# Theory

Superconductivity in MoS2 surface

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## Dispersion

$$\varepsilon_{\text{Mo}}(\mathbf{k}) = 2t_1 \left( \cos k_y a + 2\cos \frac{\sqrt{3}}{2} k_x a \cos \frac{1}{2} k_y a \right)$$

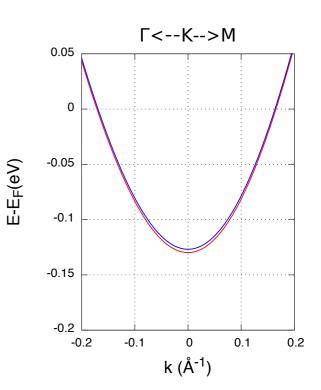
$$+ 2t_2 \left( \cos \sqrt{3} k_x a + 2\cos \frac{\sqrt{3}}{2} k_x a \cos \frac{3}{2} k_y a \right)$$

$$+ 2t_3 \left( \cos 2k_y a + 2\cos \sqrt{3} k_x a \cos k_y a \right) - \mu$$

Band calculation at mono-layer G.B Lin et.al:PRB  $t_2/t_1 = -0.40$ 

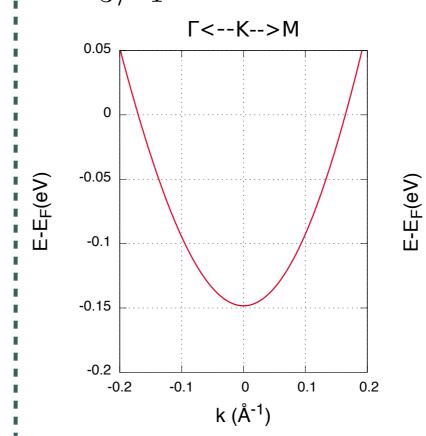
$$t_3/t_1 = 0.25$$

$$t_1 = 146 \ meV$$

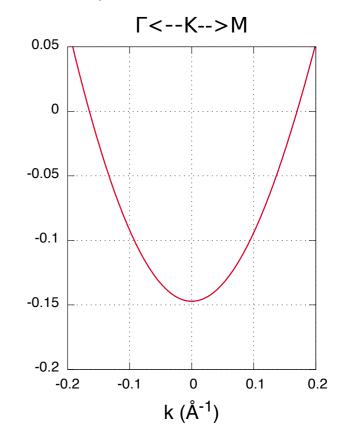


$$N \sim 8.9 \times 10^{13} cm^{-2}$$

$$t_3/t_1 = 0.25$$



$$t_3/t_1 = 0.05$$



## Dispersion

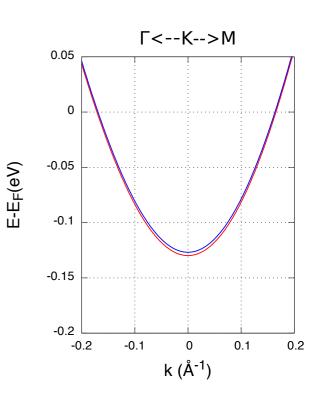
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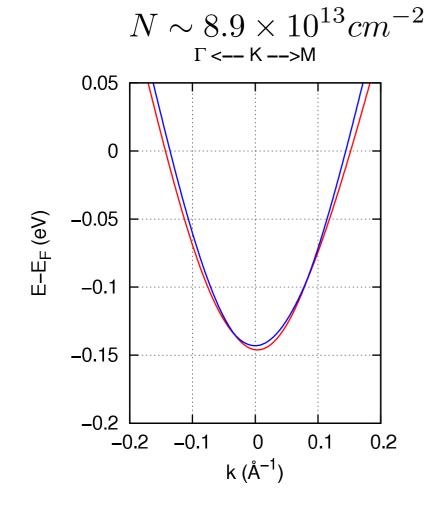
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Band calculation at mono-layer G.B Lin et.al:PRB  $t_2/t_1 = -0.40$   $t_3/t_1 = 0.25$ 

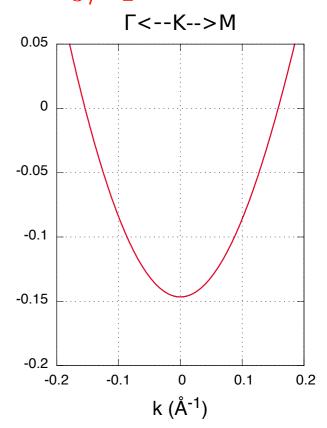
 $t_1 = 146 \ meV$ 



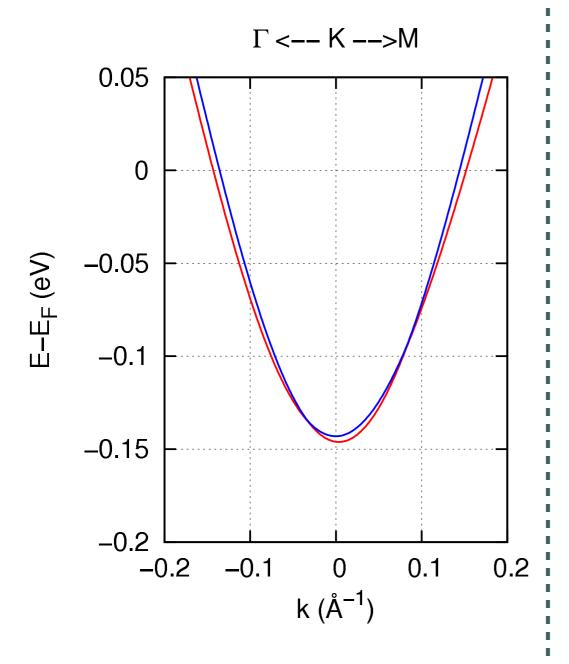


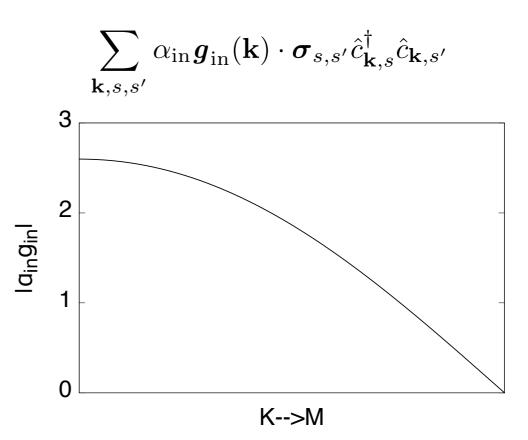
$$N \sim 7.7 \times 10^{13} cm^{-2}$$

$$t_3/t_1 = 0.05$$



## Spin split





$$\sum_{\mathbf{k},s,s'} \alpha_{\mathrm{in}} \boldsymbol{g}_{\mathrm{in}}(\mathbf{k}) \cdot \boldsymbol{\sigma}_{s,s'} [\tanh{(\boldsymbol{x}|f(\mathbf{k})-f(K)|)} - \boldsymbol{\delta}] \hat{c}_{\mathbf{k},s}^{\dagger} \hat{c}_{\mathbf{k},s'}$$

# Spin split

$$\hat{H}_{\text{in}} = \sum_{\mathbf{k}, s, s'} \alpha_{\text{in}} \mathbf{g}_{\text{in}}(\mathbf{k}) \cdot \boldsymbol{\sigma}_{s, s'} \left[ \tanh \left( \mathbf{x} | f(\mathbf{k}) - f(K) | \right) - \boldsymbol{\delta} \right] \hat{c}_{\mathbf{k}, s}^{\dagger} \hat{c}_{\mathbf{k}, s'}$$

$$\mathbf{g}_{\text{in}}(\mathbf{k}) = \left( 0, 0, \sin k_{y} - 2 \cos \frac{\sqrt{3}}{2} k_{x} \sin \frac{1}{2} k_{y} \right)$$

$$\hat{H}_{\text{ra}} = \sum_{\mathbf{k}, s, s'} \alpha_{\text{ra}} \mathbf{g}_{\text{ra}}(\mathbf{k}) \cdot \boldsymbol{\sigma}_{s, s'} \hat{c}_{\mathbf{k}, s}^{\dagger} \hat{c}_{\mathbf{k}, s'}$$

$$\mathbf{g}_{\text{ra}}(\mathbf{k}) = \left( -\sin k_{y} - \cos \frac{\sqrt{3}}{2} k_{x} \sin \frac{1}{2} k_{y}, \sqrt{3} \sin \frac{\sqrt{3}}{2} k_{x} \cos \frac{1}{2} k_{y}, 0 \right)$$

Spin splitを決める変数は4つ

Parameter  $(\alpha_{\rm in}, \alpha_{\rm ra}, x, \delta)$ 

## パラメーターの決定

### 束縛条件

$$\frac{|\alpha_{\rm ra}g_{\rm ra}(k_{\rm F})|}{\left|\alpha_{\rm in}g_{\rm in}(k_{\rm F})\tilde{f}^{(x,\delta)}(k_{\rm F})\right|} = 0.02$$

$$2\sqrt{\left[\alpha_{\rm ra}g_{\rm ra}(k_{\rm F})\right]^2 + \left[\alpha_{\rm in}g_{\rm in}(k_{\rm F})\tilde{f}^{(x,\delta)}(k_{\rm F})\right]^2} = 13 \quad (meV)$$

$$2\sqrt{\left[\alpha_{\rm ra}g_{\rm ra}(K)\right]^2 + \left[\alpha_{\rm in}g_{\rm in}(K)\tilde{f}^{(x,\delta)}(K)\right]^2} = 3 \quad (meV)$$

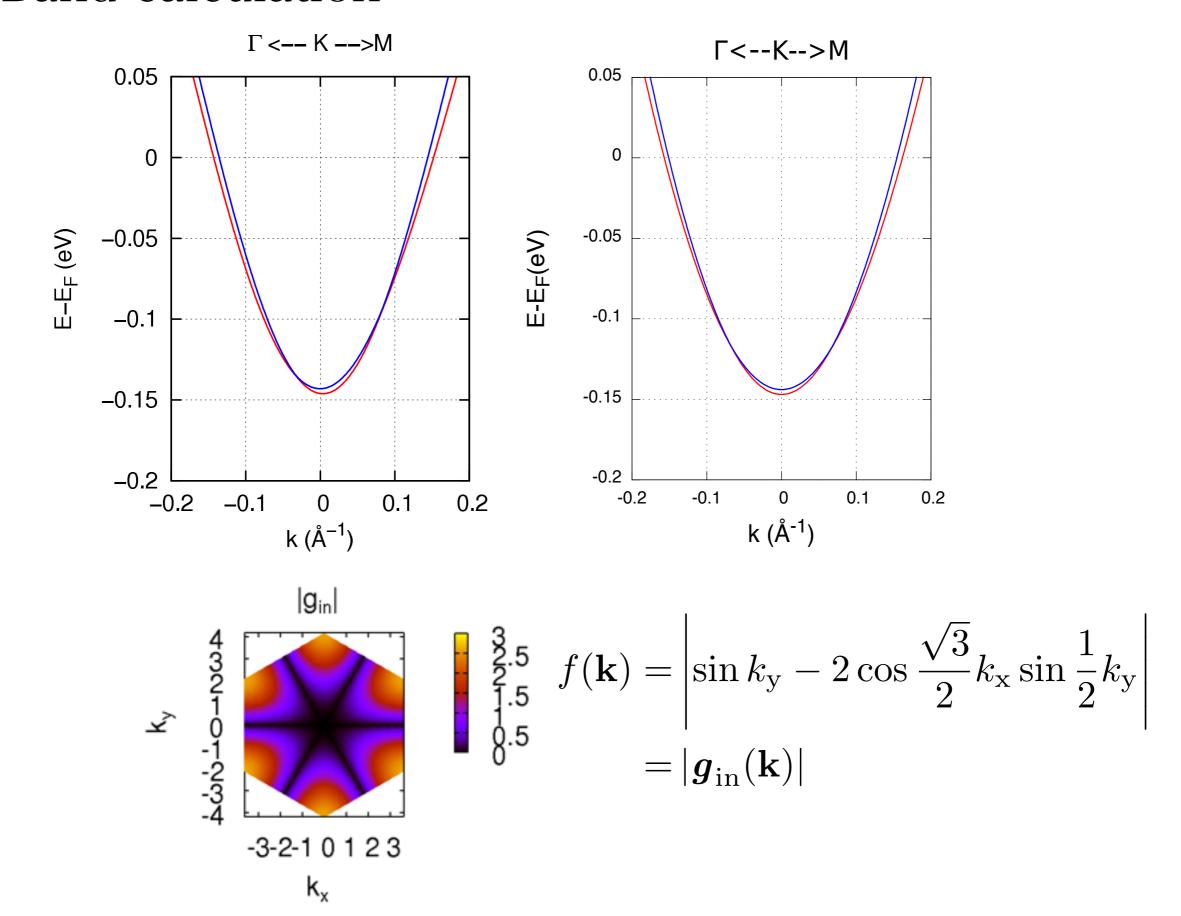
$$\tilde{f}^{(x,\delta)}(\mathbf{k}) = \tanh(x|f(\mathbf{k}) - f(K)|) - \delta$$

### Definition of k<sub>F</sub>:

$$\frac{E_{+}(k_{\rm F}) + E_{-}(k_{\rm F})}{2} = 0$$

変数4つに対して束縛条件が3つ

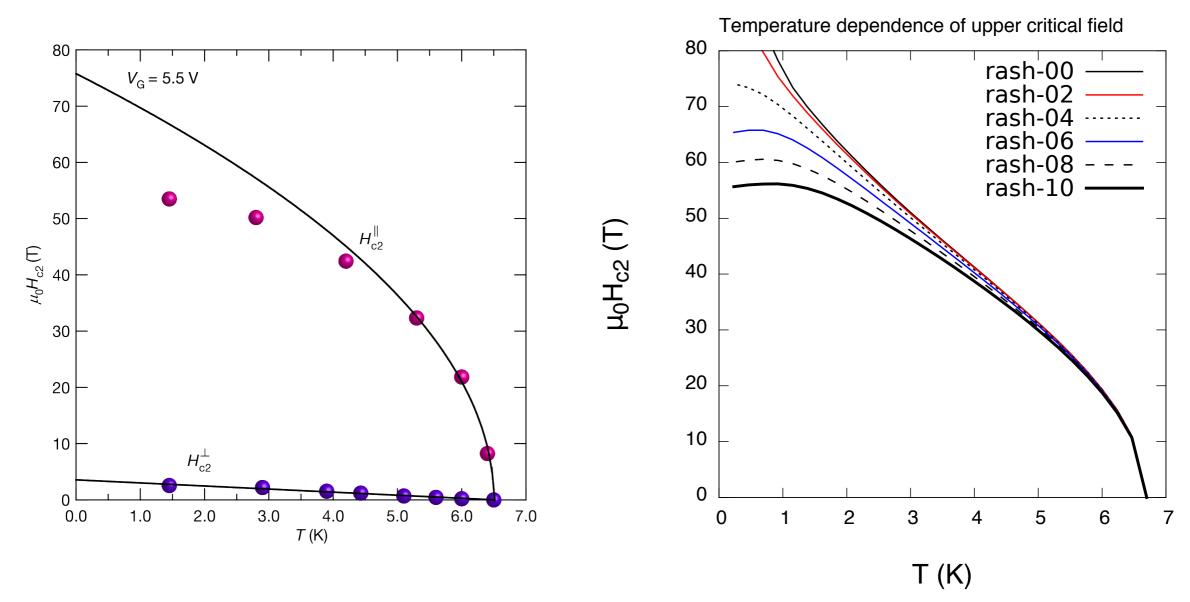
変数を一つを決めれば他がユニークに決まる



### 実験との比較

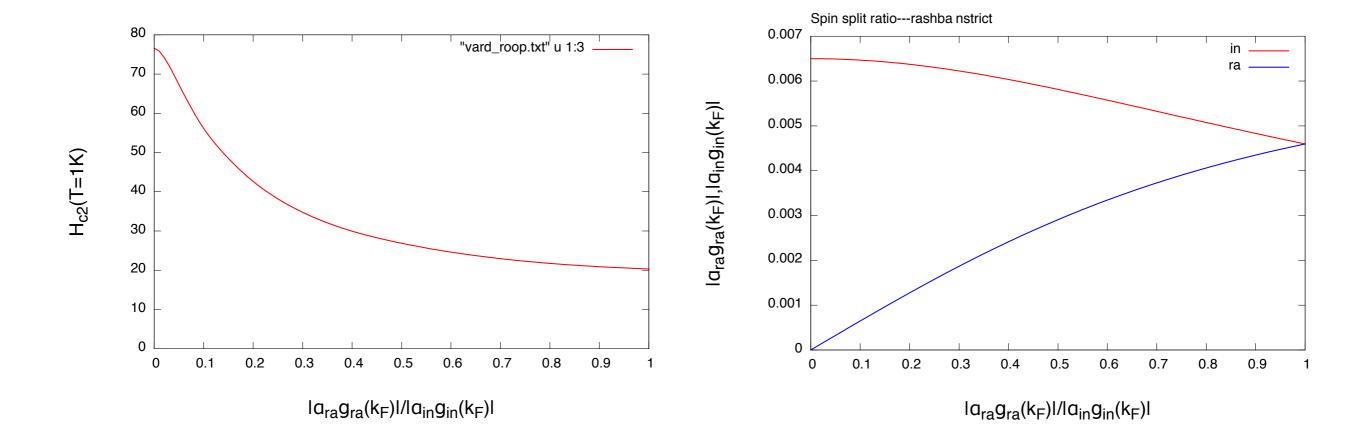


理論  $H \parallel [1,0,0]$ 



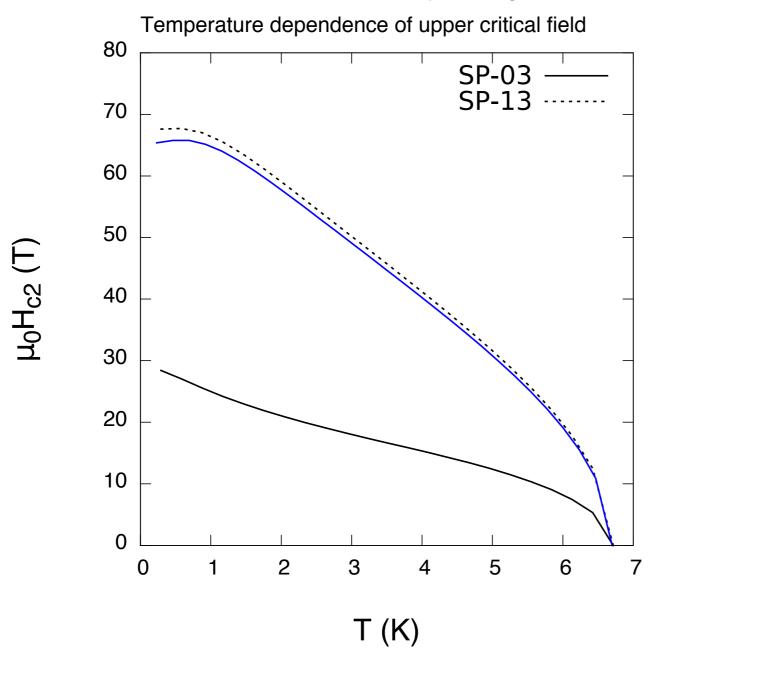
- Rashba型ASOCがInstinctASOCの10%程度で実験とほぼ一致
- ・Rashba型ASOCがInstinctASOCの6%程度から 低温高磁場領域でHc2が温度に対してフラットになる

### ASOCの比とHc2

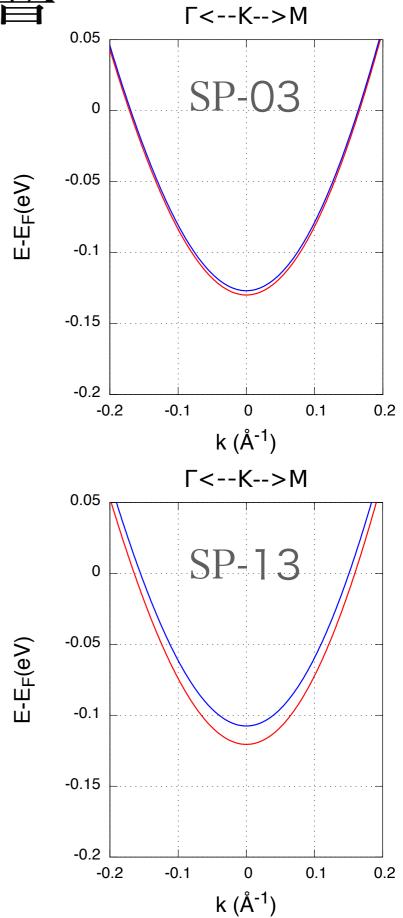


Rashba型ASOCによるSpin splitの割合が小さくてもHc2は 大きく減少する

### バンドが変化する影響

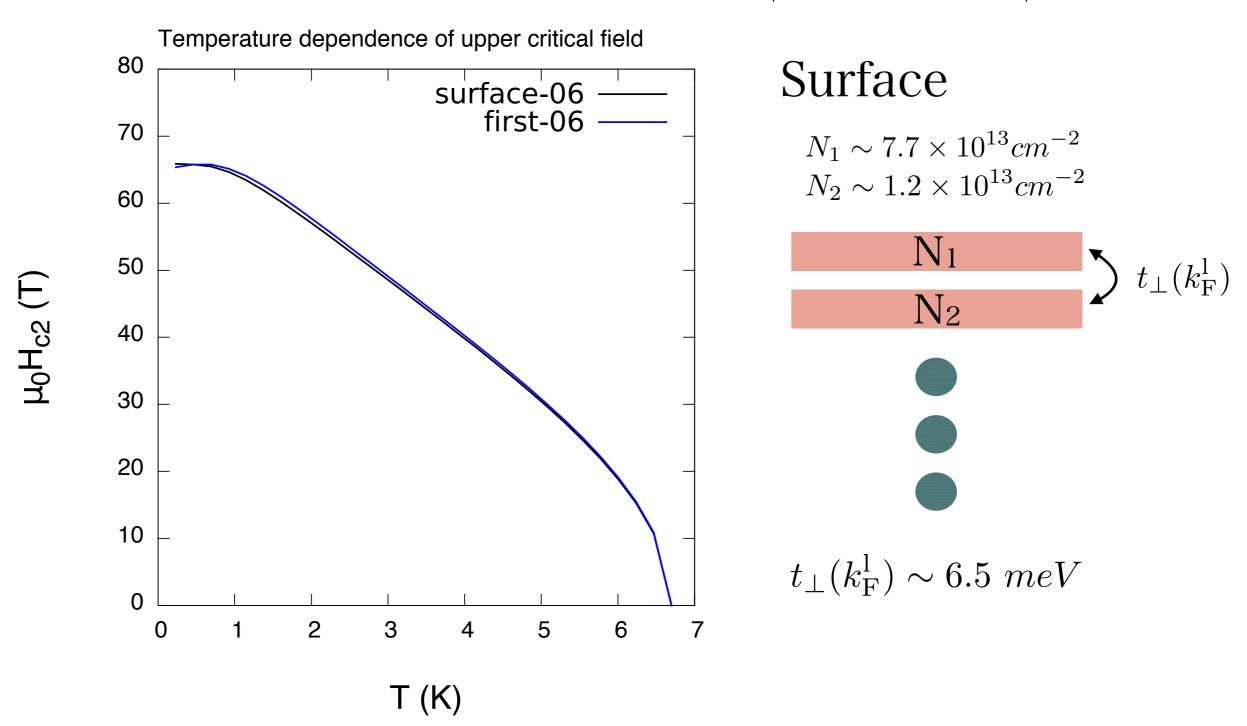


・通常のmono-layerの場合と異なり Fermi levelでのspin splitが13meVあることが重要



### 2層目の影響

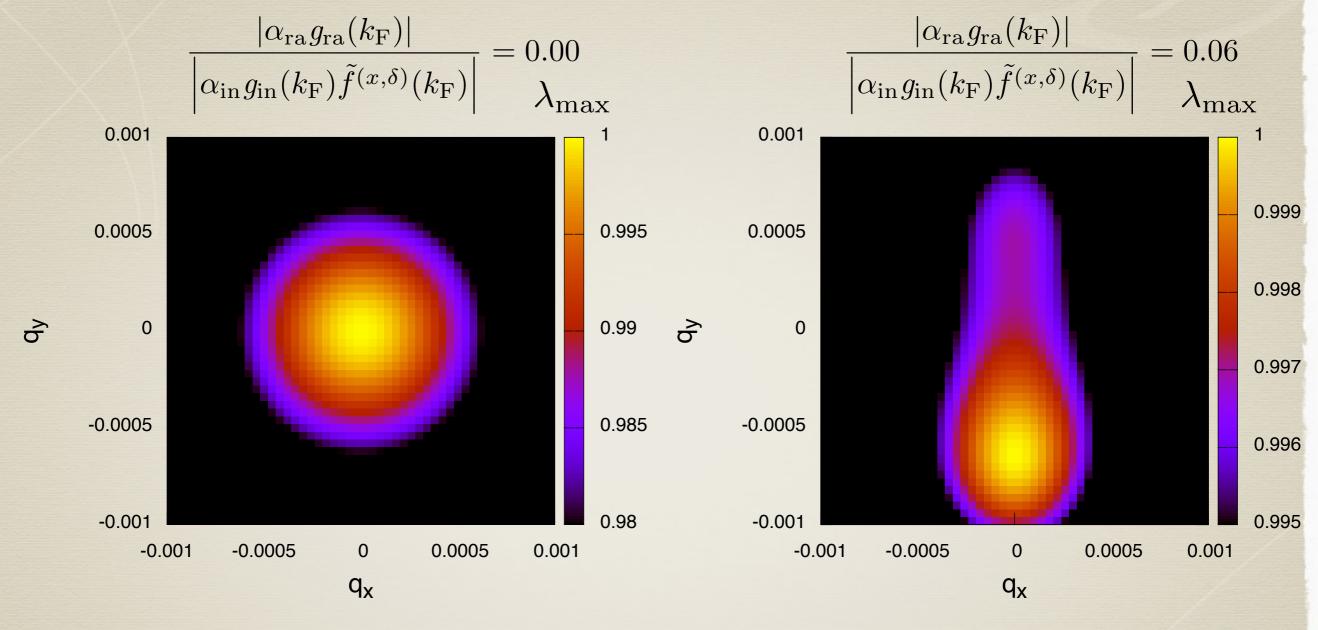
$$\frac{|\alpha_{\rm ra}g_{\rm ra}(k_{\rm F})|}{\left|\alpha_{\rm in}g_{\rm in}(k_{\rm F})\tilde{f}^{(x,\delta)}(k_{\rm F})\right|} = 0.06$$



理論的にも1層目までの計算で十分であると考えられる

### Helical 超伝導

 $T \sim 1K$ 



BCS超伝導

Helical超伝導