#### Contents 1 18 1 Basic 1.1 Run . 2 Data Structure 2 3 Graph 4 Flow & Matching 5 String DP

### 1 Basic

#### 1.1 Run

```
1  #use -> sh run.sh {name}
2  g++ -02 -std=c++14 -Wall -Wextra -Wshadow -o $1 $1.cpp
3  ./$1 < t.in > t.out
```

#### 1.2 Default

```
#include <bits/stdc++.h>
using namespace std;
using LL = long long;
#define IOS ios_base::sync_with_stdio(0); cin.tie(0);
#define pb push_back
#define eb emplace_back
const int INF = le9;
const int MOD = le9 + 7;
const double EPS = le-6;
const int MAXN = 0;
int main() {
```

#### 1.3 Black Magic

14 }

```
1 #include <bits/stdc++.h>
2 #include <ext/pb_ds/assoc_container.hpp>
3 #include <ext/pb_ds/tree_policy.hpp>
4 #include <ext/pb_ds/priority_queue.hpp>
5 using namespace std;
6 using namespace __gnu_pbds;
7 using set t =
    tree<int, null_type, less<int>, rb_tree_tag,
      tree_order_statistics_node_update>;
10 using map_t =
   tree<int, int, less<int>, rb_tree_tag,
11
12
      tree_order_statistics_node_update>;
13 using heap_t =
   __gnu_pbds::priority_queue<int>;
```

```
15 using ht_t =
     gp_hash_table<int, int>;
16
   int main() {
17
     //set----
19
     set_t st;
     st.insert(5); st.insert(6);
20
     st.insert(3); st.insert(1);
     // the smallest is (0), biggest is (n-1), kth small
         is (k-1)
24
     int num = *st.find_by_order(0);
     cout << num << '\n'; // print 1
25
26
27
     num = *st.find_by_order(st.size() - 1);
28
     cout << num << '\n'; // print 6</pre>
29
     // find the index
30
31
     int index = st.order_of_key(6);
     cout << index << '\n'; // print 3
32
33
     // check if there exists x
34
35
     int x = 5;
36
     int check = st.erase(x);
     if (check == 0) printf("st not contain 5\n");
     else if (check == 1) printf("st contain 5\n");
38
39
     //tree policy like set
41
     st.insert(5); st.insert(5);
42
     cout << st.size() << '\n'; // print 4</pre>
43
44
45
     map_t mp;
46
     mp[1] = 2;
47
     cout << mp[1] << '\n';
48
     auto tmp = *mp.find_by_order(0); // pair
49
     cout << tmp.first << " " << tmp.second << '\n';</pre>
50
     //heap------
     heap_t h1, h2;
53
     h1.push(1); h1.push(3);
     h2.push(2); h2.push(4);
55
     h1.join(h2);
     cout << h1.size() << h2.size() << h1.top() << '\n';</pre>
56
57
58
59
     //hash-table-----
60
     ht_t ht;
     ht[85] = 5;
61
62
     ht[89975] = 234;
     for (auto i : ht) {
63
       cout << i.first << " " << i.second << '\n';</pre>
     }
65
66 }
```

#### 2 Data Structure

### 2.1 Disjoint Set

```
1 // 0-base
2 const int MAXN = 1000;
3 int boss[MAXN];
4 void init(int n) {
    for (int i = 0; i < n; i++) {</pre>
      boss[i] = -1;
6
7
    }
8 }
9
  int find(int x) {
10
   if (boss[x] < 0) {
11
      return x;
    }
12
13
    return boss[x] = find(boss[x]);
14 }
15 bool uni(int a, int b) {
  a = find(a);
16
```

```
17
     b = find(b);
     if (a == b) {
18
       return false;
19
20
21
     if (boss[a] > boss[b]) {
22
       swap(a, b);
23
24
     boss[a] += boss[b];
25
     boss[b] = a;
26
     return true;
27 }
```

## 2.2 BIT RARSQ

```
1 // 1-base
2 #define lowbit(k) (k & -k)
4 int n:
5 vector<int> B1, B2;
7
  void add(vector<int> &tr, int id, int val) {
8
    for (; id <= n; id += lowbit(id)) {</pre>
      tr[id] += val;
9
10
    }
11 }
12 void range_add(int 1, int r, int val) {
13
    add(B1, 1, val);
    add(B1, r + 1, -val);
14
    add(B2, 1, val * (1 - 1));
16
    add(B2, r + 1, -val * r);
17 }
18 int sum(vector<int> &tr, int id) {
    int ret = 0;
19
    for (; id >= 1; id -= lowbit(id)) {
20
      ret += tr[id];
21
22
    }
23
    return ret;
24 }
25 int prefix_sum(int id) {
   return sum(B1, id) * id - sum(B2, id);
26
27 }
28 int range_sum(int 1, int r) {
    return prefix_sum(r) - prefix_sum(l - 1);
30 }
```

# 2.3 zkw RMQ

```
1 // 0-base
2 const int INF = 1e9;
3 const int MAXN = ;
5 int n;
6 int a[MAXN], tr[MAXN << 1];</pre>
8 // !!! remember to call this function
9 void build() {
    for (int i = 0; i < n; i++) {
10
11
      tr[i + n] = a[i];
12
13
    for (int i = n - 1; i > 0; i--) {
      tr[i] = max(tr[i << 1], tr[i << 1 | 1]);
14
15
16 }
17 void update(int id, int val) {
   for (tr[id += n] = val; id > 1; id >>= 1) {
18
19
      tr[id >> 1] = max(tr[id], tr[id ^ 1]);
   }
20
21 }
22 int query(int 1, int r) { // [1, r)
23
    int ret = -INF;
24
    for (1 += n, r += n; 1 < r; 1 >>= 1, r >>= 1) {
25
      if (1 & 1) {
        ret = max(ret, tr[1++]);
26
```

# 3 Graph

## 3.1 Dijkstra

```
1 // 0-base
2 const LL INF = 1e18;
  const int MAXN = ;
 4 struct Edge {
    int at;
    LL cost:
    bool operator < (const Edge &other) const {</pre>
      return cost > other.cost;
    }
9
10 };
11
12 int n;
13 LL dis[MAXN];
14 vector < Edge > G[MAXN];
15
16 void init() {
    for (int i = 0; i < n; i++) {</pre>
17
18
       G[i].clear();
19
       dis[i] = INF;
20
21 }
22 void Dijkstra(int st, int ed = -1) {
    priority_queue < Edge > pq;
23
     pq.push({st, 0});
25
     dis[st] = 0;
26
     while (!pq.empty()) {
27
       auto now = pq.top();
28
       pq.pop();
       if (now.at == ed) {
29
30
         return;
31
32
       if (now.cost > dis[now.at]) {
33
         continue;
34
       for (auto &e : G[now.at]) {
35
         if (dis[e.at] > now.cost + e.cost) {
36
37
           dis[e.at] = now.cost + e.cost;
38
           pq.push({ e.at, dis[e.at] });
39
40
41
     }
42 }
```

# 3.2 SPFA(negative cycle)

```
1 // 0-base
2 const LL INF = 1e18;
3 const int MAXN = ;
  struct Edge {
   int at:
    LL cost;
7 };
  int n;
10 LL dis[MAXN]:
11 vector < Edge > G[MAXN];
12
13 void init() {
    for (int i = 0; i < n; i++) {
14
15
      G[i].clear();
```

```
16
       dis[i] = INF;
17
    }
18 }
19 bool SPFA(int st) {
20
    vector<int> cnt(n, 0);
     vector<bool> inq(n, false);
21
     queue<int> q;
22
23
     q.push(st);
24
     dis[st] = 0;
25
26
     inq[st] = true;
     while (!q.empty()) {
27
28
       int now = q.front();
29
       q.pop();
30
       inq[now] = false;
       for (auto &e : G[now]) {
31
         if (dis[e.at] > dis[now] + e.cost) {
32
33
           dis[e.at] = dis[now] + e.cost;
           if (!inq[e.at]) {
34
35
              cnt[e.at]++;
              if (cnt[e.at] > n) {
36
37
                // negative cycle
38
                return false;
39
40
              inq[e.at] = true;
41
              q.push(e.at);
42
43
44
45
     }
46
     return true;
```

## 3.3 Floyd Warshall

```
1 // 0-base
2 // G[i][i] < 0 \rightarrow negative cycle
3 const LL INF = 1e18;
4 const int MAXN = ;
6 int n;
7 LL G[MAXN][MAXN];
9 void init() {
    for (int i = 0; i < n; i++) {
10
11
       for (int j = 0; j < n; j++) {
         G[i][j] = INF;
12
13
       G[i][i] = 0;
14
15
    }
16 }
17 void floyd() {
18
     for (int k = 0; k < n; k++) {
       for (int i = 0; i < n; i++) {</pre>
19
         for (int j = 0; j < n; j++) {
20
           if (G[i][k] != INF && G[k][j] != INF) {
21
22
             G[i][j] = min(G[i][j], G[i][k] + G[k][j]);
23
           }
24
         }
25
     }
26
27 }
```

# 3.4 Topological Sort

```
1 // 0-base
2 // if ret.size < n -> cycle
3 int n;
4 vector<vector<int>> G;
5
6 vector<int> topoSort() {
7 vector<int> indeg(n), ret;
8 for (auto &li : G) {
```

```
9
       for (int x : li) {
10
         ++indeg[x];
11
       }
    }
12
13
     // use priority queue for lexic. largest ans
14
     queue<int> q;
15
     for (int i = 0; i < n; i++) {
16
       if (!indeg[i]) {
         q.push(i);
17
       }
18
19
     }
     while (!q.empty()) {
20
21
       int u = q.front();
       q.pop();
22
23
       ret.pb(u);
       for (int v : G[u]) {
24
25
         if (--indeg[v] == 0) {
26
           q.push(v);
27
28
       }
    }
29
30
     return ret;
31 }
```

## 3.5 Kosaraju

```
1 // 0-base
2 int n;
3 vector<vector<int>>> G, G2; // G2 = G rev
  vector < bool > vis;
  vector<int> s, color;
  int sccCnt;
6
  void dfs1(int u) {
     vis[u] = true;
     for (int v : G[u]) {
9
10
      if (!vis[v]) {
11
        dfs1(v);
12
13
    }
14
    s.pb(u);
15 }
  void dfs2(int u) {
16
     color[u] = sccCnt;
18
     for (int v : G2[u]) {
19
      if (!color[v]) {
20
         dfs2(v);
21
22
    }
23 }
24
  void Kosaraju() {
25
     sccCnt = 0;
     for (int i = 0; i < n; i++) {</pre>
26
27
       if (!vis[i]) {
28
         dfs1(i);
29
30
31
     for (int i = n - 1; i >= 0; i--) {
32
       if (!color[s[i]]) {
         ++sccCnt;
33
         dfs2(s[i]);
34
       }
35
36
    }
37 }
```

#### 3.6 Tree Diameter

```
1 // 0-base;
2 const int MAXN = ;
3
4 struct Edge {
   int to;
   int cost;
7 };
```

48

49

50

int run() {

```
9 | int n, d = 0;
10 int d1[MAXN], d2[MAXN];
11 vector < Edge > G[MAXN];
12 // dfs(0, -1);
13 void dfs(int u, int from) {
     d1[u] = d2[u] = 0;
14
15
     for (auto e : G[u]) {
       if (e.to == from) {
16
17
         continue;
18
       dfs(e.to, u);
19
20
       int t = d1[e.to] + e.cost;
       if (t > d1[u]) {
21
22
         d2[u] = d1[u];
         d1[u] = t;
23
       } else if (t > d2[u]) {
24
25
         d2[u] = t;
26
27
     }
     d = max(d, d1[u] + d2[u]);
28
29 }
```

# 4 Flow & Matching

#### 4.1 KM

```
1 const int INF = 1e9;
  const int MAXN = ;
3 struct KM { //1-base
     int n, G[MAXN][MAXN];
     int lx[MAXN], ly[MAXN], my[MAXN];
6
     bool vx[MAXN], vy[MAXN];
7
     void init(int _n) {
       n = _n;
8
       for (int i = 1; i <= n; i++) {</pre>
         for (int j = 1; j <= n; j++) {</pre>
10
11
           G[i][j] = 0;
12
       }
13
     }
14
15
     bool match(int i) {
16
       vx[i] = true;
17
       for (int j = 1; j <= n; j++) {</pre>
         if (lx[i] + ly[j] == G[i][j] && !vy[j]) {
18
19
            vy[j] = true;
            if (!my[j] || match(my[j])) {
20
21
              my[j] = i;
22
              return true;
           }
23
         }
24
25
       }
26
       return false;
27
     void update() {
28
29
       int delta = INF;
       for (int i = 1; i <= n; i++) {</pre>
30
31
          if (vx[i]) {
            for (int j = 1; j <= n; j++) {</pre>
32
33
              if (!vy[j]) {
34
                delta = min(delta, lx[i] + ly[j] -
                     G[i][j]);
35
           }
36
37
         }
38
39
       for (int i = 1; i <= n; i++) {</pre>
40
         if (vx[i]) {
           lx[i] -= delta;
41
42
         if (vy[i]) {
43
44
            ly[i] += delta;
45
46
```

#### 51 for (int j = 1; j <= n; j++) {</pre> 52 lx[i] = max(lx[i], G[i][j]);53 54 55 for (int i = 1; i <= n; i++) { 56 while (true) { 57 for (int i = 1; i <= n; i++) {</pre> vx[i] = vy[i] = 0;58 59 if (match(i)) { 60 61 break; } else { 62 update(); 63 } 64 65 } 66 int ans = 0; 67 68 for (int i = 1; i <= n; i++) { 69 ans += lx[i] + ly[i];70 71 return ans; 72 73 };

for (int i = 1; i <= n; i++) {

lx[i] = ly[i] = my[i] = 0;

#### 4.2 Dinic

```
1 #define eb emplace_back
2 const LL INF = 1e18;
3 const int MAXN = ;
4 struct Edge {
    int to;
    LL cap;
    int rev:
    Edge(int v, LL c, int r) : to(v), cap(c), rev(r) {}
9 };
10 struct Dinic {
11
    int n;
    int level[MAXN], now[MAXN];
12
     vector<Edge> G[MAXN];
13
14
     void init(int _n) {
      n = _n;
15
       for (int i = 0; i <= n; i++) {</pre>
16
17
         G[i].clear();
18
      }
    }
19
20
     void add_edge(int u, int v, LL c) {
      G[u].eb(v, c, G[v].size());
21
       // directed graph
22
23
      G[v].eb(u, 0, G[u].size() - 1);
       // undirected graph
24
25
       // G[v].eb(u, c, G[u].size() - 1);
26
27
     bool bfs(int st, int ed) {
28
       fill(level, level + n + 1, -1);
       queue < int > q;
29
30
       q.push(st);
31
       level[st] = 0;
32
       while (!q.empty()) {
33
         int u = q.front();
         q.pop();
34
35
         for (const auto &e : G[u]) {
           if (e.cap > 0 && level[e.to] == -1) {
36
37
             level[e.to] = level[u] + 1;
38
             q.push(e.to);
39
           }
40
         }
41
42
       return level[ed] != -1;
43
44
    LL dfs(int u, int ed, LL limit) {
       if (u == ed) {
45
         return limit;
```

```
47
       LL ret = 0;
48
49
       for (int &i = now[u]; i < G[u].size(); i++) {</pre>
         auto &e = G[u][i];
50
         if (e.cap > 0 && level[e.to] == level[u] + 1) {
51
           LL f = dfs(e.to, ed, min(limit, e.cap));
52
           ret += f;
53
           limit -= f;
           e.cap -= f;
55
           G[e.to][e.rev].cap += f;
56
57
           if (!limit) {
58
              return ret;
59
           }
         }
60
61
       if (!ret) {
62
         level[u] = -1;
63
64
65
       return ret;
66
     LL flow(int st, int ed) {
67
       LL ret = 0;
68
       while (bfs(st, ed)) {
69
70
         fill(now, now + n + 1, 0);
71
         ret += dfs(st, ed, INF);
72
73
       return ret;
74
     }
75 };
```

# 5 String

## 5.1 Manacher

```
1 int p[2 * MAXN];
2 int Manacher(const string &s) {
     string st = "@#";
3
     for (char c : s) {
       st += c;
       st += '#';
6
    st += '$';
8
    int id = 0, mx = 0, ans = 0;
9
10
     for (int i = 1; i < st.length() - 1; i++) {</pre>
      p[i] = (mx > i ? min(p[2 * id - i], mx - i) : 1);
11
12
       for (; st[i - p[i]] == st[i + p[i]]; p[i]++);
       if (mx < i + p[i]) {
13
         mx = i + p[i];
14
15
         id = i;
16
       }
17
       ans = max(ans, p[i] - 1);
    }
18
19
     return ans;
20 }
```

# 6 DP

#### 6.1 LIS

```
1 int LIS(vector<int> &a) {
2   vector<int> s;
3   for (int i = 0; i < a.size(); i++) {
4     if (s.empty() || s.back() < a[i]) {
5         s.push_back(a[i]);
6     } else {
7         *lower_bound(s.begin(), s.end(), a[i],
8         [](int x, int y) {return x < y;}) = a[i];
9     }
10   }
11   return s.size();
12 }</pre>
```

# 7 Math

#### 7.1 Extended GCD

```
1 // ax + by = c
  int extgcd(int a, int b, int c, int &x, int &y) {
    if (b == 0) {
      x = c / a;
      y = 0;
5
6
      return a;
7
    }
8
    int d = extgcd(b, a % b, c, x, y);
9
    int tmp = x;
    x = y;
10
    y = tmp - (a / b) * y;
11
12
    return d;
13 }
```