

3-5 同步电机定子三相通入直流, $i_A = 1, i_B = -1, i_C = 3$, 转子转速为 ω_N , $\alpha = \alpha_0 + \omega_N t$, 求转换到 dq0 坐标系的 i_d, i_q 和 i_0 。

$$\dot{i}_d = \frac{2}{3} [i_A \cos \alpha + i_B \cos(\alpha - 120^\circ) + i_C \cos(\alpha + 120^\circ)]$$

$$= \frac{2}{3} [\cos \alpha - \cos(\alpha - 120^\circ) + \frac{1}{2} \cos(\alpha + 120^\circ)]$$

$$= -\frac{4}{3} \sqrt{3} \sin \alpha = -\frac{4}{3} \sqrt{3} \sin(\alpha_0 + \omega_N t)$$

$$\dot{i}_q = \frac{2}{3} [i_A \sin \alpha + i_B \sin(\alpha - 120^\circ) + i_C \sin(\alpha + 120^\circ)]$$

$$= \frac{2}{3} [\sin \alpha - \sin(\alpha - 120^\circ) + \frac{1}{2} \sin(\alpha + 120^\circ)]$$

$$= 2\sqrt{3} \cos \alpha = 2\sqrt{3} \cos(\alpha_0 + \omega_N t)$$

$$\dot{i}_0 = \frac{1}{3} (i_A + i_B + i_C) = 1$$

3-6 同步电机定子通以负序电流, $i_A = \cos \omega_N t$, $i_B = \cos(\omega_N t + 120^\circ)$, $i_C = \cos(\omega_N t - 120^\circ)$, 求转换到 dq0 坐标系的 i_d, i_q 和 i_0 。

$$\text{设: } \alpha = \alpha_0 + \omega_N t$$

$$\dot{i}_d = \frac{2}{3} [i_A \cos \alpha + i_B \cos(\alpha - 120^\circ) + i_C \cos(\alpha + 120^\circ)]$$

$$= \frac{2}{3} [\cos \omega_N t \cos \alpha + \cos(\omega_N t + 120^\circ) \cos(\alpha - 120^\circ) + \cos(\omega_N t - 120^\circ) \cos(\alpha + 120^\circ)]$$

$$= \cos(\omega_N t + \alpha) = \cos(\alpha_0 + 2\omega_N t)$$

$$\dot{i}_q = \frac{2}{3} [i_A \sin \alpha + i_B \sin(\alpha - 120^\circ) + i_C \sin(\alpha + 120^\circ)]$$

$$= \frac{2}{3} [\cos \omega_N t \sin \alpha + \cos(\omega_N t + 120^\circ) \sin(\alpha - 120^\circ) + \cos(\omega_N t - 120^\circ) \sin(\alpha + 120^\circ)]$$

$$= \sin(\alpha + \omega_N t) = \sin(\alpha_0 + 2\omega_N t)$$

$$\dot{i}_0 = \frac{1}{3} (i_A + i_B + i_C) = 0$$

