# Codeforces Round #642 (Div. 3)

# A. Most Unstable Array

1 second, 256 megabytes

You are given two integers n and m. You have to construct the array a of length n consisting of **non-negative integers** (i.e. integers greater than or equal to zero) such that the sum of elements of this array is **exactly** m

and the value  $\sum\limits_{i=1}^{n-1} |a_i-a_{i+1}|$  is the maximum possible. Recall that |x| is

the absolute value of x

In other words, you have to maximize the sum of absolute differences between adjacent (consecutive) elements. For example, if the array a = [1, 3, 2, 5, 5, 0] then the value above for this array is  $|1-3|+|3-2|+|2-5|+|5-5|+|5-0|=2+1+3+0+5 = 111 \ n \leq 30; 0 \leq k \leq n) - \text{the number of elements in } a \text{ and } b \text{ and the } b = 111 \ n \leq 30; 0 \leq k \leq n$ . Note that this example doesn't show the optimal answer but it shows how the required value for some array is calculated.

You have to answer t independent test cases.

The first line of the input contains one integer t ( $1 < t < 10^4$ ) — the number of test cases. Then t test cases follow.

The only line of the test case contains two integers n and m (  $1 < n, m < 10^9$ ) — the length of the array and its sum correspondingly.

#### Output

1000000000

2000000000

For each test case, print the answer — the maximum possible value of  $\sum^{n-1} |a_i - a_{i+1}|$  for the array a consisting of n non-negative integers with the sum m.

# input 5 1 100 2 2 5 5 2 1000000000 1000000000 1000000000 output 0 2 10

In the first test case of the example, the only possible array is [100] and the answer is obviously 0.

In the second test case of the example, one of the possible arrays is [2,0]and the answer is |2-0|=2.

In the third test case of the example, one of the possible arrays is [0, 2, 0, 3, 0] and the answer is

|0-2|+|2-0|+|0-3|+|3-0|=10.

# B. Two Arrays And Swaps

1 second, 256 megabytes

You are given two arrays a and b both consisting of n positive (greater than zero) integers. You are also given an integer k.

In one move, you can choose two indices i and j  $(1 \leq i, j \leq n)$  and swap  $a_i$  and  $b_j$  (i.e.  $a_i$  becomes  $b_j$  and vice versa). Note that i and j can be equal or different (in particular, swap  $a_2$  with  $b_2$  or swap  $a_3$  and  $b_0$ both are acceptable moves).

Your task is to find the maximum possible sum you can obtain in the array a if you can do no more than (i.e. at most) k such moves (swaps).

You have to answer t independent test cases.

The first line of the input contains one integer t ( $1 \leq t \leq 200$ ) — the number of test cases. Then t test cases follow.

The first line of the test case contains two integers n and k ( maximum number of moves you can do. The second line of the test case contains n integers  $a_1, a_2, \ldots, a_n$  ( $1 \le a_i \le 30$ ), where  $a_i$  is the i-th element of a. The third line of the test case contains n integers  $b_1, b_2, \ldots, b_n$   $(1 \leq b_i \leq 30)$ , where  $b_i$  is the *i*-th element of  $b_i$ 

#### Output

For each test case, print the answer — the **maximum** possible sum you can obtain in the array a if you can do no more than (i.e. at most) kswaps.

```
input
2 1
1 2
3 4
5 5
5 5 6 6 5
1 2 5 4 3
5 3
1 2 3 4 5
10 9 10 10 9
4 0
2 2 4 3
2 4 2 3
4 4
1 2 2 1
4 4 5 4
output
6
27
39
11
```

In the first test case of the example, you can swap  $a_1=1$  and  $b_2=4$ , so a = [4, 2] and b = [3, 1].

In the second test case of the example, you don't need to swap anything.

In the third test case of the example, you can swap  $a_1 = 1$  and  $b_1 = 10$ ,  $a_3=3$  and  $b_3=10$  and  $a_2=2$  and  $b_4=10$ , so a = [10, 10, 10, 4, 5] and b = [1, 9, 3, 2, 9].

In the fourth test case of the example, you cannot swap anything.

In the fifth test case of the example, you can swap arrays a and b, so a = [4, 4, 5, 4] and b = [1, 2, 2, 1].

# C. Board Moves

1 second, 256 megabytes

You are given a board of size  $n \times n$ , where n is **odd** (not divisible by 2). Initially, each cell of the board contains one figure.

In one move, you can select **exactly one figure** presented in some cell and move it to one of the cells **sharing a side or a corner with the current cell**, i.e. from the cell (i,j) you can move the figure to cells:

• (i-1,j-1); • (i-1,j); • (i-1,j+1); • (i,j-1); • (i,j+1); • (i+1,j-1); • (i+1,j);

Of course, you **can not** move figures to cells out of the board. It is allowed that after a move there will be several figures in one cell.

Your task is to find the minimum number of moves needed to get **all the figures** into **one** cell (i.e.  $n^2-1$  cells should contain 0 figures and one cell should contain  $n^2$  figures).

You have to answer t independent test cases.

#### Input

The first line of the input contains one integer t ( $1 \le t \le 200$ ) — the number of test cases. Then t test cases follow.

The only line of the test case contains one integer n ( $1 \le n < 5 \cdot 10^5$ ) — the size of the board. It is guaranteed that n is odd (not divisible by 2).

It is guaranteed that the sum of n over all test cases does not exceed  $5\cdot 10^5~(\sum n \le 5\cdot 10^5)$ .

## **Output**

For each test case print the answer — the minimum number of moves needed to get **all the figures** into **one** cell.

```
input

3
1
5
499993

output

0
40
41664916690999888
```

# D. Constructing the Array

1 second, 256 megabytes

You are given an array a of length n consisting of zeros. You perform n actions with this array: during the i-th action, the following sequence of operations appears:

- Choose the maximum by length subarray (continuous subsegment)
  consisting only of zeros, among all such segments choose the
  leftmost one;
- 2. Let this segment be [l;r]. If r-l+1 is odd (not divisible by 2) then assign (set)  $a[\frac{l+r}{2}]:=i$  (where i is the number of the current action), otherwise (if r-l+1 is even) assign (set)  $a[\frac{l+r-1}{2}]:=i$ .

Consider the array a of length 5 (initially a=[0,0,0,0,0]). Then it changes as follows:

1. Firstly, we choose the segment [1;5] and assign a[3]:=1, so a becomes [0,0,1,0,0]:

- 2. then we choose the segment [1;2] and assign a[1]:=2, so a becomes [2,0,1,0,0];
- 3. then we choose the segment [4;5] and assign a[4]:=3, so a becomes [2,0,1,3,0];
- 4. then we choose the segment [2;2] and assign a[2]:=4, so a becomes [2,4,1,3,0];
- 5. and at last we choose the segment [5;5] and assign a[5]:=5, so a becomes [2,4,1,3,5].

Your task is to find the array a of length n after performing all n actions. Note that the answer exists and unique.

You have to answer *t* independent test cases.

#### Inpu

The first line of the input contains one integer t ( $1 \le t \le 10^4$ ) — the number of test cases. Then t test cases follow.

The only line of the test case contains one integer n ( $1 \le n \le 2 \cdot 10^5$ ) — the length of a.

It is guaranteed that the sum of n over all test cases does not exceed  $2\cdot 10^5~(\sum n \le 2\cdot 10^5)$ .

#### Output

For each test case, print the answer — the array a of length n after performing n actions described in the problem statement. Note that the answer exists and unique.

```
input

6
1
2
3
4
5
6

output

1
1 2
2 1 3
3 1 2 4
2 4 1 3 5
3 4 1 5 2 6
```

# E. K-periodic Garland

1 second, 256 megabytes

You are given a garland consisting of n lamps. States of the lamps are represented by the string s of length n. The i-th character of the string  $s_i$  equals '0' if the i-th lamp is turned off or '1' if the i-th lamp is turned on. You are also given a positive integer k.

In one move, you can choose **one lamp** and change its state (i.e. turn it on if it is turned off and vice versa).

The garland is called k-periodic if the distance between **each pair of adjacent turned on lamps** is **exactly** k. Consider the case k=3. Then garlands "00010010", "1001001", "00010" and "0" are good but garlands "00101001", "1000001" and "01001100" are not. Note that **the garland is not cyclic**, i.e. the first turned on lamp is not going after the last turned on lamp and vice versa.

Your task is to find the minimum number of moves you need to make to obtain k-periodic garland from the given one.

You have to answer t independent test cases.

#### Input

The first line of the input contains one integer t ( $1 \le t \le 25~000$ ) — the number of test cases. Then t test cases follow.

The first line of the test case contains two integers n and k (  $1 \leq n \leq 10^6; 1 \leq k \leq n$ ) — the length of s and the required period. The second line of the test case contains the string s consisting of n characters '0' and '1'.

It is guaranteed that the sum of n over all test cases does not exceed  $10^6$  (  $\sum n \leq 10^6$  ).

## **Output**

For each test case, print the answer — the **minimum** number of moves you need to make to obtain *k*-periodic garland from the given one.

```
input
9 2
010001010
9 3
111100000
7 4
1111111
10 3
1001110101
1 1
1
1 1
0
output
1
2
5
4
0
0
```

# F. Decreasing Heights

2.5 seconds, 256 megabytes

You are playing one famous sandbox game with the three-dimensional world. The map of the world can be represented as a matrix of size  $n \times m$ , where the height of the cell (i,j) is  $a_{i,j}$ .

You are in the cell (1,1) right now and want to get in the cell (n,m). You can move only down (from the cell (i,j) to the cell (i+1,j)) or right (from the cell (i,j) to the cell (i,j+1)). There is an additional **restriction**: if the height of the current cell is x then you can move only to the cell with height x+1.

**Before the first move** you can perform several operations. During one operation, you can decrease the height of **any** cell by one. I.e. you choose some cell (i,j) and assign (set)  $a_{i,j}:=a_{i,j}-1$ . Note that you **can** make heights **less than or equal to zero**. Also note that you **can** decrease the height of the cell (1,1).

Your task is to find the **minimum** number of operations you have to perform to obtain at least one suitable path from the cell (1,1) to the cell (n,m). It is guaranteed that the answer exists.

You have to answer t independent test cases.

### Input

The first line of the input contains one integer t ( $1 \le t \le 100$ ) — the number of test cases. Then t test cases follow.

The first line of the test case contains two integers n and m (  $1 \leq n, m \leq 100$ ) — the number of rows and the number of columns in the map of the world. The next n lines contain m integers each, where the j-th integer in the i-th line is  $a_{i,j}$  ( $1 \leq a_{i,j} \leq 10^{15}$ ) — the height of the cell (i,j).

It is guaranteed that the sum of n (as well as the sum of m) over all test cases does not exceed  $100~(\sum n \le 100; \sum m \le 100)$ .

#### **Output**

For each test case, print the answer — the **minimum** number of operations you have to perform to obtain at least one suitable path from the cell (1,1) to the cell (n,m). It is guaranteed that the answer exists.

```
input
5
3 4
1 2 3 4
5 6 7 8
9 10 11 12
5 5
2 5 4 8 3
9 10 11 5 1
12 8 4 2 5
2 2 5 4 1
6 8 2 4 2
2 2
100 10
10 1
1 2
123456789876543 987654321234567
output
49
111
864197531358023
0
```

<u>Codeforces</u> (c) Copyright 2010-2020 Mike Mirzayanov The only programming contests Web 2.0 platform