#### Contents int main() { 12 13 1 14 } 1 Basic 1.1 Run . 1.3 Black Magic 1 #include <bits/stdc++.h> 2 Data Structure 2 #include <ext/pb\_ds/assoc\_container.hpp> 2.1 Disjoint Set #include <ext/pb\_ds/tree\_policy.hpp> 2.3 zkw RMO . . . #include <ext/pb\_ds/priority\_queue.hpp> using namespace std; 6 using namespace \_\_gnu\_pbds; 3 Graph 7 using set\_t = tree<int, null\_type, less<int>, rb\_tree\_tag, 8 9 tree\_order\_statistics\_node\_update>; 10 using map\_t = 4 11 tree<int, int, less<int>, rb\_tree\_tag, tree\_order\_statistics\_node\_update>; 12 3.7 Kosaraju SCC . using heap\_t = \_\_gnu\_pbds::priority\_queue<<mark>int</mark>>; 14 using ht\_t = 6 4 Flow & Matching 16 gp\_hash\_table<int, int>; 4.1 Relation 6 17 6 int main() { //set-----7 18 19 set t st: 8 st.insert(5); st.insert(6); 21 st.insert(3); st.insert(1); 5 String 23 // the smallest is (0), biggest is (n-1), kth small is (k-1) int num = \*st.find\_by\_order(0); 9 cout << num << '\n'; // print 1 25 27 num = \*st.find\_by\_order(st.size() - 1); 7 Math cout << num << '\n'; // print 6 28 29 7.2 Extended GCD 9 // find the index 30 7.3 Gaussian Elimination + det . . . . . . . . . . . . . . . . . . 9 10 31 int index = st.order\_of\_key(6); 7.5 Phi . . . . cout << index << '\n'; // print 3</pre> 32 33 // check if there exists x int x = 5;35 int check = st.erase(x); if (check == 0) printf("st not contain $5\n"$ ); 37 else if (check == 1) printf("st contain 5\n"); 39 40 //tree policy like set 41 st.insert(5); st.insert(5); cout << st.size() << '\n'; // print 4</pre> 42 43 //map-----44 Basic 45 map t mp: 46 mp[1] = 2;47 cout << mp[1] << '\n';</pre> 1.1 Run auto tmp = \*mp.find\_by\_order(0); // pair 48 cout << tmp.first << " " << tmp.second << $' \setminus n'$ ; 49 1 | #use -> sh run.sh {name} 50 2 g++ -02 -std=c++14 -Wall -Wextra -Wshadow -o \$1 \$1.cpp //heap------51 3 | ./\$1 < t.in > t.outheap\_t h1, h2; 52 53 h1.push(1); h1.push(3); h2.push(2); h2.push(4); 54 55 h1.join(h2); 1.2 Default cout << h1.size() << h2.size() << h1.top() << '\n';</pre> 56 57 1 #include <bits/stdc++.h> 58 //hash-table-----59 2 using namespace std; 3 using LL = long long; ht t ht: ht[85] = 5;4 #define IOS ios\_base::sync\_with\_stdio(0); cin.tie(0); 61 5 #define pb push\_back 62 ht[89975] = 234;6 #define eb emplace\_back 63 for (auto i : ht) { cout << i.first << " " << i.second << '\n';</pre> 7 const int INF = 1e9; 64 65 } 8 const int MOD = 1e9 + 7; 9 const double EPS = 1e-6; 66 }

10 const int MAXN = 0;

#### 1.4 Python

```
1 ### EOF
2 while True:
3
    try:
      pass
    except EOFError:
6
      break
7 ###math
8 import math
10 math.ceil(x)#上高斯
11 math.floor(x)#下高斯
12 math.factorial(x)#接乘
13 math.fabs(x)#絕對值
14 math.fsum(arr)#跟sum - 樣但更精確(小數點問題)
15 math.gcd(x, y)#bj4
16 math.exp(x)#e^x
17 math.log(x, base)
18 math.log2(x)#2為底
19 math.log10(x)#10為底
20 math.sqrt(x)
21 | math.pow(x, y, mod)#精確些(float型態) MOD!!!
22 math.sin(x)# cos tan asin acos atan atan2(弧度) sinh
      cosh tanh acosh asinh atanh
23 | math.hypot(x, y)#歐幾里德範數
24 | math.degrees(x)#x從弧度轉角度
25 | math.radians(x)#x從角度轉弧度
26 math.gamma(x)#x的gamma函數
27 | math.pi#常數
28 math.e#常數
29 math.inf
31 ### ascii
32 ord(x)#char to asc
33 chr(x)#asc to char
34
35 x.encode().hex()#string to hex
36 ### reverse string
37 string = "abc"
```

#### 1.5 Binary Search

38 string\_reverse = string[::-1]

```
      1 | lower_bound(a, a + n, k);
      //最左邊 ≥ k 的位置

      2 | upper_bound(a, a + n, k);
      //最左邊 > k 的位置

      3 | upper_bound(a, a + n, k) - 1;
      //最右邊 ≤ k 的位置

      4 | lower_bound(a, a + n, k) - 1;
      //最右邊 < k 的位置</td>

      5 | [lower_bound, upper_bound)
      //等於 k 的範圍

      6 | equal_range(a, a + n, k);
```

#### 1.6 Ternary Search

```
1 const double EPS = 1e-6;
2 // target function
3 double f(double x) { return x * x; }
4 double ternarySearch() {
    double L = -1e5, R = 1e5;
    while (R - L > EPS) {
       double mr = (L + R) / 2.0;
7
       double ml = (L + mr) / 2.0;
      if (f(ml) < f(mr)) {</pre>
9
10
        R = mr;
11
      } else {
         L = ml;
12
      }
13
    }
14
15
    return L;
16 }
```

### 2 Data Structure

#### 2.1 Disjoint Set

```
1 // 0-base
  const int MAXN = 1000;
  int boss[MAXN];
  void init(int n) {
    for (int i = 0; i < n; i++) {
      boss[i] = -1;
6
7
    }
8 }
  int find(int x) {
9
10
    if (boss[x] < 0) {
       return x;
11
    }
12
13
    return boss[x] = find(boss[x]);
14 }
15
  bool uni(int a, int b) {
    a = find(a);
16
17
    b = find(b);
18
    if (a == b) {
       return false;
19
20
    if (boss[a] > boss[b]) {
21
22
       swap(a, b);
    }
23
24
    boss[a] += boss[b];
25
    boss[b] = a;
26
    return true;
27 }
```

#### 2.2 BIT RARSQ

```
1 // 1-base
2 #define lowbit(k) (k & -k)
3
4
  int n;
5 vector<int> B1, B2;
7
  void add(vector<int> &tr, int id, int val) {
    for (; id <= n; id += lowbit(id)) {</pre>
9
      tr[id] += val;
    }
10
11 }
12 void range_add(int 1, int r, int val) {
13
    add(B1, 1, val);
    add(B1, r + 1, -val);
14
    add(B2, 1, val * (1 - 1));
15
16
    add(B2, r + 1, -val * r);
17 }
18
  int sum(vector<int> &tr, int id) {
    int ret = 0;
19
    for (; id >= 1; id -= lowbit(id)) {
21
      ret += tr[id];
22
    }
23
    return ret;
24 }
25 int prefix_sum(int id) {
26
  return sum(B1, id) * id - sum(B2, id);
27
28 int range_sum(int 1, int r) {
    return prefix_sum(r) - prefix_sum(l - 1);
29
30 }
```

#### 2.3 zkw RMQ

```
1 // 0-base
2 const int INF = 1e9;
3 const int MAXN = ;
4
5 int n;
```

```
6 int a[MAXN], tr[MAXN << 1];</pre>
                                                                44
                                                                         return:
                                                                45
8 // !!! remember to call this function
                                                                       T->push();
                                                                46
9 void build() {
                                                                47
                                                                       int mid = (1 + r) / 2;
    for (int i = 0; i < n; i++) {</pre>
10
                                                                48
                                                                       if (qr <= mid) {
11
       tr[i + n] = a[i];
                                                                49
                                                                          update(T->lc, l, mid, ql, qr, v);
                                                                       } else if (mid < ql) {</pre>
12
                                                                50
13
     for (int i = n - 1; i > 0; i--) {
                                                                51
                                                                         update(T->rc, mid + 1, r, ql, qr, v);
       tr[i] = max(tr[i << 1], tr[i << 1 | 1]);
                                                                52
14
                                                                       } else {
15
                                                                53
                                                                          update(T->lc, 1, mid, ql, mid, v);
16 }
                                                                54
                                                                         update(T->rc, mid + 1, r, mid + 1, qr, v);
17 void update(int id, int val) {
                                                                55
     for (tr[id += n] = val; id > 1; id >>= 1) {
                                                                56
                                                                       T->pull();
       tr[id >> 1] = max(tr[id], tr[id ^ 1]);
                                                                57
19
20
                                                                58
                                                                     int query(Node* &T, int 1, int r, int q1, int qr) {
21 }
                                                                       if (ql <= l && r <= qr) {</pre>
                                                                59
22 int query(int 1, int r) { // [1, r)
                                                                         return T->val;
                                                                60
23
    int ret = -INF;
                                                                61
    for (1 += n, r += n; 1 < r; 1 >>= 1, r >>= 1) {
                                                                       T->push();
                                                                62
24
25
       if (1 & 1) {
                                                                63
                                                                       int mid = (1 + r) / 2;
                                                                       if (qr <= mid) {
26
         ret = max(ret, tr[1++]);
                                                                64
27
                                                                65
                                                                          return query(T->lc, 1, mid, ql, qr);
28
       if (r & 1) {
                                                                66
                                                                       } else if (mid < ql) {</pre>
         ret = max(ret, tr[--r]);
                                                                67
                                                                          return query(T->rc, mid + 1, r, ql, qr);
29
30
                                                                68
                                                                       } else {
31
    }
                                                                69
                                                                         return max(query(T->lc, 1, mid, ql, mid),
32
     return ret;
                                                                70
                                                                              query(T->rc, mid + 1, r, mid + 1, qr));
33 }
                                                                71
                                                                72
                                                                     }
                                                                73 };
```

#### 2.4 Segment Tree RARMQ

```
1 struct Node {
2
     int val, tag;
3
     Node *lc, *rc;
     Node() : lc(nullptr), rc(nullptr), tag(0) {}
     void pull() {
       if (!1c) {
6
         val = rc->val;
       } else if (!rc) {
8
9
         val = lc->val;
10
       } else {
11
         val = max(lc->val, rc->val);
       }
12
13
     }
14
     void push() {
15
       if (lc) {
         lc->tag += tag;
16
17
         lc->val += tag;
18
19
       if (rc) {
20
         rc->tag += tag;
         rc->val += tag;
21
22
       tag = 0;
23
24
25 };
26 struct SegmentTree {
27
     Node *root;
     SegmentTree() : root(nullptr) {}
28
     void build(Node* &T, int 1, int r, const
29
         vector<int> &o) {
30
       T = new Node();
31
       if (l == r) {
         T->val = o[1];
32
33
         return;
34
35
       int mid = (1 + r) / 2;
36
       build(T->lc, l, mid, o);
37
       build(T->rc, mid + 1, r, o);
38
       T->pull();
39
     void update(Node* &T, int 1, int r, int ql, int qr,
40
         int v) {
41
       if (ql <= l && r <= qr) {</pre>
         T->val += v;
42
         T->tag += v;
43
```

### 3 Graph

### 3.1 Dijkstra

```
1 // 0-base
  const LL INF = 1e18;
  const int MAXN = ;
 3
  struct Edge {
    int to:
    LL cost;
 7
     Edge(int v, LL c) : to(v), cost(c) {}
 8
     bool operator < (const Edge &other) const {</pre>
9
       return cost > other.cost;
10
    }
11 };
12
13 int n;
14 LL dis[MAXN];
15 vector < Edge > G[MAXN];
16
17
  void init() {
     for (int i = 0; i < n; i++) {
19
       G[i].clear();
20
       dis[i] = INF;
    }
21
22 }
  void Dijkstra(int st, int ed = -1) {
23
24
     priority_queue < Edge > pq;
25
     pq.emplace(st, 0);
26
     dis[st] = 0;
27
     while (!pq.empty()) {
28
       auto now = pq.top();
29
       pq.pop();
30
       if (now.to == ed) {
31
         return;
32
33
       if (now.cost > dis[now.to]) {
34
         continue;
35
36
       for (auto &e : G[now.to]) {
37
         if (dis[e.to] > now.cost + e.cost) {
38
           dis[e.to] = now.cost + e.cost;
           pq.emplace(e.to, dis[e.to]);
39
```

```
40 }
41 }
42 }
43 }
```

## 3.2 SPFA(negative cycle)

```
1 // 0-base
2 const LL INF = 1e18;
3 const int MAXN = ;
4 struct Edge {
5
    int to;
    LL cost;
6
     Edge(int v, LL c) : to(v), cost(c) {}
8 };
9
10 int n;
11 LL dis[MAXN];
12 vector < Edge > G[MAXN];
13
14 void init() {
     for (int i = 0; i < n; i++) {</pre>
15
       G[i].clear();
16
17
       dis[i] = INF;
     }
18
19
  }
20 bool SPFA(int st) {
    vector<int> cnt(n, 0);
21
     vector<bool> inq(n, false);
     queue<int> q;
23
24
25
     q.push(st);
     dis[st] = 0;
26
27
     inq[st] = true;
     while (!q.empty()) {
28
29
       int now = q.front();
30
       q.pop();
       inq[now] = false;
31
32
       for (auto &e : G[now]) {
         if (dis[e.to] > dis[now] + e.cost) {
33
34
           dis[e.to] = dis[now] + e.cost;
           if (!inq[e.to]) {
35
36
              cnt[e.to]++;
37
              if (cnt[e.to] > n) {
                // negative cycle
38
39
                return false;
              }
40
41
              inq[e.to] = true;
              q.push(e.to);
42
43
44
         }
       }
45
46
     }
47
     return true;
```

#### 3.3 Floyd Warshall

```
1 // 0-base
2 // G[i][i] < 0 -> negative cycle
3 const LL INF = 1e18;
4 const int MAXN = ;
7 LL G[MAXN][MAXN];
9
  void init() {
    for (int i = 0; i < n; i++) {</pre>
10
11
       for (int j = 0; j < n; j++) {
12
         G[i][j] = INF;
13
14
      G[i][i] = 0;
15
```

```
16 }
  void floyd() {
17
     for (int k = 0; k < n; k++) {
       for (int i = 0; i < n; i++) {</pre>
19
20
         for (int j = 0; j < n; j++) {
           if (G[i][k] != INF && G[k][j] != INF) {
21
22
             G[i][j] = min(G[i][j], G[i][k] + G[k][j]);
23
24
         }
25
26
    }
27 }
```

### 3.4 Topological Sort

```
1 // 0-base
2
  // if ret.size < n -> cycle
3 int n;
  vector<vector<int>> G;
6
  vector<int> topoSort() {
    vector<int> indeg(n), ret;
    for (auto &li : G) {
9
       for (int x : li) {
         ++indeg[x];
10
11
    }
12
13
    // use priority queue for lexic. largest ans
14
     queue<int> q;
15
     for (int i = 0; i < n; i++) {
       if (!indeg[i]) {
16
17
         q.push(i);
18
19
20
    while (!q.empty()) {
21
       int u = q.front();
22
       q.pop();
23
       ret.pb(u);
24
       for (int v : G[u]) {
25
         if (--indeg[v] == 0) {
26
           q.push(v);
         }
27
       }
28
    }
29
30
    return ret;
31 }
```

#### 3.5 Tree Diameter

```
1 // 0-base;
  const int MAXN = ;
  struct Edge {
 4
    int to;
    int cost;
    Edge(int v, int c) : to(v), cost(c) {}
7
 8 };
10 int n, d = 0;
11 int d1[MAXN], d2[MAXN];
12 vector < Edge > G[MAXN];
13
  // dfs(0, -1);
14 void dfs(int u, int from) {
     d1[u] = d2[u] = 0;
16
     for (auto e : G[u]) {
17
       if (e.to == from) {
18
         continue;
19
20
       dfs(e.to, u);
21
       int t = d1[e.to] + e.cost;
22
       if (t > d1[u]) {
23
         d2[u] = d1[u];
         d1[u] = t;
```

```
H2J
25
       } else if (t > d2[u]) {
         d2[u] = t;
26
27
       }
     }
28
     d = max(d, d1[u] + d2[u]);
29
30 }
  3.6 Directed MST
1 // 0-base
2 const LL INF = 1e18;
3 const int MAXN = ;
5 struct Edge {
6
    int from;
7
     int to;
8
     LL cost;
     Edge(int u, int v, LL c) : from(u), to(v), cost(c)
9
         {}
10 };
11
12 struct DMST {
13
    int n:
     int vis[MAXN], pre[MAXN], id[MAXN];
14
15
     LL in[MAXN];
16
     vector < Edge > edges;
17
     void init(int _n) {
       n = _n;
18
19
       edges.clear();
20
     void add_edge(int from, int to, LL cost) {
21
       edges.eb(from, to, cost);
22
23
     LL run(int root) {
24
       LL ret = 0;
25
26
       while (true) {
         for (int i = 0; i < n; i++) {</pre>
27
           in[i] = INF;
28
         }
29
30
31
         // find in edge
         for (auto &e : edges) {
32
            if (e.cost < in[e.to] && e.from != e.to) {</pre>
33
34
              pre[e.to] = e.from;
35
              in[e.to] = e.cost;
36
           }
37
38
         // check in edge
39
40
         for (int i = 0; i < n; i++) {</pre>
           if (i == root) {
41
             continue;
42
43
           }
           if (in[i] == INF) {
44
45
              return -1;
           }
46
47
48
         int nodenum = 0;
49
         memset(id, -1, sizeof(id));
50
         memset(vis, -1, sizeof(vis));
51
52
         in[root] = 0;
53
         // find cycles
54
         for (int i = 0; i < n; i++) {</pre>
55
           ret += in[i];
56
            int v = i;
57
            while (vis[v] != i && id[v] == -1 && v !=
58
                root) {
59
              vis[v] = i;
60
             v = pre[v];
61
           if (id[v] == -1 && v != root) {
62
63
              for (int j = pre[v]; j != v; j = pre[j]) {
64
                id[j] = nodenum;
```

65

```
66
              id[v] = nodenum++;
           }
67
         }
68
69
70
          // no cycle
         if (nodenum == 0) {
71
72
           break:
73
74
75
          for (int i = 0; i < n; i++) {</pre>
            if (id[i] == -1) {
76
77
              id[i] = nodenum++;
78
           }
         }
79
80
          // grouping the vertices
81
82
         for (auto &e : edges) {
83
            int to = e.to;
            e.from = id[e.from];
84
85
            e.to = id[e.to];
            if (e.from != e.to) {
86
              e.cost -= in[to]; //!!!
            }
88
         }
89
90
91
         n = nodenum;
         root = id[root];
92
93
94
       return ret:
95
     }
96 };
```

### 3.7 Kosaraju SCC

```
1 // 0-base
2 int n;
  vector<vector<int>>> G, G2; // G2 = G rev
  vector<bool> vis;
  vector<int> s, color;
  int sccCnt;
  void dfs1(int u) {
    vis[u] = true;
     for (int v : G[u]) {
      if (!vis[v]) {
10
11
         dfs1(v);
12
       }
    }
13
14
     s.pb(u);
15 }
16 void dfs2(int u) {
17
     color[u] = sccCnt;
     for (int v : G2[u]) {
18
19
      if (!color[v]) {
20
        dfs2(v);
21
22
    }
  }
23
24
  void Kosaraju() {
25
     sccCnt = 0;
     for (int i = 0; i < n; i++) {</pre>
27
      if (!vis[i]) {
28
         dfs1(i);
       }
29
    }
30
31
     for (int i = n - 1; i >= 0; i--) {
       if (!color[s[i]]) {
32
33
         ++sccCnt;
34
         dfs2(s[i]);
35
36
    }
37 }
```

#### 3.8 BCC

```
1 typedef pair<int, int> PII;
2 int low[MXV], depth[MXV];
3 bool is_cut_vertex[MXV], visit[MXV];
4 vector<int> G[MXV];
5 vector < PII > BCC[MXV];
6 int bcc_cnt = 0;
7 stack<PII> st;
9 vector<pair<int, int>> my_cut_edge;
10
11 void dfs(int now, int cur_depth, int f) {
    visit[now] = true;
12
    depth[now] = low[now] = cur_depth;
13
    int cut_son = 0;
14
15
     for (auto i : G[now]) {
      if (i == f) continue;
16
17
       if (visit[i]) { // ancestor
         if (depth[i] < depth[now]) { // #</pre>
18
           low[now] = min(low[now], depth[i]);
19
20
           st.push({now, i});
        }
21
22
      } else { // offspring
         st.push({now, i});
23
         dfs(i, cur_depth + 1, now);
24
25
         cut_son += 1;
         low[now] = min(low[now], low[i]);
26
         if (low[i] >= depth[now]) {
27
           is_cut_vertex[now] = true;
28
29
           auto t = st.top();
30
           st.pop();
           while (t != make_pair(now, i)) {
31
32
             BCC[bcc_cnt].push_back(t);
             t = st.top();
33
             st.pop();
34
           }
35
           BCC[bcc_cnt].push_back(t);
36
37
           ++bcc_cnt;
         }
38
39
         if (low[i] > depth[now])
40
41
           my_cut_edge.push_bach({now, i});
42
43
    if (cur_depth == 0)
44
      is_cut_vertex[now] = (cut_son != 1);
45
46
     return:
47 }
48
49 bool is_2_edge_connected(int n) {
    memset(visit, 0, sizeof(visit));
50
51
    dfs(1, 0, -1);
52
    return my_cut_edge.size() == 0;
53 }
```

### 3.9 LCA

```
1 const int LOG = 20;
2 vector<int> tin(MAXN), tout(MAXN), depth(MAXN);
3 int par[MAXN][LOG];
4 int timer = 0;
5 vector<int> G[MAXN];
7 void dfs(int u, int f) {
    tin[u] = ++timer;
8
9
    par[u][0] = f;
10
    for (int v : G[u]) {
11
      if (v != f) {
         depth[v] = depth[u] + 1;
12
13
         dfs(v, u);
14
    }
15
    tout[u] = ++timer;
16
17 }
18
19 void Doubling(int n) {
   for (int j = 1; j < LOG; ++j) {
```

```
21
       for (int i = 1; i <= n; ++i) {
         par[i][j] = par[par[i][j - 1]][j - 1];
22
23
       }
    }
24
25 }
26
  bool anc(int u, int v) { return tin[u] <= tin[v] &&</pre>
27
       tout[v] <= tout[u]; }
28
  int LCA(int u, int v) {
29
30
    if (depth[u] > depth[v]) {
31
       swap(u, v);
32
    if (anc(u, v)) {
33
34
      return u;
35
     for (int j = LOG - 1; j >= 0; --j) {
36
37
       if (!anc(par[u][j], v)) u = par[u][j];
38
39
     return par[u][0];
40 }
42 int dis(int u, int v) {
43
    int lca = LCA(u, v);
     return depth[u] + depth[v] - 2 * depth[lca];
44
45 }
46
47 /*
48 dfs(root, root);
49 Doubling(n);
50 */
```

### 4 Flow & Matching

#### 4.1 Relation

```
1 | 1. 一般圖
2 | 1最大匹配 | + |最小邊覆蓋 | = |V|
3 | 1最大獨立集 | + |最小點覆蓋 | = |V|
4 | 最大圖 | = |補圖的最大獨立集 |
5 | 2. 二分圖
6 | 1最大匹配 | = |最小點覆蓋 |
7 | 1最大獨立集 | = |日最小邊覆蓋 |
8 | 1最大獨立集 | = |V| - |最大匹配 |
9 | 日最大圖 | = |補圖的最大獨立集 |
```

#### 4.2 Bipartite Matching

```
1 // 0-base
  const int MAXN = ;
 3
  int n;
  vector<int> G[MAXN];
  int vy[MAXN], my[MAXN];
 7
  bool match(int u) {
    for (int v : G[u]) {
 8
       if (vy[v]) {
10
         continue;
11
12
       vy[v] = true;
       if (my[v] == -1 || match(my[v])) {
13
14
         my[v] = u;
15
         return true;
16
       }
17
    }
18
    return false;
19 }
20 int sol() {
21
    int cnt = 0;
22
     memset(my, -1, sizeof(my));
    for (int i = 0; i < n; i++) {</pre>
```

```
24
       memset(vy, 0, sizeof(vy));
                                                                    66
25
       if (match(i)) {
                                                                    67
                                                                            int ans = 0:
26
                                                                            for (int i = 1; i <= n; i++) {</pre>
          cnt++;
                                                                    68
                                                                              ans += lx[i] + ly[i];
27
       }
                                                                    69
28
     }
                                                                    70
29
     return cnt;
                                                                    71
                                                                            return ans;
30 }
                                                                    72
                                                                    73 };
```

#### 4.3 KM

```
1 const int INF = 1e9;
  const int MAXN = ;
3 struct KM { //1-base
     int n, G[MAXN][MAXN];
     int lx[MAXN], ly[MAXN], my[MAXN];
6
     bool vx[MAXN], vy[MAXN];
7
     void init(int _n) {
8
       n = n:
       for (int i = 1; i <= n; i++) {</pre>
9
         for (int j = 1; j <= n; j++) {</pre>
10
            G[i][j] = 0;
11
12
13
       }
14
     }
15
     bool match(int i) {
16
       vx[i] = true;
       for (int j = 1; j <= n; j++) {</pre>
17
          if (lx[i] + ly[j] == G[i][j] && !vy[j]) {
18
19
            vy[j] = true;
20
            if (!my[j] || match(my[j])) {
21
              my[j] = i;
22
              return true;
23
            }
         }
24
25
       }
26
       return false;
27
28
     void update() {
       int delta = INF;
29
       for (int i = 1; i <= n; i++) {</pre>
30
31
          if (vx[i]) {
            for (int j = 1; j \le n; j++) {
32
              if (!vy[j]) {
33
34
                delta = min(delta, lx[i] + ly[j] -
                     G[i][j]);
35
              }
           }
36
37
         }
38
39
       for (int i = 1; i <= n; i++) {</pre>
40
         if (vx[i]) {
           lx[i] -= delta;
41
42
         if (vy[i]) {
43
44
           ly[i] += delta;
         }
45
       }
46
47
     }
48
     int run() {
49
       for (int i = 1; i <= n; i++) {
50
         lx[i] = ly[i] = my[i] = 0;
51
         for (int j = 1; j <= n; j++) {
52
           lx[i] = max(lx[i], G[i][j]);
53
54
       for (int i = 1; i <= n; i++) {</pre>
55
56
          while (true) {
            for (int i = 1; i <= n; i++) {
57
58
              vx[i] = vy[i] = 0;
59
            if (match(i)) {
60
61
              break;
62
            } else {
63
              update();
64
            }
65
```

#### 4.4 Dinic

```
1 #define eb emplace_back
2 const LL INF = 1e18;
  const int MAXN = ;
  struct Edge {
    int to;
    LL cap;
    int rev:
    Edge(int v, LL c, int r) : to(v), cap(c), rev(r) {}
9 };
10 struct Dinic {
11
    int n;
12
     int level[MAXN], now[MAXN];
13
     vector<Edge> G[MAXN];
14
     void init(int _n) {
15
       n = _n;
       for (int i = 0; i \le n; i ++) {
16
         G[i].clear();
17
18
       }
19
     void add_edge(int u, int v, LL c) {
20
       G[u].eb(v, c, G[v].size());
21
22
       // directed graph
23
       G[v].eb(u, 0, G[u].size() - 1);
       // undirected graph
24
25
       // G[v].eb(u, c, G[u].size() - 1);
26
27
     bool bfs(int st, int ed) {
28
       fill(level, level + n + 1, -1);
       queue<int> q;
29
30
       q.push(st);
31
       level[st] = 0;
       while (!q.empty()) {
32
33
         int u = q.front();
34
         q.pop();
35
         for (const auto &e : G[u]) {
           if (e.cap > 0 && level[e.to] == -1) {
36
37
             level[e.to] = level[u] + 1;
             q.push(e.to);
38
39
         }
40
       }
41
42
       return level[ed] != -1;
43
44
     LL dfs(int u, int ed, LL limit) {
       if (u == ed) {
45
46
         return limit;
       }
47
48
       LL ret = 0;
49
       for (int &i = now[u]; i < G[u].size(); i++) {</pre>
         auto &e = G[u][i];
50
51
         if (e.cap > 0 && level[e.to] == level[u] + 1) {
52
           LL f = dfs(e.to, ed, min(limit, e.cap));
53
           ret += f;
54
           limit -= f;
           e.cap -= f;
55
           G[e.to][e.rev].cap += f;
57
           if (!limit) {
58
             return ret:
59
         }
60
61
       if (!ret) {
62
63
         level[u] = -1;
64
65
       return ret;
```

8

```
66
                                                                63
                                                                                  negcycle = true;
    LL flow(int st, int ed) {
67
                                                                64
                                                                                 break;
       LL ret = 0;
                                                                65
68
69
       while (bfs(st, ed)) {
                                                                66
70
         fill(now, now + n + 1, 0);
                                                                67
71
         ret += dfs(st, ed, INF);
                                                                68
                                                                         }
72
                                                                69
73
       return ret;
                                                                70
74
                                                                71
                                                                       return dis[ed] != INF;
75 };
                                                                72
                                                                73
                                                                    LL sendFlow(int v, LL curFlow) {
                                                                       if (pre[v] == -1) {
                                                                74
                                                                75
                                                                         return curFlow;
  4.5 MCMF
                                                                76
                                                                77
                                                                       int i = pre[v];
1 // 0-base
                                                                       int u = edges[i].u;
                                                                78
2 const LL INF = 1e18;
                                                                79
                                                                       LL cost = edges[i].cost;
3 const int MAXN = ;
                                                                80
  struct Edge {
                                                                       LL f = sendFlow(u, min(curFlow, edges[i].cap));
                                                                81
    int u, v;
                                                                82
    LL cost;
                                                                       ans_cost += f * cost;
                                                                83
7
    LL cap;
                                                                84
                                                                       edges[i].cap -= f;
    Edge(int _u, int _v, LL _c, LL _cap) : u(_u),
                                                                85
                                                                       edges[i ^ 1].cap += f;
         v(_v), cost(_c), cap(_cap) {}
                                                                86
                                                                       return f;
9 }:
                                                                87
10 struct MCMF {
                      // inq times
                                                               88
                                                                    pair<LL, LL> run(int st, int ed) {
    int n, pre[MAXN], cnt[MAXN];
11
                                                                       ans_flow = ans_cost = 0;
                                                                89
12
     LL ans_flow, ans_cost, dis[MAXN];
                                                                90
                                                                       while (SPFA(st, ed)) {
13
     bool inq[MAXN];
                                                                91
                                                                         ans_flow += sendFlow(ed, INF);
     vector<int> G[MAXN];
14
                                                                92
15
     vector < Edge > edges;
                                                                93
                                                                       return make_pair(ans_flow, ans_cost);
16
     void init(int _n) {
                                                                94
                                                                    }
17
       n = _n;
                                                                95 };
18
       edges.clear();
19
       for (int i = 0; i < n; i++) {
20
         G[i].clear();
21
       }
                                                                       String
22
     void add_edge(int u, int v, LL c, LL cap) {
23
24
       // directed
                                                                  5.1
                                                                         Manacher
25
       G[u].pb(edges.size());
26
       edges.eb(u, v, c, cap);
                                                                1 int p[2 * MAXN];
27
       G[v].pb(edges.size());
                                                                  int Manacher(const string &s) {
28
       edges.eb(v, u, -c, 0);
                                                                    string st = "@#";
29
                                                                    for (char c : s) {
30
     bool SPFA(int st, int ed) {
                                                                       st += c;
31
       for (int i = 0; i < n; i++) {
                                                                       st += '#';
                                                                6
32
         pre[i] = -1;
                                                                    }
                                                                7
         dis[i] = INF;
33
                                                                    st += '$';
                                                                8
34
         cnt[i] = 0;
                                                                    int id = 0, mx = 0, ans = 0;
                                                                9
         inq[i] = false;
35
                                                                     for (int i = 1; i < st.length() - 1; i++) {</pre>
                                                                10
36
                                                                11
                                                                       p[i] = (mx > i ? min(p[2 * id - i], mx - i) : 1);
37
       queue < int > q;
                                                                       for (; st[i - p[i]] == st[i + p[i]]; p[i]++);
                                                                12
       bool negcycle = false;
38
                                                                13
                                                                       if (mx < i + p[i]) {</pre>
39
                                                                         mx = i + p[i];
                                                                14
       dis[st] = 0;
40
                                                                15
                                                                         id = i;
41
       cnt[st] = 1;
                                                                       }
                                                                16
       inq[st] = true;
42
                                                                17
                                                                       ans = max(ans, p[i] - 1);
43
       q.push(st);
                                                                    }
                                                                18
44
                                                                19
                                                                    return ans;
       while (!q.empty() && !negcycle) {
45
46
         int u = q.front();
47
         q.pop();
48
         inq[u] = false;
49
         for (int i : G[u]) {
                                                                  5.2 Trie
           int v = edges[i].v;
50
51
           LL cost = edges[i].cost;
           LL cap = edges[i].cap;
                                                                1 const int MAXL = :
52
53
                                                                  const int MAXC = ;
           if (dis[v] > dis[u] + cost && cap > 0) {
54
                                                                  struct Trie {
55
             dis[v] = dis[u] + cost;
                                                                    int nex[MAXL][MAXC];
56
             pre[v] = i;
                                                                    int len[MAXL];
             if (!inq[v]) {
57
                                                                    int sz:
                                                                6
                                                                7
                                                                     void init() {
               q.push(v);
                                                                       memset(nex, 0, sizeof(nex));
59
                cnt[v]++;
                                                                8
60
               inq[v] = true;
                                                                9
                                                                       memset(len, 0, sizeof(len));
61
                                                                10
                                                                       sz = 0;
```

}

11

if (cnt[v] == n + 2) {

62

```
12
     void insert(const string &str) {
       int p = 0;
13
       for (char c : str) {
14
         int id = c - 'a';
15
         if (!nex[p][id]) {
16
17
           nex[p][id] = ++sz;
18
19
         p = nex[p][id];
20
21
       len[p] = str.length();
22
     vector<int> find(const string &str, int i) {
23
       int p = 0;
24
       vector<int> ans;
25
26
       for (; i < str.length(); i++) {</pre>
         int id = str[i] - 'a';
27
         if (!nex[p][id]) {
28
29
           return ans;
         }
30
31
         p = nex[p][id];
         if (len[p]) {
32
33
           ans.pb(len[p]);
34
35
36
       return ans;
37
38 };
```

#### 5.3 Z-value

```
1 // 0-base
2 // 對於個長度為 n 的字串 s
3 // 定義函數 z[i] 表示 s 和 s[i, n - 1]
4 // (即以 s[i] 開頭的後綴) 的最長公共前綴 (LCP) 的長度
5 // z[0] = 0 \circ
6 vector<int> z_function(string s) {
    int n = (int)s.length();
8
    vector<int> z(n);
    for (int i = 1, l = 0, r = 0; i < n; ++i) {
      if (i <= r && z[i - 1] < r - i + 1) {</pre>
10
        z[i] = z[i - 1];
11
12
      } else {
        z[i] = max(0, r - i + 1);
13
        while (i + z[i] < n \&\& s[z[i]] == s[i + z[i]])
14
            ++z[i]:
15
      if (i + z[i] - 1 > r) l = i, r = i + z[i] - 1;
16
    }
17
18
    return z;
19 }
```

#### 6 DP

#### 6.1 LIS

```
int LIS(vector<int> &a) {
   vector<int> s;
   for (int i = 0; i < a.size(); i++) {
      if (s.empty() || s.back() < a[i]) {
        s.push_back(a[i]);
      } else {
        *lower_bound(s.begin(), s.end(), a[i],
            [](int x, int y) {return x < y;}) = a[i];
      }
   }
   return s.size();
}</pre>
```

#### 6.2 LCS

```
1 int LCS(string s1, string s2) {
                                int n1 = s1.size(), n2 = s2.size();
                                 vector < vector < int >> dp(n1 + 1, vector < int > (n2 + 1, vector < int > (
                                                            0));
                                 for (int i = 1; i <= n1; i++) {
                                              for (int j = 1; j <= n2; j++) {</pre>
     5
                                                           if (s1[i - 1] == s2[j - 1]) {
     6
     7
                                                                         dp[i][j] = dp[i - 1][j - 1] + 1;
     8
                                                           } else {
                                                                         dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]);
     9
 10
                                            }
11
12
                             }
13
                                 return dp[n1][n2];
```

#### 7 Math

#### 7.1 Number Theory

```
• Inversion: aa^{-1} \equiv 1 \ (\text{mod } m). \ a^{-1} \ \text{exists iff } \gcd(a,m) = 1.
• Linear inversion:
   a^{-1} \equiv (m - \lfloor \frac{m}{a} \rfloor) \times (m \mod a)^{-1} \pmod{m}
• Fermat's little theorem:
    a^p \equiv a \pmod{p} if p is prime.

    Euler function:

    \phi(n) = n \prod_{p|n} \frac{p-1}{p}
· Euler theorem:
    a^{\phi(n)} \equiv 1 \pmod{n} if \gcd(a, n) = 1.

    Extended Euclidean algorithm:

    ax + by = \gcd(a, b) = \gcd(b, a \mod b) = \gcd(b, a - \lfloor \frac{a}{b} \rfloor b) = bx_1 + (a - \lfloor \frac{a}{b} \rfloor b)
    \left\lfloor \frac{a}{b} \right\rfloor b) y_1 = a y_1 + b \left( x_1 - \left\lfloor \frac{a}{b} \right\rfloor y_1 \right)
· Divisor function:
    \sigma_x(n) = \sum_{d|n} d^x. n = \prod_{i=1}^r p_i^{a_i}.
   \sigma_x(n) = \prod_{i=1}^r \frac{p_i^{(a_i+1)x} - 1}{p_i^x - 1} \text{ if } x \neq 0. \ \ \sigma_0(n) = \prod_{i=1}^r (a_i + 1).
· Chinese remainder theorem:
    x \equiv a_i \pmod{m_i}.
   M = \prod_i m_i. \ M_i = M/m_i. \ t_i = M_i^{-1}. x = kM + \sum_i a_i t_i M_i, \ k \in \mathbb{Z}.
```

### 7.2 Extended GCD

```
1 // ax + by = c
  int extgcd(int a, int b, int c, int &x, int &y) {
    if (b == 0) {
3
4
      x = c / a;
      y = 0;
5
      return a;
    }
7
    int d = extgcd(b, a % b, c, y, x);
8
    y -= (a / b) * x;
9
10
    return d;
```

#### 7.3 Gaussian Elimination + det

```
1     const double EPS = 1e-6;
2     double Gauss(vector<vector<double>> &d) {
3        int n = d.size(), m = d[0].size();
4        double det = 1;
5        for (int i = 0; i < m; i++) {
6            int p = -1;
7            for (int j = i; j < n; j++) {
8                if (fabs(d[j][i]) < EPS) {
9                     continue;
10            }
</pre>
```

```
if (p == -1 || fabs(d[j][i]) > fabs(d[p][i])) {
11
12
           p = j;
         }
13
14
       }
       if (p == -1) {
15
16
         continue;
17
18
       if (p != i) {
         det *= -1;
19
20
21
       for (int j = 0; j < m; j++) {
         swap(d[p][j], d[i][j]);
22
23
       for (int j = 0; j < n; j++) {
24
25
         if (i == j) {
26
           continue;
27
28
         double z = d[j][i] / d[i][i];
         for (int k = 0; k < m; k++) {
29
           d[j][k] -= z * d[i][k];
30
31
32
33
    }
     for (int i = 0; i < n; i++) {
34
35
       det *= d[i][i];
36
37
     return det;
38 }
```

### 7.4 Prime Table

```
1 | vector<int> p;
2 bitset < MAXN > is_notp;
3 void PrimeTable(int n) {
     is_notp.reset();
     is_notp[0] = is_notp[1] = 1;
     for (int i = 2; i \le n; ++i) {
6
       if (!is_notp[i]) {
7
         p.push_back(i);
9
10
       for (int j = 0; j < (int)p.size(); ++j) {</pre>
11
         if (i * p[j] > n) {
           break;
12
         }
13
         is_notp[i * p[j]] = 1;
14
15
         if (i % p[j] == 0) {
16
           break;
17
18
       }
19
     }
20 }
```

### 7.5 Phi

```
· 歐拉函數計算對於一個整數 N,小於等於 N 的正整數中,有幾個和 N 互質
```

```
・ 如果 gcd(p,q) = 1, \Phi(p) \cdot \Phi(q) = \Phi(p \cdot q)
```

```
• \Phi(p^k) = p^{k-1} \times (p-1)
```

```
1 void phi_table(int n) {
    phi[1] = 1;
3
     for (int i = 2; i <= n; i++) {
       if (phi[i]) {
5
         continue;
6
       for (int j = i; j < n; j += i) {
7
8
         if (!phi[j]) {
9
          phi[j] = j;
10
11
         phi[j] = phi[j] / i * (i - 1);
12
13
    }
14 }
```

#### 7.6 Chinese Remainder Thm

```
1 | //参数可为负数的扩展欧几里德定理
void exOJLD(int a, int b, int& x, int& y) {
   //根据欧几里德定理
    if (b == 0) { //任意数与0的最大公约数为其本身。
5
     x = 1;
6
      y = 0;
7
    } else {
      int x1, y1;
8
      exOJLD(b, a % b, x1, y1);
9
      if (a * b < 0) { //异号取反
10
       x = -y1;
11
12
        y = a / b * y1 - x1;
      } else { //同号
13
       x = y1;
14
15
        y = x1 - a / b * y1;
16
17
   }
18 }
19 //剩余定理
20 int calSYDL(int a[], int m[], int k) {
   int N[k]; //这个可以删除
21
    int mm = 1; //最小公倍数
22
23
    int result = 0;
    for (int i = 0; i < k; i++) {
24
25
     mm *= m[i];
    }
26
27
    for (int j = 0; j < k; j++) {
28
     int L, J;
      exOJLD(mm / m[j], -m[j], L, J);
29
      N[j] = m[j] * J + 1; // 1
30
31
      N[j] = mm / m[j] * L; // 2
         1和2这两个值应该是相等的。
      result += N[j] * a[j];
32
    }
33
34
    return (result % mm + mm) % mm;
    //落在(0.
35
        mm)之间,这么写是为了防止result初始为负数,本例中不可能为
    //写成: return result%mm;即可。
36
37 }
38
39
  int main() {
   int a[3] = {2, 3, 6}; // a[i]=n%m[i]
40
41
    int m[3] = \{3, 5, 7\};
42
    cout << calSYDL(a, m, 3) << endl;</pre>
    //輸出為滿足兩條陣列的最小n,第3參數為陣列長度
43
    //所有滿足答案的數字集合為n+gcd(m0, m1, m2...)*k,
        k為正數
45
    return 0;
46 }
```

#### 7.7 Josephus

```
1 int josephus(int n, int k) { //
     有n個人圍成一圈,每k個一次
  return n > 1 ? (josephus(n - 1, k) + k) % n : 0;
3 } // 回傳最後一人的編號, 0 index
```

#### 7.8 Catalan

5

$$C_0 = 1 \quad \text{and} \quad C_{n+1} = \frac{2(2n+1)}{n+2}C_n$$
 
$$\begin{array}{c} 1 \\ 2 \\ \text{int main()} \\ 3 \\ \text{for (int i = 1; i <= 100; i++)} \\ 4 \\ \text{f[i] = f[i - 1] * (4 * i - 2) \% mod;} \\ \text{for (t = i + 1, p = mod - 2; p; t = (t * t) \% \\ mod, p >>= 1LL) \\ 6 \\ \text{if (p \& 1)} \\ 7 \\ \text{f[i] *= t;} \end{array}$$

```
8 f[i] %= mod;
9 }
10 }
11 }
12 }
```

### 7.9 Matrix Multiplication

```
1 struct Matrix {
2
    int row, col;
     vector<vector<int>> v;
     Matrix() : row(0), col(0) {}
     Matrix(int r, int c) : row(r), col(c) {
       v = vector<vector<int>>(r, vector<int>(c, 0));
7
8 };
9 Matrix operator * (Matrix &a, Matrix &b) {
    assert(a.col == b.row);
10
11
     Matrix ret(a.row, b.col);
     for (int i = 0; i < a.row; i++) {</pre>
12
13
       for (int j = 0; j < b.col; j++) {</pre>
         for (int k = 0; k < a.col; k++) {</pre>
14
           ret.v[i][j] += a.v[i][k] * b.v[k][j];
15
16
17
       }
18
    }
19
     return ret;
20 }
21 Matrix mPow(Matrix a, int n) {
    assert(a.row == a.col);
22
23
     Matrix ret(a.row, a.col);
     ret.v[0][0] = ret.v[1][1] = 1;
24
25
     while (n > 0) {
       if (n & 1) {
26
27
         ret = ret * a;
       }
28
       a = a * a;
29
30
       n >>= 1;
31
    }
32
     return ret;
```

#### 7.10 Fibonacci

33 }

$$f(n) = f(n-1) + f(n-2)$$

$$\begin{bmatrix} f(n) \\ f(n-1) \end{bmatrix} = \begin{bmatrix} 1 & 1 \\ 1 & 0 \end{bmatrix}^{(n-1)} \begin{bmatrix} 1 \\ 0 \end{bmatrix}$$

$$O(\log n)$$

```
1 LL fib(int n) {
2    if (n <= 1) {
3        return n;
4    }
5    Matrix a(2, 2), b(2, 1);
6    a.v[0][0] = a.v[0][1] = a.v[1][0] = 1;
7    b.v[0][0] = 1;
8    auto t = mPow(a, n - 1);
9    t = t * b;
10    return t.v[0][0];
11 }</pre>
```

# 8 Geometry

#### 8.1 Point

```
1 // notice point type!!!
2 using dvt = int;
  const double EPS = 1e-6;
  const double PI = acos(-1);
6
  struct Pt {
   dvt x;
7
  dvt y;
8
9 };
10 bool operator < (const Pt &a, const Pt &b) {
11
   return a.x == b.x ? a.y < b.y : a.x < b.x;</pre>
12 }
13 bool operator == (const Pt &a, const Pt &b) {
   return a.x == b.x && a.y == b.y;
14
15
16 Pt operator + (const Pt &a, const Pt &b) {
17
   return {a.x + b.x, a.y + b.y};
18 }
19 Pt operator - (const Pt &a, const Pt &b) {
20
   return {a.x - b.x, a.y - b.y};
21 }
22
  // multiply constant
23 Pt operator * (const Pt &a, const dvt c) {
   return {a.x * c, a.y * c};
24
25
26 Pt operator / (const Pt &a, const dvt c) {
27
   return {a.x / c, a.y / c};
28 }
29
  // |a| x |b| x cos(x)
  dvt iproduct(const Pt &a, const Pt &b) {
   return a.x * b.x + a.y * b.y;
31
32 }
33 // |a| \times |b| \times \sin(x)
34 dvt cross(const Pt &a, const Pt &b) {
35
   return a.x * b.y - a.y * b.x;
36 }
37 dvt dis_pp(const Pt &a, const Pt, &b) {
  dvt dx = a.x - b.x;
38
    dvt dy = a.y - b.y;
40
    return sqrt(dx * dx, dy * dy);
```

#### 8.2 Line

$$d(P, L) = \frac{|ax_0 + by_0 + c|}{\sqrt{a^2 + b^2}}$$

```
1 struct Line {
    Pt st;
 3
    Pt ed;
4 };
  // return point side
5
  // left, on line, right -> 1, 0, -1
 7
  int side(Line 1, Pt a) {
     dvt cross_val = cross(a - 1.st, 1.ed - 1.st);
    if (cross_val > EPS) {
9
      return 1;
10
11
    } else if (cross_val < -EPS) {</pre>
      return -1;
12
13
    } else {
14
       return 0;
15
16 }
17
  // AB infinity, CD segment
18
  bool has_intersection(Line AB, Line CD) {
    int c = side(AB, CD.st);
19
     int d = side(AB, CD.ed);
    if (c == 0 || d == 0) {
21
22
      return true;
23
     } else {
      // different side
24
       return c == -d;
25
26
    }
27 }
  // find intersection point, two line, not seg
29 pair<int, Pt> intersection(Line a, Line b) {
```

```
30
     Pt A = a.ed - a.st;
                                                                17
     Pt B = b.ed - b.st;
                                                                18
31
     Pt C = b.st - a.st;
                                                                19
                                                                        ret[m++] = a[i];
32
                                                                     }
33
     dvt mom = cross(A, B);
                                                                20
34
     dvt son = cross(C, B);
                                                                21
                                                                     if (sz > 1) {
35
     if (std::abs(mom) <= EPS) {</pre>
                                                                22
                                                                        m - -;
       if (std::abs(son) <= EPS) {</pre>
                                                                23
                                                                     }
36
37
         return {1, {}}; // same line
                                                                24
                                                                     ret.resize(m);
                                                                25
38
       } else {
                                                                     return ret;
         return {2, {}}; // parallel
                                                                26 }
39
40
       }
41
     } else {
42
       return {0, a.st + A * (son / mom)};
     }
43
44 }
45 // line to point distance
46 dvt dis_lp(Line 1, Pt a) {
47
   return area3x2(1.st, 1.ed, a) / dis_pp(1.st, 1.ed);
48 }
```

#### 8.3 Area

```
1 // triangle
2 dvt area3(Pt a, Pt b, Pt c) {
return std::abs(cross(b - a, c - a) / 2);
4 }
5 dvt area3x2(Pt a, Pt b, Pt c) { // for integer
    return std::abs(cross(b - a, c - a));
6
7 }
8 // simple convex area(can in)
9 dvt area(vector <Pt> &a) {
10
    dvt ret = 0;
    for (int i = 0, sz = a.size(); i < sz; i++) {</pre>
11
12
      ret += cross(a[i], a[(i + 1) % sz]);
    }
13
    return std::abs(ret) / 2;
14
15 }
16 // check point in/out a convex
17 int io_convex(vector<Pt> convex, Pt q) {
     // convex is Counterclockwise
18
19
     for (int i = 0, sz = convex.size(); i < sz; i++) {</pre>
       Pt cur = convex[i] - q;
20
       Pt nex = convex[(i + 1) \% sz] - q;
21
       dvt cross_val = cross(cur, nex);
22
23
       if (std::abs(cross_val) <= EPS) {</pre>
24
         return 0; // on edge
25
       if (cross_val < 0) {</pre>
26
27
         return -1; // outside
       }
28
29
    }
30
     return 1;
                    // inside
```

### 8.4 Convex Hull

```
1 vector < Pt > convex_hull(vector < Pt > &a) {
    sort(a.begin(), a.end());
2
3
    a.erase(unique(a.begin(), a.end());
    int sz = a.size(), m = 0;
    vector<Pt> ret(sz + 5); // safe 1 up
5
6
    for (int i = 0; i < sz; i++) {</pre>
7
       while (m > 1 &&
         cross(ret[m - 1] - ret[m - 2], a[i] - ret[m -
8
             2]) <= EPS) {
9
        m - -;
10
      }
11
      ret[m++] = a[i];
    }
12
    int k = m;
13
14
    for (int i = sz - 2; i >= 0; i--) {
15
      while (m > k \&\&
         cross(ret[m - 1] - ret[m - 2], a[i] - ret[m -
16
             2]) <= EPS) {
```