1

1

2

5

6

6

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Basic

1.1 Run

```
1 #use -> sh run.sh {name}
2 g++ -02 -std=c++14 -Wall -Wextra -Wshadow -o $1 $1.cpp
3 ./$1 < t.in > t.out
```

Ternary Search

```
1 const double EPS = 1e-6;
2 // target function
3 double f(double x) { return x * x; }
4 double ternarySearch() {
     double L = -1e5, R = 1e5;
    while (R - L > EPS) {
       double mr = (L + R) / 2.0;
8
       double ml = (L + mr) / 2.0;
      if (f(ml) < f(mr)) {</pre>
9
10
        R = mr;
      } else {
11
12
         L = ml;
13
14
    }
15
     return L;
16 }
```

Data Structure

2.1 BIT RARSQ

```
1 // 1-base
2 #define lowbit(k) (k & -k)
3
 int n;
5
 vector<int> B1, B2;
```

```
void add(vector<int> &tr, int id, int val) {
       for (; id <= n; id += lowbit(id)) {</pre>
   9
         tr[id] += val;
1 10
      }
    }
  11
    void range_add(int 1, int r, int val) {
1 12
       add(B1, 1, val);
  13
  14
       add(B1, r + 1, -val);
 15
       add(B2, 1, val * (1 - 1));
       add(B2, r + 1, -val * r);
  16
  17 }
  18 int sum(vector<int> &tr, int id) {
  19
       int ret = 0;
       for (; id >= 1; id -= lowbit(id)) {
  20
  21
        ret += tr[id];
  22
  23
       return ret;
  24 }
  25 int prefix_sum(int id) {
  26
      return sum(B1, id) * id - sum(B2, id);
  27 }
  28 int range_sum(int 1, int r) {
  29
      return prefix_sum(r) - prefix_sum(l - 1);
```

2.2 zkw RMQ

```
1 // 0-base
  const int INF = 1e9;
  const int MAXN = ;
5
  int n;
  int a[MAXN], tr[MAXN << 1];</pre>
6
  // !!! remember to call this function
8
  void build() {
    for (int i = 0; i < n; i++) {</pre>
10
      tr[i + n] = a[i];
11
12
    for (int i = n - 1; i > 0; i--) {
13
14
      tr[i] = max(tr[i << 1], tr[i << 1 | 1]);
    }
15
  }
16
  void update(int id, int val) {
17
18
    for (tr[id += n] = val; id > 1; id >>= 1) {
19
      tr[id >> 1] = max(tr[id], tr[id ^ 1]);
20
21 }
22
  int query(int 1, int r) { // [1, r)
23
    int ret = -INF;
24
    for (1 += n, r += n; 1 < r; 1 >>= 1, r >>= 1) {
25
      if (1 & 1) {
26
         ret = max(ret, tr[1++]);
      }
27
      if (r & 1) {
28
         ret = max(ret, tr[--r]);
29
30
31
    }
32
    return ret;
33
```

2.3 Segment Tree RARMQ

```
1 struct Node {
    int val, tag;
3
    Node *lc, *rc;
    Node() : lc(nullptr), rc(nullptr), tag(0) {}
    void pull() {
     if (!lc) {
7
        val = rc->val;
      } else if (!rc) {
8
        val = lc->val;
9
      } else {
```

```
11
         val = max(lc->val, rc->val);
       }
12
     }
13
     void push() {
14
15
       if (lc) {
16
         lc->tag += tag;
         lc->val += tag;
17
18
       if (rc) {
19
20
         rc->tag += tag;
21
         rc->val += tag;
       }
22
23
       tag = 0;
     }
24
25 };
26 struct SegmentTree {
     Node *root;
27
28
     SegmentTree() : root(nullptr) {}
     void build(Node* &T, int 1, int r, const
29
         vector<int> &o) {
       T = new Node();
30
31
       if (1 == r) {
32
         T->val = o[1];
         return;
33
34
       int mid = (1 + r) / 2;
35
       build(T->lc, 1, mid, o);
36
37
       build(T->rc, mid + 1, r, o);
38
       T->pull():
39
     }
     void update(Node* &T, int 1, int r, int ql, int qr,
40
         int v) {
41
       if (q1 <= 1 && r <= qr) {</pre>
42
         T->val += v;
43
         T->tag += v;
44
         return:
45
       }
       T->push();
46
       int mid = (1 + r) / 2;
47
       if (qr <= mid) {
48
49
         update(T->lc, l, mid, ql, qr, v);
50
       } else if (mid < ql) {</pre>
         update(T->rc, mid + 1, r, ql, qr, v);
51
52
       } else {
53
         update(T->lc, 1, mid, ql, mid, v);
         update(T->rc, mid + 1, r, mid + 1, qr, v);
54
55
       T->pull();
56
57
     int query(Node* &T, int 1, int r, int q1, int qr) {
58
59
       if (ql <= 1 && r <= qr) {
60
         return T->val;
61
       T->push();
62
       int mid = (1 + r) / 2;
63
       if (qr <= mid) {
64
         return query(T->lc, 1, mid, ql, qr);
65
       } else if (mid < ql) {</pre>
66
67
         return query(T->rc, mid + 1, r, ql, qr);
68
       } else {
         return max(query(T->lc, l, mid, ql, mid),
69
70
              query(T->rc, mid + 1, r, mid + 1, qr));
71
72
     }
73 };
```

2.4 Treap

```
1  struct Treap {
2    int val, pri, sz;
3    Treap *lc, *rc;
4    Treap() {}
5    Treap(int _val) {
6     val = _val;
7    pri = rand();
8    sz = 1;
```

```
9
       lc = rc = NULL;
    }
10
11 };
12 int getSize(Treap *a) { return (a == NULL ? 0 :
       a->sz); }
13
  void split(Treap *t, Treap *&a, Treap *&b, int k) {
    if (t == NULL) {
14
15
       a = b = NULL;
16
       return;
17
18
     if (getSize(t->lc) < k) {</pre>
19
20
       split(t->rc, a->rc, b, k - getSize(t->lc) - 1);
21
    } else {
22
       b = t;
       split(t->lc, a, b->lc, k);
23
24
    }
25 }
26
  Treap *merge(Treap *a, Treap *b) {
27
     if (!a || !b) {
28
      return (a ? a : b);
29
    if (a->pri > b->pri) {
30
31
       a->rc = merge(a->rc, b);
32
       return a;
33
    } else {
       b->lc = merge(a, b->lc);
34
35
       return b;
36
37
  }
38 void Insert(Treap *&t, int x, int p) {
    Treap *a, *b;
40
     split(t, a, b, x);
41
    t = merge(a, merge(new Treap(p), b));
42 }
43 void Delete(Treap *&t, int x) {
44
    Treap *a, *b, *c;
45
    split(t, b, c, x);
46
     split(b, a, b, x - 1);
47
     t = merge(a, c);
48 }
49
50
  Usage
52 Treap *root = NULL; // declare
53 root = merge(root, new Treap(val)); // push back
54 Insert(root, x, y); // insert y after x-th element
  Delete(root, x); // delete x-th element
55
56
```

3 Graph

3.1 Directed MST

```
1 // 0-base
2 const LL INF = 1e18;
  const int MAXN = ;
3
5
  struct Edge {
    int from;
7
    int to;
8
    LL cost;
9
    Edge(int u, int v, LL c) : from(u), to(v), cost(c)
         {}
10 };
11
12 struct DMST {
13
    int n;
    int vis[MAXN], pre[MAXN], id[MAXN];
14
15
    LL in[MAXN];
16
    vector<Edge> edges;
17
     void init(int _n) {
18
      n = _n;
      edges.clear();
19
```

96 };

```
20
     void add_edge(int from, int to, LL cost) {
21
       edges.eb(from, to, cost);
22
23
24
     LL run(int root) {
25
       LL ret = 0;
       while (true) {
26
27
         for (int i = 0; i < n; i++) {</pre>
           in[i] = INF;
28
29
30
          // find in edge
31
32
         for (auto &e : edges) {
           if (e.cost < in[e.to] && e.from != e.to) {</pre>
33
34
              pre[e.to] = e.from;
              in[e.to] = e.cost;
35
           }
36
         }
37
38
39
          // check in edge
         for (int i = 0; i < n; i++) {</pre>
40
41
            if (i == root) {
42
              continue;
43
            if (in[i] == INF) {
44
45
              return -1;
46
         }
47
48
49
          int nodenum = 0;
         memset(id, -1, sizeof(id));
50
51
          memset(vis, -1, sizeof(vis));
52
         in[root] = 0;
53
          // find cycles
54
55
         for (int i = 0; i < n; i++) {
56
            ret += in[i];
            int v = i;
57
            while (vis[v] != i && id[v] == -1 && v !=
58
                root) {
59
              vis[v] = i;
60
              v = pre[v];
61
            if (id[v] == -1 && v != root) {
62
              for (int j = pre[v]; j != v; j = pre[j]) {
63
               id[j] = nodenum;
64
65
              }
              id[v] = nodenum++;
66
67
           }
         }
68
69
70
          // no cycle
71
         if (nodenum == 0) {
72
           break:
73
74
75
         for (int i = 0; i < n; i++) {
            if (id[i] == -1) {
76
77
              id[i] = nodenum++;
           }
78
79
         }
80
81
          // grouping the vertices
82
         for (auto &e : edges) {
           int to = e.to;
83
84
            e.from = id[e.from];
            e.to = id[e.to];
85
            if (e.from != e.to) {
86
87
              e.cost -= in[to]; //!!!
            }
88
89
         }
90
91
         n = nodenum;
         root = id[root];
92
93
94
       return ret;
95
     }
```

3.2 LCA

```
1 const int LOG = 20;
  vector<int> tin(MAXN), tout(MAXN), depth(MAXN);
  int par[MAXN][LOG];
 3
  int timer = 0;
  vector<int> G[MAXN];
 7
  void dfs(int u, int f) {
 8
     tin[u] = ++timer;
     par[u][0] = f;
10
     for (int v : G[u]) {
11
       if (v != f) {
12
         depth[v] = depth[u] + 1;
13
         dfs(v, u);
14
15
    }
16
     tout[u] = ++timer;
17 }
18
19
  void Doubling(int n) {
    for (int j = 1; j < LOG; ++j) {</pre>
20
21
       for (int i = 1; i <= n; ++i) {
22
         par[i][j] = par[par[i][j - 1]][j - 1];
23
24
    }
25 }
26
  bool anc(int u, int v) { return tin[u] <= tin[v] &&</pre>
27
       tout[v] <= tout[u]; }</pre>
28
  int LCA(int u, int v) {
29
    if (depth[u] > depth[v]) {
30
31
       swap(u, v);
    }
32
33
     if (anc(u, v)) {
34
      return u;
35
     for (int j = LOG - 1; j >= 0; --j) {
36
37
       if (!anc(par[u][j], v)) u = par[u][j];
    }
38
39
     return par[u][0];
40
  }
41
42
  int dis(int u, int v) {
    int lca = LCA(u, v);
43
     return depth[u] + depth[v] - 2 * depth[lca];
44
45 }
46
47
48 dfs(root, root);
49
  Doubling(n);
50
```

3.3 Euler Circuit

七橋問題根據起點與終點是否相同,分成 Euler path(不同)及 Euler circuit(相同)。

- 判斷法
- · 無向圖部分,將點分成奇點(度數為奇數)和偶點(度數為偶數)。
 - Euler path:奇點數為 0 或 2
 - Euler circuit:沒有奇點
- · 有向圖部分,將點分成出點 (出度 入度 = 1) 和入點 (入度 出度 = 1) 還 有平衡點 (出度 = 入度)。
 - Euler path:出點和入點個數同時為 0 或 1。
 - Euler circuit:只有平衡點。
- · 求出一組解

```
• 用 DFS 遍歷整張圖,設 S 為離開的順序,無向圖的答案為 S ,有向圖的答案
       為反向的 S 。
     - Euler path:無向圖選擇任意一個奇點,有向圖選擇出點。
          - Euler circuit:任意一點。
 1 // Code from Eric
2 #define 11 long long
3 #define PB push_back
4 #define EB emplace_back
5 #define PII pair<int, int>
6 #define MP make_pair
7 #define all(x) x.begin(), x.end()
 8 #define maxn 50000+5
10 //structure
11 struct Eular {
    vector<PII> adj[maxn];
12
    vector < bool > edges;
    vector < PII > path;
14
15
     int chk[maxn];
16
    int n;
17
     void init(int _n) {
18
19
       n = _n;
20
       for (int i = 0; i <= n; i++) adj[i].clear();</pre>
21
       edges.clear();
       path.clear();
22
23
       memset(chk, 0, sizeof(chk));
    }
24
25
     void dfs(int v) {
26
27
       for (auto i : adj[v]) {
28
         if (edges[i.first] == true) {
           edges[i.first] = false;
29
           dfs(i.second);
30
           path.EB(MP(i.second, v));
31
32
       }
33
    }
34
35
     void add_Edge(int from, int to) {
36
       edges.PB(true);
37
38
39
       // for bi-directed graph
40
       adj[from].PB(MP(edges.size() - 1, to));
       adj[to].PB(MP(edges.size() - 1, from));
41
42
       chk[from]++;
       chk[to]++;
43
44
       // for directed graph
45
       // adj[from].PB(MP(edges.size()-1, to));
46
47
       // check[from]++;
48
49
50
     bool eular_path() {
       int st = -1;
51
       for (int i = 1; i <= n; i++) {</pre>
52
         if (chk[i] % 2 == 1) {
53
54
           st = i;
55
           break;
56
        }
57
       }
       if (st == -1) {
58
59
         return false;
60
61
       dfs(st);
62
       return true;
63
64
     void print_path(void) {
65
       for (auto i : path) {
66
67
         printf("%d %d\n", i.first, i.second);
68
69
    }
70 };
```

```
1 // Code from allen(lexicographic order)
 2 #include <bits/stdc++.h>
  using namespace std;
 4 const int ALP = 30;
  const int MXN = 1005;
  int n;
  int din[ALP], dout[ALP];
 8 int par[ALP];
  vector<string> vs[MXN], ans;
9
10 bitset < MXN > vis, used[ALP];
  void djsInit() {
12
    for (int i = 0; i != ALP; ++i) {
13
      par[i] = i;
14
15
16 }
17
18
  int Find(int x) { return (x == par[x] ? (x) : (par[x]
       = Find(par[x])); }
19
20 void init() {
     djsInit();
    memset(din, 0, sizeof(din));
22
23
     memset(dout, 0, sizeof(dout));
24
     vis.reset();
    for (int i = 0; i != ALP; ++i) {
25
       vs[i].clear();
26
       used[i].reset();
27
28
    }
29
     return:
30 }
31
  void dfs(int u) {
32
33
     for (int i = 0; i != (int)vs[u].size(); ++i) {
34
       if (used[u][i]) {
35
         continue;
36
       }
       used[u][i] = 1;
37
       string s = vs[u][i];
38
       int v = s[s.size() - 1] - 'a';
39
40
       dfs(v);
41
       ans.push_back(s);
42
    }
43 }
44
45
  bool solve() {
46
    int cnt = 1;
47
     for (int i = 0; i != n; ++i) {
48
       string s;
49
       cin >> s;
50
       int from = s[0] - 'a', to = s.back() - 'a';
51
       ++din[to];
52
       ++dout[from];
53
       vs[from].push_back(s);
       vis[from] = vis[to] = true;
54
55
       if ((from = Find(from)) != (to = Find(to))) {
56
         par[from] = to;
57
         ++cnt:
58
      }
59
60
     if ((int)vis.count() != cnt) {
61
      return false;
62
63
     int root, st, pin = 0, pout = 0;
     for (int i = ALP - 1; i >= 0; --i) {
64
65
       sort(vs[i].begin(), vs[i].end());
       if (vs[i].size()) root = i;
66
       int d = dout[i] - din[i];
67
       if (d == 1) {
68
69
         ++pout;
70
         st = i;
71
       } else if (d == -1) {
72
         ++pin;
       } else if (d != 0) {
73
74
         return false;
75
       }
76
    }
```

4

```
77
     if (pin != pout || pin > 1) {
78
       return false;
79
     }
80
     ans.clear();
81
     dfs((pin ? st : root));
82
     return true;
83 }
84
85 int main() {
86
     int t;
87
     cin >> t;
     while (t--) {
88
       cin >> n;
89
       init();
90
91
       if (!solve()) {
         cout << "***\n";
92
         continue;
93
94
       for (int i = ans.size() - 1; i >= 0; --i) {
95
96
         cout << ans[i] << ".\n"[i == 0];
97
98
99 }
```

4 Connectivity

4.1 Articulation Point

```
1 // from aizu
2 typedef long long int 11;
 3 typedef unsigned long long int ull;
4 #define BIG_SIZE 2000000000
5 #define MOD 1000000007
6 #define EPS 0.000000001
7 using namespace std;
9 #define SIZE 100000
10
11 vector<int> G[SIZE];
12 int N:
13 bool visited[SIZE];
14 int visited_order[SIZE], parent[SIZE], lowest[SIZE],
       number;
15
16 void dfs(int cur, int pre_node) {
17
     visited_order[cur] = lowest[cur] = number;
18
     number++;
19
     visited[cur] = true;
20
21
     int next;
22
23
24
     for (int i = 0; i < G[cur].size(); i++) {</pre>
25
       next = G[cur][i];
       if (!visited[next]) {
26
27
         parent[next] = cur;
28
         dfs(next, cur);
29
         lowest[cur] = min(lowest[cur], lowest[next]);
       } else if (visited[next] == true && next !=
30
           pre_node) {
31
         lowest[cur] = min(lowest[cur],
              visited_order[next]);
32
    }
33
34 }
35
36 void art_points() {
37
     for (int i = 0; i < N; i++) visited[i] = false;</pre>
38
     number = 1;
39
40
     dfs(0, -1);
41
42
     int tmp_parent, root_num = 0;
43
```

```
44
     vector<int> V;
45
46
     for (int i = 1; i < N; i++) {</pre>
47
       tmp_parent = parent[i];
48
       if (tmp_parent == 0) {
49
         root_num++;
       } else if (visited_order[tmp_parent] <=</pre>
50
            lowest[i]) {
51
         V.push_back(tmp_parent);
52
53
     }
     if (root_num >= 2) {
54
55
       V.push_back(0);
56
57
     sort(V.begin(), V.end());
     V.erase(unique(V.begin(), V.end()), V.end());
58
59
60
     for (int i = 0; i < V.size(); i++) {</pre>
61
       printf("%d \setminus n", V[i]);
62
63 }
64
65 int main() {
66
    int E;
     scanf("%d %d", &N, &E);
67
68
     int from, to;
     for (int i = 0; i < E; i++) {
69
70
       scanf("%d %d", &from, &to);
71
       G[from].push_back(to);
72
       G[to].push_back(from);
    }
73
74
     art_points();
75 }
```

4.2 Bridges

```
1 // from aizu
  typedef long long int 11;
  typedef unsigned long long int ull;
  #define BIG_NUM 2000000000
  #define MOD 1000000007
  #define EPS 0.000000001
  using namespace std;
9
  struct Edge {
10
     bool operator<(const struct Edge &arg) const {</pre>
       if (s != arg.s) {
11
         return s < arg.s;</pre>
       } else {
13
14
         return t < arg.t;</pre>
15
       }
    }
16
17
    int s, t;
18 };
19
  struct Info {
20
    Info(int arg_to, int arg_edge_id) {
       to = arg_to;
21
22
       edge_id = arg_edge_id;
    }
23
24
     int to, edge_id;
25 };
26
27 int V, E, number;
  int order[100000], lowlink[100000];
28
29
  bool visited[100000];
30
  Edge edge[100000]:
  vector < Info > G[100000];
32
33
  void recursive(int cur) {
     order[cur] = number++;
    lowlink[cur] = order[cur];
35
36
37
     int next;
38
     for (int i = 0; i < G[cur].size(); i++) {</pre>
39
       next = G[cur][i].to;
40
```

```
41
       if (order[next] == -1) {
42
43
         visited[G[cur][i].edge_id] = true;
44
         recursive(next);
45
         lowlink[cur] = min(lowlink[cur], lowlink[next]);
46
       } else if (visited[G[cur][i].edge_id] == false) {
47
48
         lowlink[cur] = min(lowlink[cur], order[next]);
49
50
     }
51 }
52
53 int main() {
     scanf("%d %d", &V, &E);
54
55
     for (int i = 0; i < E; i++) {
       scanf("%d %d", &edge[i].s, &edge[i].t);
56
57
       if (edge[i].s > edge[i].t) {
58
         swap(edge[i].s, edge[i].t);
59
60
       G[edge[i].s].push_back(Info(edge[i].t, i));
61
       G[edge[i].t].push_back(Info(edge[i].s, i));
62
63
     sort(edge, edge + E);
64
65
     number = 0;
66
     for (int i = 0; i < V; i++) {</pre>
67
       order[i] = -1;
68
       lowlink[i] = -1;
69
70
     for (int i = 0; i < E; i++) {</pre>
71
72
       visited[i] = false;
73
    }
74
75
     recursive(0);
76
77
     int from, to;
     for (int i = 0; i < E; i++) {
78
79
       from = edge[i].s;
80
       to = edge[i].t;
81
       if (order[edge[i].s] > order[edge[i].t]) {
82
         swap(from, to);
83
       if (order[from] < lowlink[to]) {</pre>
84
         printf("%d %d\n", edge[i].s, edge[i].t);
85
86
87
    }
88
     return 0;
89 }
```

5 Flow & Matching

5.1 Relation

```
1 | 1. 一般圖
2 | |最大匹配 | + |最小邊覆蓋 | = |V|
3 | |最大獨立集 | + |最小點覆蓋 | = |V|
4 | |最大圖 | = |補圖的最大獨立集 |
5 | 2. 二分圖
6 | |最大匹配 | = |最小點覆蓋 |
7 | |最大獨立集 | = |根小邊覆蓋 |
8 | |最大獨立集 | = |V| - |最大匹配 |
9 | |最大圖 | = |補圖的最大獨立集 |
```

5.2 Bipartite Matching

```
1 // 0-base
2 const int MAXN = ;
3 int n;
4 vector<int> G[MAXN];
5 int vy[MAXN], my[MAXN];
```

```
bool match(int u) {
7
     for (int v : G[u]) {
       if (vy[v]) {
9
10
         continue;
11
       vy[v] = true;
12
13
       if (my[v] == -1 || match(my[v])) {
14
         my[v] = u;
15
         return true;
16
17
    }
18
     return false;
19 }
20
  int sol() {
    int cnt = 0;
21
     memset(my, -1, sizeof(my));
22
23
     for (int i = 0; i < n; i++) {
       memset(vy, 0, sizeof(vy));
24
25
       if (match(i)) {
26
         cnt++;
27
    }
28
29
     return cnt;
30 }
```

5.3 KM

```
1 const int INF = 1e9;
  const int MAXN = ;
  struct KM { //1-base
 3
     int n, G[MAXN][MAXN];
     int lx[MAXN], ly[MAXN], my[MAXN];
 6
     bool vx[MAXN], vy[MAXN];
7
     void init(int _n) {
       n = _n;
       for (int i = 1; i <= n; i++) {</pre>
9
         for (int j = 1; j \le n; j++) {
10
           G[i][j] = 0;
11
12
13
       }
14
     }
15
     bool match(int i) {
16
       vx[i] = true;
17
       for (int j = 1; j \le n; j++) {
18
         if (lx[i] + ly[j] == G[i][j] && !vy[j]) {
            vy[j] = true;
19
20
            if (!my[j] || match(my[j])) {
21
              my[j] = i;
22
              return true;
           }
23
24
         }
25
       }
26
       return false;
27
28
     void update() {
       int delta = INF;
29
       for (int i = 1; i <= n; i++) {
30
31
         if (vx[i]) {
32
            for (int j = 1; j <= n; j++) {</pre>
33
             if (!vy[j]) {
34
                delta = min(delta, lx[i] + ly[j] -
                    G[i][j]);
35
36
           }
         }
37
38
       for (int i = 1; i <= n; i++) {
39
40
         if (vx[i]) {
41
           lx[i] -= delta;
42
43
         if (vy[i]) {
44
           ly[i] += delta;
45
46
       }
47
     }
```

```
48
     int run() {
                                                                   48
                                                                          LL ret = 0;
       for (int i = 1; i <= n; i++) {</pre>
                                                                          for (int &i = now[u]; i < G[u].size(); i++) {</pre>
                                                                   49
49
          lx[i] = ly[i] = my[i] = 0;
                                                                   50
                                                                             auto &e = G[u][i];
50
                                                                   51
                                                                             if (e.cap > 0 && level[e.to] == level[u] + 1) {
51
          for (int j = 1; j <= n; j++) {</pre>
52
            lx[i] = max(lx[i], G[i][j]);
                                                                   52
                                                                               LL f = dfs(e.to, ed, min(limit, e.cap));
53
                                                                   53
                                                                               ret += f;
                                                                               limit -= f;
54
                                                                   54
                                                                               e.cap -= f;
55
       for (int i = 1; i <= n; i++) {
                                                                   55
          while (true) {
                                                                   56
                                                                               G[e.to][e.rev].cap += f;
56
            for (int i = 1; i <= n; i++) {</pre>
57
                                                                   57
                                                                               if (!limit) {
58
              vx[i] = vy[i] = 0;
                                                                   58
                                                                                 return ret;
                                                                               }
                                                                   59
59
            if (match(i)) {
                                                                   60
                                                                            }
60
              break;
                                                                   61
61
62
            } else {
                                                                   62
                                                                          if (!ret) {
63
              update();
                                                                   63
                                                                            level[u] = -1;
64
                                                                   64
65
         }
                                                                   65
                                                                          return ret;
       }
                                                                   66
66
67
       int ans = 0;
                                                                   67
                                                                        LL flow(int st, int ed) {
       for (int i = 1; i <= n; i++) {</pre>
                                                                          LL ret = 0;
68
                                                                   68
69
         ans += lx[i] + ly[i];
                                                                   69
                                                                          while (bfs(st, ed)) {
70
                                                                   70
                                                                            fill(now, now + n + 1, 0);
71
                                                                   71
                                                                            ret += dfs(st, ed, INF);
       return ans;
72
                                                                   72
73 };
                                                                   73
                                                                          return ret;
                                                                   74
                                                                        }
                                                                   75 };
```

5.4 Dinic

```
1 #define eb emplace_back
2 const LL INF = 1e18;
3 const int MAXN = ;
 4 struct Edge {
5
    int to;
    LL cap;
6
     int rev;
7
    Edge(int v, LL c, int r) : to(v), cap(c), rev(r) {}
8
10 struct Dinic {
11
    int n:
12
     int level[MAXN], now[MAXN];
     vector<Edge> G[MAXN];
13
14
     void init(int _n) {
15
       n = _n;
       for (int i = 0; i <= n; i++) {</pre>
16
17
         G[i].clear();
18
19
     void add_edge(int u, int v, LL c) {
20
21
       G[u].eb(v, c, G[v].size());
22
       // directed graph
       G[v].eb(u, 0, G[u].size() - 1);
23
       // undirected graph
24
25
       // G[v].eb(u, c, G[u].size() - 1);
26
     bool bfs(int st, int ed) {
27
       fill(level, level + n + 1, -1);
28
       queue<int> q;
29
       q.push(st);
30
31
       level[st] = 0;
32
       while (!q.empty()) {
33
         int u = q.front();
34
         q.pop();
         for (const auto &e : G[u]) {
35
36
           if (e.cap > 0 && level[e.to] == -1) {
             level[e.to] = level[u] + 1;
37
38
             q.push(e.to);
           }
39
40
         }
41
       }
       return level[ed] != -1;
42
43
44
     LL dfs(int u, int ed, LL limit) {
45
       if (u == ed) {
         return limit;
46
47
```

5.5 MCMF

```
1 // 0-base
2 const LL INF = 1e18;
3 const int MAXN = ;
  struct Edge {
    int u, v;
    LL cost;
    LL cap;
    Edge(int _u, int _v, LL _c, LL _cap) : u(_u),
8
         v(_v), cost(_c), cap(_cap) {}
9 };
10 struct MCMF {
                     // ing times
    int n, pre[MAXN], cnt[MAXN];
12
    LL ans_flow, ans_cost, dis[MAXN];
13
    bool ing[MAXN];
14
    vector<int> G[MAXN];
    vector < Edge > edges;
15
16
     void init(int _n) {
17
       n = n;
18
       edges.clear();
       for (int i = 0; i < n; i++) {</pre>
19
         G[i].clear();
20
21
       }
22
23
     void add_edge(int u, int v, LL c, LL cap) {
24
       // directed
25
       G[u].pb(edges.size());
26
       edges.eb(u, v, c, cap);
27
       G[v].pb(edges.size());
28
       edges.eb(v, u, -c, 0);
29
30
     bool SPFA(int st, int ed) {
31
       for (int i = 0; i < n; i++) {
32
         pre[i] = -1;
33
         dis[i] = INF;
         cnt[i] = 0;
34
35
         inq[i] = false;
       }
36
37
       queue < int > q;
38
       bool negcycle = false;
39
       dis[st] = 0;
40
41
       cnt[st] = 1;
42
       inq[st] = true;
43
       q.push(st);
```

20 }

```
45
       while (!q.empty() && !negcycle) {
         int u = q.front();
46
47
         q.pop();
48
         inq[u] = false;
49
         for (int i : G[u]) {
50
           int v = edges[i].v;
           LL cost = edges[i].cost;
51
52
           LL cap = edges[i].cap;
53
           if (dis[v] > dis[u] + cost && cap > 0) {
54
55
              dis[v] = dis[u] + cost;
              pre[v] = i;
56
57
              if (!inq[v]) {
                q.push(v);
58
59
                cnt[v]++;
                inq[v] = true;
60
61
62
                if (cnt[v] == n + 2) {
                  negcycle = true;
63
64
                  break;
                }
65
             }
66
           }
67
         }
68
69
70
       return dis[ed] != INF;
71
72
     }
73
     LL sendFlow(int v, LL curFlow) {
74
       if (pre[v] == -1) {
75
         return curFlow;
76
       int i = pre[v];
77
78
       int u = edges[i].u;
79
       LL cost = edges[i].cost;
80
81
       LL f = sendFlow(u, min(curFlow, edges[i].cap));
82
       ans_cost += f * cost;
83
       edges[i].cap -= f;
84
       edges[i ^ 1].cap += f;
85
86
       return f;
87
     pair<LL, LL> run(int st, int ed) {
88
89
       ans_flow = ans_cost = 0;
       while (SPFA(st, ed)) {
90
91
         ans_flow += sendFlow(ed, INF);
92
93
       return make_pair(ans_flow, ans_cost);
     }
94
95 };
```

String

6.1 Manacher

```
1 int p[2 * MAXN];
  int Manacher(const string &s) {
2
    string st = "@#";
3
    for (char c : s) {
5
       st += c;
6
       st += '#';
7
    }
    st += '$':
8
    int id = 0, mx = 0, ans = 0;
    for (int i = 1; i < st.length() - 1; i++) {</pre>
10
11
       p[i] = (mx > i ? min(p[2 * id - i], mx - i) : 1);
12
       for (; st[i - p[i]] == st[i + p[i]]; p[i]++);
       if (mx < i + p[i]) {</pre>
13
         mx = i + p[i];
14
         id = i;
15
16
17
       ans = max(ans, p[i] - 1);
18
```

```
6.2
   Trie
```

return ans;

```
1 const int MAXL = ;
  const int MAXC = ;
2
  struct Trie {
     int nex[MAXL][MAXC];
 5
     int len[MAXL];
 6
     int sz;
 7
     void init() {
       memset(nex, 0, sizeof(nex));
9
       memset(len, 0, sizeof(len));
10
11
12
     void insert(const string &str) {
       int p = 0;
13
       for (char c : str) {
14
         int id = c - 'a';
15
16
         if (!nex[p][id]) {
           nex[p][id] = ++sz;
17
18
         }
         p = nex[p][id];
19
20
21
       len[p] = str.length();
22
     }
23
     vector<int> find(const string &str, int i) {
24
       int p = 0;
25
       vector<int> ans;
       for (; i < str.length(); i++) {</pre>
26
27
         int id = str[i] - 'a';
28
         if (!nex[p][id]) {
29
           return ans;
         }
30
         p = nex[p][id];
31
         if (len[p]) {
32
33
           ans.pb(len[p]);
34
35
       return ans;
36
37
    }
38 };
```

Math

7.1 Number Theory

```
· Inversion:
   aa^{-1} \equiv 1 \pmod{m}. a^{-1} exists iff gcd(a, m) = 1.
· Linear inversion:
    a^{-1} \equiv (m - \lfloor \tfrac{m}{a} \rfloor) \times (m \bmod a)^{-1} \ (\mathsf{mod} \ m)
• Fermat's little theorem:
    a^p \equiv a \pmod{p} if p is prime.

    Euler function:

    \phi(n) = n \prod_{p \mid n} \frac{p-1}{p}
• Euler theorem:
   a^{\phi(n)} \equiv 1 \pmod{n} \text{ if } \gcd(a,n) = 1.

    Extended Euclidean algorithm:

    ax + by = \gcd(a, b) = \gcd(b, a \mod b) = \gcd(b, a - \lfloor \frac{a}{b} \rfloor b) = bx_1 + (a - \lfloor \frac{a}{b} \rfloor b)
    \lfloor \frac{a}{b} \rfloor b) y_1 = ay_1 + b(x_1 - \lfloor \frac{a}{b} \rfloor y_1)
· Divisor function:
    \sigma_x(n) = \sum_{d|n} d^x. n = \prod_{i=1}^r p_i^{a_i}.
   \sigma_x(n) = \prod_{i=1}^r \frac{p_i^{(a_i+1)x} - 1}{p_i^x - 1} \text{ if } x \neq 0. \ \ \sigma_0(n) = \prod_{i=1}^r (a_i + 1).
• Chinese remainder theorem:
    x \equiv a_i \pmod{m_i}.
    M = \prod_{i=1}^{n} m_i. \quad M_i = M/m_i. \quad t_i = M_i^{-1}. 
 x = kM + \sum_{i=1}^{n} a_i t_i M_i, \quad k \in \mathbb{Z}.
```

7.2 Extended GCD

```
1  // ax + by = c
2  int extgcd(int a, int b, int c, int &x, int &y) {
3   if (b == 0) {
4      x = c / a;
5      y = 0;
6      return a;
7   }
8   int d = extgcd(b, a % b, c, y, x);
9   y -= (a / b) * x;
return d;
11 }
```

7.3 Gaussian Elimination

```
1 const int MAXN = 300;
2 const double EPS = 1e-8;
3 int n;
4 double A[MAXN][MAXN];
5 void Gauss() {
     for (int i = 0; i < n; i++) {</pre>
       bool ok = 0;
7
8
       for (int j = i; j < n; j++) {
         if (fabs(A[j][i]) > EPS) {
9
10
           swap(A[j], A[i]);
11
           ok = 1;
12
           break;
        }
13
       }
14
15
       if (!ok) continue;
       double fs = A[i][i];
16
17
       for (int j = i + 1; j < n; j++) {
         double r = A[j][i] / fs;
18
         for (int k = i; k < n; k++) {
19
20
           A[j][k] -= A[i][k] * r;
        }
21
22
       }
    }
23
24 }
```