

# Guaranteeing Safety and Liveness of Unmanned Aerial Vehicle Platoons on Air Highways

Mo Chen<sup>a</sup>

*Business or Academic Affiliation 1, City, State, Zip Code*

Third C. Author<sup>b</sup>

*Business or Academic Affiliation 2, City, Province, Zip Code, Country*

Fourth D. Author<sup>c</sup>

*Business or Academic Affiliation 2, City, State, Zip Code*

## Nomenclature

(Nomenclature entries should have the units identified)

$x$  = System state

<sup>a</sup> Insert Job Title, Department Name, Address/Mail Stop, and AIAA Member Grade (if any) for first author.

<sup>b</sup> Insert Job Title, Department Name, Address/Mail Stop, and AIAA Member Grade (if any) for third author.

<sup>c</sup> Insert Job Title, Department Name, Address/Mail Stop, and AIAA Member Grade (if any) for fourth author (etc.).

## I. Introduction

## II. Air Highways

### A. Problem Formulation

### B. The Eikonal Equation – Cost-Minimizing Path

### C. Results

## III. Unmanned Aerial Vehicle Platooning

### A. Problem Formulation

#### 1. Vehicle Dynamics

Consider a UAV whose dynamics are given by

$$\dot{x} = f(x, u) \quad (1)$$

where  $x \in \mathbb{R}^n$  represents the state, and  $u \in \mathbb{R}^{n_u}$  represents the control action. In this paper, we will assume that each vehicle has the following simple model of a quadrotor:

$$\begin{aligned} \dot{p}_x &= v_x, & \dot{p}_y &= v_y \\ \dot{v}_x &= u_x, & \dot{v}_y &= u_y, & |u_x|, |u_y| &\leq u_{\max} \end{aligned} \quad (2)$$

where the state  $x = (p_x, v_x, p_y, v_y) \in \mathbb{R}^4$  represents the quadrotor's position in the  $x$ -direction, its velocity in the  $x$ -direction, and its position and velocity in the  $y$ -direction, respectively. For convenience, we will denote the position and velocity  $p = (p_x, p_y)$ ,  $v = (v_x, v_y)$ , respectively. We will consider a group of  $N$  quadrotors  $Q_i, i = 1 \dots, N$ .

In general, the problem of collision avoidance among  $N$  vehicles cannot be tractably solved using traditional dynamic programming approaches because the computation complexity of these approaches scales exponentially with the number of vehicles. Thus, in our present work, we will consider the situation where UAVs travel on air highways in platoons, defined in the following sections. The structure imposed by air highways and the platoon enables us to analyze the liveness and safety of the vehicles in a tractable manner.

## 2. Vehicles in a Platoon

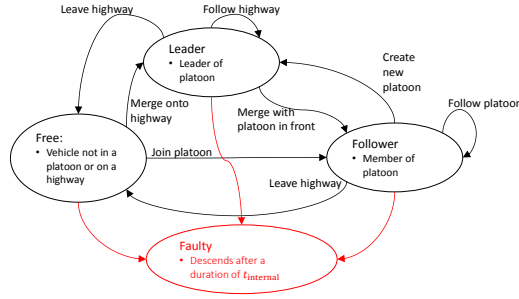
We consider a platoon of quadrotors to be a group of  $M$  quadrotors  $Q_{P_1}, \dots, Q_{P_M}$  in a single-file formation. Not all of the  $N$  quadrotors need to be in a platoon:  $\{P_j\}_{j=1}^M \subseteq \{i\}_{i=1}^N$ .  $Q_{P_1}$  is the leader of the platoon, and  $Q_{P_2}, \dots, Q_{P_M}$  are the followers. We will assume that the quadrotors in a platoon travel along an air highway, which is defined by as a path inside a pre-defined altitude range. The quadrotors maintain a separation distance of  $b$ . In order to allow for close proximity of the quadrotors and the ability to resolve multiple simultaneous safety breaches, we assume that in the event of a malfunction, a quadrotor will be able to exit the altitude range of the highway within a duration of  $t_{\text{internal}} = 1.5$ . Such a requirement may be implemented practically as an emergency landing procedure to which the quadrotors revert when a malfunction is detected.

As part of a platoon, each quadrotor must be capable of performing a number of essential cooperative maneuvers. In this paper, we consider the following:

- safely merging onto an air highway;
- safely joining a platoon;
- reacting to a malfunctioning vehicle in the platoon;
- reacting to an intruder vehicle;
- following the highway, a curve defined in space at constant altitude, at a specified speed;
- maintaining a constant relative position and velocity with the leader of a platoon.

## 3. Vehicles as Hybrid Systems

A UAV in general may be in a number of modes of operations, depending on whether it is part of a platoon, and in the affirmative case, whether it is a leader or a follower. Therefore, it is natural to model quadrotors as hybrid systems [? ? ]. In this paper, we restrict the available maneuvers of each quadrotor depending on the mode. We assume that each quadrotor in the airspace has the following modes:



**Fig. 1 Hybrid modes for vehicles in platoons.**

- Free: Vehicle not in a platoon. Available maneuvers: merge onto a highway, join a platoon on a highway.
- Leader: Leader of platoon (could be by itself). Available maneuvers: travel along the highway at a pre-specified speed, merge current platoon with a platoon in front, leave the highway.
- Follower: Vehicle following the platoon leader. Available maneuvers: follow a platoon, create a new platoon.
- Faulty: Malfunctioned vehicle in a platoon: reverts to default behavior and descends after a duration of  $t_{\text{internal}}$ .

The available maneuvers and associated mode transitions are shown in Figure 1.

#### 4. Objectives

Using the previously-mentioned modeling assumptions, we would like to address the following questions:

1. How do vehicles form platoons?
2. How can the safety of the vehicles be ensured during normal operation and when there is a malfunctioning vehicle within the platoon?
3. How can the platoon respond to intruders such as unresponsive UAVs, birds, or other aerial objects?

The answers to these questions can be broken down into the maneuvers listed in Section III A 2. In general, the control strategies of each quadrotor have a liveness component, which specifies a set of states towards which the quadrotor aims to reach, and a safety component, which specifies a set of states that it must avoid. In this paper, we address both the liveness and safety component using reachability analysis.

**B. Hamilton-Jacobi Reachability**

**C. Intra-Platoon Controllers**

**D. Inter-Platoon Controllers**

**E. Safety Analysis**

**F. Numerical Simulations**

**IV. Conclusions**

**Appendix**

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