1.2

Default

Contents

```
1 #include <bits/stdc++.h>
 1 Basic
                                   using namespace std;
                                   using LL = long long;
                                  3
  1.2 Default . . . . . . . . . . . . . . . . . .
                                   #define IOS ios_base::sync_with_stdio(0); cin.tie(0);
  #define pb push_back
  #define eb emplace_back
  const int INF = 1e9;
  const int MOD = 1e9 + 7;
 2 Data Structure
                                   const double EPS = 1e-6;
  2.1 Disjoint Set
                                   const int MAXN = 0;
  3

      2.4 Segment Tree RARMQ
      ...

      2.5 Segment Tree RURMQ
      ...

      2.6 Treap
      ...

                                 12 int main() {
                                 13
                                 14 }
 3 Graph
  1.3 Black Magic
  #include <bits/stdc++.h>
  #include <ext/pb_ds/assoc_container.hpp>
  #include <ext/pb_ds/tree_policy.hpp>
  #include <ext/pb_ds/priority_queue.hpp>
 4 Connectivity
                                   using namespace std;
  using namespace __gnu_pbds;
  4.2 BCC . . . .
                                   using set_t =
  tree<int, null_type, less<int>, rb_tree_tag,
  tree_order_statistics_node_update>;
 5 Flow & Matching
                                 10
                                   using map t =
                                10
  5.1 Relation . .
                                10
                                    tree<int, int, less<int>, rb_tree_tag,
  12
                                    tree_order_statistics_node_update>;
                                10
                                   using heap_t =
  14
                                    __gnu_pbds::priority_queue<int>;
  15
                                   using ht_t =
  12
                                    gp_hash_table<int, int>;
  5.7 Max General Graph Matching . . . . . . . . . . . . . .
                                 17
                                   int main() {
                                13
                                    //set-----
 6 String
                                 19
                                    set_t st;
  20
                                    st.insert(5); st.insert(6);
  21
                                    st.insert(3); st.insert(1);
                                 22
                                    // the smallest is (0), biggest is (n-1), kth small
  13
  is (k-1)
                               13
                                 24
                                    int num = *st.find_by_order(0);
  14
                                    cout << num << '\n'; // print 1
                                 25
  26
                                    num = *st.find_by_order(st.size() - 1);
                                    cout << num << '\n'; // print 6
 8 Math
                                15 28
  // find the index
                                 30
  int index = st.order_of_key(6);
                                 31
                                    cout << index << '\n'; // print 3
  33
                               16
                                    // check if there exists x
  int x = 5;
                                 35
  int check = st.erase(x);
                               17 36
                                    if (check == 0) printf("st not contain 5\n");
                                 37
                                    else if (check == 1) printf("st contain 5\n");
                                 38
 9 Geometry
                                17
                                 39
  17
                                 40
                                    //tree policy like set
  17
                               18 41
                                    st.insert(5); st.insert(5);
  cout << st.size() << '\n'; // print 4</pre>
  43
                                 44
                                    //map------
                                    map_t mp;
                                 45
                                 46
                                    mp[1] = 2;
   Basic
                                    cout << mp[1] << '\n';
                                 47
                                    auto tmp = *mp.find_by_order(0); // pair
cout << tmp.first << " " << tmp.second << '\n';</pre>
                                 48
                                 49
 1.1
    Run
                                 50
                                 51
                                    //heap------
                                    heap_t h1, h2;
1 #use -> sh run.sh {name}
                                 52
g++ -O2 -std=c++14 -Wall -Wextra -Wshadow -o $1 $1.cpp
                                    h1.push(1); h1.push(3);
                                 53
3 | ./$1 < t.in > t.out
                                    h2.push(2); h2.push(4);
```

h1.join(h2);

```
56
    cout << h1.size() << h2.size() << h1.top() << '\n';</pre>
                                                                   double L = -1e5, R = 1e5;
                                                                   while (R - L > EPS) {
57
                                                               6
                                                               7
                                                                     double mr = (L + R) / 2.0;
58
    //hash-table-----
                                                                     double ml = (L + mr) / 2.0;
59
                                                               8
60
    ht_t ht;
                                                               9
                                                                     if (f(ml) < f(mr)) {
61
    ht[85] = 5;
                                                              10
                                                                       R = mr;
    ht[89975] = 234;
                                                                     } else {
62
                                                              11
    for (auto i : ht) {
                                                              12
                                                                       L = m1;
       cout << i.first << " " << i.second << '\n';</pre>
64
                                                              13
                                                                   }
65
                                                              14
66 }
                                                              15
                                                                   return L;
                                                              16 }
```

1.4 Python

```
1 ### EOF
2 while True:
3
    try:
      pass
4
    except EOFError:
5
6
      break
7 ###math
8 import math
10 math.ceil(x)#上高斯
11 math.floor(x)#下高斯
12 math.factorial(x)#接乘
13 math.fabs(x)#絕對值
14 math.fsum(arr)#跟sum一樣但更精確(小數點問題)
15 math.gcd(x, y)#bj4
16 math.exp(x)#e^x
17 math.log(x, base)
18 math.log2(x)#2為底
19 math.log10(x)#10為底
20 math.sqrt(x)
21 math.pow(x, y, mod)#精確些(float型態) MOD!!!
22 math.sin(x)# cos tan asin acos atan atan2(弧度) sinh
      cosh tanh acosh asinh atanh
23 math.hypot(x, y)#歐幾里德範數
24 math.degrees(x)#x從弧度轉角度
25 math.radians(x)#x從角度轉弧度
26 math.gamma(x)#x的gamma函數
27 math.pi#常數
28 math.e#常數
29 math.inf
30
31 ### ascii
32 ord(x)#char to asc
33 chr(x)#asc to char
35 x.encode().hex()#string to hex
36 ### reverse string
37 string = "abc"
38 string_reverse = string[::-1]
```

1.5 Binary Search

1.6 Ternary Search

```
const double EPS = 1e-6;
// target function
double f(double x) { return x * x; }
double ternarySearch() {
```

2 Data Structure

2.1 Disjoint Set

```
1 // 0-base
2 const int MAXN = 1000;
3 int boss[MAXN];
  void init(int n) {
    for (int i = 0; i < n; i++) {</pre>
       boss[i] = -1;
    }
7
8 }
9
  int find(int x) {
10
    if (boss[x] < 0) {
11
      return x;
12
13
     return boss[x] = find(boss[x]);
  }
14
15
  bool uni(int a, int b) {
    a = find(a);
16
     b = find(b);
17
     if (a == b) {
18
19
      return false;
20
     if (boss[a] > boss[b]) {
21
22
       swap(a, b);
23
24
     boss[a] += boss[b];
25
     boss[b] = a;
26
     return true;
27 }
```

2.2 BIT RARSQ

```
1 // 1-base
  #define lowbit(k) (k & -k)
4
  int n;
5
  vector<int> B1, B2;
7
  void add(vector<int> &tr, int id, int val) {
    for (; id <= n; id += lowbit(id)) {</pre>
8
9
      tr[id] += val;
    }
10
11 }
12 void range_add(int 1, int r, int val) {
    add(B1, 1, val);
13
14
    add(B1, r + 1, -val);
    add(B2, 1, val * (1 - 1));
15
16
    add(B2, r + 1, -val * r);
17 }
18 int sum(vector<int> &tr, int id) {
19
    int ret = 0;
    for (; id >= 1; id -= lowbit(id)) {
20
21
      ret += tr[id];
    }
22
23
    return ret;
24 }
25 int prefix_sum(int id) {
```

```
return sum(B1, id) * id - sum(B2, id);

return sum(B1, id) * id - sum(B2, id);

int range_sum(int 1, int r) {
    return prefix_sum(r) - prefix_sum(1 - 1);

2.3 zkw RMQ

// 0-base
const int INF = 1e9;
const int MAXN = ;

int n;
int a[MAXN], tr[MAXN << 1];

// !!! remember to call this function
```

```
void build() {
    for (int i = 0; i < n; i++) {
10
11
      tr[i + n] = a[i];
12
    for (int i = n - 1; i > 0; i--) {
13
       tr[i] = max(tr[i << 1], tr[i << 1 | 1]);
14
15
16 }
17 void update(int id, int val) {
    for (tr[id += n] = val; id > 1; id >>= 1) {
18
19
      tr[id >> 1] = max(tr[id], tr[id ^ 1]);
20
    }
21 }
22 int query(int 1, int r) { // [1, r)
    int ret = -INF;
23
24
     for (1 += n, r += n; 1 < r; 1 >>= 1, r >>= 1) {
      if (1 & 1) {
25
26
         ret = max(ret, tr[1++]);
      }
27
28
      if (r & 1) {
29
         ret = max(ret, tr[--r]);
```

2.4 Segment Tree RARMQ

vector<int> &o) {

return ret;

30

31 }

32

33 }

```
1 struct Node {
2
     int val, tag;
3
     Node *lc, *rc;
     Node() : lc(nullptr), rc(nullptr), tag(0) {}
     void pull() {
       if (!lc) {
6
7
         val = rc->val;
       } else if (!rc) {
8
         val = lc->val;
9
       } else {
10
11
         val = max(lc->val, rc->val);
       }
12
13
    }
     void push() {
14
15
       if (lc) {
16
         lc->tag += tag;
17
         lc->val += tag;
18
19
       if (rc) {
         rc->tag += tag;
20
21
         rc->val += tag;
       }
22
23
       tag = 0;
24
    }
25 }:
26 struct SegmentTree {
27
     Node *root;
28
     SegmentTree() : root(nullptr) {}
29
     void build(Node* &T, int 1, int r, const
```

```
30
       T = new Node();
       if (1 == r) {
31
         T->val = o[1];
32
33
         return;
34
35
       int mid = (1 + r) / 2;
       build(T->lc, l, mid, o);
36
37
       build(T->rc, mid + 1, r, o);
38
       T->pull();
39
40
     void update(Node* &T, int 1, int r, int q1, int qr,
         int v) {
41
       if (ql <= 1 && r <= qr) {</pre>
         T->val += v;
42
43
         T->tag += v;
44
         return;
45
       }
46
       T->push();
47
       int mid = (1 + r) / 2;
48
       if (qr <= mid) {
         update(T->lc, 1, mid, ql, qr, v);
49
50
       } else if (mid < ql) {</pre>
51
         update(T->rc, mid + 1, r, ql, qr, v);
52
       } else {
53
         update(T->lc, 1, mid, ql, mid, v);
         update(T->rc, mid + 1, r, mid + 1, qr, v);
54
55
56
       T->pull();
57
58
     int query(Node* &T, int 1, int r, int q1, int qr) {
       if (ql <= 1 && r <= qr) {</pre>
59
60
         return T->val;
61
       }
62
       T->push();
63
       int mid = (1 + r) / 2;
64
       if (qr <= mid) {
65
         return query(T->lc, 1, mid, ql, qr);
       } else if (mid < ql) {</pre>
66
67
         return query(T->rc, mid + 1, r, ql, qr);
68
       } else {
69
         return max(query(T->lc, 1, mid, ql, mid),
70
              query(T->rc, mid + 1, r, mid + 1, qr));
71
72
    }
```

2.5 Segment Tree RURMQ

73 };

```
1 // from aizu
2 const 11 maxn = 1e6 + 5;
  const 11 INF = 2147483647;
  11 tree[maxn << 2], a[maxn], laze[maxn << 2];</pre>
  void push_down(int rt, int ln, int rn) {
    if (laze[rt] != -1) {
       laze[rt << 1] = laze[rt];</pre>
       laze[rt << 1 | 1] = laze[rt];
 8
9
       tree[rt << 1] = laze[rt];
10
       tree[rt << 1 | 1] = laze[rt];
11
       laze[rt] = -1;
12
    }
13 }
  void push_up(int rt) { tree[rt] = min(tree[rt << 1 |</pre>
14
       1], tree[rt << 1]); }
  void build(ll l, ll r, ll rt) {
15
16
     if (1 == r) {
17
       tree[rt] = a[1];
18
       return:
19
    11 m = (1 + r) >> 1;
20
     build(1, m, rt << 1);
21
    build(m + 1, r, rt << 1 | 1);
22
23
    push_up(rt);
24 }
25 //区间更新
26 void update(ll L, ll R, ll c, ll l, ll r, ll rt) {
```

```
27
     if (L <= 1 && r <= R) {</pre>
       laze[rt] = c;
28
       tree[rt] = c;
29
30
       return;
31
32
     11 m = (1 + r) >> 1;
     push_down(rt, m - 1 + 1, r - m);
33
     if (m >= L) update(L, R, c, l, m, rt << 1);</pre>
     if (m < R) update(L, R, c, m + 1, r, rt << 1 | 1);</pre>
35
36
     push_up(rt);
37 }
38
39 //区间更新的区间查询
40 | 11 query(11 L, 11 R, 11 1, 11 r, 11 rt) {
     if (L <= 1 && r <= R) {</pre>
41
42
       return tree[rt];
43
44
     11 m = (1 + r) >> 1, sum = INF;
45
     push_down(rt, m - 1 + 1, r - m);
     if (m \ge L) sum = min(sum, query(L, R, 1, m, rt <<
46
     if (m < R) sum = min(sum, query(L, R, m + 1, r, rt
47
         << 1 | 1));
48
     return sum;
49 }
50 void init() {
     for (int i = 0; i < maxn; i++) a[i] = INF;</pre>
51
     for (int i = 0; i < maxn * 4; i++) laze[i] = -1;</pre>
     build(0, n - 1, 1);
53
54 }
55 /*
56 update(x,y,z,0,n-1,1);
57 |query(x,y,0,n-1,1)|
58 */
```

2.6 Treap

```
1 struct Treap {
    int val, pri, sz;
2
     Treap *lc, *rc;
     Treap() {}
     Treap(int _val) {
6
       val = _val;
7
       pri = rand();
8
       sz = 1;
       1c = rc = NULL;
9
10
    }
11|};
12 int getSize(Treap *a) { return (a == NULL ? 0 :
       a->sz); }
13 void split(Treap *t, Treap *&a, Treap *&b, int k) {
    if (t == NULL) {
       a = b = NULL;
15
16
       return;
17
     if (getSize(t->lc) < k) {</pre>
18
19
20
       split(t->rc, a->rc, b, k - getSize(t->lc) - 1);
21
     } else {
       b = t;
22
23
       split(t->lc, a, b->lc, k);
24
25 }
26
  Treap *merge(Treap *a, Treap *b) {
27
    if (!a || !b) {
28
       return (a ? a : b);
29
30
     if (a->pri > b->pri) {
31
       a->rc = merge(a->rc, b);
32
       return a;
33
     } else {
34
       b->lc = merge(a, b->lc);
35
       return b;
36
     }
37 }
```

```
38 void Insert(Treap *&t, int x, int p) {
    Treap *a, *b;
39
    split(t, a, b, x);
40
41
    t = merge(a, merge(new Treap(p), b));
42
  }
43
  void Delete(Treap *&t, int x) {
    Treap *a, *b, *c;
44
45
    split(t, b, c, x);
    split(b, a, b, x - 1);
46
47
    t = merge(a, c);
48 }
49
50
51
  Usage
  Treap *root = NULL; // declare
  root = merge(root, new Treap(val)); // push back
53
54 Insert(root, x, y); // insert y after x-th element
55 Delete(root, x); // delete x-th element
56 */
```

3 Graph

3.1 Dijkstra

```
1 // 0-base
  const LL INF = 1e18;
  const int MAXN = ;
  struct Edge {
    int to;
    LL cost;
    Edge(int v, LL c) : to(v), cost(c) {}
    bool operator < (const Edge &other) const {</pre>
       return cost > other.cost;
9
10
    }
11 };
12
13 int n;
14 LL dis[MAXN];
15 vector < Edge > G[MAXN];
16
17
  void init() {
    for (int i = 0; i < n; i++) {
18
       G[i].clear();
19
20
       dis[i] = INF;
21
    }
22
  void Dijkstra(int st, int ed = -1) {
23
24
    priority_queue < Edge > pq;
25
    pq.emplace(st, 0);
    dis[st] = 0:
26
27
     while (!pq.empty()) {
28
       auto now = pq.top();
29
       pq.pop();
30
       if (now.to == ed) {
31
         return:
32
33
       if (now.cost > dis[now.to]) {
34
         continue;
35
36
       for (auto &e : G[now.to]) {
37
         if (dis[e.to] > now.cost + e.cost) {
           dis[e.to] = now.cost + e.cost;
38
39
           pq.emplace(e.to, dis[e.to]);
40
         }
41
42
    }
43 }
```

3.2 SPFA(negative cycle)

```
1 // 0-base
2 const LL INF = 1e18;
```

```
3 const int MAXN = ;
4 struct Edge {
    int to;
    LL cost;
     Edge(int v, LL c) : to(v), cost(c) {}
8 };
9
10 int n;
11 LL dis[MAXN];
12 vector < Edge > G[MAXN];
13
14 void init() {
15
     for (int i = 0; i < n; i++) {
       G[i].clear();
16
17
       dis[i] = INF;
    }
18
19 }
20 bool SPFA(int st) {
    vector<int> cnt(n, 0);
21
22
     vector < bool > inq(n, false);
     queue<int> q;
23
24
25
     q.push(st);
     dis[st] = 0;
26
27
     inq[st] = true;
     while (!q.empty()) {
28
       int now = q.front();
29
30
       q.pop();
31
       inq[now] = false;
32
       for (auto &e : G[now]) {
         if (dis[e.to] > dis[now] + e.cost) {
33
34
           dis[e.to] = dis[now] + e.cost;
           if (!inq[e.to]) {
35
36
              cnt[e.to]++;
37
              if (cnt[e.to] > n) {
                // negative cycle
38
39
                return false;
              }
40
              inq[e.to] = true;
41
42
              q.push(e.to);
           }
43
44
         }
45
       }
     }
46
47
     return true;
48 }
```

3.3 Floyd Warshall

```
1 // 0-base
2 // G[i][i] < 0 -> negative cycle
3 const LL INF = 1e18;
 4 const int MAXN = ;
6 int n;
7 LL G[MAXN][MAXN];
9 void init() {
    for (int i = 0; i < n; i++) {
10
11
       for (int j = 0; j < n; j++) {
         G[i][j] = INF;
12
13
14
       G[i][i] = 0;
15
    }
16 }
  void floyd() {
17
18
    for (int k = 0; k < n; k++) {
       for (int i = 0; i < n; i++) {
19
20
         for (int j = 0; j < n; j++) {
           if (G[i][k] != INF && G[k][j] != INF) {
21
             G[i][j] = min(G[i][j], G[i][k] + G[k][j]);
22
           }
23
24
         }
25
    }
26
27 }
```

3.4 Topological Sort

```
1 // 0-base
2 // if ret.size < n -> cycle
3
  int n;
  vector<vector<int>> G;
  vector<int> topoSort() {
    vector<int> indeg(n), ret;
     for (auto &li : G) {
      for (int x : li) {
9
        ++indeg[x];
10
11
12
    }
13
    // use priority queue for lexic. largest ans
     queue<int> q;
14
     for (int i = 0; i < n; i++) {
15
16
      if (!indeg[i]) {
         q.push(i);
17
18
    }
19
20
    while (!q.empty()) {
21
      int u = q.front();
22
      q.pop();
23
       ret.pb(u);
      for (int v : G[u]) {
24
25
         if (--indeg[v] == 0) {
26
           q.push(v);
27
28
      }
    }
29
30
    return ret;
31 }
```

3.5 Tree Diameter

```
1 // 0-base;
2
  const int MAXN = ;
3
4 struct Edge {
    int to;
6
    int cost;
7
    Edge(int v, int c) : to(v), cost(c) {}
8 };
10 int n, d = 0;
11 int d1[MAXN], d2[MAXN];
  vector<Edge> G[MAXN];
  // dfs(0, -1);
13
14 void dfs(int u, int from) {
15
    d1[u] = d2[u] = 0;
16
    for (auto e : G[u]) {
17
       if (e.to == from) {
         continue;
18
19
      dfs(e.to, u);
20
21
      int t = d1[e.to] + e.cost;
22
      if (t > d1[u]) {
         d2[u] = d1[u];
23
24
         d1[u] = t;
25
      } else if (t > d2[u]) {
26
         d2[u] = t;
27
28
29
    d = max(d, d1[u] + d2[u]);
```

3.6 Directed MST

```
1 // 0-base
2 const LL INF = 1e18;
3 const int MAXN = ;
4
```

```
5 struct Edge {
    int from:
     int to;
R
     LL cost;
9
     Edge(int u, int v, LL c) : from(u), to(v), cost(c)
10 };
11
12 struct DMST {
13
     int n;
14
     int vis[MAXN], pre[MAXN], id[MAXN];
     LL in[MAXN];
15
     vector < Edge > edges;
     void init(int _n) {
17
18
       n = _n;
19
       edges.clear();
20
21
     void add_edge(int from, int to, LL cost) {
       edges.eb(from, to, cost);
22
23
     LL run(int root) {
24
25
       LL ret = 0;
26
       while (true) {
27
         for (int i = 0; i < n; i++) {</pre>
28
           in[i] = INF;
29
30
         // find in edge
31
         for (auto &e : edges) {
32
33
           if (e.cost < in[e.to] && e.from != e.to) {</pre>
             pre[e.to] = e.from;
34
              in[e.to] = e.cost;
35
           }
36
37
38
         // check in edge
39
40
         for (int i = 0; i < n; i++) {
           if (i == root) {
41
42
              continue;
43
           if (in[i] == INF) {
44
45
              return -1;
           }
46
47
48
         int nodenum = 0;
49
50
         memset(id, -1, sizeof(id));
         memset(vis, -1, sizeof(vis));
51
52
         in[root] = 0;
53
54
         // find cycles
         for (int i = 0; i < n; i++) {</pre>
55
56
           ret += in[i];
57
            int v = i;
           while (vis[v] != i && id[v] == -1 && v !=
58
                root) {
59
              vis[v] = i;
60
              v = pre[v];
61
           if (id[v] == -1 && v != root) {
62
              for (int j = pre[v]; j != v; j = pre[j]) {
64
               id[j] = nodenum;
65
66
             id[v] = nodenum++;
67
68
         }
69
70
         // no cycle
71
         if (nodenum == 0) {
72
           break;
73
74
75
         for (int i = 0; i < n; i++) {
           if (id[i] == -1) {
76
77
             id[i] = nodenum++;
78
           }
79
         }
```

```
80
81
         // grouping the vertices
         for (auto &e : edges) {
82
           int to = e.to;
83
84
           e.from = id[e.from];
           e.to = id[e.to];
85
           if (e.from != e.to) {
86
87
              e.cost -= in[to]; //!!!
88
           }
89
90
91
         n = nodenum;
92
         root = id[root];
93
94
       return ret;
    }
95
96 };
```

3.7 LCA

```
1 const int LOG = 20;
  vector<int> tin(MAXN), tout(MAXN), depth(MAXN);
3
  int par[MAXN][LOG];
  int timer = 0;
  vector<int> G[MAXN];
7
  void dfs(int u, int f) {
    tin[u] = ++timer;
8
    par[u][0] = f;
10
    for (int v : G[u]) {
      if (v != f) {
11
         depth[v] = depth[u] + 1;
12
13
         dfs(v, u);
14
15
    }
16
    tout[u] = ++timer;
17 }
18
19
  void Doubling(int n) {
    for (int j = 1; j < LOG; ++j) {</pre>
20
21
      for (int i = 1; i <= n; ++i) {
22
         par[i][j] = par[par[i][j - 1]][j - 1];
23
24
    }
25 }
26
  bool anc(int u, int v) { return tin[u] <= tin[v] &&</pre>
27
       tout[v] <= tout[u]; }</pre>
28
  int LCA(int u, int v) {
29
30
    if (depth[u] > depth[v]) {
31
      swap(u, v);
32
33
    if (anc(u, v)) {
34
       return u;
35
    for (int j = LOG - 1; j >= 0; --j) {
36
37
       if (!anc(par[u][j], v)) u = par[u][j];
    }
38
39
    return par[u][0];
40 }
41
42 int dis(int u, int v) {
43
    int lca = LCA(u, v);
    return depth[u] + depth[v] - 2 * depth[lca];
44
45 }
46
47
48 dfs(root, root);
49
  Doubling(n);
50
  */
```

3.8

12

13

14

15

16 17

18

19

20

21

22

23

24

25

26

27

28 29

30 31

32

33

34

35

36

37

38

39

40

41

42

43

44

45

46

47

48

49

50

51

52

int st = -1;

for (int i = 1; i <= n; i++) {</pre>

```
Euler Circuit
                                                             53
                                                                     if (chk[i] % 2 == 1) {
                                                                       st = i;
                                                             54
  七橋問題根據起點與終點是否相同,分成 Euler path(不同)及 Euler circuit(相
                                                            55
                                                                       break;
                                                                     }
                                                             56
                                                             57
     • 判斷法
                                                                   if (st == -1) {
                                                             58
                                                             59
                                                                     return false;
     · 無向圖部分,將點分成奇點(度數為奇數)和偶點(度數為偶數)。
                                                             60
          - Euler path:奇點數為 0 或 2
                                                                   dfs(st);
                                                             61
                                                             62
                                                                   return true;
         - Euler circuit:沒有奇點
                                                             63
     · 有向圖部分,將點分成出點(出度 - 入度 = 1)和入點(入度 - 出度 = 1)還
       有平衡點(出度 = 入度)。
                                                                 void print_path(void) {
                                                                   for (auto i : path) {
                                                             66
         - Euler path:出點和入點個數同時為 0 或 1。
                                                             67
                                                                     printf("%d %d\n", i.first, i.second);
         - Euler circuit:只有平衡點。
                                                             68
                                                             69
                                                                 }
     · 求出一組解
                                                             70 };
     · 用 DFS 遍歷整張圖,設 S 為離開的順序,無向圖的答案為 S ,有向圖的答案
       為反向的 S 。
                                                             1 // Code from allen(lexicographic order)
                                                             2 #include <bits/stdc++.h>
     · DFS 起點選定:
                                                               using namespace std;
                                                               const int ALP = 30;
         - Euler path:無向圖選擇任意一個奇點,有向圖選擇出點。
                                                               const int MXN = 1005;
         - Euler circuit:任意一點。
                                                               int n;
                                                               int din[ALP], dout[ALP];
1 // Code from Eric
                                                               int par[ALP];
                                                             8
2 #define 11 long long
                                                               vector<string> vs[MXN], ans;
3 #define PB push_back
                                                             10 bitset < MXN > vis, used[ALP];
4 #define EB emplace_back
                                                             11
5 #define PII pair<int, int>
                                                             12
                                                               void djsInit() {
6 #define MP make_pair
                                                                 for (int i = 0; i != ALP; ++i) {
                                                            13
  #define all(x) x.begin(), x.end()
                                                                   par[i] = i;
                                                             14
8 #define maxn 50000+5
                                                             15
                                                             16 }
10 //structure
                                                             17
11 struct Eular {
                                                               int Find(int x) { return (x == par[x] ? (x) : (par[x]
                                                             18
    vector<PII> adj[maxn];
                                                                    = Find(par[x])); }
    vector<bool> edges;
                                                             19
    vector<PII> path;
                                                               void init() {
                                                             20
    int chk[maxn];
                                                                 djsInit();
                                                             21
    int n;
                                                             22
                                                                 memset(din, 0, sizeof(din));
                                                             23
                                                                 memset(dout, 0, sizeof(dout));
    void init(int _n) {
                                                                 vis.reset();
                                                             24
                                                             25
                                                                 for (int i = 0; i != ALP; ++i) {
      n = _n;
      for (int i = 0; i <= n; i++) adj[i].clear();</pre>
                                                             26
                                                                   vs[i].clear();
      edges.clear();
                                                             27
                                                                   used[i].reset();
      path.clear();
                                                             28
                                                                 }
      memset(chk, 0, sizeof(chk));
                                                             29
                                                                 return:
    }
                                                             30 }
                                                             31
    void dfs(int v) {
                                                             32
                                                               void dfs(int u) {
                                                                 for (int i = 0; i != (int)vs[u].size(); ++i) {
      for (auto i : adj[v]) {
                                                             33
        if (edges[i.first] == true) {
                                                                   if (used[u][i]) {
                                                             34
          edges[i.first] = false;
                                                             35
                                                                     continue;
          dfs(i.second);
                                                             36
                                                                   }
          path.EB(MP(i.second, v));
                                                             37
                                                                   used[u][i] = 1;
                                                                   string s = vs[u][i];
        }
                                                             38
      }
                                                             39
                                                                   int v = s[s.size() - 1] - 'a';
    }
                                                             40
                                                                   dfs(v):
                                                             41
                                                                   ans.push_back(s);
    void add_Edge(int from, int to) {
                                                             42
                                                                 }
                                                             43 }
      edges.PB(true);
                                                             44
      // for bi-directed graph
                                                             45 bool solve() {
      adj[from].PB(MP(edges.size() - 1, to));
                                                             46
                                                                 int cnt = 1;
      adj[to].PB(MP(edges.size() - 1, from));
                                                             47
                                                                 for (int i = 0; i != n; ++i) {
      chk[from]++;
                                                                   string s;
                                                             48
      chk[to]++;
                                                             49
                                                                   cin >> s;
                                                                   int from = s[0] - 'a', to = s.back() - 'a';
                                                             50
      // for directed graph
                                                             51
                                                                   ++din[to];
       // adj[from].PB(MP(edges.size()-1, to));
                                                             52
                                                                    ++dout[from];
                                                                   vs[from].push_back(s);
      // check[from]++;
                                                             53
                                                                    vis[from] = vis[to] = true;
                                                             54
                                                             55
                                                                   if ((from = Find(from)) != (to = Find(to))) {
    bool eular_path() {
                                                             56
                                                                     par[from] = to;
```

57

58

++cnt;

```
59
     if ((int)vis.count() != cnt) {
60
61
       return false;
62
     }
63
     int root, st, pin = 0, pout = 0;
     for (int i = ALP - 1; i >= 0; --i) {
64
       sort(vs[i].begin(), vs[i].end());
65
       if (vs[i].size()) root = i;
       int d = dout[i] - din[i];
67
       if (d == 1) {
68
69
          ++pout;
         st = i;
70
71
       } else if (d == -1) {
72
         ++pin;
73
       } else if (d != 0) {
          return false;
74
75
       }
76
     }
77
     if (pin != pout || pin > 1) {
78
       return false;
79
80
     ans.clear();
81
     dfs((pin ? st : root));
     return true;
82
83 }
84
85 int main() {
86
    int t;
87
     cin >> t;
88
     while (t--) {
       cin >> n;
89
90
       init();
91
       if (!solve()) {
92
         cout << "***\n";
93
          continue;
94
95
       for (int i = ans.size() - 1; i >= 0; --i) {
         cout << ans[i] << ".\n"[i == 0];</pre>
96
97
98
99 }
```

4 Connectivity

4.1 Kosaraju SCC

```
1 // 0-base
2 int n;
3 vector<vector<int>>> G, G2; // G2 = G rev
4 vector < bool > vis;
5 vector<int> s, color;
6 int sccCnt;
7
  void dfs1(int u) {
8
    vis[u] = true;
    for (int v : G[u]) {
10
      if (!vis[v]) {
11
         dfs1(v);
12
      }
    }
13
    s.pb(u);
14
15 }
16 void dfs2(int u) {
17
    color[u] = sccCnt;
    for (int v : G2[u]) {
18
19
      if (!color[v]) {
         dfs2(v);
20
21
      }
    }
22
23 }
24 void Kosaraju() {
    sccCnt = 0;
25
    for (int i = 0; i < n; i++) {
26
27
      if (!vis[i]) {
         dfs1(i);
28
```

1 typedef pair<int, int> PII;

4.2 BCC

```
int low[MXV], depth[MXV];
  bool is_cut_vertex[MXV], visit[MXV];
  vector<int> G[MXV];
  vector < PII > BCC[MXV];
  int bcc_cnt = 0;
  stack<PII> st;
9
  vector<pair<int, int>> my_cut_edge;
10
  void dfs(int now, int cur_depth, int f) {
11
     visit[now] = true;
     depth[now] = low[now] = cur_depth;
13
14
     int cut_son = 0;
     for (auto i : G[now]) {
15
16
       if (i == f) continue;
17
       if (visit[i]) { // ancestor
         if (depth[i] < depth[now]) { // #</pre>
18
           low[now] = min(low[now], depth[i]);
19
20
           st.push({now, i});
21
22
       } else { // offspring
         st.push({now, i});
23
         dfs(i, cur_depth + 1, now);
24
25
         cut_son += 1;
         low[now] = min(low[now], low[i]);
26
27
         if (low[i] >= depth[now]) {
28
           is_cut_vertex[now] = true;
29
           auto t = st.top();
           st.pop();
30
           while (t != make_pair(now, i)) {
32
             BCC[bcc_cnt].push_back(t);
33
             t = st.top();
34
             st.pop();
35
           BCC[bcc_cnt].push_back(t);
36
37
           ++bcc_cnt;
38
39
         if (low[i] > depth[now])
40
41
           my_cut_edge.push_bach({now, i});
       }
42
43
     if (cur_depth == 0)
44
45
       is_cut_vertex[now] = (cut_son != 1);
46
     return;
47 }
49 bool is_2_edge_connected(int n) {
50
    memset(visit, 0, sizeof(visit));
     dfs(1, 0, -1);
52
    return my_cut_edge.size() == 0;
53 }
```

4.3 Articulation Point

```
1 // from aizu
2 typedef long long int ll;
3 typedef unsigned long long int ull;
4 #define BIG_SIZE 200000000
5 #define MOD 1000000007
```

```
7 using namespace std;
9 #define SIZE 100000
10
11 vector<int> G[SIZE];
12 int N:
13 bool visited[SIZE];
14 int visited_order[SIZE], parent[SIZE], lowest[SIZE],
15
16 void dfs(int cur, int pre_node) {
     visited_order[cur] = lowest[cur] = number;
17
     number++;
18
19
     visited[cur] = true;
20
21
22
     int next;
23
24
     for (int i = 0; i < G[cur].size(); i++) {</pre>
25
       next = G[cur][i];
26
       if (!visited[next]) {
27
          parent[next] = cur;
28
         dfs(next, cur);
          lowest[cur] = min(lowest[cur], lowest[next]);
29
       } else if (visited[next] == true && next !=
30
            pre_node) {
31
          lowest[cur] = min(lowest[cur],
              visited_order[next]);
32
     }
33
34 }
35
36 void art_points() {
     for (int i = 0; i < N; i++) visited[i] = false;</pre>
37
38
39
     number = 1;
     dfs(0, -1);
40
41
42
     int tmp_parent, root_num = 0;
43
     vector<int> V;
44
45
     for (int i = 1; i < N; i++) {</pre>
46
       tmp_parent = parent[i];
47
       if (tmp_parent == 0) {
48
49
         root_num++;
       } else if (visited_order[tmp_parent] <=</pre>
50
            lowest[i]) {
51
          V.push_back(tmp_parent);
52
       }
53
     }
54
     if (root_num >= 2) {
55
       V.push_back(0);
56
     sort(V.begin(), V.end());
57
     V.erase(unique(V.begin(), V.end()), V.end());
58
59
60
     for (int i = 0; i < V.size(); i++) {</pre>
       printf("%d \setminus n", V[i]);
61
     }
62
63 }
64
65 int main() {
    int E:
66
     scanf("%d %d", &N, &E);
67
     int from, to;
68
     for (int i = 0; i < E; i++) {</pre>
69
       scanf("%d %d", &from, &to);
70
71
       G[from].push_back(to);
72
       G[to].push_back(from);
73
     }
     art_points();
74
75 }
```

6 #define EPS 0.000000001

4.4 Bridges

```
// from aizu
2 typedef long long int 11;
3 typedef unsigned long long int ull;
4 #define BIG_NUM 2000000000
  #define MOD 1000000007
  #define EPS 0.000000001
  using namespace std;
  struct Edge {
    bool operator<(const struct Edge &arg) const {</pre>
10
       if (s != arg.s) {
11
12
         return s < arg.s;</pre>
13
       } else {
14
         return t < arg.t;</pre>
15
    }
16
17
    int s, t;
18 };
19
  struct Info {
20
    Info(int arg_to, int arg_edge_id) {
21
       to = arg_to;
22
       edge_id = arg_edge_id;
23
    }
    int to, edge_id;
24
25
26
27 int V, E, number;
28 int order[100000], lowlink[100000];
  bool visited[100000];
29
30
  Edge edge[100000];
  vector < Info > G[100000];
31
32
33
  void recursive(int cur) {
     order[cur] = number++;
34
35
     lowlink[cur] = order[cur];
36
37
     int next;
38
39
     for (int i = 0; i < G[cur].size(); i++) {</pre>
40
       next = G[cur][i].to;
41
       if (order[next] == -1) {
42
43
         visited[G[cur][i].edge_id] = true;
44
         recursive(next);
45
         lowlink[cur] = min(lowlink[cur], lowlink[next]);
46
47
       } else if (visited[G[cur][i].edge_id] == false) {
         lowlink[cur] = min(lowlink[cur], order[next]);
48
49
    }
50
51 }
52
53
  int main() {
     scanf("%d %d", &V, &E);
     for (int i = 0; i < E; i++) {</pre>
55
       scanf("%d %d", &edge[i].s, &edge[i].t);
56
57
       if (edge[i].s > edge[i].t) {
58
         swap(edge[i].s, edge[i].t);
59
60
       G[edge[i].s].push_back(Info(edge[i].t, i));
61
       G[edge[i].t].push_back(Info(edge[i].s, i));
62
63
64
     sort(edge, edge + E);
65
66
     number = 0;
     for (int i = 0; i < V; i++) {</pre>
67
68
       order[i] = -1;
69
       lowlink[i] = -1;
70
71
     for (int i = 0; i < E; i++) {
72
       visited[i] = false;
73
74
     recursive(0);
```

9

```
76
77
     int from, to;
     for (int i = 0; i < E; i++) {
78
79
       from = edge[i].s;
80
       to = edge[i].t;
81
       if (order[edge[i].s] > order[edge[i].t]) {
82
         swap(from, to);
83
       if (order[from] < lowlink[to]) {</pre>
84
         printf("%d %d\n", edge[i].s, edge[i].t);
85
86
    }
87
88
     return 0;
89 }
```

5 Flow & Matching

5.1 Relation

```
1 | 1. 一般圖
2 | |最大匹配 | + |最小邊覆蓋 | = |V|
3 | |最大獨立集 | + |最小點覆蓋 | = |V|
4 | |最大圖 | = |補圖的最大獨立集 |
5 | 2. 二分圖
6 | |最大匹配 | = |最小點覆蓋 |
7 | |最大獨立集 | = |最小邊覆蓋 |
8 | |最大獨立集 | = |V| - |最大匹配 |
9 | |最大圖 | = |補圖的最大獨立集 |
```

5.2 Bipartite Matching

```
1 // 0-base
2 const int MAXN = ;
3 int n;
4 vector<int> G[MAXN];
5 int vy[MAXN], my[MAXN];
7
  bool match(int u) {
8
    for (int v : G[u]) {
       if (vy[v]) {
10
         continue;
11
12
       vy[v] = true;
       if (my[v] == -1 || match(my[v])) {
13
14
         my[v] = u;
15
         return true;
16
17
18
    return false;
19 }
20 int sol() {
21
    int cnt = 0;
22
    memset(my, -1, sizeof(my));
    for (int i = 0; i < n; i++) {
23
       memset(vy, 0, sizeof(vy));
       if (match(i)) {
25
26
         cnt++;
27
    }
28
29
     return cnt;
30 }
```

5.3 KM

```
const int INF = 1e9;
const int MAXN = ;
struct KM { //1-base
int n, G[MAXN][MAXN];
int lx[MAXN], ly[MAXN], my[MAXN];
```

```
bool vx[MAXN], vy[MAXN];
     void init(int _n) {
 7
       n = _n;
       for (int i = 1; i <= n; i++) {</pre>
9
10
         for (int j = 1; j <= n; j++) {</pre>
11
           G[i][j] = 0;
12
13
       }
14
15
     bool match(int i) {
16
       vx[i] = true;
       for (int j = 1; j <= n; j++) {</pre>
17
18
         if (lx[i] + ly[j] == G[i][j] && !vy[j]) {
            vy[j] = true;
19
20
            if (!my[j] || match(my[j])) {
21
              my[j] = i;
22
              return true;
23
            }
24
         }
25
26
       return false;
27
28
     void update() {
       int delta = INF;
29
       for (int i = 1; i <= n; i++) {
30
31
         if (vx[i]) {
            for (int j = 1; j \le n; j++) {
32
33
              if (!vy[j]) {
                delta = min(delta, lx[i] + ly[j] -
34
                     G[i][j]);
35
36
            }
         }
37
38
39
       for (int i = 1; i <= n; i++) {
40
         if (vx[i]) {
41
           lx[i] -= delta;
42
         if (vy[i]) {
43
44
            ly[i] += delta;
45
46
       }
47
     }
48
     int run() {
       for (int i = 1; i <= n; i++) {</pre>
49
50
         lx[i] = ly[i] = my[i] = 0;
51
         for (int j = 1; j <= n; j++) {
            lx[i] = max(lx[i], G[i][j]);
52
53
54
55
       for (int i = 1; i <= n; i++) {
56
         while (true) {
57
            for (int i = 1; i <= n; i++) {
58
             vx[i] = vy[i] = 0;
59
            if (match(i)) {
60
61
              break;
62
            } else {
              update();
63
            }
64
65
         }
       }
66
67
       int ans = 0;
       for (int i = 1; i <= n; i++) {
68
69
         ans += lx[i] + ly[i];
70
71
       return ans;
72
73 };
```

5.4 Dinic

```
1 #define eb emplace_back
2 const LL INF = 1e18;
3 const int MAXN = ;
4 struct Edge {
```

```
5
     int to;
                                                                 3 const int MAXN = ;
                                                                   struct Edge {
     LL cap:
6
7
     int rev;
                                                                     int u, v;
     Edge(int v, LL c, int r) : to(v), cap(c), rev(r) {}
8
                                                                     LL cost;
9
  };
                                                                     LL cap;
10 struct Dinic {
                                                                     Edge(int _u, int _v, LL _c, LL _cap) : u(_u),
                                                                          v(_v), cost(_c), cap(_cap) {}
11
     int n:
12
     int level[MAXN], now[MAXN];
                                                                 9 };
     vector < Edge > G[MAXN];
                                                                10 struct MCMF {
                                                                                      // ing times
13
                                                                     int n, pre[MAXN], cnt[MAXN];
14
     void init(int _n) {
                                                                11
15
       n = _n;
                                                                12
                                                                     LL ans_flow, ans_cost, dis[MAXN];
       for (int i = 0; i <= n; i++) {</pre>
                                                                     bool ing[MAXN];
16
                                                                13
17
         G[i].clear();
                                                                     vector<int> G[MAXN];
                                                                14
                                                                     vector < Edge > edges;
       }
                                                                15
18
19
     }
                                                                16
                                                                     void init(int _n) {
                                                                       n = _n;
     void add_edge(int u, int v, LL c) {
                                                                17
20
       G[u].eb(v, c, G[v].size());
                                                                18
                                                                        edges.clear();
21
                                                                        for (int i = 0; i < n; i++) {</pre>
22
       // directed graph
                                                                19
                                                                20
23
       G[v].eb(u, 0, G[u].size() - 1);
                                                                          G[i].clear();
       // undirected graph
                                                                21
24
       // G[v].eb(u, c, G[u].size() - 1);
25
                                                                22
26
                                                                23
                                                                     void add_edge(int u, int v, LL c, LL cap) {
27
     bool bfs(int st, int ed) {
                                                                24
                                                                        // directed
       fill(level, level + n + 1, -1);
                                                                25
                                                                       G[u].pb(edges.size());
28
29
       queue<int> q;
                                                                26
                                                                        edges.eb(u, v, c, cap);
30
       q.push(st);
                                                                27
                                                                       G[v].pb(edges.size());
31
       level[st] = 0;
                                                                28
                                                                        edges.eb(v, u, -c, 0);
32
       while (!q.empty()) {
                                                                29
                                                                     }
                                                                     bool SPFA(int st, int ed) {
33
         int u = q.front();
                                                                30
34
         q.pop();
                                                                31
                                                                        for (int i = 0; i < n; i++) {
                                                                          pre[i] = -1;
         for (const auto &e : G[u]) {
35
                                                                32
36
           if (e.cap > 0 && level[e.to] == -1) {
                                                                33
                                                                          dis[i] = INF;
37
             level[e.to] = level[u] + 1;
                                                                34
                                                                          cnt[i] = 0;
38
             q.push(e.to);
                                                                35
                                                                          inq[i] = false;
                                                                       }
39
           }
                                                                36
40
         }
                                                                37
                                                                       queue < int > q;
41
       }
                                                                38
                                                                       bool negcycle = false;
       return level[ed] != -1;
42
                                                                39
43
                                                                40
                                                                        dis[st] = 0;
     LL dfs(int u, int ed, LL limit) {
44
                                                                41
                                                                        cnt[st] = 1;
                                                                        inq[st] = true;
45
       if (u == ed) {
                                                                42
46
         return limit;
                                                                43
                                                                       q.push(st);
47
                                                                44
       LL ret = 0;
                                                                45
                                                                        while (!q.empty() && !negcycle) {
48
       for (int &i = now[u]; i < G[u].size(); i++) {</pre>
                                                                          int u = q.front();
49
                                                                46
         auto &e = G[u][i];
                                                                47
                                                                          q.pop();
50
51
         if (e.cap > 0 && level[e.to] == level[u] + 1) {
                                                                48
                                                                          inq[u] = false;
           LL f = dfs(e.to, ed, min(limit, e.cap));
                                                                49
                                                                          for (int i : G[u]) {
52
53
           ret += f;
                                                                50
                                                                            int v = edges[i].v;
           limit -= f;
                                                                            LL cost = edges[i].cost;
54
                                                                51
55
           e.cap -= f;
                                                                52
                                                                            LL cap = edges[i].cap;
56
           G[e.to][e.rev].cap += f;
                                                                53
57
           if (!limit) {
                                                                54
                                                                            if (dis[v] > dis[u] + cost && cap > 0) {
58
                                                                55
                                                                              dis[v] = dis[u] + cost;
             return ret;
                                                                              pre[v] = i:
59
                                                                56
         }
                                                                              if (!inq[v]) {
60
                                                                57
       }
61
                                                                58
                                                                                q.push(v);
62
       if (!ret) {
                                                                59
                                                                                cnt[v]++;
63
         level[u] = -1;
                                                                60
                                                                                inq[v] = true;
64
                                                                61
                                                                                if (cnt[v] == n + 2) {
65
       return ret;
                                                                62
                                                                                  negcycle = true;
66
     }
                                                                63
67
     LL flow(int st, int ed) {
                                                                64
                                                                                   break;
68
       LL ret = 0;
                                                                65
                                                                                }
       while (bfs(st, ed)) {
                                                                66
                                                                              }
69
70
         fill(now, now + n + 1, 0);
                                                                67
                                                                            }
71
         ret += dfs(st, ed, INF);
                                                                68
                                                                         }
72
                                                                69
73
       return ret;
                                                                70
     }
74
                                                                71
                                                                       return dis[ed] != INF;
75 };
                                                                72
                                                                73
                                                                     LL sendFlow(int v, LL curFlow) {
                                                                        if (pre[v] == -1) {
                                                                74
                                                                75
                                                                         return curFlow;
  5.5 MCMF
                                                                76
                                                                77
                                                                       int i = pre[v];
 1 // 0-base
                                                                78
                                                                       int u = edges[i].u;
```

2 const LL INF = 1e18;

```
79
       LL cost = edges[i].cost;
80
       LL f = sendFlow(u, min(curFlow, edges[i].cap));
81
82
83
       ans_cost += f * cost;
84
       edges[i].cap -= f;
       edges[i ^ 1].cap += f;
85
86
       return f:
87
88
    pair<LL, LL> run(int st, int ed) {
89
       ans_flow = ans_cost = 0;
       while (SPFA(st, ed)) {
90
91
         ans_flow += sendFlow(ed, INF);
92
93
       return make_pair(ans_flow, ans_cost);
94
95 };
```

5.6 Stable Matching

```
1 int t, n, b[N][N], bi[N], g[N][N], bg[N], gb[N];
3 void sol() {
     deque<int> dq;
     memset(gb, 0, sizeof(gb));
6
     memset(bi, 0, sizeof(bi));
7
     for (int i = 1; i <= n; i++) dq.push_back(i);</pre>
     while (!dq.empty()) {
8
       int x = dq.front();
10
       dq.pop_front();
11
       int y = b[x][++bi[x]];
12
       if (!gb[y]) {
          gb[y] = x;
13
14
          bg[x] = y;
15
       } else if (g[y][x] < g[y][gb[y]]) {</pre>
16
          dq.push_back(gb[y]);
17
          gb[y] = x;
          bg[x] = y;
18
19
       } else {
20
          dq.push_back(x);
21
22
     }
     for (int i = 1; i <= n; i++) {
23
       cout << bg[i] << '\n';
24
25
26
27
28 int main() {
29
     int x;
     cin >> t;
30
     for (int i = 0; i < t; i++) {</pre>
31
32
       cin >> n;
33
       for (int i = 1; i <= n; i++) {
34
          for (int j = 1; j <= n; j++) {</pre>
35
            cin >> b[i][j];
36
37
       for (int i = 1; i <= n; i++) {</pre>
38
39
          for (int j = 1; j <= n; j++) {</pre>
40
            cin >> x;
41
            g[i][x] = j;
         }
42
43
       if (i) cout << '\n';</pre>
44
45
       sol();
46
47 }
```

5.7 Max General Graph Matching

```
vector<int> g[maxn];
  queue<int> q;
 5
  void Init(int n) {
    for (int i = 0; i <= n; ++i) match[i] = pre[i] = n;</pre>
    for (int i = 0; i < n; ++i) g[i].clear();</pre>
 8
9 }
10 void AddEdge(int u, int v) {
    g[u].push_back(v);
12
    g[v].push_back(u);
13
  }
14
  int Find(int u) { return u == fa[u] ? u : fa[u] =
       Find(fa[u]); }
15 int LCA(int x, int y, int n) {
    static int tk = 0;
16
17
     x = Find(x), y = Find(y);
18
19
     for (;; swap(x, y)) {
20
       if (x != n) {
         if (v[x] == tk) return x;
21
22
         v[x] = tk;
23
         x = Find(pre[match[x]]);
24
    }
25
26 }
27
  void Blossom(int x, int y, int 1) {
28
     while (Find(x) != 1) {
29
30
       pre[x] = y, y = match[x];
31
       if (s[y] == 1) q.push(y), s[y] = 0;
32
       if (fa[x] == x) fa[x] = 1;
       if (fa[y] == y) fa[y] = 1;
33
34
       x = pre[y];
35
    }
36 }
37
38 bool Bfs(int r, int n) {
     for (int i = 0; i \le n; ++i) fa[i] = i, s[i] = -1;
39
     while (!q.empty()) q.pop();
40
41
     q.push(r);
42
     s[r] = 0;
43
     while (!q.empty()) {
44
       int x = q.front();
45
       q.pop();
46
       for (int u : g[x]) {
         if (s[u] == -1) {
47
48
           pre[u] = x, s[u] = 1;
49
           if (match[u] == n) {
             for (int a = u, b = x, last; b != n; a =
50
                  last, b = pre[a])
               last = match[b], match[b] = a, match[a] =
51
                   b :
52
             return true;
           }
53
           q.push(match[u]);
54
           s[match[u]] = 0:
55
         } else if (!s[u] && Find(u) != Find(x)) {
57
           int 1 = LCA(u, x, n);
58
           Blossom(x, u, 1);
59
           Blossom(u, x, 1);
60
61
       }
    }
62
63
     return false;
64 }
65
66 int Solve(int n) {
67
    int res = 0;
     for (int x = 0; x < n; ++x) {
69
       if (match[x] == n) res += Bfs(x, n);
70
71
     return res;
72 }
```

6 String

6.1 Manacher

```
1 int p[2 * MAXN];
  int Manacher(const string &s) {
    string st = "@#";
    for (char c : s) {
       st += c;
       st += '#';
6
7
    }
    st += '$';
8
    int id = 0, mx = 0, ans = 0;
    for (int i = 1; i < st.length() - 1; i++) {</pre>
10
       p[i] = (mx > i ? min(p[2 * id - i], mx - i) : 1);
11
12
       for (; st[i - p[i]] == st[i + p[i]]; p[i]++);
       if (mx < i + p[i]) {</pre>
13
14
         mx = i + p[i];
         id = i;
15
16
17
       ans = max(ans, p[i] - 1);
18
19
    return ans;
20 }
```

6.2 Trie

```
1 const int MAXL = ;
2 const int MAXC = ;
3 struct Trie {
    int nex[MAXL][MAXC];
    int len[MAXL];
    int sz;
6
     void init() {
       memset(nex, 0, sizeof(nex));
8
9
       memset(len, 0, sizeof(len));
10
       sz = 0;
11
     void insert(const string &str) {
12
13
       int p = 0;
14
       for (char c : str) {
15
         int id = c - 'a'
         if (!nex[p][id]) {
16
17
           nex[p][id] = ++sz;
         }
18
19
         p = nex[p][id];
20
21
       len[p] = str.length();
22
     }
     vector<int> find(const string &str, int i) {
23
24
       int p = 0;
25
       vector<int> ans;
26
       for (; i < str.length(); i++) {</pre>
27
         int id = str[i] - 'a';
         if (!nex[p][id]) {
28
29
           return ans;
         }
30
31
         p = nex[p][id];
         if (len[p]) {
32
           ans.pb(len[p]);
33
34
35
       }
36
       return ans;
     }
37
```

6.3 Z-value

38 };

```
1 | // 0-base
2 | // 對於個長度為 n 的字串 s
3 | // 定義函數 z[i] 表示 s 和 s[i, n - 1]
```

```
4 // (即以 s[i] 開頭的後綴)的最長公共前綴 (LCP)的長度
  // z[0] = 0 \circ
  vector<int> z_function(string s) {
    int n = (int)s.length();
    vector<int> z(n);
    for (int i = 1, l = 0, r = 0; i < n; ++i) {
9
      if (i <= r && z[i - l] < r - i + 1) {</pre>
10
11
        z[i] = z[i - 1];
12
      } else {
        z[i] = max(0, r - i + 1);
13
14
        while (i + z[i] < n \&\& s[z[i]] == s[i + z[i]])
             ++z[i];
15
      if (i + z[i] - 1 > r) l = i, r = i + z[i] - 1;
16
17
    }
18
    return z;
19 }
```

7 DP

7.1 LIS

```
1 int LIS(vector<int> &a) {
    vector<int> s;
3
     for (int i = 0; i < a.size(); i++) {</pre>
       if (s.empty() || s.back() < a[i]) {</pre>
         s.push_back(a[i]);
5
       } else {
7
         *lower_bound(s.begin(), s.end(), a[i],
8
           [](int x, int y) {return x < y;}) = a[i];
9
    }
10
11
    return s.size();
12 }
```

7.2 LCS

```
1 int LCS(string s1, string s2) {
    int n1 = s1.size(), n2 = s2.size();
3
     vector<vector<int>> dp(n1 + 1, vector<int>(n2 + 1,
         0));
     for (int i = 1; i <= n1; i++) {</pre>
5
       for (int j = 1; j <= n2; j++) {
         if (s1[i - 1] == s2[j - 1]) {
6
7
           dp[i][j] = dp[i - 1][j - 1] + 1;
8
         } else {
           dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]);
10
11
    }
12
13
    return dp[n1][n2];
14 }
```

7.3 Huge Knapsack

```
1 // from aizu
2 #include <bits/stdc++.h>
3 typedef long long int 11;
  typedef unsigned long long int ull;
5 #define BIG_NUM 2000000000
  #define MOD 1000000007
8
  #define EPS 0.000000001
9
  using namespace std;
10
  #define SIZE 25
11
12
13
  struct Info {
   Info() { value = 0, weight = 0; }
  Info(ll arg_value, ll arg_weight) {
```

```
16
       value = arg_value;
       weight = arg_weight;
17
18
     bool operator<(const struct Info &arg) const {</pre>
19
          return weight < arg.weight; }</pre>
20
21
     ll value, weight;
22 };
23
24 11 N, W;
25 | 11 POW[SIZE];
26 ll table_B[1 << 21];
27 Info info[45];
28
29 int main() {
30
     POW[0] = 1;
     for (int i = 1; i < SIZE; i++) {</pre>
31
32
       POW[i] = POW[i - 1] * 2;
33
34
     scanf("%11d %11d", &N, &W);
35
36
37
     for (int i = 0; i < N; i++) {
       scanf("%11d %11d", &info[i].value,
38
            &info[i].weight);
39
     }
40
     if (N == 1) {
41
       if (info[0].weight <= W) {</pre>
42
43
         printf("%11d\n", info[0].value);
       } else {
44
45
         printf("\emptyset \setminus n");
46
47
48
       return 0;
49
50
51
     vector<int> A, B;
     for (int i = 0; i < N / 2; i++) {
52
53
       A.push_back(i);
54
55
     for (int i = N / 2; i < N; i++) {
56
       B.push_back(i);
57
58
     vector<Info> vec_A, vec_B;
59
60
     for (int state = 0; state < POW[A.size()]; state++)</pre>
         {
61
       11 \text{ sum\_w} = 0;
       11 sum_value = 0;
62
63
       for (int loop = 0; loop < A.size(); loop++) {</pre>
         if (state & POW[loop]) {
64
65
            sum_w += info[A[loop]].weight;
            sum_value += info[A[loop]].value;
66
         }
67
       }
68
69
       vec_A.push_back(Info(sum_value, sum_w));
70
71
     sort(vec_A.begin(), vec_A.end());
72
     for (int state = 0; state < POW[B.size()]; state++)</pre>
73
74
       11 \text{ sum\_w} = 0;
75
       11 sum_value = 0;
       for (int loop = 0; loop < B.size(); loop++) {</pre>
76
77
         if (state & POW[loop]) {
            sum_w += info[B[loop]].weight;
78
79
            sum_value += info[B[loop]].value;
80
       }
81
       vec_B.push_back(Info(sum_value, sum_w));
82
83
     sort(vec_B.begin(), vec_B.end());
84
85
     table_B[0] = vec_B[0].value;
86
87
     for (int i = 1; i < vec_B.size(); i++) {</pre>
       //ある重さ以下の最大価値を求める
88
```

```
89
        table_B[i] = max(table_B[i - 1], vec_B[i].value);
90
91
92
      int tail = vec_B.size() - 1;
93
      11 \text{ ans} = 0;
94
      for (int i = 0; i < vec_A.size(); i++) {</pre>
        while (tail >= 0 && vec_A[i].weight +
95
             vec_B[tail].weight > W) tail--;
96
        if (tail < 0) break;</pre>
97
98
        ans = max(ans, vec_A[i].value + table_B[tail]);
99
100
      printf("%11d\n", ans);
101
102
      return 0;
103 }
```

7.4 Coin Change

```
1 // from aizu
  int main() {
     int n, m, min, tmp;
     scanf("%d", &n);
     int minimum[n + 1];
     scanf("%d", &m);
6
     int coin[m];
     for (int i = 0; i < m; i++) scanf("%d", &coin[i]);</pre>
8
     minimum[0] = 0;
10
     minimum \lceil 1 \rceil = 1:
11
12
     for (int i = 2; i <= n; i++) {
13
       min = n + 1;
       for (int k = 0; k < m; k++) {
14
15
         if (coin[k] <= i) {</pre>
            tmp = 1 + minimum[i - coin[k]];
16
17
            min = (min <= tmp) ? min : tmp;
         }
18
       }
19
20
       minimum[i] = min;
21
22
     printf("%d \setminus n", minimum[n]);
23
25
     return 0;
26 }
```

7.5 Edit Distance

```
1 // from aizu
 2 typedef long long int 11;
  typedef unsigned long long int ull;
 3
  #define BIG_NUM 200000000
  #define MOD 1000000007
  #define EPS 0.000000001
 8
  int main() {
     char A[1001], B[1001];
10
     int len_A, len_B;
11
     scanf("%s %s", A, B);
12
     for (len_A = 0; A[len_A] != '\0'; len_A++);
13
     for (len_B = 0; B[len_B] != '\0'; len_B++);
15
16
     int** dp = new int*[len_B + 1];
17
18
     for (int row = 0; row <= len_B; row++) {</pre>
19
       dp[row] = new int[len_A + 1];
20
21
22
     for (int col = 0; col <= len_A; col++) {</pre>
23
       dp[0][col] = col;
24
25
```

```
26
     for (int row = 1; row <= len_B; row++) {</pre>
27
       dp[row][0] = row;
     }
28
29
30
     int cost;
31
     for (int row = 1; row <= len_B; row++) {</pre>
32
33
       for (int col = 1; col <= len_A; col++) {</pre>
         if (A[col - 1] == B[row - 1]) {
34
            cost = 0;
35
36
         } else {
            cost = 1;
37
         }
38
          dp[row][col] = min(dp[row - 1][col - 1] + cost,
39
40
            min(dp[row - 1][col] + 1, dp[row][col - 1] +
                1));
41
       }
42
     }
43
44
     printf("%d\n", dp[len_B][len_A]);
45 }
```

7.6 Maximum Subrectangle

```
1 int kadane2D(int array[N][M]) {
2
    // Modify the array's elements to now hold the sum
3
    // of all the numbers that are above that element
         in its column
    for (int i = 1; i < N; i++) {
      for (int j = 0; j < M; j++) {
6
         array[i][j] += array[i - 1][j];
8
    }
9
    int ans = 0; // Holds the maximum sum matrix found
10
         till now
11
12
     for (int bottom = 0; bottom < N; bottom++) {</pre>
       for (int top = bottom; top < N; top++) {</pre>
13
14
         // loop over all the N^2 sub problems
         int[] sums = new int[N];
15
16
         // store the sum of numbers between the two rows
17
         // in the sums array
18
19
         for (int i = 0; i < M; i++) {
           if (bottom > 0) {
20
             sums[i] = array[top][i] - array[bottom -
21
                 1][i];
           } else {
22
23
             sums[i] = array[top][i];
           }
24
25
         }
26
27
         // O(n) time to run 1D kadane's on this sums
             array
28
         ans = Math.max(ans, kadane1d(sums));
29
    }
30
31
     return ans;
32 | }
```

8 Math

8.1 Number Theory

```
Hive sion: aa^{-1} \equiv 1 \pmod{m}, \quad a^{-1} \text{ exists iff } \gcd(a,m) = 1.
• Linear inversion: a^{-1} \equiv (m - \lfloor \frac{m}{a} \rfloor) \times (m \bmod a)^{-1} \pmod{m}
• Fermat's little theorem: a^p \equiv a \pmod{p} \text{ if } p \text{ is prime.}
```

```
\begin{array}{l} \cdot \text{ Euler function: } \\ \phi(n) = n \prod_{p \mid n} \frac{p-1}{p} \\ \cdot \\ \cdot \text{ Euler theorem: } \\ a^{\phi(n)} \equiv 1 \pmod{n} \text{ if } \gcd(a,n) = 1. \\ \cdot \text{ Extended Euclidean algorithm: } \\ ax + by = \gcd(a,b) = \gcd(b,a \mod b) = \gcd(b,a - \lfloor \frac{a}{b} \rfloor b) = bx_1 + (a - \lfloor \frac{a}{b} \rfloor b)y_1 = ay_1 + b(x_1 - \lfloor \frac{a}{b} \rfloor y_1) \\ \cdot \text{ Divisor function: } \\ \sigma_x(n) = \sum_{d \mid n} d^x \cdot n = \prod_{i=1}^r p_i^{a_i} \cdot \\ \sigma_x(n) = \prod_{i=1}^r \frac{p_i^{(a_i+1)x}-1}{p_i^x-1} \text{ if } x \neq 0. \quad \sigma_0(n) = \prod_{i=1}^r (a_i+1). \\ \cdot \text{ Chinese remainder theorem: } \\ x \equiv a_i \pmod{m_i}. \\ M = \prod_i m_i \cdot M_i = M/m_i \cdot t_i = M_i^{-1} \cdot \\ x = kM + \sum_i a_i t_i M_i, \quad k \in \mathbb{Z}. \end{array}
```

8.2 Extended GCD

```
1 / / ax + by = c
  int extgcd(int a, int b, int c, int &x, int &y) {
    if (b == 0) {
3
      x = c / a;
      y = 0;
5
      return a;
    }
7
8
    int d = extgcd(b, a % b, c, y, x);
9
    y -= (a / b) * x;
10
    return d;
```

8.3 Gaussian Elimination + det

```
1 const double EPS = 1e-6;
  double Gauss(vector<vector<double>> &d) {
    int n = d.size(), m = d[0].size();
     double det = 1;
     for (int i = 0; i < m; i++) {
       int p = -1;
6
       for (int j = i; j < n; j++) {
8
         if (fabs(d[j][i]) < EPS) {</pre>
9
           continue;
10
         if (p == -1 || fabs(d[j][i]) > fabs(d[p][i])) {
11
12
         }
13
14
       if (p == -1) {
15
16
         continue;
17
       if (p != i) {
18
19
         det *= -1;
20
       for (int j = 0; j < m; j++) {
21
22
         swap(d[p][j], d[i][j]);
23
24
       for (int j = 0; j < n; j++) {
         if (i == j) {
25
26
           continue;
27
28
         double z = d[j][i] / d[i][i];
29
         for (int k = 0; k < m; k++) {
           d[j][k] -= z * d[i][k];
30
31
      }
32
33
     for (int i = 0; i < n; i++) {
34
      det *= d[i][i];
35
36
37
    return det;
38 }
  // new
39
40 const int MAXN = 300;
```

```
41 const double EPS = 1e-8;
42 int n:
43 double A[MAXN][MAXN];
44 void Gauss() {
45
    for (int i = 0; i < n; i++) {
46
       bool ok = 0;
       for (int j = i; j < n; j++) {
47
48
         if (fabs(A[j][i]) > EPS) {
           swap(A[j], A[i]);
49
           ok = 1;
50
51
           break:
         }
52
53
       }
       if (!ok) continue;
54
55
       double fs = A[i][i];
       for (int j = i + 1; j < n; j++) {
56
         double r = A[j][i] / fs;
57
         for (int k = i; k < n; k++) {</pre>
58
           A[j][k] -= A[i][k] * r;
59
60
       }
61
62
    }
63 }
```

8.4 Prime Table

```
1 vector<int> p;
2 bitset < MAXN > is_notp;
3 void PrimeTable(int n) {
     is_notp.reset();
     is_notp[0] = is_notp[1] = 1;
     for (int i = 2; i <= n; ++i) {</pre>
       if (!is_notp[i]) {
7
8
         p.push_back(i);
9
       for (int j = 0; j < (int)p.size(); ++j) {</pre>
10
         if (i * p[j] > n) {
11
           break;
12
13
14
         is_notp[i * p[j]] = 1;
15
         if (i % p[j] == 0) {
           break;
16
17
18
     }
19
20 }
```

8.5 Phi

· 歐拉函數計算對於一個整數 N,小於等於 N 的正整數中,有幾個和 N 互質

```
• \Phi(p^k) = p^{k-1} \times (p-1)
1 void phi_table(int n) {
     phi[1] = 1;
     for (int i = 2; i <= n; i++) {</pre>
       if (phi[i]) {
          continue;
6
7
       for (int j = i; j < n; j += i) {
          if (!phi[j]) {
8
            phi[j] = j;
10
          phi[j] = phi[j] / i * (i - 1);
11
12
     }
13
14 }
```

・ 如果 $gcd(p,q) = 1, \Phi(p) \cdot \Phi(q) = \Phi(p \cdot q)$

8.6 Chinese Remainder Thm

```
1 / / 参数可为负数的扩展欧几里德定理
void exOJLD(int a, int b, int& x, int& y) {
   //根据欧几里德定理
    if (b == 0) { //任意数与0的最大公约数为其本身。
5
     x = 1;
6
      y = 0;
7
    } else {
      int x1, y1;
8
      exOJLD(b, a % b, x1, y1);
9
      if (a * b < 0) { //异号取反
10
       x = -y1;
11
        y = a / b * y1 - x1;
12
      } else { //同号
13
       x = y1;
14
15
        y = x1 - a / b * y1;
16
17
   }
18 }
19 //剩余定理
20 int calSYDL(int a[], int m[], int k) {
   int N[k]; //这个可以删除
int mm = 1; //最小公倍数
21
22
23
    int result = 0;
    for (int i = 0; i < k; i++) {
24
25
     mm *= m[i];
    }
26
27
    for (int j = 0; j < k; j++) {
28
     int L, J;
      exOJLD(mm / m[j], -m[j], L, J);
29
      N[j] = m[j] * J + 1; // 1
30
31
      N[j] = mm / m[j] * L; // 2
         1和2这两个值应该是相等的。
      result += N[j] * a[j];
32
    }
33
    return (result % mm + mm) % mm;
34
    //落在(0, mm)之间,这么写是为了防止result初始为负数
35
    //本例中不可能为负可以直接
36
37
    //写成:return result%mm;即可。
38 }
39
40
  int main() {
   int a[3] = {2, 3, 6}; // a[i]=n%m[i]
41
   int m[3] = \{3, 5, 7\};
42
43
    cout << calSYDL(a, m, 3) << endl;</pre>
    //輸出為滿足兩條陣列的最小n,第3參數為陣列長度
    //所有滿足答案的數字集合為n+gcd(m0,m1,m2...)*k,
        k為正數
46
    return 0;
47 }
```

8.7 Josephus

8.8 Catalan

$$C_0 = 1 \quad \text{and} \quad C_{n+1} = \frac{2(2n+1)}{n+2}C_n$$

$$\begin{array}{c} 1 \\ 2 \\ \text{int main()} \\ 3 \\ \text{for (int i = 1; i <= 100; i++)} \\ 4 \\ \text{f[i] = f[i - 1] * (4 * i - 2) % mod;} \\ \text{for (t = i + 1, p = mod - 2; p; t = (t * t) %} \\ \text{mod, p >>= 1LL)} \\ 6 \\ \text{if (p \& 1)} \\ 7 \\ \text{f[i] *= t;} \end{array}$$

```
8 f[i] %= mod;
9 }
10 }
11 }
12 }
```

8.9 Matrix Multiplication

```
1 struct Matrix {
2
    int row, col;
     vector<vector<int>> v;
     Matrix() : row(0), col(0) {}
     Matrix(int r, int c) : row(r), col(c) {
       v = vector<vector<int>>(r, vector<int>(c, 0));
7
8 };
9 Matrix operator * (Matrix &a, Matrix &b) {
    assert(a.col == b.row);
10
11
     Matrix ret(a.row, b.col);
     for (int i = 0; i < a.row; i++) {</pre>
12
13
       for (int j = 0; j < b.col; j++) {</pre>
         for (int k = 0; k < a.col; k++) {</pre>
14
           ret.v[i][j] += a.v[i][k] * b.v[k][j];
15
16
17
       }
18
    }
19
     return ret;
20 }
21 Matrix mPow(Matrix a, int n) {
    assert(a.row == a.col);
22
23
     Matrix ret(a.row, a.col);
     ret.v[0][0] = ret.v[1][1] = 1;
24
25
     while (n > 0) {
       if (n & 1) {
26
27
         ret = ret * a;
28
       a = a * a;
29
30
       n >>= 1;
31
    }
32
     return ret;
```

8.10 Fibonacci

33 }

$$f(n) = f(n-1) + f(n-2)$$

$$\begin{bmatrix} f(n) \\ f(n-1) \end{bmatrix} = \begin{bmatrix} 1 & 1 \\ 1 & 0 \end{bmatrix}^{(n-1)} \begin{bmatrix} 1 \\ 0 \end{bmatrix}$$

$$O(\log n)$$

```
1 LL fib(int n) {
2    if (n <= 1) {
3        return n;
4    }
5    Matrix a(2, 2), b(2, 1);
6    a.v[0][0] = a.v[0][1] = a.v[1][0] = 1;
7    b.v[0][0] = 1;
8    auto t = mPow(a, n - 1);
9    t = t * b;
10    return t.v[0][0];
11 }</pre>
```

9 Geometry

9.1 Point

```
1 // notice point type!!!
2 using dvt = int;
  const double EPS = 1e-6;
  const double PI = acos(-1);
6
  struct Pt {
   dvt x;
7
  dvt y;
8
9 };
10 bool operator < (const Pt &a, const Pt &b) {
11
   return a.x == b.x ? a.y < b.y : a.x < b.x;</pre>
12 }
13 bool operator == (const Pt &a, const Pt &b) {
   return a.x == b.x && a.y == b.y;
14
15
16 Pt operator + (const Pt &a, const Pt &b) {
17
   return {a.x + b.x, a.y + b.y};
18 }
19 Pt operator - (const Pt &a, const Pt &b) {
20
   return {a.x - b.x, a.y - b.y};
21 }
22
  // multiply constant
23 Pt operator * (const Pt &a, const dvt c) {
   return {a.x * c, a.y * c};
24
25
26 Pt operator / (const Pt &a, const dvt c) {
27
   return {a.x / c, a.y / c};
28 }
29
  // |a| x |b| x cos(x)
  dvt iproduct(const Pt &a, const Pt &b) {
   return a.x * b.x + a.y * b.y;
31
32 }
33 // |a| \times |b| \times \sin(x)
34 dvt cross(const Pt &a, const Pt &b) {
35
   return a.x * b.y - a.y * b.x;
36 }
37 dvt dis_pp(const Pt &a, const Pt, &b) {
  dvt dx = a.x - b.x;
38
    dvt dy = a.y - b.y;
40
    return sqrt(dx * dx, dy * dy);
```

9.2 Line

$$d(P, L) = \frac{|ax_0 + by_0 + c|}{\sqrt{a^2 + b^2}}$$

```
1 struct Line {
    Pt st;
3
    Pt ed;
4 };
  // return point side
  // left, on line, right -> 1, 0, -1
7
  int side(Line 1, Pt a) {
    dvt cross_val = cross(a - 1.st, 1.ed - 1.st);
    if (cross_val > EPS) {
9
      return 1;
10
11
    } else if (cross_val < -EPS) {</pre>
      return -1;
12
13
    } else {
14
      return 0;
15
16 }
17
  // AB infinity, CD segment
18
  bool has_intersection(Line AB, Line CD) {
    int c = side(AB, CD.st);
19
    int d = side(AB, CD.ed);
    if (c == 0 || d == 0) {
21
22
      return true;
23
    } else {
      // different side
24
       return c == -d;
25
26
    }
  // find intersection point, two line, not seg
29 pair<int, Pt> intersection(Line a, Line b) {
```

```
30
    Pt A = a.ed - a.st;
    Pt B = b.ed - b.st;
31
     Pt C = b.st - a.st;
32
33
     dvt mom = cross(A, B);
34
     dvt son = cross(C, B);
35
     if (std::abs(mom) <= EPS) {</pre>
      if (std::abs(son) <= EPS) {</pre>
36
37
         return {1, {}}; // same line
38
       } else {
39
         return {2, {}}; // parallel
40
       }
41
                          // ok
    } else {
       return {0, a.st + A * (son / mom)};
42
43
    }
44 }
45 // line to point distance
46 dvt dis_lp(Line 1, Pt a) {
47
    return area3x2(1.st, 1.ed, a) / dis_pp(1.st, 1.ed);
48 }
```

9.3 Area

```
1 // triangle
2 dvt area3(Pt a, Pt b, Pt c) {
3
    return std::abs(cross(b - a, c - a) / 2);
4 }
5 dvt area3x2(Pt a, Pt b, Pt c) { // for integer
6
    return std::abs(cross(b - a, c - a));
7 }
8 // simple convex area(can in)
9 dvt area(vector <Pt> &a) {
10
    dvt ret = 0;
    for (int i = 0, sz = a.size(); i < sz; i++) {</pre>
11
12
      ret += cross(a[i], a[(i + 1) % sz]);
    }
13
14
    return std::abs(ret) / 2;
15 }
16 // check point in/out a convex
17 int io_convex(vector<Pt> convex, Pt q) {
    // convex is Counterclockwise
18
19
    for (int i = 0, sz = convex.size(); i < sz; i++) {</pre>
      Pt cur = convex[i] - q;
20
      Pt nex = convex[(i + 1) \% sz] - q;
21
       dvt cross_val = cross(cur, nex);
22
23
      if (std::abs(cross_val) <= EPS) {</pre>
24
         return 0; // on edge
25
      if (cross_val < 0) {</pre>
26
27
         return -1; // outside
      }
28
29
    }
30
     return 1;
                    // inside
```

9.4 Convex Hull

```
1 vector Pt> convex_hull(vector Pt> &a) {
    sort(a.begin(), a.end());
3
    a.erase(unique(a.begin(), a.end()), a.end());
    int sz = a.size(), m = 0;
    vector<Pt> ret(sz + 5); // safe 1 up
5
    for (int i = 0; i < sz; i++) {</pre>
6
7
       while (m > 1 &&
         cross(ret[m - 1] - ret[m - 2], a[i] - ret[m -
8
             2]) <= EPS) {
9
        m - -;
10
      }
11
      ret[m++] = a[i];
    }
12
13
    int k = m;
14
    for (int i = sz - 2; i >= 0; i--) {
15
       while (m > k \&\&
         cross(ret[m - 1] - ret[m - 2], a[i] - ret[m -
16
             2]) <= EPS) {
```

```
17
18
       ret[m++] = a[i];
19
     }
20
21
     if (sz > 1) {
22
       m - -;
     }
23
24
     ret.resize(m);
25
     return ret;
26
```

9.5 Closest Pair

```
1 // from aizu
  struct Info {
2
    Info() { x = y = 0; }
     Info(double arg_x, double arg_y) {
5
       x = arg_x;
 6
       y = arg_y;
    }
7
 8
     bool operator<(const struct Info& arg) const {</pre>
 9
       return x < arg.x;</pre>
     };
10
11
     double x, y;
12 };
13
14 int N;
15
16
  bool compare_y(Info left, Info right) {
17
    return left.y < right.y;</pre>
18 }
19
20 Info* info;
21
  double closest_pair(Info* array, int tmp_N) {
22
    if (tmp_N <= 1) return DBL_MAX;</pre>
23
24
25
     int mid = tmp_N / 2;
26
     double x = array[mid].x;
     double dist =
27
         min(closest_pair(array, mid),
28
              closest_pair(array + mid, tmp_N - mid));
29
     inplace_merge(array, array + mid, array + tmp_N,
         compare_y);
30
     vector < Info > V;
31
     for (int i = 0; i < tmp_N; i++) {</pre>
32
33
       if (fabs(array[i].x - x) >= dist) continue;
34
35
       for (int j = 0; j < V.size(); j++) {</pre>
36
         double dx = array[i].x - V[V.size() - j - 1].x;
         double dy = array[i].y - V[V.size() - j - 1].y;
37
38
         if (dy >= dist) break;
         dist = min(dist, sqrt(dx * dx + dy * dy));
39
40
41
       V.push_back(array[i]);
42
     }
43
     return dist;
44 }
45
46 int main() {
47
     scanf("%d", &N);
48
     info = (Info*)malloc(sizeof(Info) * N);
49
     for (int i = 0; i < N; i++) {</pre>
      scanf("%lf %lf", &info[i].x, &info[i].y);
51
52
53
54
     sort(info, info + N);
55
56
     printf("%.71f\n", closest_pair(info, N));
57 }
```