1.2

Default

Contents

```
1 #include <bits/stdc++.h>
1 Basic
                             using namespace std;
 using LL = long long;
                            3
  #define IOS ios_base::sync_with_stdio(0); cin.tie(0);
  #define pb push_back
 #define eb emplace_back
 const int INF = 1e9;
 const int MOD = 1e9 + 7;
                             const double EPS = 1e-6;
2 Data Structure
 const int MAXN = 0;
 12 int main() {
 13
                            14 }
3 Graph
  1.3 Black Magic
  #include <bits/stdc++.h>
 #include <ext/pb_ds/assoc_container.hpp>
  #include <ext/pb_ds/tree_policy.hpp>
  #include <ext/pb_ds/priority_queue.hpp>
                             using namespace std;
4 Connectivity
 using namespace __gnu_pbds;
  using set_t =
  tree<int, null_type, less<int>, rb_tree_tag,
  tree_order_statistics_node_update>;
                            10
                             using map t =
5 Flow & Matching
                           9
                              tree<int, int, less<int>, rb_tree_tag,
 9
                            12
                               tree_order_statistics_node_update>;
 using heap_t =
                          10
 10
                              __gnu_pbds::priority_queue<int>;
  using ht_t =
                            15
 gp_hash_table<int, int>;
 17
                             int main() {
6 String
                              set_t st;
                            19
  12
                              st.insert(5); st.insert(6);
                            20
  st.insert(3); st.insert(1);
 13
                              // the smallest is (0), biggest is (n-1), kth small
 13
                                is (k-1)
  int num = *st.find_by_order(0);
  13
                              cout << num << '\n'; // print 1
                            25
 26
 num = *st.find_by_order(st.size() - 1);
                              cout << num << '\n'; // print 6
8 Math
 // find the index
                            30
                              int index = st.order_of_key(6);
                              cout << index << '\n'; // print 3
 // check if there exists x
 int x = 5;
                            35
  int check = st.erase(x);
                            36
 16
                              if (check == 0) printf("st not contain 5\n");
                            37
                              else if (check == 1) printf("st contain 5\n");
                            38
                            39
 Geometry
                            40
                              //tree policy like set
  st.insert(5); st.insert(5);
 9.3 Area
                              cout << st.size() << '\n'; // print 4</pre>
 43
                            44
                              //map------
                            45
                              map_t mp;
   Basic
                            46
                              mp[1] = 2;
                              cout << mp[1] << '\n';
                            47
                              auto tmp = *mp.find_by_order(0); // pair
cout << tmp.first << " " << tmp.second << '\n';</pre>
                            48
                            49
1.1
   Run
                            50
                            51
                              //heap------
1 #use -> sh run.sh {name}
                              heap_t h1, h2;
                            52
g++ -O2 -std=c++14 -Wall -Wextra -Wshadow -o $1 $1.cpp
                              h1.push(1); h1.push(3);
                            53
3 | ./$1 < t.in > t.out
                              h2.push(2); h2.push(4);
```

55

h1.join(h2);

```
56
    cout << h1.size() << h2.size() << h1.top() << '\n';</pre>
                                                                   double L = -1e5, R = 1e5;
                                                                   while (R - L > EPS) {
57
                                                               6
                                                               7
                                                                     double mr = (L + R) / 2.0;
58
    //hash-table-----
                                                                     double ml = (L + mr) / 2.0;
59
                                                               8
60
    ht_t ht;
                                                               9
                                                                     if (f(ml) < f(mr)) {
61
    ht[85] = 5;
                                                              10
                                                                       R = mr;
    ht[89975] = 234;
                                                                     } else {
62
                                                              11
    for (auto i : ht) {
                                                              12
                                                                       L = m1;
       cout << i.first << " " << i.second << '\n';</pre>
64
                                                              13
                                                                   }
65
                                                              14
66 }
                                                              15
                                                                   return L;
                                                              16 }
```

1.4 Python

```
1 ### EOF
2 while True:
3
    try:
      pass
4
    except EOFError:
5
6
      break
7 ###math
8 import math
10 math.ceil(x)#上高斯
11 math.floor(x)#下高斯
12 math.factorial(x)#接乘
13 math.fabs(x)#絕對值
14 math.fsum(arr)#跟sum一樣但更精確(小數點問題)
15 math.gcd(x, y)#bj4
16 math.exp(x)#e^x
17 math.log(x, base)
18 math.log2(x)#2為底
19 math.log10(x)#10為底
20 math.sqrt(x)
21 math.pow(x, y, mod)#精確些(float型態) MOD!!!
22 math.sin(x)# cos tan asin acos atan atan2(弧度) sinh
      cosh tanh acosh asinh atanh
23 math.hypot(x, y)#歐幾里德範數
24 math.degrees(x)#x從弧度轉角度
25 math.radians(x)#x從角度轉弧度
26 math.gamma(x)#x的gamma函數
27 math.pi#常數
28 math.e#常數
29 math.inf
30
31 ### ascii
32 ord(x)#char to asc
33 chr(x)#asc to char
35 x.encode().hex()#string to hex
36 ### reverse string
37 string = "abc"
38 string_reverse = string[::-1]
```

1.5 Binary Search

1.6 Ternary Search

```
const double EPS = 1e-6;
// target function
double f(double x) { return x * x; }
double ternarySearch() {
```

2 Data Structure

2.1 Disjoint Set

```
1 // 0-base
2 const int MAXN = 1000;
3 int boss[MAXN];
  void init(int n) {
    for (int i = 0; i < n; i++) {</pre>
       boss[i] = -1;
    }
7
8 }
9
  int find(int x) {
10
    if (boss[x] < 0) {
11
      return x;
12
13
     return boss[x] = find(boss[x]);
  }
14
15
  bool uni(int a, int b) {
    a = find(a);
16
     b = find(b);
17
     if (a == b) {
18
19
      return false;
20
     if (boss[a] > boss[b]) {
21
22
       swap(a, b);
23
24
     boss[a] += boss[b];
25
     boss[b] = a;
26
     return true;
27 }
```

2.2 BIT RARSQ

```
1 // 1-base
  #define lowbit(k) (k & -k)
4
  int n;
5
  vector<int> B1, B2;
  void add(vector<int> &tr, int id, int val) {
    for (; id <= n; id += lowbit(id)) {</pre>
8
9
      tr[id] += val;
    }
10
11 }
12 void range_add(int 1, int r, int val) {
    add(B1, 1, val);
13
14
    add(B1, r + 1, -val);
    add(B2, 1, val * (1 - 1));
15
16
    add(B2, r + 1, -val * r);
17 }
18 int sum(vector<int> &tr, int id) {
19
    int ret = 0;
    for (; id >= 1; id -= lowbit(id)) {
20
21
      ret += tr[id];
    }
22
23
    return ret;
24 }
25 int prefix_sum(int id) {
```

```
26    return sum(B1, id) * id - sum(B2, id);
27  }
28  int range_sum(int 1, int r) {
29    return prefix_sum(r) - prefix_sum(1 - 1);
30  }
```

2.3 zkw RMQ

```
1 // 0-base
2 const int INF = 1e9;
3 const int MAXN = ;
5 int n;
6 int a[MAXN], tr[MAXN << 1];</pre>
8 // !!! remember to call this function
  void build() {
    for (int i = 0; i < n; i++) {</pre>
10
11
       tr[i + n] = a[i];
12
    for (int i = n - 1; i > 0; i--) {
13
       tr[i] = max(tr[i << 1], tr[i << 1 | 1]);
14
15
16 }
17 void update(int id, int val) {
    for (tr[id += n] = val; id > 1; id >>= 1) {
18
19
       tr[id >> 1] = max(tr[id], tr[id ^ 1]);
    }
20
21 }
22 int query(int 1, int r) { // [1, r)
    int ret = -INF;
23
24
     for (1 += n, r += n; 1 < r; 1 >>= 1, r >>= 1) {
       if (1 & 1) {
25
26
         ret = max(ret, tr[1++]);
       }
27
28
       if (r & 1) {
29
         ret = max(ret, tr[--r]);
30
31
    }
32
     return ret;
33 }
```

2.4 Segment Tree RARMQ

```
1 struct Node {
2
     int val, tag;
     Node *lc, *rc;
3
     Node() : lc(nullptr), rc(nullptr), tag(0) {}
5
     void pull() {
       if (!1c) {
6
7
         val = rc->val;
       } else if (!rc) {
8
         val = lc->val;
9
       } else {
10
11
         val = max(lc->val, rc->val);
       }
12
13
    }
14
     void push() {
15
       if (lc) {
16
         lc->tag += tag;
17
         lc->val += tag;
18
19
       if (rc) {
         rc->tag += tag;
20
21
         rc->val += tag;
       }
22
23
       tag = 0;
24
    }
25 }:
26 struct SegmentTree {
27
    Node *root;
28
     SegmentTree() : root(nullptr) {}
29
     void build(Node* &T, int 1, int r, const
         vector<int> &o) {
```

```
30
       T = new Node();
       if (1 == r) {
31
         T->val = o[1];
32
33
         return;
34
35
       int mid = (1 + r) / 2;
       build(T->lc, l, mid, o);
36
37
       build(T->rc, mid + 1, r, o);
38
       T->pull();
39
40
     void update(Node* &T, int 1, int r, int q1, int qr,
         int v) {
41
       if (ql <= 1 && r <= qr) {</pre>
         T->val += v;
42
43
         T->tag += v;
44
         return;
45
       }
46
       T->push();
47
       int mid = (1 + r) / 2;
       if (qr <= mid) {
48
         update(T->lc, 1, mid, ql, qr, v);
49
50
       } else if (mid < ql) {</pre>
51
         update(T->rc, mid + 1, r, ql, qr, v);
52
       } else {
53
         update(T->lc, 1, mid, ql, mid, v);
         update(T->rc, mid + 1, r, mid + 1, qr, v);
54
55
       T->pull();
56
57
58
     int query(Node* &T, int 1, int r, int q1, int qr) {
       if (ql <= 1 && r <= qr) {</pre>
59
60
         return T->val;
61
       }
62
       T->push();
63
       int mid = (1 + r) / 2;
64
       if (qr <= mid) {
65
         return query(T->lc, 1, mid, ql, qr);
66
       } else if (mid < ql) {</pre>
67
         return query(T->rc, mid + 1, r, ql, qr);
68
       } else {
69
         return max(query(T->lc, 1, mid, ql, mid),
70
              query(T->rc, mid + 1, r, mid + 1, qr));
71
72
    }
73 };
```

2.5 Treap

```
1 struct Treap {
     int val, pri, sz;
 3
     Treap *lc, *rc;
     Treap() {}
 5
    Treap(int _val) {
       val = _val;
 6
 7
       pri = rand();
8
       sz = 1;
       1c = rc = NULL;
9
    }
10
11 };
12
13 int getSize(Treap *a) { return (a == NULL ? 0 :
       a->sz); }
14
  void split(Treap *t, Treap *&a, Treap *&b, int k) {
15
16
     if (t == NULL) {
       a = b = NULL;
17
18
       return;
    }
19
20
    if (getSize(t->lc) < k) {</pre>
21
       split(t->rc, a->rc, b, k - getSize(t->lc) - 1);
22
23
     } else {
24
       b = t;
25
       split(t->lc, a, b->lc, k);
26
27 }
```

```
28
  Treap *merge(Treap *a, Treap *b) {
29
    if (!a || !b) {
30
      return (a ? a : b);
31
32
    if (a->pri > b->pri) {
33
      a->rc = merge(a->rc, b);
34
35
      return a;
36
    } else {
      b->lc = merge(a, b->lc);
37
38
       return b;
    }
39
40 }
41
42
  void Insert(Treap *&t, int x, int p) {
43
    Treap *a, *b;
    split(t, a, b, x);
44
45
    t = merge(a, merge(new Treap(p), b));
46 }
47
48 void Delete(Treap *&t, int x) {
    Treap *a, *b, *c;
49
50
    split(t, b, c, x);
51
    split(b, a, b, x - 1);
52
    t = merge(a, c);
53 }
54
55 /*
56 Usage
57 Treap *root = NULL; // declare
58 root = merge(root, new Treap(val)); // push back
59 Insert(root, x, y); // insert y after x-th element
60 Delete(root, x); // delete x-th element
61 */
```

3 Graph

3.1 Dijkstra

```
1 // 0-base
2 const LL INF = 1e18;
3 const int MAXN = ;
4 struct Edge {
    int to;
     LL cost;
     Edge(int v, LL c) : to(v), cost(c) {}
     bool operator < (const Edge &other) const {</pre>
8
9
       return cost > other.cost;
    }
10
11 };
12
13 int n;
14 LL dis[MAXN];
15 vector < Edge > G[MAXN];
16
17 void init() {
     for (int i = 0; i < n; i++) {</pre>
18
19
       G[i].clear();
20
       dis[i] = INF;
21
22 }
  void Dijkstra(int st, int ed = -1) {
23
24
     priority_queue < Edge > pq;
25
     pq.emplace(st, 0);
26
     dis[st] = 0;
27
     while (!pq.empty()) {
       auto now = pq.top();
28
29
       pq.pop();
       if (now.to == ed) {
30
31
         return;
32
       if (now.cost > dis[now.to]) {
33
34
         continue;
35
```

3.2 SPFA(negative cycle)

```
1 // 0-base
  const LL INF = 1e18;
  const int MAXN = ;
  struct Edge {
    int to;
    LL cost;
    Edge(int v, LL c) : to(v), cost(c) {}
7
8 };
10 int n;
11 LL dis[MAXN];
12 vector < Edge > G[MAXN];
13
14 void init() {
15
    for (int i = 0; i < n; i++) {
16
      G[i].clear();
17
       dis[i] = INF;
18
    }
19 }
20
  bool SPFA(int st) {
    vector<int> cnt(n, 0);
21
22
     vector<bool> inq(n, false);
23
     queue < int > q;
24
25
     q.push(st);
26
     dis[st] = 0;
     inq[st] = true;
27
28
     while (!q.empty()) {
29
       int now = q.front();
30
       q.pop();
       inq[now] = false;
31
       for (auto &e : G[now]) {
32
         if (dis[e.to] > dis[now] + e.cost) {
33
34
           dis[e.to] = dis[now] + e.cost;
35
           if (!inq[e.to]) {
36
             cnt[e.to]++:
              if (cnt[e.to] > n) {
37
38
                // negative cycle
39
                return false;
40
41
             inq[e.to] = true;
42
             q.push(e.to);
           }
43
44
       }
45
46
    }
47
     return true;
48 3
```

3.3 Floyd Warshall

```
12
         G[i][j] = INF;
13
14
       G[i][i] = 0;
15
    }
16 }
17 void floyd() {
    for (int k = 0; k < n; k++) {
18
19
       for (int i = 0; i < n; i++) {</pre>
         for (int j = 0; j < n; j++) {
20
           if (G[i][k] != INF && G[k][j] != INF) {
21
22
              G[i][j] = min(G[i][j], G[i][k] + G[k][j]);
23
24
         }
25
       }
26
     }
27 }
```

3.4 Topological Sort

```
1 // 0-base
2 // if ret.size < n -> cycle
3 int n;
4 vector<vector<int>> G;
6 vector<int> topoSort() {
    vector<int> indeg(n), ret;
    for (auto &li : G) {
8
      for (int x : li) {
10
         ++indeg[x];
11
      }
12
     // use priority queue for lexic. largest ans
13
    queue<int> q;
14
15
     for (int i = 0; i < n; i++) {
      if (!indeg[i]) {
16
17
         q.push(i);
      }
18
19
20
    while (!q.empty()) {
21
      int u = q.front();
22
      q.pop();
23
       ret.pb(u);
       for (int v : G[u]) {
24
25
         if (--indeg[v] == 0) {
26
           q.push(v);
27
28
      }
    }
29
30
     return ret;
```

3.5 Tree Diameter

```
1 // 0-base;
2 const int MAXN = ;
3
4 struct Edge {
    int to;
    int cost;
7
    Edge(int v, int c) : to(v), cost(c) {}
8 };
10 | int n, d = 0;
11 int d1[MAXN], d2[MAXN];
12 vector < Edge > G[MAXN];
13 // dfs(0, -1);
14 void dfs(int u, int from) {
    d1[u] = d2[u] = 0;
15
     for (auto e : G[u]) {
16
17
      if (e.to == from) {
18
         continue;
19
       dfs(e.to, u);
20
```

```
21
       int t = d1[e.to] + e.cost;
       if (t > d1[u]) {
22
23
         d2[u] = d1[u];
         d1[u] = t;
24
25
       } else if (t > d2[u]) {
26
         d2[u] = t;
27
28
29
    d = max(d, d1[u] + d2[u]);
30
```

3.6 Directed MST

```
1 // 0-base
   const LL INF = 1e18;
   const int MAXN = ;
 3
   struct Edge {
 5
    int from;
     int to;
     LL cost;
     Edge(int u, int v, LL c) : from(u), to(v), cost(c)
9
          {}
10 };
11
12
   struct DMST {
13
     int n;
     int vis[MAXN], pre[MAXN], id[MAXN];
14
15
     LL in[MAXN];
16
     vector < Edge > edges;
     void init(int _n) {
17
       n = _n;
18
19
       edges.clear();
     }
20
     void add_edge(int from, int to, LL cost) {
21
22
       edges.eb(from, to, cost);
23
     LL run(int root) {
24
       LL ret = 0;
25
26
       while (true) {
27
         for (int i = 0; i < n; i++) {
           in[i] = INF;
28
29
30
31
          // find in edge
32
         for (auto &e : edges) {
            if (e.cost < in[e.to] && e.from != e.to) {</pre>
33
34
              pre[e.to] = e.from;
35
              in[e.to] = e.cost;
36
         }
37
38
39
          // check in edge
         for (int i = 0; i < n; i++) {</pre>
40
41
            if (i == root) {
42
              continue;
43
            if (in[i] == INF) {
44
45
              return -1;
46
         }
47
48
49
         int nodenum = 0;
         memset(id, -1, sizeof(id));
memset(vis, -1, sizeof(vis));
50
51
         in[root] = 0:
52
53
          // find cycles
54
55
         for (int i = 0; i < n; i++) {</pre>
56
            ret += in[i];
57
            int v = i;
58
            while (vis[v] != i && id[v] == -1 && v !=
                 root) {
59
              vis[v] = i;
60
              v = pre[v];
```

```
62
            if (id[v] == -1 && v != root) {
              for (int j = pre[v]; j != v; j = pre[j]) {
63
                id[j] = nodenum;
64
              }
65
66
              id[v] = nodenum++;
           }
67
68
69
          // no cycle
70
          if (nodenum == 0) {
71
72
            break:
73
74
75
          for (int i = 0; i < n; i++) {</pre>
76
           if (id[i] == -1) {
77
              id[i] = nodenum++;
78
         }
79
80
81
          // grouping the vertices
          for (auto &e : edges) {
82
83
           int to = e.to;
84
            e.from = id[e.from];
            e.to = id[e.to];
85
            if (e.from != e.to) {
86
              e.cost -= in[to]; //!!!
87
88
89
         }
90
91
         n = nodenum;
         root = id[root];
92
93
94
       return ret;
95
     }
96 };
```

3.7 LCA

```
1 const int LOG = 20;
2 vector<int> tin(MAXN), tout(MAXN), depth(MAXN);
3 int par[MAXN][LOG];
4 \mid int timer = 0:
 5 vector<int> G[MAXN];
6
7
  void dfs(int u, int f) {
8
     tin[u] = ++timer;
     par[u][0] = f;
10
     for (int v : G[u]) {
       if (v != f) {
11
12
         depth[v] = depth[u] + 1;
13
         dfs(v, u);
       }
14
15
     }
     tout[u] = ++timer;
16
17 }
18
19 void Doubling(int n) {
20
     for (int j = 1; j < LOG; ++j) {</pre>
       for (int i = 1; i <= n; ++i) {
21
22
         par[i][j] = par[par[i][j - 1]][j - 1];
23
24
     }
25 }
26
27
   bool anc(int u, int v) { return tin[u] <= tin[v] &&</pre>
       tout[v] <= tout[u]; }</pre>
28
29 int LCA(int u, int v) {
30
    if (depth[u] > depth[v]) {
31
       swap(u, v);
32
     if (anc(u, v)) {
33
34
       return u;
35
     for (int j = LOG - 1; j >= 0; --j) {
36
       if (!anc(par[u][j], v)) u = par[u][j];
37
```

```
39
    return par[u][0];
40 }
41
42
  int dis(int u, int v) {
43
    int lca = LCA(u, v);
    return depth[u] + depth[v] - 2 * depth[lca];
44
45 }
46
47
48
  dfs(root, root);
49 Doubling(n);
50 */
```

3.8 Euler Circuit

七橋問題根據起點與終點是否相同,分成 Euler path(不同)及 Euler circuit(相同)。

- 判斷法
- · 無向圖部分,將點分成奇點(度數為奇數)和偶點(度數為偶數)。
 - Euler path: 奇點數為 0 或 2
 - Euler circuit:沒有奇點
- · 有向圖部分,將點分成出點 (出度 入度 = 1) 和入點 (入度 出度 = 1) 還 有平衡點 (出度 = 入度)。
 - Euler path:出點和入點個數同時為 0 或 1。
 - Euler circuit:只有平衡點。
- 求出一組解
- 用 DFS 遍歷整張圖,設 S 為離開的順序,無向圖的答案為 S ,有向圖的答案 為反向的 S 。
- · DFS 起點選定:
 - Euler path:無向圖選擇任意一個奇點,有向圖選擇出點。
 - Euler circuit:任意一點。

```
1 // Code from Eric
 2 #define 11 long long
  #define PB push_back
  #define EB emplace_back
  #define PII pair<int, int>
  #define MP make_pair
  #define all(x) x.begin(), x.end()
  #define maxn 50000+5
10
  //structure
11
  struct Eular {
    vector<PII> adj[maxn];
12
13
     vector<bool> edges;
     vector<PII> path;
14
     int chk[maxn];
15
16
     int n;
17
18
     void init(int _n) {
       n = _n;
19
20
       for (int i = 0; i <= n; i++) adj[i].clear();</pre>
21
       edges.clear();
22
       path.clear();
23
       memset(chk, 0, sizeof(chk));
24
25
     void dfs(int v) {
26
27
       for (auto i : adj[v]) {
28
         if (edges[i.first] == true) {
29
           edges[i.first] = false;
30
           dfs(i.second);
           path.EB(MP(i.second, v));
31
32
         }
33
       }
34
35
     void add_Edge(int from, int to) {
36
```

```
37
       edges.PB(true);
38
       // for bi-directed graph
39
       adj[from].PB(MP(edges.size() - 1, to));
40
41
       adj[to].PB(MP(edges.size() - 1, from));
42
       chk[from]++;
43
       chk[to]++:
44
       // for directed graph
45
       // adj[from].PB(MP(edges.size()-1, to));
46
47
       // check[from]++;
48
49
     bool eular_path() {
50
51
       int st = -1;
       for (int i = 1; i <= n; i++) {
52
         if (chk[i] % 2 == 1) {
53
54
           st = i;
           break;
55
56
         }
57
       if (st == -1) {
58
59
         return false;
60
       dfs(st);
61
62
       return true;
63
64
65
     void print_path(void) {
66
       for (auto i : path) {
         printf("%d %d\n", i.first, i.second);
67
68
       }
69
    }
70 };
1 // Code from allen(lexicographic order)
2 #include <bits/stdc++.h>
3 using namespace std;
4 const int ALP = 30;
5 const int MXN = 1005;
6 int n;
7 int din[ALP], dout[ALP];
8 int par[ALP];
9| vector<string> vs[MXN], ans;
10 bitset < MXN > vis, used[ALP];
11
12 void djsInit() {
13
    for (int i = 0; i != ALP; ++i) {
14
       par[i] = i;
15
    }
16 }
17
18 int Find(int x) { return (x == par[x] ? (x) : (par[x]
       = Find(par[x])); }
19
20 void init() {
21
     djsInit();
     memset(din, 0, sizeof(din));
22
     memset(dout, 0, sizeof(dout));
23
24
     vis.reset();
     for (int i = 0; i != ALP; ++i) {
25
26
       vs[i].clear();
27
       used[i].reset();
28
    }
29
     return;
30 }
32| void dfs(int u) {
33
     for (int i = 0; i != (int)vs[u].size(); ++i) {
       if (used[u][i]) {
34
35
         continue:
36
       used[u][i] = 1;
37
       string s = vs[u][i];
38
       int v = s[s.size() - 1] - 'a';
39
40
       dfs(v);
41
       ans.push_back(s);
42
```

```
43 }
44
45
  bool solve() {
46
    int cnt = 1;
47
     for (int i = 0; i != n; ++i) {
48
       string s;
49
       cin >> s:
50
       int from = s[0] - 'a', to = s.back() - 'a';
51
       ++din[to];
52
       ++dout[from];
53
       vs[from].push_back(s);
       vis[from] = vis[to] = true;
54
55
       if ((from = Find(from)) != (to = Find(to))) {
56
         par[from] = to;
57
         ++cnt:
       }
58
59
60
     if ((int)vis.count() != cnt) {
61
      return false;
62
     int root, st, pin = 0, pout = 0;
63
64
     for (int i = ALP - 1; i >= 0; --i) {
65
       sort(vs[i].begin(), vs[i].end());
66
       if (vs[i].size()) root = i;
67
       int d = dout[i] - din[i];
       if (d == 1) {
68
69
         ++pout;
70
         st = i;
71
       } else if (d == -1) {
72
       } else if (d != 0) {
73
74
         return false;
75
      }
76
     if (pin != pout || pin > 1) {
77
78
      return false;
79
80
     ans.clear();
81
     dfs((pin ? st : root));
82
     return true:
83 }
84
85 int main() {
86
    int t;
     cin >> t;
87
88
     while (t--) {
89
       cin >> n;
90
       init();
91
       if (!solve()) {
         cout << "***\n";
92
93
         continue:
       }
94
95
       for (int i = ans.size() - 1; i >= 0; --i) {
96
         cout << ans[i] << ".\n"[i == 0];</pre>
97
    }
98
99 }
```

4 Connectivity

4.1 Kosaraju SCC

```
1 // 0-base
2 int n:
  vector<vector<int>>> G, G2; // G2 = G rev
4 vector < bool > vis;
  vector<int> s, color;
  int sccCnt;
  void dfs1(int u) {
7
    vis[u] = true;
9
    for (int v : G[u]) {
10
      if (!vis[v]) {
11
         dfs1(v);
12
```

```
13
    }
    s.pb(u);
14
15 }
16 void dfs2(int u) {
17
    color[u] = sccCnt;
18
     for (int v : G2[u]) {
       if (!color[v]) {
19
20
         dfs2(v);
       }
21
    }
22
23 }
24 void Kosaraju() {
     sccCnt = 0;
25
     for (int i = 0; i < n; i++) {
26
27
       if (!vis[i]) {
         dfs1(i);
28
29
       }
30
    }
     for (int i = n - 1; i >= 0; i--) {
31
32
       if (!color[s[i]]) {
         ++sccCnt:
33
34
         dfs2(s[i]);
       }
35
    }
36
37 }
```

4.2 BCC

```
1 typedef pair<int, int> PII;
2 int low[MXV], depth[MXV];
3 bool is_cut_vertex[MXV], visit[MXV];
4 vector<int> G[MXV];
5 vector < PII > BCC[MXV];
6 int bcc_cnt = 0;
7 stack<PII> st;
9 vector<pair<int, int>> my_cut_edge;
11 void dfs(int now, int cur_depth, int f) {
    visit[now] = true;
12
13
    depth[now] = low[now] = cur_depth;
    int cut son = 0:
14
     for (auto i : G[now]) {
15
      if (i == f) continue;
16
17
       if (visit[i]) { // ancestor
18
         if (depth[i] < depth[now]) { // #</pre>
           low[now] = min(low[now], depth[i]);
19
20
           st.push({now, i});
         }
21
22
       } else { // offspring
23
         st.push({now, i});
         dfs(i, cur_depth + 1, now);
24
25
         cut_son += 1;
         low[now] = min(low[now], low[i]);
26
27
         if (low[i] >= depth[now]) {
28
           is_cut_vertex[now] = true;
           auto t = st.top();
29
30
           st.pop();
           while (t != make_pair(now, i)) {
31
32
             BCC[bcc_cnt].push_back(t);
             t = st.top();
33
34
             st.pop();
35
           }
           BCC[bcc_cnt].push_back(t);
36
37
           ++bcc_cnt;
         }
38
         // ###
39
         if (low[i] > depth[now])
40
41
           my_cut_edge.push_bach({now, i});
42
      }
43
     if (cur_depth == 0)
44
45
       is_cut_vertex[now] = (cut_son != 1);
46
     return;
47 }
48
```

```
49 bool is_2_edge_connected(int n) {
50    memset(visit, 0, sizeof(visit));
51    dfs(1, 0, -1);
52    return my_cut_edge.size() == 0;
53 }
```

8

4.3 Articulation Point

```
1 // from aizu
 2 typedef long long int 11;
  typedef unsigned long long int ull;
  #define BIG_SIZE 200000000
  #define MOD 1000000007
  #define EPS 0.000000001
  using namespace std;
9
  #define SIZE 100000
10
11 vector<int> G[SIZE];
12 int N;
13
  bool visited[SIZE];
  int visited_order[SIZE], parent[SIZE], lowest[SIZE],
14
       number:
15
  void dfs(int cur, int pre_node) {
16
17
     visited_order[cur] = lowest[cur] = number;
     number++;
18
19
20
     visited[cur] = true;
21
22
     int next;
23
24
     for (int i = 0; i < G[cur].size(); i++) {</pre>
25
       next = G[cur][i];
26
       if (!visited[next]) {
27
         parent[next] = cur;
28
         dfs(next. cur):
         lowest[cur] = min(lowest[cur], lowest[next]);
29
       } else if (visited[next] == true && next !=
30
           pre node) {
31
         lowest[cur] = min(lowest[cur],
              visited_order[next]);
32
33
    }
34
35
36
  void art points() {
37
     for (int i = 0; i < N; i++) visited[i] = false;</pre>
38
39
     number = 1;
     dfs(0, -1);
40
41
42
     int tmp_parent, root_num = 0;
43
44
     vector<int> V;
45
     for (int i = 1; i < N; i++) {
46
47
       tmp_parent = parent[i];
48
       if (tmp_parent == 0) {
49
         root_num++;
50
       } else if (visited_order[tmp_parent] <=</pre>
           lowest[i]) {
51
         V.push_back(tmp_parent);
52
53
     if (root_num >= 2) {
54
55
       V.push_back(0);
56
57
     sort(V.begin(), V.end());
58
     V.erase(unique(V.begin(), V.end()), V.end());
59
60
     for (int i = 0; i < V.size(); i++) {</pre>
       printf("%d \setminus n", V[i]);
61
62
63 }
64
```

63

```
65 int main() {
    int E:
66
    scanf("%d %d", &N, &E);
    int from, to;
68
69
    for (int i = 0; i < E; i++) {
      scanf("%d %d", &from, &to);
70
      G[from].push_back(to);
71
72
      G[to].push_back(from);
    }
73
74
    art_points();
75 }
  4.4 Bridges
```

```
1 // from aizu
2 typedef long long int 11;
3 typedef unsigned long long int ull;
 4 #define BIG_NUM 2000000000
5 #define MOD 1000000007
6 #define EPS 0.000000001
7 using namespace std;
9 struct Edge {
    bool operator<(const struct Edge &arg) const {</pre>
10
11
       if (s != arg.s) {
12
         return s < arg.s;</pre>
13
       } else {
14
         return t < arg.t;</pre>
15
       }
16
    }
17
    int s, t;
18 };
19 struct Info {
20
    Info(int arg_to, int arg_edge_id) {
21
       to = arg_to;
22
       edge_id = arg_edge_id;
23
24
    int to, edge_id;
25 };
26
27 int V, E, number;
28 int order[100000], lowlink[100000];
29 bool visited[100000];
30 Edge edge[100000];
31 vector < Info > G[100000];
32
33 void recursive(int cur) {
    order[cur] = number++;
    lowlink[cur] = order[cur];
35
36
37
     int next;
38
     for (int i = 0; i < G[cur].size(); i++) {</pre>
39
       next = G[cur][i].to;
40
41
       if (order[next] == -1) {
42
         visited[G[cur][i].edge_id] = true;
43
44
         recursive(next);
45
         lowlink[cur] = min(lowlink[cur], lowlink[next]);
46
47
       } else if (visited[G[cur][i].edge_id] == false) {
48
         lowlink[cur] = min(lowlink[cur], order[next]);
49
    }
50
51 }
52
53 int main() {
     scanf("%d %d", &V, &E);
54
55
     for (int i = 0; i < E; i++) {</pre>
       scanf("%d %d", &edge[i].s, &edge[i].t);
56
       if (edge[i].s > edge[i].t) {
57
         swap(edge[i].s, edge[i].t);
58
59
60
       G[edge[i].s].push_back(Info(edge[i].t, i));
61
       G[edge[i].t].push_back(Info(edge[i].s, i));
62
```

```
sort(edge, edge + E);
64
65
66
     number = 0;
     for (int i = 0; i < V; i++) {
67
68
       order[i] = -1;
       lowlink[i] = -1;
69
70
71
     for (int i = 0; i < E; i++) {
72
       visited[i] = false;
73
74
75
     recursive(0);
76
77
     int from, to;
     for (int i = 0; i < E; i++) {
78
79
       from = edge[i].s;
80
       to = edge[i].t;
       if (order[edge[i].s] > order[edge[i].t]) {
81
82
         swap(from, to);
83
84
       if (order[from] < lowlink[to]) {</pre>
85
         printf("%d %d\n", edge[i].s, edge[i].t);
86
87
    }
88
     return 0;
```

5 Flow & Matching

5.1 Relation

```
1 | 1. 一般圖
2 | |最大匹配| + |最小邊覆蓋| = |V|
3 | |最大獨立集| + |最小點覆蓋| = |V|
4 |最大圖| = |補圖的最大獨立集|
5 | 2. 二分圖
6 | |最大匹配| = |最小點覆蓋|
7 | |最大獨立集| = |艮小邊覆蓋|
8 | |最大獨立集| = |V| - |最大匹配|
9 | |最大圖| = |補圖的最大獨立集|
```

5.2 Bipartite Matching

```
1 // 0-base
  const int MAXN = ;
2
3 int n;
  vector<int> G[MAXN];
  int vy[MAXN], my[MAXN];
  bool match(int u) {
    for (int v : G[u]) {
       if (vy[v]) {
10
         continue;
11
       vy[v] = true;
12
13
       if (my[v] == -1 || match(my[v])) {
14
         my[v] = u;
15
         return true;
16
    }
17
18
    return false;
19 }
20 int sol() {
    int cnt = 0;
21
    memset(my, -1, sizeof(my));
22
     for (int i = 0; i < n; i++) {</pre>
23
24
       memset(vy, 0, sizeof(vy));
25
       if (match(i)) {
26
         cnt++;
```

```
28 }
29 return cnt;
30 }
70 }
71 return ans;
72 }
73 };
```

5.3 KM

```
1 const int INF = 1e9;
2 const int MAXN = ;
3 struct KM { //1-base
     int n, G[MAXN][MAXN];
     int lx[MAXN], ly[MAXN], my[MAXN];
6
     bool vx[MAXN], vy[MAXN];
     void init(int _n) {
7
       n = _n;
       for (int i = 1; i <= n; i++) {</pre>
9
10
          for (int j = 1; j <= n; j++) {</pre>
11
            G[i][j] = 0;
12
13
       }
     }
14
15
     bool match(int i) {
16
       vx[i] = true;
17
       for (int j = 1; j <= n; j++) {</pre>
18
          if (lx[i] + ly[j] == G[i][j] && !vy[j]) {
            vy[j] = true;
19
20
            if (!my[j] || match(my[j])) {
21
              my[j] = i;
              return true;
22
23
            }
         }
24
25
       }
26
       return false;
27
28
     void update() {
       int delta = INF;
29
       for (int i = 1; i <= n; i++) {</pre>
30
          if (vx[i]) {
31
            for (int j = 1; j <= n; j++) {
32
33
              if (!vy[j]) {
                delta = min(delta, lx[i] + ly[j] -
34
                     G[i][j]);
              }
35
            }
36
37
         }
38
39
       for (int i = 1; i <= n; i++) {
          if (vx[i]) {
40
41
            lx[i] -= delta;
42
43
          if (vy[i]) {
44
            ly[i] += delta;
45
46
       }
47
48
     int run() {
       for (int i = 1; i <= n; i++) {
49
          lx[i] = ly[i] = my[i] = 0;
50
51
          for (int j = 1; j <= n; j++) {</pre>
            lx[i] = max(lx[i], G[i][j]);
52
53
54
55
       for (int i = 1; i <= n; i++) {</pre>
56
          while (true) {
57
            for (int i = 1; i <= n; i++) {</pre>
58
              vx[i] = vy[i] = 0;
59
60
            if (match(i)) {
61
              break;
62
            } else {
63
              update();
64
65
         }
66
       }
       int ans = 0;
67
       for (int i = 1; i <= n; i++) {</pre>
68
          ans += lx[i] + ly[i];
69
```

5.4 Dinic

```
1 #define eb emplace_back
  const LL INF = 1e18;
  const int MAXN = ;
  struct Edge {
     int to;
    LL cap;
     int rev;
    Edge(int v, LL c, int r) : to(v), cap(c), rev(r) {}
 8
9
  };
10
  struct Dinic {
11
    int n:
12
     int level[MAXN], now[MAXN];
     vector<Edge> G[MAXN];
13
14
     void init(int _n) {
15
       n = _n;
16
       for (int i = 0; i <= n; i++) {</pre>
17
         G[i].clear();
18
19
     void add_edge(int u, int v, LL c) {
20
21
       G[u].eb(v, c, G[v].size());
22
       // directed graph
       G[v].eb(u, 0, G[u].size() - 1);
23
24
       // undirected graph
       // G[v].eb(u, c, G[u].size() - 1);
25
26
27
     bool bfs(int st, int ed) {
28
       fill(level, level + n + 1, -1);
29
       queue < int > q;
       q.push(st);
30
       level[st] = 0;
       while (!q.empty()) {
32
33
         int u = q.front();
34
         q.pop();
         for (const auto &e : G[u]) {
35
           if (e.cap > 0 && level[e.to] == -1) {
36
37
             level[e.to] = level[u] + 1;
             q.push(e.to);
38
39
           }
         }
40
41
       return level[ed] != -1;
42
43
     LL dfs(int u, int ed, LL limit) {
44
45
       if (u == ed) {
46
         return limit;
47
48
       LL ret = 0;
       for (int &i = now[u]; i < G[u].size(); i++) {</pre>
49
         auto &e = G[u][i];
50
51
         if (e.cap > 0 && level[e.to] == level[u] + 1) {
           LL f = dfs(e.to, ed, min(limit, e.cap));
52
53
           ret += f;
           limit -= f;
54
55
           e.cap -= f;
56
           G[e.to][e.rev].cap += f;
57
           if (!limit) {
58
             return ret;
           }
59
60
         }
       }
61
62
       if (!ret) {
63
         level[u] = -1;
64
65
       return ret;
66
67
     LL flow(int st, int ed) {
68
       LL ret = 0;
       while (bfs(st, ed)) {
```

```
70
         fill(now, now + n + 1, 0);
                                                                67
                                                                         }
71
         ret += dfs(st, ed, INF);
                                                                68
72
                                                                69
                                                                       }
73
       return ret;
                                                                70
74
                                                                71
                                                                       return dis[ed] != INF;
75 };
                                                                72
                                                                73
                                                                     LL sendFlow(int v, LL curFlow) {
                                                                74
                                                                       if (pre[v] == -1) {
                                                                75
                                                                         return curFlow;
  5.5 MCMF
                                                                76
                                                                77
                                                                       int i = pre[v];
1 // 0-base
                                                                       int u = edges[i].u;
                                                                78
2 const LL INF = 1e18;
                                                                79
                                                                       LL cost = edges[i].cost;
3 const int MAXN = ;
                                                                80
4 struct Edge {
                                                                81
                                                                       LL f = sendFlow(u, min(curFlow, edges[i].cap));
    int u, v;
                                                                82
6
    LL cost;
                                                                83
                                                                       ans_cost += f * cost;
7
     LL cap;
                                                                84
                                                                       edges[i].cap -= f;
8
     Edge(int _u, int _v, LL _c, LL _cap) : u(_u),
                                                                85
                                                                       edges[i ^ 1].cap += f;
         v(_v), cost(_c), cap(_cap) {}
                                                                86
                                                                       return f;
9 };
                                                                87
10 struct MCMF {
                      // ing times
                                                                88
                                                                     pair<LL, LL> run(int st, int ed) {
    int n, pre[MAXN], cnt[MAXN];
11
                                                                89
                                                                       ans_flow = ans_cost = 0;
12
     LL ans_flow, ans_cost, dis[MAXN];
                                                                       while (SPFA(st, ed)) {
                                                                90
     bool inq[MAXN];
13
                                                                91
                                                                         ans_flow += sendFlow(ed, INF);
     vector<int> G[MAXN];
14
                                                                92
     vector<Edge> edges;
15
                                                                93
                                                                       return make_pair(ans_flow, ans_cost);
16
     void init(int _n) {
                                                                     }
                                                                94
17
       n = _n;
                                                                95 };
       edges.clear();
18
19
       for (int i = 0; i < n; i++) {
20
         G[i].clear();
                                                                        Stable Matching
21
22
23
     void add_edge(int u, int v, LL c, LL cap) {
                                                                 1 int t, n, b[N][N], bi[N], g[N][N], bg[N], gb[N];
24
       // directed
                                                                 2
                                                                   void sol() {
       G[u].pb(edges.size());
                                                                 3
25
26
       edges.eb(u, v, c, cap);
                                                                     deque<int> dq;
       G[v].pb(edges.size());
                                                                     memset(gb, 0, sizeof(gb));
27
28
       edges.eb(v, u, -c, 0);
                                                                     memset(bi, 0, sizeof(bi));
                                                                     for (int i = 1; i <= n; i++) dq.push_back(i);</pre>
29
                                                                 7
     bool SPFA(int st, int ed) {
                                                                     while (!dq.empty()) {
30
                                                                 8
                                                                       int x = dq.front();
31
       for (int i = 0; i < n; i++) {
                                                                 9
         pre[i] = -1;
                                                                10
                                                                       dq.pop_front();
32
         dis[i] = INF;
                                                                11
                                                                       int y = b[x][++bi[x]];
33
34
         cnt[i] = 0;
                                                                12
                                                                       if (!gb[y]) {
35
         inq[i] = false;
                                                                13
                                                                         gb[y] = x;
36
                                                                14
                                                                         bg[x] = y;
                                                                       } else if (g[y][x] < g[y][gb[y]]) {</pre>
37
       queue < int > a:
                                                                15
38
       bool negcycle = false;
                                                                16
                                                                         dq.push_back(gb[y]);
39
                                                                17
                                                                         gb[y] = x;
40
       dis[st] = 0;
                                                                18
                                                                         bg[x] = y;
41
       cnt[st] = 1;
                                                                19
                                                                       } else {
       inq[st] = true;
                                                                20
42
                                                                         dq.push_back(x);
43
       q.push(st);
                                                                21
                                                                22
44
45
       while (!q.empty() && !negcycle) {
                                                                23
                                                                     for (int i = 1; i <= n; i++) {
                                                                       cout << bg[i] << '\n';
46
         int u = q.front();
                                                                24
                                                                     }
47
         q.pop();
                                                                25
48
         inq[u] = false;
                                                                26 }
49
         for (int i : G[u]) {
                                                                27
50
                                                                28
                                                                   int main() {
           int v = edges[i].v;
51
           LL cost = edges[i].cost;
                                                                29
                                                                     int x;
52
           LL cap = edges[i].cap;
                                                                30
                                                                     cin >> t;
53
                                                                31
                                                                     for (int i = 0; i < t; i++) {
           if (dis[v] > dis[u] + cost && cap > 0) {
                                                                32
                                                                       cin >> n;
54
55
             dis[v] = dis[u] + cost;
                                                                33
                                                                       for (int i = 1; i <= n; i++) {
             pre[v] = i;
                                                                         for (int j = 1; j <= n; j++) {</pre>
56
                                                                34
57
             if (!inq[v]) {
                                                                35
                                                                            cin >> b[i][j];
                                                                         }
58
                q.push(v);
                                                                36
59
                cnt[v]++;
                                                                37
60
                inq[v] = true;
                                                                38
                                                                       for (int i = 1; i <= n; i++) {
                                                                         for (int j = 1; j <= n; j++) {</pre>
                                                                39
61
                                                                            cin >> x;
                if (cnt[v] == n + 2) {
                                                                40
62
63
                  negcycle = true;
                                                                41
                                                                            g[i][x] = j;
                  break;
                                                                42
64
65
                }
                                                                43
             }
                                                                       if (i) cout << '\n';
66
```

```
45
       sol();
                                                                67
                                                                      int res = 0;
   }
                                                                      for (int x = 0; x < n; ++x) {
46
                                                                68
47 }
                                                                69
                                                                        if (match[x] == n) res += Bfs(x, n);
                                                                70
                                                                     }
                                                                71
                                                                     return res;
                                                                72 }
```

5.7 Max General Graph Matching

```
1 #define maxn
2
  int fa[maxn], pre[maxn], match[maxn], s[maxn],
       v[maxn];
4 vector<int> g[maxn];
  queue<int> q;
6 void Init(int n) {
    for (int i = 0; i <= n; ++i) match[i] = pre[i] = n;</pre>
8
    for (int i = 0; i < n; ++i) g[i].clear();</pre>
9 }
10 void AddEdge(int u, int v) {
    g[u].push_back(v);
11
12
     g[v].push_back(u);
13 }
14 int Find(int u) { return u == fa[u] ? u : fa[u] =
       Find(fa[u]); }
15 int LCA(int x, int y, int n) {
    static int tk = 0;
17
     tk++;
18
     x = Find(x), y = Find(y);
19
     for (;; swap(x, y)) {
       if (x != n) {
20
21
         if (v[x] == tk) return x;
22
         v[x] = tk;
23
         x = Find(pre[match[x]]);
24
25
    }
26 }
27
   void Blossom(int x, int y, int 1) {
28
     while (Find(x) != 1) {
29
       pre[x] = y, y = match[x];
30
       if (s[y] == 1) q.push(y), s[y] = 0;
31
       if (fa[x] == x) fa[x] = 1;
32
33
       if (fa[y] == y) fa[y] = 1;
34
       x = pre[y];
35
36 }
37
38 bool Bfs(int r, int n) {
    for (int i = 0; i \le n; ++i) fa[i] = i, s[i] = -1;
39
40
     while (!q.empty()) q.pop();
41
     q.push(r);
42
     s[r] = 0;
     while (!q.empty()) {
43
       int x = q.front();
44
       q.pop();
45
46
       for (int u : g[x]) {
47
         if (s[u] == -1) {
48
           pre[u] = x, s[u] = 1;
           if (match[u] == n) {
49
50
             for (int a = u, b = x, last; b != n; a =
                  last, b = pre[a])
51
                last = match[b], match[b] = a, match[a] =
                   b;
52
             return true;
53
           }
54
           q.push(match[u]);
55
           s[match[u]] = 0;
         } else if (!s[u] && Find(u) != Find(x)) {
56
57
           int 1 = LCA(u, x, n);
58
           Blossom(x, u, 1);
           Blossom(u, x, 1);
59
60
       }
61
62
     }
63
     return false;
64 }
65
66 int Solve(int n) {
```

5 String

6.1 Manacher

```
1 int p[2 * MAXN];
 2
  int Manacher(const string &s) {
     string st = "@#";
     for (char c : s) {
       st += c;
6
       st += '#';
 7
     st += '$';
 8
     int id = 0, mx = 0, ans = 0;
10
     for (int i = 1; i < st.length() - 1; i++) {</pre>
       p[i] = (mx > i ? min(p[2 * id - i], mx - i) : 1);
11
12
       for (; st[i - p[i]] == st[i + p[i]]; p[i]++);
       if (mx < i + p[i]) {</pre>
13
         mx = i + p[i];
14
15
         id = i;
16
17
       ans = max(ans, p[i] - 1);
    }
18
19
     return ans;
20 }
```

6.2 Trie

```
1 const int MAXL = ;
  const int MAXC = ;
  struct Trie {
    int nex[MAXL][MAXC];
     int len[MAXL];
6
     int sz;
7
     void init() {
8
       memset(nex, 0, sizeof(nex));
       memset(len, 0, sizeof(len));
9
10
     }
11
12
     void insert(const string &str) {
13
       int p = 0;
       for (char c : str) {
14
15
         int id = c - 'a';
         if (!nex[p][id]) {
16
17
           nex[p][id] = ++sz;
18
         }
19
         p = nex[p][id];
20
21
       len[p] = str.length();
     vector<int> find(const string &str, int i) {
23
24
       int p = 0;
25
       vector<int> ans;
26
       for (; i < str.length(); i++) {</pre>
27
         int id = str[i] - 'a';
         if (!nex[p][id]) {
28
29
           return ans;
30
31
         p = nex[p][id];
32
         if (len[p]) {
33
           ans.pb(len[p]);
34
       }
35
36
       return ans;
37
    }
38 };
```

6.3 Z-value

```
1 // 0-base
2 // 對於個長度為 n 的字串 s
3 // 定義函數 z[i] 表示 s 和 s[i, n - 1]
4 // (即以 s[i] 開頭的後綴)的最長公共前綴 (LCP)的長度
5 | // z[0] = 0 \circ
6 vector<int> z_function(string s) {
    int n = (int)s.length();
7
    vector<int> z(n):
    for (int i = 1, l = 0, r = 0; i < n; ++i) {
10
      if (i <= r && z[i - 1] < r - i + 1) {</pre>
11
        z[i] = z[i - 1];
12
      } else {
        z[i] = max(0, r - i + 1);
13
14
        while (i + z[i] < n \&\& s[z[i]] == s[i + z[i]])
            ++z[i];
15
      if (i + z[i] - 1 > r) l = i, r = i + z[i] - 1;
16
17
    }
18
    return z;
19 }
```

7 DP

7.1 LIS

```
1 int LIS(vector<int> &a) {
2
    vector<int> s;
3
    for (int i = 0; i < a.size(); i++) {</pre>
       if (s.empty() || s.back() < a[i]) {</pre>
         s.push_back(a[i]);
6
      } else {
         *lower_bound(s.begin(), s.end(), a[i],
8
           [](int x, int y) {return x < y;}) = a[i];
10
    }
11
    return s.size();
12 }
```

7.2 LCS

```
1 int LCS(string s1, string s2) {
2
    int n1 = s1.size(), n2 = s2.size();
    vector<vector<int>> dp(n1 + 1, vector<int>(n2 + 1,
3
         0));
    for (int i = 1; i <= n1; i++) {
      for (int j = 1; j \le n2; j++) {
         if (s1[i - 1] == s2[j - 1]) {
6
           dp[i][j] = dp[i - 1][j - 1] + 1;
         } else {
9
           dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]);
10
      }
11
    }
12
13
    return dp[n1][n2];
14 }
```

7.3 Huge Knapsack

```
10
  #define SIZE 25
11
12
13
  struct Info {
14
     Info() { value = 0, weight = 0; }
     Info(ll arg_value, ll arg_weight) {
15
       value = arg_value;
16
17
       weight = arg_weight;
18
19
     bool operator<(const struct Info &arg) const {</pre>
          return weight < arg.weight; }</pre>
20
21
     11 value, weight;
22 };
23
24
  11 N, W;
25 11 POW[SIZE];
26 | 11 table_B[1 << 21];
  Info info[45];
27
  int main() {
29
     POW[0] = 1;
30
     for (int i = 1; i < SIZE; i++) {</pre>
31
32
       POW[i] = POW[i - 1] * 2;
33
34
     scanf("%11d %11d", &N, &W);
35
36
37
     for (int i = 0; i < N; i++) {</pre>
38
       scanf("%11d %11d", &info[i].value,
            &info[i].weight);
39
     }
40
41
     if (N == 1) {
42
       if (info[0].weight <= W) {</pre>
43
         printf("%11d\n", info[0].value);
44
       } else {
         printf("\emptyset \setminus n");
45
46
47
48
       return 0;
49
     }
50
51
     vector<int> A, B;
     for (int i = 0; i < N / 2; i++) {
52
53
       A.push_back(i);
54
55
     for (int i = N / 2; i < N; i++) {
56
       B.push_back(i);
57
58
59
     vector<Info> vec_A, vec_B;
60
     for (int state = 0; state < POW[A.size()]; state++)</pre>
       11 \text{ sum\_w} = 0;
61
       11 sum_value = 0;
62
       for (int loop = 0; loop < A.size(); loop++) {</pre>
63
64
         if (state & POW[loop]) {
65
            sum_w += info[A[loop]].weight;
            sum_value += info[A[loop]].value;
66
67
         }
       }
68
       vec_A.push_back(Info(sum_value, sum_w));
69
70
71
     sort(vec_A.begin(), vec_A.end());
72
73
     for (int state = 0; state < POW[B.size()]; state++)</pre>
74
       11 \text{ sum\_w} = 0;
75
       11 sum_value = 0;
76
       for (int loop = 0; loop < B.size(); loop++) {</pre>
77
         if (state & POW[loop]) {
            sum_w += info[B[loop]].weight;
78
79
            sum_value += info[B[loop]].value;
80
81
       vec_B.push_back(Info(sum_value, sum_w));
82
```

```
83
     }
     sort(vec_B.begin(), vec_B.end());
84
85
     table_B[0] = vec_B[0].value;
86
     for (int i = 1; i < vec_B.size(); i++) {</pre>
87
       //ある重さ以下の最大価値を求める
88
        table_B[i] = max(table_B[i - 1], vec_B[i].value);
89
90
91
     int tail = vec_B.size() - 1;
92
93
     11 \text{ ans} = 0;
     for (int i = 0; i < vec_A.size(); i++) {</pre>
94
       while (tail >= 0 && vec_A[i].weight +
95
            vec_B[tail].weight > W) tail--;
       if (tail < 0) break;</pre>
96
97
       ans = max(ans, vec_A[i].value + table_B[tail]);
98
99
100
101
     printf("%11d\n", ans);
102
     return 0;
103 }
```

7.4 Coin Change

```
1 // from aizu
2 int main() {
    int n, m, min, tmp;
3
     scanf("%d", &n);
    int minimum[n + 1];
     scanf("%d", &m);
6
7
     int coin[m];
     for (int i = 0; i < m; i++) scanf("%d", &coin[i]);</pre>
8
10
     minimum[0] = 0;
11
     minimum[1] = 1;
     for (int i = 2; i <= n; i++) {</pre>
12
       min = n + 1;
13
14
       for (int k = 0; k < m; k++) {
         if (coin[k] <= i) {</pre>
15
16
           tmp = 1 + minimum[i - coin[k]];
           min = (min <= tmp) ? min : tmp;
17
18
       }
19
       minimum[i] = min;
20
21
22
23
     printf("%d\n", minimum[n]);
24
25
     return 0:
26 }
```

7.5 Edit Distance

```
1 // from aizu
2 typedef long long int 11;
3 typedef unsigned long long int ull;
4 #define BIG_NUM 2000000000
5 #define MOD 1000000007
6 #define EPS 0.000000001
8
  int main() {
    char A[1001], B[1001];
9
    int len_A, len_B;
    scanf("%s %s", A, B);
11
12
    for (len_A = 0; A[len_A] != '\0'; len_A++);
13
    for (len_B = 0; B[len_B] != '\0'; len_B++);
14
15
    int** dp = new int*[len_B + 1];
16
17
     for (int row = 0; row <= len_B; row++) {</pre>
18
       dp[row] = new int[len_A + 1];
19
```

```
20
     }
21
22
     for (int col = 0; col <= len_A; col++) {</pre>
       dp[0][col] = col;
23
24
25
     for (int row = 1; row <= len_B; row++) {</pre>
26
27
       dp[row][0] = row;
28
29
30
     int cost;
31
32
     for (int row = 1; row <= len_B; row++) {</pre>
       for (int col = 1; col <= len_A; col++) {</pre>
33
         if (A[col - 1] == B[row - 1]) {
34
           cost = 0;
35
36
         } else {
37
           cost = 1;
38
39
         dp[row][col] = min(dp[row - 1][col - 1] + cost,
           min(dp[row - 1][col] + 1, dp[row][col - 1] +
40
41
       }
    }
42
43
44
     printf("%d\n", dp[len_B][len_A]);
```

Math

8.1 Number Theory

```
aa^{-1} \equiv 1 \pmod{m}. a^{-1} exists iff gcd(a, m) = 1.
· Linear inversion:
   a^{-1} \equiv (m - \lfloor \frac{m}{a} \rfloor) \times (m \bmod a)^{-1} \pmod m
· Fermat's little theorem:
   a^p \equiv a \pmod{p} if p is prime.
• Euler function:
   \phi(n) = n \prod_{p|n} \frac{p-1}{p}
• Euler theorem:
   a^{\phi(n)} \equiv 1 \pmod{n} \text{ if } \gcd(a,n) = 1.
• Extended Euclidean algorithm:
   ax + by = \gcd(a, b) = \gcd(b, a \mod b) = \gcd(b, a - \lfloor \frac{a}{b} \rfloor b) = bx_1 + (a - \lfloor \frac{a}{b} \rfloor b)
   \lfloor \frac{a}{b} \rfloor b) y_1 = ay_1 + b(x_1 - \lfloor \frac{a}{b} \rfloor y_1)
· Divisor function:
   \sigma_x(n) = \sum_{d \mid n} d^x . n = \prod_{i=1}^r p_i^{a_i} .
   \sigma_x(n) = \prod_{i=1}^r \frac{p_i^{(a_i+1)x}_{-1}}{p_i^x - 1} \text{ if } x \neq 0. \ \sigma_0(n) = \prod_{i=1}^r (a_i + 1).
· Chinese remainder theorem:
   x \equiv a_i \pmod{m_i}.
   M = \prod m_i. M_i = M/m_i. t_i = M_i^{-1}.
   x = kM + \sum a_i t_i M_i, k \in \mathbb{Z}.
```

8.2 Extended GCD

```
1 // ax + by = c
  int extgcd(int a, int b, int c, int &x, int &y) {
    if (b == 0) {
      x = c / a;
5
      y = 0;
6
      return a;
7
    }
    int d = extgcd(b, a % b, c, y, x);
    y -= (a / b) * x;
9
10
    return d;
11 }
```

8.3 Gaussian Elimination + det

```
1 const double EPS = 1e-6;
2 double Gauss(vector<vector<double>> &d) {
     int n = d.size(), m = d[0].size();
3
4
     double det = 1;
     for (int i = 0; i < m; i++) {</pre>
       int p = -1;
       for (int j = i; j < n; j++) {</pre>
7
8
         if (fabs(d[j][i]) < EPS) {</pre>
9
           continue;
10
         if (p == -1 || fabs(d[j][i]) > fabs(d[p][i])) {
11
12
13
       }
14
       if (p == -1) {
15
         continue;
16
17
       if (p != i) {
18
19
         det *= -1;
20
21
       for (int j = 0; j < m; j++) {
         swap(d[p][j], d[i][j]);
22
23
24
       for (int j = 0; j < n; j++) {</pre>
25
         if (i == j) {
26
           continue;
27
28
         double z = d[j][i] / d[i][i];
         for (int k = 0; k < m; k++) {
29
           d[j][k] -= z * d[i][k];
30
31
       }
32
33
     for (int i = 0; i < n; i++) {
34
       det *= d[i][i];
35
    }
36
37
     return det;
38 }
39 // new
40 const int MAXN = 300;
41 const double EPS = 1e-8;
42 int n;
43 double A[MAXN][MAXN];
44 void Gauss() {
     for (int i = 0; i < n; i++) {
45
       bool ok = 0;
46
       for (int j = i; j < n; j++) {
47
48
         if (fabs(A[j][i]) > EPS) {
49
           swap(A[j], A[i]);
50
           ok = 1;
           break;
51
52
         }
53
54
       if (!ok) continue;
55
       double fs = A[i][i];
56
       for (int j = i + 1; j < n; j++) {
57
         double r = A[j][i] / fs;
         for (int k = i; k < n; k++) {
58
           A[j][k] -= A[i][k] * r;
59
60
61
       }
62
    }
63 }
```

8.4 Prime Table

```
1 vector < int > p;
2 bitset < MAXN > is_notp;
3 void PrimeTable(int n) {
4    is_notp.reset();
5    is_notp[0] = is_notp[1] = 1;
6    for (int i = 2; i <= n; ++i) {
7     if (!is_notp[i]) {</pre>
```

```
8
         p.push_back(i);
9
10
       for (int j = 0; j < (int)p.size(); ++j) {</pre>
11
         if (i * p[j] > n) {
12
           break;
13
         is_notp[i * p[j]] = 1;
14
15
         if (i % p[j] == 0) {
16
           break;
17
18
19
    }
20 }
```

8.5 Phi

```
・ 歐拉函數計算對於一個整數 N,小於等於 N 的正整數中,有幾個和 N 互質
```

```
・ 如果 gcd(p,q) = 1, \Phi(p) \cdot \Phi(q) = \Phi(p \cdot q)
```

```
• \Phi(p^k) = p^{k-1} \times (p-1)
```

```
1 void phi_table(int n) {
    phi[1] = 1;
    for (int i = 2; i <= n; i++) {
3
      if (phi[i]) {
5
         continue;
6
7
      for (int j = i; j < n; j += i) {
         if (!phi[j]) {
8
9
          phi[j] = j;
10
11
         phi[j] = phi[j] / i * (i - 1);
12
13
    }
14
```

8.6 Chinese Remainder Thm

```
1 / / 参数可为负数的扩展欧几里德定理
2 void exOJLD(int a, int b, int& x, int& y) {
3
    //根据欧几里德定理
    if (b == 0) { //任意数与0的最大公约数为其本身。
5
      x = 1;
      y = 0;
6
7
    } else {
8
      int x1, y1;
9
      exOJLD(b, a % b, x1, y1);
10
      if (a * b < 0) { //异号取反
11
        x = -y1;
12
        y = a / b * y1 - x1;
      } else { //同号
13
        x = y1;
14
        y = x1 - a / b * y1;
15
16
17
    }
18 }
19
  //剩余定理
  int calSYDL(int a[], int m[], int k) {
20
    int N[k];
               //这个可以刪除
21
    int mm = 1; //最小公倍数
22
    int result = 0;
23
    for (int i = 0; i < k; i++) {
25
     mm *= m[i];
26
27
    for (int j = 0; j < k; j++) {
     int L, J;
28
      exOJLD(mm / m[j], -m[j], L, J);
29
      N[j] = m[j] * J + 1; // 1
30
31
      N[j] = mm / m[j] * L;
          1和2这两个值应该是相等的。
32
      result += N[j] * a[j];
    }
33
```

```
return (result % mm + mm) % mm;
   //落在(0, mm)之间,这么写是为了防止result初始为负数
35
   //本例中不可能为负可以直接
36
   //写成:return result%mm;即可。
37
38 }
39
40 int main() {
   int a[3] = {2, 3, 6}; // a[i]=n%m[i]
41
   int m[3] = \{3, 5, 7\};
42
   cout << calSYDL(a, m, 3) << endl;</pre>
43
   //輸出為滿足兩條陣列的最小n,第3參數為陣列長度
44
45
   //所有滿足答案的數字集合為n+gcd(m0,m1,m2...)*k,
       k為 正數
46
    return 0;
47 | }
```

8.7 Josephus

```
1 int josephus(int n, int k) { // 有 n個人圍成一圈,每 k個一次 2 return n > 1 ? (josephus(n - 1, k) + k) % n : 0; 3 } // 回傳最後一人的編號, 0 index
```

8.8 Catalan

$$C_0 = 1$$
 and $C_{n+1} = \frac{2(2n+1)}{n+2}C_n$

```
1 long long f[N] = {1}, i, t, p;
2 int main() {
3
    for (int i = 1; i <= 100; i++) {
       f[i] = f[i - 1] * (4 * i - 2) % mod;
4
       for (t = i + 1, p = mod - 2; p; t = (t * t) %
5
           mod, p >>= 1LL) {
         if (p & 1) {
6
7
           f[i] *= t;
8
           f[i] %= mod;
9
10
      }
11
    }
12 }
```

8.9 Matrix Multiplication

```
1 struct Matrix {
2
    int row, col;
    vector<vector<int>> v;
    Matrix() : row(0), col(0) {}
    Matrix(int r, int c) : row(r), col(c) {
6
      v = vector<vector<int>>(r, vector<int>(c, 0));
    }
7
8 };
9 Matrix operator * (Matrix &a, Matrix &b) {
    assert(a.col == b.row);
10
    Matrix ret(a.row, b.col);
11
    for (int i = 0; i < a.row; i++) {</pre>
12
      for (int j = 0; j < b.col; j++) {</pre>
13
14
         for (int k = 0; k < a.col; k++) {</pre>
15
          ret.v[i][j] += a.v[i][k] * b.v[k][j];
16
      }
17
18
    }
19
    return ret;
20 }
21 Matrix mPow(Matrix a, int n) {
    assert(a.row == a.col);
22
    Matrix ret(a.row, a.col);
23
24
    ret.v[0][0] = ret.v[1][1] = 1;
25
    while (n > 0) {
      if (n & 1) {
26
        ret = ret * a;
27
```

8.10 Fibonacci

```
 \begin{bmatrix} f(n) \\ f(n-1) \end{bmatrix} = \begin{bmatrix} 1 & 1 \\ 1 & 0 \end{bmatrix}^{(n-1)} 
                                       O(logn)
 1|LL fib(int n) {
      if (n <= 1) {
3
         return n;
 5
      Matrix a(2, 2), b(2, 1);
      a.v[0][0] = a.v[0][1] = a.v[1][0] = 1;
 6
      b.v[0][0] = 1;
      auto t = mPow(a, n - 1);
 8
      t = t * b;
      return t.v[0][0];
10
11 }
```

f(n) = f(n-1) + f(n-2)

9 Geometry

9.1 Point

```
1 // notice point type!!!
  using dvt = int;
  const double EPS = 1e-6;
  const double PI = acos(-1);
  struct Pt {
   dvt x;
7
8
    dvt y;
9 };
10 bool operator < (const Pt &a, const Pt &b) {
  return a.x == b.x ? a.y < b.y : a.x < b.x;
12 }
13
  bool operator == (const Pt &a, const Pt &b) {
  return a.x == b.x && a.y == b.y;
14
15 }
16 Pt operator + (const Pt &a, const Pt &b) {
   return {a.x + b.x, a.y + b.y};
17
18 }
19 Pt operator - (const Pt &a, const Pt &b) {
20
   return {a.x - b.x, a.y - b.y};
21 }
22
  // multiply constant
23 Pt operator * (const Pt &a, const dvt c) {
  return {a.x * c, a.y * c};
24
25 }
26 Pt operator / (const Pt &a, const dvt c) {
27
   return {a.x / c, a.y / c};
28 }
29 // |a| \times |b| \times cos(x)
30 dvt iproduct(const Pt &a, const Pt &b) {
31
  return a.x * b.x + a.y * b.y;
32 }
  // |a| x |b| x sin(x)
33
34 dvt cross(const Pt &a, const Pt &b) {
35
  return a.x * b.y - a.y * b.x;
36 }
37 dvt dis_pp(const Pt &a, const Pt, &b) {
  dvt dx = a.x - b.x;
38
  dvt dy = a.y - b.y;
39
40
   return sqrt(dx * dx, dy * dy);
41 }
```

9.2 Line

```
d(P,L) = \frac{|ax_0 + by_0 + c|}{-}
                                 \sqrt{a^2+b^2}
1 struct Line {
2
    Pt st;
     Pt ed;
3
4 };
5 // return point side
6 // left, on line, right -> 1, 0, -1
7 int side(Line 1, Pt a) {
     dvt cross_val = cross(a - 1.st, 1.ed - 1.st);
9
     if (cross_val > EPS) {
      return 1;
10
     } else if (cross_val < -EPS) {</pre>
11
12
       return -1;
13
     } else {
14
       return 0;
15
16 }
17 // AB infinity, CD segment
18 bool has_intersection(Line AB, Line CD) {
19
    int c = side(AB, CD.st);
     int d = side(AB, CD.ed);
20
21
     if (c == 0 || d == 0) {
22
       return true;
23
     } else {
       // different side
24
25
       return c == -d;
26
     }
27 }
28 // find intersection point, two line, not seg
29 pair<int, Pt> intersection(Line a, Line b) {
     Pt A = a.ed - a.st;
30
31
     Pt B = b.ed - b.st;
     Pt C = b.st - a.st;
32
     dvt mom = cross(A, B);
33
     dvt son = cross(C, B);
34
     if (std::abs(mom) <= EPS) {</pre>
35
      if (std::abs(son) <= EPS) {</pre>
36
37
         return {1, {}}; // same line
38
       } else {
         return {2, {}}; // parallel
39
       }
40
41
     } else {
                          // ok
42
       return {0, a.st + A * (son / mom)};
43
44 }
45 // line to point distance
46 dvt dis_lp(Line 1, Pt a) {
    return area3x2(1.st, l.ed, a) / dis_pp(l.st, l.ed);
48 }
```

9.3 Area

```
1 // triangle
2 dvt area3(Pt a, Pt b, Pt c) {
    return std::abs(cross(b - a, c - a) / 2);
3
4 }
5 dvt area3x2(Pt a, Pt b, Pt c) { // for integer
6
    return std::abs(cross(b - a, c - a));
7
  }
8 // simple convex area(can in)
9 dvt area(vector <Pt> &a) {
    dvt ret = 0;
    for (int i = 0, sz = a.size(); i < sz; i++) {</pre>
11
12
      ret += cross(a[i], a[(i + 1) % sz]);
   }
13
    return std::abs(ret) / 2;
14
15 }
16 // check point in/out a convex
17 int io_convex(vector<Pt> convex, Pt q) {
18
    // convex is Counterclockwise
   for (int i = 0, sz = convex.size(); i < sz; i++) {</pre>
```

```
20
       Pt cur = convex[i] - q;
       Pt nex = convex[(i + 1) % sz] - q;
21
       dvt cross_val = cross(cur, nex);
22
       if (std::abs(cross_val) <= EPS) {</pre>
23
         return 0; // on edge
24
25
       if (cross_val < 0) {</pre>
26
27
         return -1; // outside
28
    }
29
30
     return 1;
                     // inside
31 }
```

9.4 Convex Hull

```
1 | vector <Pt> convex_hull(vector <Pt> &a) {
    sort(a.begin(), a.end());
    a.erase(unique(a.begin(), a.end());
3
    int sz = a.size(), m = 0;
    vector<Pt> ret(sz + 5); // safe 1 up
5
    for (int i = 0; i < sz; i++) {</pre>
6
7
       while (m > 1 &&
         cross(ret[m - 1] - ret[m - 2], a[i] - ret[m -
8
             2]) <= EPS) {
9
      }
10
11
      ret[m++] = a[i];
12
13
     int k = m;
     for (int i = sz - 2; i >= 0; i--) {
14
       while (m > k &&
15
16
         cross(ret[m - 1] - ret[m - 2], a[i] - ret[m -
            2]) <= EPS) {
17
18
      }
19
      ret[m++] = a[i];
    }
20
21
    if (sz > 1) {
22
      m - -;
23
24
     ret.resize(m);
25
     return ret;
```