=li, if Ci<o, then xi=ui 130年(北至海シ文、(七)= 火にも)、文、(七)= 以(七) if ciro, xi6[bi, ui] top*=1"c++utc-where c==maxsci, o] and c==mexf-ci, o] min cTx st. 17x=1, x >0 (9) fix) <0, Ax=b 動心ときま; minfo(x1,x2) S.t. fi(x1) <0 相关题目 min CTX, S.t. AXSb. 记日子教化的 W+P2=0=>U*(t)=-P2(t). P*= FCTATB, ATC SO 的: myke y=Ax 所以でいるなる、文=といけ、文z=-Pz(t) €> min fo(x1) . S.t. fi(x1) ≤0. fo(x1)=int fo(x1,x1) P1-0· p2=-R(t) 辺景神: X1(0)=1、X2(0)=1、X1(1)=0. P2(1)=0 => min CTA'y , s.t. y = b . If A c <0, the optimal solution is y = b, with p* 也了于技术变换:SXI(5)-X(0)=X(5) 5 X(5)-X(0)=P(5), 5P(5)-P(6)=0

5 R(5)-P(0)=-P(5), ⇒ 5"X(5)=5"X(0)+5"X(0)+5"X(0)
-5P(0)+P(0) NN*P(N*A+4*(4)*X(0)-1, xx0-1

X(5)=±+5*-5*B(0)+5*P(0)=3

X(5)=±+5*-5*P(0)+5*P(0)=3

-5P(0)+P(0)=1+±-5*P(0)+5*P(0)=3

-5P(0)+P(0)=1+±-5*P(0)+5*P(0)=3

-5P(0)+1+±-5*P(0)+5*P(0)=3

-5P(0)+5*P(0)+5*P(0)=3

-5P(0)+5*P(0)+5*P(0)=3

-5P(0)+5*P(0)+5*P(0)=3

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-5P(0)+5*P(0)+5*P(0)=3

-5P(0)+5*P(0)+5*P(0)=3

-5P(0)+5*P(0)=3

-5P(0)+5*P(0)=3 CTATO. Otherwise, the Lp is unbourded below 必括共和国方数《テスプロ特局:Tel(x,x,v)= ABS EVOL: IFUIIXII=IXI+XI+ -+1XxI OF TO BO: IXIIO = nox(IXI, IXI, ..., IXI)) Minimize [IAX-bilos O Equivalent to thelp ▽fo(以)+至h;▽f;(以)+至V;▽h;(以)=O 如果奶汁局成多、×、ハ、V业最阳的、测减多体符件 min t. S.t. Ax-b StI, Ax-b>-tI =>-t≤akx-bk<t. > t>|axx-bk| =>
tzmax |axx-bk| =||Ax-b|| => 0.50 p*=||Ax-b|| => また(0)-かり(0), Pz(t)=Pz(0)-P(0)生利用手件 XI(1)=0, B(1)=0, Tip 2- 1/B(0)+6 P(10)=0 Minsmite. 11 Ax-611, @ Equivalent to the LP 可以解出 P.(の=6. B.(の=6. X*(は=1+t-3t2+t3 min I's s.t. Az-b < 5, Az-b > -5. => -5 K < Q x x - b K < S k . => S k > | Q x x - b k | 月では1=6(1-t). いたけ=6(t-1). Xでは1=1-6七十3七と mex r st. a; zc+Hailh & bi 和美国思;双和分子流; 以= 11., y(0)=/0. 解的語: may foly sto to to st.ATV=0 at mini as: max by-foly - foly) st.ATV=0 at motals: g(v)=by (foly)-vTy +vTax+bTV) = foly)-by v y to steriouse foly) xtemi so choose Sk= |ax x-bk => px(x)=||Ax-b|) y(0)=0. y(tf)=y(tf)=0. J=tdtj+10tbulent 2x:x=y, x=y, x(t)=(y(t), u(t)= ij(t) 2x:X(t)=AX(t)+Bu(t) X(t)=(y(t), u(t)= ij(t) 2x:X(t)=AX(t)+Bu(t) X(t)=(x) X(t)=(0) Linear - tractional program the potenty
min fo(x) st. Gxzh. Axzb

Jo(x) = crxtn. dom fo(x) = [x][x+f>0]

Z y=x/[x+f, z=1/[x+f]
min crytdz st. Gyzhz, Ay=bt. Minimise ||Ax-th|| subject to ||x|| = [3] Equivalent to the LP: min ITY (幹) H=g+Pta=tble+P,xx+P,U 機的A=(%),B=(1) 未を配:p=-HxT=> {P,=-0H,=0→P,(t)=C, s.t. - y E Ax-by , + EX SI. , XER and YER Minimide 11X11, subject to 1/Ax-61/00 <1 Equivalent to the up: min ITy SHU, AVEO St.-YSXSY, -1 SAX-661 (x, 4的注意) | Pp=-#==P1->B(t)=-C1+C2
| Minimize ||Ax-b||_1+||X||00 || Hu=bu+p2=0+u=-P2=-C2+C1+ Equivalent to: min 174+t |
| H(tf)=\frac{1}{2}bu'(tf)+p(tf)X2(tf)+B(tf)u(tf) \text{3.t.} -y \leq Ax-b \leq y, -tl \leq x \leq t1. eTy+f==1, 320. 1), $A^TV=0$ = $|V||_{x \in I}$, otherwise. $|-\infty|$, when is Quadratic Program (QP) PEST, so objective min (1/2) x Px+9/x+r. is convex 神(ない): 対すばい理な min C*x . S.t. なこれ。 あ: たん (12) (12) (12) (13) s.t. GxEh. Ax=b. quadratic +dtf=0= +bu'(tf)+ (-bu(tf))-u(tf)+dtf 三次(京本二次やなり、(QCQP)min リントズートのマントンでは、 =- 2 buitty)+dtf=0 > tf=26a (-C+C+tf) Ausdratic xxは==と+なナーメンはノ=くろーなナナイン lij & xiy & unj s.t. Unix Pix+9, x++120 , Ax=6. 22(0)=0. (3=0 . ×1(4)=x2(t)+ ×1(t)=(4- (1) t) Euler Equation: 29 (x(0), x(0),t) of 29 20 Pi EST objective and constraints are convex max-xth-Vb st. C+gx+ATV=0. 270 + C1 +3, ×1(0)=10, (4=10. toty xto 3 (x(t), x*(t), t)- 10 0 (x*(t), x*(t), t)=0 0 min fix , s.t. 11.Aix+bill, SC; x+di, Ix=9 和交通的 minimide IIAx-bili . s.t. Gx=h $t = \frac{60b}{t^{2}}$, $C_{1} = \frac{120b}{t^{2}}$ with りないなは, x*(も)、も)-最り、(x*(も, x*も, も)この も min fox, st. [Asx+0:1] sc. x + ov + v = Geometric Projection Print Projection Fix of the control kits) (f fre 3(x*(+1), x*(+1), +1)-9=(x*(+1), x*(+1), +1)x*(+1)=0 9x(x*(+1), x*(+1), +1=0. 124.14k; 1 -> \$, \$(t) -1, k -> \$

t -> \$1, t -> [x(x,t+1),x,t+1) (= (+1) - x,t+1) + 1 (x,t+1) x,t+1 (x,t+1) x,t+1 + 1 (x,t+1) x,t+1 9x-21x=0 D min CTX S.t. ITX= d osxel. 194: Wtf +gltf)-gxltf)x(tf)=0===ck ZABTECHTCHT -- + Ca XIZ -- XIZ -- XXIZ 2544: [AB] >0=>A-BE-18>0 Satisfying-1= yi=1, which is dearly true. (使赌车的庞开), 二种阿部多纳。 => C-BTA-1870