Contents

1 Basic

1.1 Run

```
#use -> sh run.sh {name}
g++ -O2 -std=c++14 -Wall -Wextra -Wshadow -o $1 $1.cpp
./$1 < t.in > t.out
```

1.2 Default

```cpp
#include <bits/stdc++.h>
using namespace std;
using LL = long long;
#define IOS ios_base::sync_with_stdio(0); cin.tie(0);
#define pb push_back
#define eb emplace_back
const int INF = 1e9;
const int MOD = 1e9 + 7;
const double EPS = 1e-6;
const int MAXN = 0;

int main() {

}
```

1.3 Black Magic

```cpp
#include <bits/stdc++.h>
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
#include <ext/pb_ds/priority_queue.hpp>
using namespace std;
using namespace __gnu_pbds;
using set_t =
  tree<int, null_type, less<int>, rb_tree_tag,
    tree_order_statistics_node_update>;
using map_t =
  tree<int, int, less<int>, rb_tree_tag,
    tree_order_statistics_node_update>;
using heap_t =
  __gnu_pbds::priority_queue<int>;
using ht_t =
  gp_hash_table<int, int>;
int main() {
  //set----------------------------------
  set_t st;
  st.insert(5); st.insert(6);
  st.insert(3); st.insert(1);

  // the smallest is (0), biggest is (n-1), kth small
      is (k-1)
  int num = *st.find_by_order(0);
  cout << num << '\n'; // print 1

  num = *st.find_by_order(st.size() - 1);
  cout << num << '\n'; // print 6

  // find the index
  int index = st.order_of_key(6);
  cout << index << '\n'; // print 3

  // check if there exists x
  int x = 5;
  int check = st.erase(x);
  if (check == 0) printf("st not contain 5\n");
  else if (check == 1) printf("st contain 5\n");

  //tree policy like set
  st.insert(5); st.insert(5);
  cout << st.size() << '\n'; // print 4

  //map----------------------------------
  map_t mp;
  mp[1] = 2;
  cout << mp[1] << '\n';
  auto tmp = *mp.find_by_order(0); // pair
  cout << tmp.first << " " << tmp.second << '\n';

  //heap----------------------------------
  heap_t h1, h2;
  h1.push(1); h1.push(3);
  h2.push(2); h2.push(4);
  h1.join(h2);
  cout << h1.size() << h2.size() << h1.top() << '\n';
  // 404

  //hash-table----------------------------
  ht_t ht;
  ht[85] = 5;
  ht[89975] = 234;
  for (auto i : ht) {
    cout << i.first << " " << i.second << '\n';
  }
}
```

1.4 Binary Search

```cpp
lower_bound(a, a + n, k);      //最左邊 ≥ k 的位置
upper_bound(a, a + n, k);      //最左邊 > k 的位置
upper_bound(a, a + n, k) - 1; //最右邊 ≤ k 的位置
```

```
lower_bound(a, a + n, k) - 1; //最右邊 < k 的位置
[lower_bound, upper_bound)    //等於 k 的範圍
equal_range(a, a + n, k);
```

1.5 Python

```
### EOF
while True:
  try:
    pass
  except EOFError:
    break
###math
import math

math.ceil(x)#上高斯
math.floor(x)#下高斯
math.factorial(x)#接乘
math.fabs(x)#絕對值
math.fsum(arr)#跟sum一樣但更精確(小數點問題)
math.gcd(x, y)#bj4
math.exp(x)#e^x
math.log(x, base)
math.log2(x)#2為底
math.log10(x)#10為底
math.sqrt(x)
math.pow(x, y, mod)#精確些(float型態) MOD!!!
math.sin(x)# cos tan asin acos atan atan2(弧度) sinh
    cosh tanh acosh asinh atanh
math.hypot(x, y)#歐幾里德範數
math.degrees(x)#x從弧度轉角度
math.radians(x)#x從角度轉弧度
math.gamma(x)#x的gamma函數
math.pi#常數
math.e#常數
math.inf

### ascii
ord(x)#char to asc
chr(x)#asc to char

x.encode().hex()#string to hex
### reverse string
string = "abc"
string_reverse = string[::-1]
```

2 Data Structure

2.1 Disjoint Set

```
// 0-base
const int MAXN = 1000;
int boss[MAXN];
void init(int n) {
  for (int i = 0; i < n; i++) {
    boss[i] = -1;
  }
}
int find(int x) {
  if (boss[x] < 0) {
    return x;
  }
  return boss[x] = find(boss[x]);
}
bool uni(int a, int b) {
  a = find(a);
  b = find(b);
  if (a == b) {
    return false;
  }
  if (boss[a] > boss[b]) {
    swap(a, b);
  }
  boss[a] += boss[b];
  boss[b] = a;
  return true;
}
```

2.2 BIT RARSQ

```
// 1-base
#define lowbit(k) (k & -k)

int n;
vector<int> B1, B2;

void add(vector<int> &tr, int id, int val) {
  for (; id <= n; id += lowbit(id)) {
    tr[id] += val;
  }
}
void range_add(int l, int r, int val) {
  add(B1, l, val);
  add(B1, r + 1, -val);
  add(B2, l, val * (l - 1));
  add(B2, r + 1, -val * r);
}
int sum(vector<int> &tr, int id) {
  int ret = 0;
  for (; id >= 1; id -= lowbit(id)) {
    ret += tr[id];
  }
  return ret;
}
int prefix_sum(int id) {
  return sum(B1, id) * id - sum(B2, id);
}
int range_sum(int l, int r) {
  return prefix_sum(r) - prefix_sum(l - 1);
}
```

2.3 zkw RMQ

```
// 0-base
const int INF = 1e9;
const int MAXN = ;

int n;
int a[MAXN], tr[MAXN << 1];

// !!! remember to call this function
void build() {
  for (int i = 0; i < n; i++) {
    tr[i + n] = a[i];
  }
  for (int i = n - 1; i > 0; i--) {
    tr[i] = max(tr[i << 1], tr[i << 1 | 1]);
  }
}
void update(int id, int val) {
  for (tr[id += n] = val; id > 1; id >>= 1) {
    tr[id >> 1] = max(tr[id], tr[id ^ 1]);
  }
}
int query(int l, int r) { // [l, r)
  int ret = -INF;
  for (l += n, r += n; l < r; l >>= 1, r >>= 1) {
    if (l & 1) {
      ret = max(ret, tr[l++]);
    }
    if (r & 1) {
      ret = max(ret, tr[--r]);
    }
```

```
  }
  return ret;
}
```

3 Graph

3.1 Dijkstra

```
// 0-base
const LL INF = 1e18;
const int MAXN = ;
struct Edge {
  int to;
  LL cost;
  Edge(int v, LL c) : to(v), cost(c) {}
  bool operator < (const Edge &other) const {
    return cost > other.cost;
  }
};

int n;
LL dis[MAXN];
vector<Edge> G[MAXN];

void init() {
  for (int i = 0; i < n; i++) {
    G[i].clear();
    dis[i] = INF;
  }
}
void Dijkstra(int st, int ed = -1) {
  priority_queue<Edge> pq;
  pq.emplace(st, 0);
  dis[st] = 0;
  while (!pq.empty()) {
    auto now = pq.top();
    pq.pop();
    if (now.to == ed) {
      return;
    }
    if (now.cost > dis[now.to]) {
      continue;
    }
    for (auto &e : G[now.to]) {
      if (dis[e.to] > now.cost + e.cost) {
        dis[e.to] = now.cost + e.cost;
        pq.emplace(e.to, dis[e.to]);
      }
    }
  }
}
```

3.2 SPFA(negative cycle)

```
// 0-base
const LL INF = 1e18;
const int MAXN = ;
struct Edge {
  int to;
  LL cost;
  Edge(int v, LL c) : to(v), cost(c) {}
};

int n;
LL dis[MAXN];
vector<Edge> G[MAXN];

void init() {
  for (int i = 0; i < n; i++) {
    G[i].clear();
    dis[i] = INF;
  }
}
bool SPFA(int st) {
  vector<int> cnt(n, 0);
  vector<bool> inq(n, false);
  queue<int> q;

  q.push(st);
  dis[st] = 0;
  inq[st] = true;
  while (!q.empty()) {
    int now = q.front();
    q.pop();
    inq[now] = false;
    for (auto &e : G[now]) {
      if (dis[e.to] > dis[now] + e.cost) {
        dis[e.to] = dis[now] + e.cost;
        if (!inq[e.to]) {
          cnt[e.to]++;
          if (cnt[e.to] > n) {
            // negative cycle
            return false;
          }
          inq[e.to] = true;
          q.push(e.to);
        }
      }
    }
  }
  return true;
}
```

3.3 Floyd Warshall

```
// 0-base
// G[i][i] < 0 -> negative cycle
const LL INF = 1e18;
const int MAXN = ;

int n;
LL G[MAXN][MAXN];

void init() {
  for (int i = 0; i < n; i++) {
    for (int j = 0; j < n; j++) {
      G[i][j] = INF;
    }
    G[i][i] = 0;
  }
}
void floyd() {
  for (int k = 0; k < n; k++) {
    for (int i = 0; i < n; i++) {
      for (int j = 0; j < n; j++) {
        if (G[i][k] != INF && G[k][j] != INF) {
          G[i][j] = min(G[i][j], G[i][k] + G[k][j]);
        }
      }
    }
  }
}
```

3.4 Topological Sort

```
// 0-base
// if ret.size < n -> cycle
int n;
vector<vector<int>> G;

vector<int> topoSort() {
  vector<int> indeg(n), ret;
  for (auto &li : G) {
    for (int x : li) {
      ++indeg[x];
```

```
    }
  }
  // use priority queue for lexic. largest ans
  queue<int> q;
  for (int i = 0; i < n; i++) {
    if (!indeg[i]) {
      q.push(i);
    }
  }
  while (!q.empty()) {
    int u = q.front();
    q.pop();
    ret.pb(u);
    for (int v : G[u]) {
      if (--indeg[v] == 0) {
        q.push(v);
      }
    }
  }
  return ret;
}
```

3.5 Kosaraju SCC

```
// 0-base
int n;
vector<vector<int>> G, G2; // G2 = G rev
vector<bool> vis;
vector<int> s, color;
int sccCnt;
void dfs1(int u) {
  vis[u] = true;
  for (int v : G[u]) {
    if (!vis[v]) {
      dfs1(v);
    }
  }
  s.pb(u);
}
void dfs2(int u) {
  color[u] = sccCnt;
  for (int v : G2[u]) {
    if (!color[v]) {
      dfs2(v);
    }
  }
}
void Kosaraju() {
  sccCnt = 0;
  for (int i = 0; i < n; i++) {
    if (!vis[i]) {
      dfs1(i);
    }
  }
  for (int i = n - 1; i >= 0; i--) {
    if (!color[s[i]]) {
      ++sccCnt;
      dfs2(s[i]);
    }
  }
}
```

3.6 Tree Diameter

```
// 0-base;
const int MAXN = ;

struct Edge {
  int to;
  int cost;
  Edge(int v, int c) : to(v), cost(c) {}
};

int n, d = 0;
int d1[MAXN], d2[MAXN];
vector<Edge> G[MAXN];
// dfs(0, -1);
void dfs(int u, int from) {
  d1[u] = d2[u] = 0;
  for (auto e : G[u]) {
    if (e.to == from) {
      continue;
    }
    dfs(e.to, u);
    int t = d1[e.to] + e.cost;
    if (t > d1[u]) {
      d2[u] = d1[u];
      d1[u] = t;
    } else if (t > d2[u]) {
      d2[u] = t;
    }
  }
  d = max(d, d1[u] + d2[u]);
}
```

3.7 Directed MST

```
// 0-base
const LL INF = 1e18;
const int MAXN = ;

struct Edge {
  int from;
  int to;
  LL cost;
  Edge(int u, int v, LL c) : from(u), to(v), cost(c)
      {}
};

struct DMST {
  int n;
  int vis[MAXN], pre[MAXN], id[MAXN];
  LL in[MAXN];
  vector<Edge> edges;
  void init(int _n) {
    n = _n;
    edges.clear();
  }
  void add_edge(int from, int to, LL cost) {
    edges.eb(from, to, cost);
  }
  LL run(int root) {
    LL ret = 0;
    while (true) {
      for (int i = 0; i < n; i++) {
        in[i] = INF;
      }

      // find in edge
      for (auto &e : edges) {
        if (e.cost < in[e.to] && e.from != e.to) {
          pre[e.to] = e.from;
          in[e.to] = e.cost;
        }
      }

      // check in edge
      for (int i = 0; i < n; i++) {
        if (i == root) {
          continue;
        }
        if (in[i] == INF) {
          return -1;
        }
      }

      int nodenum = 0;
      memset(id, -1, sizeof(id));
      memset(vis, -1, sizeof(vis));
```

```
      in[root] = 0;

      // find cycles
      for (int i = 0; i < n; i++) {
        ret += in[i];
        int v = i;
        while (vis[v] != i && id[v] == -1 && v !=
            root) {
          vis[v] = i;
          v = pre[v];
        }
        if (id[v] == -1 && v != root) {
          for (int j = pre[v]; j != v; j = pre[j]) {
            id[j] = nodenum;
          }
          id[v] = nodenum++;
        }
      }

      // no cycle
      if (nodenum == 0) {
        break;
      }

      for (int i = 0; i < n; i++) {
        if (id[i] == -1) {
          id[i] = nodenum++;
        }
      }

      // grouping the vertices
      for (auto &e : edges) {
        int to = e.to;
        e.from = id[e.from];
        e.to = id[e.to];
        if (e.from != e.to) {
          e.cost -= in[to]; //!!!
        }
      }

      n = nodenum;
      root = id[root];
    }
    return ret;
  }
};
```

3.8 BCC

```
typedef pair<int, int> PII;
int low[MXV], depth[MXV];
bool is_cut_vertex[MXV], visit[MXV];
vector<int> G[MXV];
vector<PII> BCC[MXV];
int bcc_cnt = 0;
stack<PII> st;

vector<pair<int, int>> my_cut_edge;

void dfs(int now, int cur_depth, int f) {
  visit[now] = true;
  depth[now] = low[now] = cur_depth;
  int cut_son = 0;
  for (auto i : G[now]) {
    if (i == f) continue;
    if (visit[i]) {  // ancestor
      if (depth[i] < depth[now]) { // #
        low[now] = min(low[now], depth[i]);
        st.push({now, i});
      }
    } else {  // offspring
      st.push({now, i});
      dfs(i, cur_depth + 1, now);
      cut_son += 1;
      low[now] = min(low[now], low[i]);
      if (low[i] >= depth[now]) {
        is_cut_vertex[now] = true;
        auto t = st.top();
        st.pop();
        while (t != make_pair(now, i)) {
          BCC[bcc_cnt].push_back(t);
          t = st.top();
          st.pop();
        }
        BCC[bcc_cnt].push_back(t);
        ++bcc_cnt;
      }
      // ###
      if (low[i] > depth[now])
        my_cut_edge.push_bach({now, i});
    }
  }
  if (cur_depth == 0)
    is_cut_vertex[now] = (cut_son != 1);
  return;
}

bool is_2_edge_connected(int n) {
  memset(visit, 0, sizeof(visit));
  dfs(1, 0, -1);
  return my_cut_edge.size() == 0;
}
```

4 Flow & Matching

4.1 Relation

```
1. 一般圖
|最大匹配| + |最小邊覆蓋| = |V|
|最大獨立集| + |最小點覆蓋| = |V|
|最大圖| = |補圖的最大獨立集|
2. 二分圖
|最大匹配| = |最小點覆蓋|
|最大獨立集| = |最小邊覆蓋|
|最大獨立集| = |V| - |最大匹配|
|最大圖| = |補圖的最大獨立集|
```

4.2 Bipartite Matching

```
// 0-base
const int MAXN = ;
int n;
vector<int> G[MAXN];
int vy[MAXN], my[MAXN];

bool match(int u) {
  for (int v : G[u]) {
    if (vy[v]) {
      continue;
    }
    vy[v] = true;
    if (my[v] == -1 || match(my[v])) {
      my[v] = u;
      return true;
    }
  }
  return false;
}
int sol() {
  int cnt = 0;
  memset(my, -1, sizeof(my));
  for (int i = 0; i < n; i++) {
    memset(vy, 0, sizeof(vy));
    if (match(i)) {
      cnt++;
    }
  }
```

```
  return cnt;
}
```

4.3 KM

```
const int INF = 1e9;
const int MAXN = ;
struct KM { //1-base
  int n, G[MAXN][MAXN];
  int lx[MAXN], ly[MAXN], my[MAXN];
  bool vx[MAXN], vy[MAXN];
  void init(int _n) {
    n = _n;
    for (int i = 1; i <= n; i++) {
      for (int j = 1; j <= n; j++) {
        G[i][j] = 0;
      }
    }
  }
  bool match(int i) {
    vx[i] = true;
    for (int j = 1; j <= n; j++) {
      if (lx[i] + ly[j] == G[i][j] && !vy[j]) {
        vy[j] = true;
        if (!my[j] || match(my[j])) {
          my[j] = i;
          return true;
        }
      }
    }
    return false;
  }
  void update() {
    int delta = INF;
    for (int i = 1; i <= n; i++) {
      if (vx[i]) {
        for (int j = 1; j <= n; j++) {
          if (!vy[j]) {
            delta = min(delta, lx[i] + ly[j] -
                G[i][j]);
          }
        }
      }
    }
    for (int i = 1; i <= n; i++) {
      if (vx[i]) {
        lx[i] -= delta;
      }
      if (vy[i]) {
        ly[i] += delta;
      }
    }
  }
  int run() {
    for (int i = 1; i <= n; i++) {
      lx[i] = ly[i] = my[i] = 0;
      for (int j = 1; j <= n; j++) {
        lx[i] = max(lx[i], G[i][j]);
      }
    }
    for (int i = 1; i <= n; i++) {
      while (true) {
        for (int i = 1; i <= n; i++) {
          vx[i] = vy[i] = 0;
        }
        if (match(i)) {
          break;
        } else {
          update();
        }
      }
    }
    int ans = 0;
    for (int i = 1; i <= n; i++) {
      ans += lx[i] + ly[i];
    }
    return ans;
  }
};
```

4.4 Dinic

```
#define eb emplace_back
const LL INF = 1e18;
const int MAXN = ;
struct Edge {
  int to;
  LL cap;
  int rev;
  Edge(int v, LL c, int r) : to(v), cap(c), rev(r) {}
};
struct Dinic {
  int n;
  int level[MAXN], now[MAXN];
  vector<Edge> G[MAXN];
  void init(int _n) {
    n = _n;
    for (int i = 0; i <= n; i++) {
      G[i].clear();
    }
  }
  void add_edge(int u, int v, LL c) {
    G[u].eb(v, c, G[v].size());
    // directed graph
    G[v].eb(u, 0, G[u].size() - 1);
    // undirected graph
    // G[v].eb(u, c, G[u].size() - 1);
  }
  bool bfs(int st, int ed) {
    fill(level, level + n + 1, -1);
    queue<int> q;
    q.push(st);
    level[st] = 0;
    while (!q.empty()) {
      int u = q.front();
      q.pop();
      for (const auto &e : G[u]) {
        if (e.cap > 0 && level[e.to] == -1) {
          level[e.to] = level[u] + 1;
          q.push(e.to);
        }
      }
    }
    return level[ed] != -1;
  }
  LL dfs(int u, int ed, LL limit) {
    if (u == ed) {
      return limit;
    }
    LL ret = 0;
    for (int &i = now[u]; i < G[u].size(); i++) {
      auto &e = G[u][i];
      if (e.cap > 0 && level[e.to] == level[u] + 1) {
        LL f = dfs(e.to, ed, min(limit, e.cap));
        ret += f;
        limit -= f;
        e.cap -= f;
        G[e.to][e.rev].cap += f;
        if (!limit) {
          return ret;
        }
      }
    }
    if (!ret) {
      level[u] = -1;
    }
    return ret;
  }
  LL flow(int st, int ed) {
    LL ret = 0;
    while (bfs(st, ed)) {
      fill(now, now + n + 1, 0);
```

```
      ret += dfs(st, ed, INF);
    }
    return ret;
  }
};
```

4.5 MCMF

```
// 0-base
const LL INF = 1e18;
const int MAXN = ;
struct Edge {
  int u, v;
  LL cost;
  LL cap;
  Edge(int _u, int _v, LL _c, LL _cap) : u(_u),
      v(_v), cost(_c), cap(_cap) {}
};
struct MCMF {     // inq times
  int n, pre[MAXN], cnt[MAXN];
  LL ans_flow, ans_cost, dis[MAXN];
  bool inq[MAXN];
  vector<int> G[MAXN];
  vector<Edge> edges;
  void init(int _n) {
    n = _n;
    edges.clear();
    for (int i = 0; i < n; i++) {
      G[i].clear();
    }
  }
  void add_edge(int u, int v, LL c, LL cap) {
    // directed
    G[u].pb(edges.size());
    edges.eb(u, v, c, cap);
    G[v].pb(edges.size());
    edges.eb(v, u, -c, 0);
  }
  bool SPFA(int st, int ed) {
    for (int i = 0; i < n; i++) {
      pre[i] = -1;
      dis[i] = INF;
      cnt[i] = 0;
      inq[i] = false;
    }
    queue<int> q;
    bool negcycle = false;

    dis[st] = 0;
    cnt[st] = 1;
    inq[st] = true;
    q.push(st);

    while (!q.empty() && !negcycle) {
      int u = q.front();
      q.pop();
      inq[u] = false;
      for (int i : G[u]) {
        int v = edges[i].v;
        LL cost = edges[i].cost;
        LL cap = edges[i].cap;

        if (dis[v] > dis[u] + cost && cap > 0) {
          dis[v] = dis[u] + cost;
          pre[v] = i;
          if (!inq[v]) {
            q.push(v);
            cnt[v]++;
            inq[v] = true;

            if (cnt[v] == n + 2) {
              negcycle = true;
              break;
            }
          }
        }
      }
    }

    return dis[ed] != INF;
  }
  LL sendFlow(int v, LL curFlow) {
    if (pre[v] == -1) {
      return curFlow;
    }
    int i = pre[v];
    int u = edges[i].u;
    LL cost = edges[i].cost;

    LL f = sendFlow(u, min(curFlow, edges[i].cap));

    ans_cost += f * cost;
    edges[i].cap -= f;
    edges[i ^ 1].cap += f;
    return f;
  }
  pair<LL, LL> run(int st, int ed) {
    ans_flow = ans_cost = 0;
    while (SPFA(st, ed)) {
      ans_flow += sendFlow(ed, INF);
    }
    return make_pair(ans_flow, ans_cost);
  }
};
```

5 String

5.1 Manacher

```
int p[2 * MAXN];
int Manacher(const string &s) {
  string st = "@#";
  for (char c : s) {
    st += c;
    st += '#';
  }
  st += '$';
  int id = 0, mx = 0, ans = 0;
  for (int i = 1; i < st.length() - 1; i++) {
    p[i] = (mx > i ? min(p[2 * id - i], mx - i) : 1);
    for (; st[i - p[i]] == st[i + p[i]]; p[i]++);
    if (mx < i + p[i]) {
      mx = i + p[i];
      id = i;
    }
    ans = max(ans, p[i] - 1);
  }
  return ans;
}
```

5.2 Trie

```
const int MAXL = ;
const int MAXC = ;
struct Trie {
  int nex[MAXL][MAXC];
  int len[MAXL];
  int sz;
  void init() {
    memset(nex, 0, sizeof(nex));
    memset(len, 0, sizeof(len));
    sz = 0;
  }
  void insert(const string &str) {
    int p = 0;
    for (char c : str) {
      int id = c - 'a';
      if (!nex[p][id]) {
```

```
        nex[p][id] = ++sz;
      }
      p = nex[p][id];
    }
    len[p] = str.length();
  }
  vector<int> find(const string &str, int i) {
    int p = 0;
    vector<int> ans;
    for (; i < str.length(); i++) {
      int id = str[i] - 'a';
      if (!nex[p][id]) {
        return ans;
      }
      p = nex[p][id];
      if (len[p]) {
        ans.pb(len[p]);
      }
    }
    return ans;
  }
};
```

5.3 Z-value

```
// 0-base
// 對於個長度為 n 的字串 s
// 定義函數 z[i] 表示 s 和 s[i, n - 1]
// (即以 s[i] 開頭的後綴) 的最長公共前綴 (LCP) 的長度
// z[0] = 0。
vector<int> z_function(string s) {
  int n = (int)s.length();
  vector<int> z(n);
  for (int i = 1, l = 0, r = 0; i < n; ++i) {
    if (i <= r && z[i - l] < r - i + 1) {
      z[i] = z[i - l];
    } else {
      z[i] = max(0, r - i + 1);
      while (i + z[i] < n && s[z[i]] == s[i + z[i]])
          ++z[i];
    }
    if (i + z[i] - 1 > r) l = i, r = i + z[i] - 1;
  }
  return z;
}
```

6 DP

6.1 LIS

```
int LIS(vector<int> &a) {
  vector<int> s;
  for (int i = 0; i < a.size(); i++) {
    if (s.empty() || s.back() < a[i]) {
      s.push_back(a[i]);
    } else {
      *lower_bound(s.begin(), s.end(), a[i],
        [](int x, int y) {return x < y;}) = a[i];
    }
  }
  return s.size();
}
```

6.2 LCS

```
int LCS(string s1, string s2) {
  int n1 = s1.size(), n2 = s2.size();
  vector<vector<int>> dp(n1 + 1, vector<int>(n2 + 1,
      0));
  for (int i = 1; i <= n1; i++) {
    for (int j = 1; j <= n2; j++) {
      if (s1[i - 1] == s2[j - 1]) {
        dp[i][j] = dp[i - 1][j - 1] + 1;
      } else {
        dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]);
      }
    }
  }
  return dp[n1][n2];
}
```

7 Math

7.1 Extended GCD

```
// ax + by = c
int extgcd(int a, int b, int c, int &x, int &y) {
  if (b == 0) {
    x = c / a;
    y = 0;
    return a;
  }
  int d = extgcd(b, a % b, c, y, x);
  y -= (a / b) * x;
  return d;
}
```

7.2 Gaussian Elimination

```
const double EPS = 1e-6;
double Gauss(vector<vector<double>> &d) {
  int n = d.size(), m = d[0].size();
  double det = 1;
  for (int i = 0; i < m; i++) {
    int p = -1;
    for (int j = i; j < n; j++) {
      if (fabs(d[j][i]) < EPS) {
        continue;
      }
      if (p == -1 || fabs(d[j][i]) > fabs(d[p][i])) {
        p = j;
      }
    }
    if (p == -1) {
      continue;
    }
    if (p != i) {
      det *= -1;
    }
    for (int j = 0; j < m; j++) {
      swap(d[p][j], d[i][j]);
    }
    for (int j = 0; j < n; j++) {
      if (i == j) {
        continue;
      }
      double z = d[j][i] / d[i][i];
      for (int k = 0; k < m; k++) {
        d[j][k] -= z * d[i][k];
      }
    }
  }
  for (int i = 0; i < n; i++) {
    det *= d[i][i];
  }
  return det;
}
```

7.3 Prime Table

```cpp
vector<int> p;
bitset<MAXN> is_notp;
void PrimeTable(int n) {
  is_notp.reset();
  is_notp[0] = is_notp[1] = 1;
  for (int i = 2; i <= n; ++i) {
    if (!is_notp[i]) {
      p.push_back(i);
    }
    for (int j = 0; j < (int)p.size(); ++j) {
      if (i * p[j] > n) {
        break;
      }
      is_notp[i * p[j]] = 1;
      if (i % p[j] == 0) {
        break;
      }
    }
  }
}
```

7.4 Phi Table

- 歐拉函數計算對於一個整數 N，小於等於 N 的正整數中，有幾個和 N 互質
- 如果 $gcd(p,q)=1, \Phi(p)\cdot\Phi(q)=\Phi(p\cdot q)$
- $\Phi(p^k)=p^{k-1}\times(p-1)$

```cpp
void phi_table(int n) {
  phi[1] = 1;
  for (int i = 2; i <= n; i++) {
    if (phi[i]) {
      continue;
    }
    for (int j = i; j < n; j += i) {
      if (!phi[j]) {
        phi[j] = j;
      }
      phi[j] = phi[j] / i * (i - 1);
    }
  }
}
```

7.5 Chinese Remainder Thm

```cpp
//参数可为负数的扩展欧几里德定理
void exOJLD(int a, int b, int& x, int& y) {
  //根据欧几里德定理
  if (b == 0) {  //任意数与0的最大公约数为其本身。
    x = 1;
    y = 0;
  } else {
    int x1, y1;
    exOJLD(b, a % b, x1, y1);
    if (a * b < 0) {  //异号取反
      x = -y1;
      y = a / b * y1 - x1;
    } else {  //同号
      x = y1;
      y = x1 - a / b * y1;
    }
  }
}
//剩余定理
int calSYDL(int a[], int m[], int k) {
  int N[k];     //这个可以删除
  int mm = 1;  //最小公倍数
  int result = 0;
  for (int i = 0; i < k; i++) {
    mm *= m[i];
  }
  for (int j = 0; j < k; j++) {
    int L, J;
    exOJLD(mm / m[j], -m[j], L, J);
    N[j] = m[j] * J + 1;    // 1
    N[j] = mm / m[j] * L;  // 2
        1和2这两个值应该是相等的。
    result += N[j] * a[j];
  }
  return (result % mm + mm) % mm;
  //落在(0,
      mm)之间，这么写是为了防止result初始为负数，本例中不可能为
  //写成：return result%mm;即可。
}

int main() {
  int a[3] = {2, 3, 6};  // a[i]=n%m[i]
  int m[3] = {3, 5, 7};
  cout << calSYDL(a, m, 3) << endl;
  //輸出為滿足兩條陣列的最小n,第3參數為陣列長度
  //所有滿足答案的數字集合為n+gcd(m0,m1,m2...)*k,
      k為正數
  return 0;
}
```

7.6 Josephus

```cpp
int josephus(int n, int k) {  //
    有n個人圍成一圈,每k個一次
  return n > 1 ? (josephus(n - 1, k) + k) % n : 0;
}  // 回傳最後一人的編號, 0 index
```

7.7 Catalan

$$C_0=1 \quad \text{and} \quad C_{n+1}=\frac{2(2n+1)}{n+2}C_n$$

```cpp
long long f[N] = {1}, i, t, p;
int main() {
  for (int i = 1; i <= 100; i++) {
    f[i] = f[i - 1] * (4 * i - 2) % mod;
    for (t = i + 1, p = mod - 2; p; t = (t * t) %
        mod, p >>= 1LL) {
      if (p & 1) {
        f[i] *= t;
        f[i] %= mod;
      }
    }
  }
}
```

8 Geometry

8.1 Point

```cpp
// notice point type!!!
using dvt = int;
const double EPS = 1e-6;
const double PI = acos(-1);

struct Pt {
  dvt x;
  dvt y;
};
bool operator < (const Pt &a, const Pt &b) {
  return a.x == b.x ? a.y < b.y : a.x < b.x;
}
bool operator == (const Pt &a, const Pt &b) {
  return a.x == b.x && a.y == b.y;
}
Pt operator + (const Pt &a, const Pt &b) {
```

```
  return {a.x + b.x, a.y + b.y};
}
Pt operator - (const Pt &a, const Pt &b) {
  return {a.x - b.x, a.y - b.y};
}
// multiply constant
Pt operator * (const Pt &a, const dvt c) {
  return {a.x * c, a.y * c};
}
Pt operator / (const Pt &a, const dvt c) {
  return {a.x / c, a.y / c};
}
// |a| x |b| x cos(x)
dvt iproduct(const Pt &a, const Pt &b) {
  return a.x * b.x + a.y * b.y;
}
// |a| x |b| x sin(x)
dvt cross(const Pt &a, const Pt &b) {
  return a.x * b.y - a.y * b.x;
}
dvt dis_pp(const Pt &a, const Pt, &b) {
  dvt dx = a.x - b.x;
  dvt dy = a.y - b.y;
  return sqrt(dx * dx, dy * dy);
}
```

8.2 Line

```
struct Line {
  Pt st;
  Pt ed;
};
// return point side
// left, on line, right -> 1, 0, -1
int side(Line l, Pt a) {
  dvt cross_val = cross(a - l.st, l.ed - l.st);
  if (cross_val > EPS) {
    return 1;
  } else if (cross_val < -EPS) {
    return -1;
  } else {
    return 0;
  }
}
// AB infinity, CD segment
bool has_intersection(Line AB, Line CD) {
  int c = side(AB, CD.st);
  int d = side(AB, CD.ed);
  if (c == 0 || d == 0) {
    return true;
  } else {
    // different side
    return c == -d;
  }
}
// find intersection point, two line, not seg
pair<int, Pt> intersection(Line a, Line b) {
  Pt A = a.ed - a.st;
  Pt B = b.ed - b.st;
  Pt C = b.st - a.st;
  dvt mom = cross(A, B);
  dvt son = cross(C, B);
  if (std::abs(mom) <= EPS) {
    if (std::abs(son) <= EPS) {
      return {1, {}}; // same line
    } else {
      return {2, {}}; // parallel
    }
  } else {            // ok
    return {0, a.st + A * (son / mom)};
  }
}
// line to point distance
dvt dis_lp(Line l, Pt a) {
  return area3x2(l.st, l.ed, a) / dis_pp(l.st, l.ed);
}
```

$$d(P, L) = \frac{|ax_0 + by_0 + c|}{\sqrt{a^2 + b^2}}$$

8.3 Area

```
// triangle
dvt area3(Pt a, Pt b, Pt c) {
  return std::abs(cross(b - a, c - a) / 2);
}
dvt area3x2(Pt a, Pt b, Pt c) { // for integer
  return std::abs(cross(b - a, c - a));
}
// simple convex area(can in)
dvt area(vector<Pt> &a) {
  dvt ret = 0;
  for (int i = 0, sz = a.size(); i < sz; i++) {
    ret += cross(a[i], a[(i + 1) % sz]);
  }
  return std::abs(ret) / 2;
}
// check point in/out a convex
int io_convex(vector<Pt> convex, Pt q) {
  // convex is Counterclockwise
  for (int i = 0, sz = convex.size(); i < sz; i++) {
    Pt cur = convex[i] - q;
    Pt nex = convex[(i + 1) % sz] - q;
    dvt cross_val = cross(cur, nex);
    if (std::abs(cross_val) <= EPS) {
      return 0;  // on edge
    }
    if (cross_val < 0) {
      return -1; // outside
    }
  }
  return 1;      // inside
}
```

8.4 Convex Hull

```
vector<Pt> convex_hull(vector<Pt> &a) {
  sort(a.begin(), a.end());
  a.erase(unique(a.begin(), a.end()), a.end());
  int sz = a.size(), m = 0;
  vector<Pt> ret(sz + 5); // safe 1 up
  for (int i = 0; i < sz; i++) {
    while (m > 1 &&
      cross(ret[m - 1] - ret[m - 2], a[i] - ret[m -
          2]) <= EPS) {
      m--;
    }
    ret[m++] = a[i];
  }
  int k = m;
  for (int i = sz - 2; i >= 0; i--) {
    while (m > k &&
      cross(ret[m - 1] - ret[m - 2], a[i] - ret[m -
          2]) <= EPS) {
      m--;
    }
    ret[m++] = a[i];
  }
  if (sz > 1) {
    m--;
  }
  ret.resize(m);
  return ret;
}
```