1.2

Default

Contents

```
1 #include <bits/stdc++.h>
 1 Basic
                                            using namespace std;
   using LL = long long;
                                           3
   #define IOS ios_base::sync_with_stdio(0); cin.tie(0);
   #define pb push_back
   #define eb emplace_back
   const int INF = 1e9;
   const int MOD = 1e9 + 7;
                                            const double EPS = 1e-6;
 2 Data Structure
                                            const int MAXN = 0;
   2.1 Disjoint Set
                                         2 11
   3 12 int main() {
   3
                                           13
                                           14 }
 3 Graph
                                         3
  3.1 Dijkstra . . . .
   1.3 Black Magic
   #include <bits/stdc++.h>
   #include <ext/pb_ds/assoc_container.hpp>
   3.7 LCA . . . .
   #include <ext/pb_ds/tree_policy.hpp>
                                            #include <ext/pb_ds/priority_queue.hpp>
 4 Connectivity
                                            using namespace std;
   6
                                            using namespace __gnu_pbds;
   using set_t =
   tree<int, null_type, less<int>, rb_tree_tag,
   tree_order_statistics_node_update>;
                                           10
                                            using map t =
 5 Flow & Matching
                                         q
   tree<int, int, less<int>, rb_tree_tag,
                                         9
                                           12
   9
                                               tree_order_statistics_node_update>;
   using heap_t =
   10
                                              __gnu_pbds::priority_queue<int>;
   using ht_t =
                                           15
   gp_hash_table<int, int>;
                                           17
                                            int main() {
 6 String
                                              //set-----
   set_t st;
                                           19
   st.insert(5); st.insert(6);
                                           20
  21
                                              st.insert(3); st.insert(1);
                                         12 22
 7 DP
                                              // the smallest is (0), biggest is (n-1), kth small
   is (k-1)
   int num = *st.find_by_order(0);
   cout << num << '\n'; // print 1
   num = *st.find_by_order(st.size() - 1);
 8 Math
                                              cout << num << '\n'; // print 6
                                           28
   // find the index
                                           30
   int index = st.order_of_key(6);
   cout << index << '\n'; // print 3

      8.6 Chinese Remainder Thm
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      <t
                                              // check if there exists x
  int x = 5;
  int check = st.erase(x);
                                              if (check == 0) printf("st not contain 5\n");
                                              else if (check == 1) printf("st contain 5\n");
                                           38
                                         15
 9 Geometry
                                           39
   15
                                           40
                                              //tree policy like set
   st.insert(5); st.insert(5);
   42
                                              cout << st.size() << '\n'; // print 4</pre>
   43
                                              //map------
                                           44
                                           45
                                              map_t mp;
    Basic
                                           46
                                              mp[1] = 2;
                                              cout << mp[1] << '\n';
                                           47
                                              auto tmp = *mp.find_by_order(0); // pair
cout << tmp.first << " " << tmp.second << '\n';</pre>
                                           48
 1.1 Run
                                           49
                                           50
                                           51
                                              //heap------
1 #use -> sh run.sh {name}
                                              heap_t h1, h2;
                                           52
2 g++ -02 -std=c++14 -Wall -Wextra -Wshadow -o $1 $1.cpp
                                              h1.push(1); h1.push(3);
                                           53
3 ./$1 < t.in > t.out
                                              h2.push(2); h2.push(4);
                                           55
                                              h1.join(h2);
```

```
56
    cout << h1.size() << h2.size() << h1.top() << '\n';</pre>
                                                                   double L = -1e5, R = 1e5;
                                                                   while (R - L > EPS) {
57
                                                               6
                                                               7
                                                                     double mr = (L + R) / 2.0;
58
    //hash-table-----
                                                                     double ml = (L + mr) / 2.0;
59
                                                               8
60
    ht_t ht;
                                                               9
                                                                     if (f(ml) < f(mr)) {
61
    ht[85] = 5;
                                                              10
                                                                       R = mr;
    ht[89975] = 234;
                                                                     } else {
62
                                                              11
    for (auto i : ht) {
                                                              12
                                                                       L = m1;
       cout << i.first << " " << i.second << '\n';</pre>
64
                                                              13
                                                                   }
65
                                                              14
66 }
                                                              15
                                                                   return L;
                                                              16 }
```

1.4 Python

```
1 ### EOF
2 while True:
3
    try:
      pass
4
    except EOFError:
5
6
      break
7 ###math
8 import math
10 math.ceil(x)#上高斯
11 math.floor(x)#下高斯
12 math.factorial(x)#接乘
13 math.fabs(x)#絕對值
14 math.fsum(arr)#跟sum一樣但更精確(小數點問題)
15 math.gcd(x, y)#bj4
16 math.exp(x)#e^x
17 math.log(x, base)
18 math.log2(x)#2為底
19 math.log10(x)#10為底
20 math.sqrt(x)
21 math.pow(x, y, mod)#精確些(float型態) MOD!!!
22 math.sin(x)# cos tan asin acos atan atan2(弧度) sinh
      cosh tanh acosh asinh atanh
23 math.hypot(x, y)#歐幾里德範數
24 math.degrees(x)#x從弧度轉角度
25 math.radians(x)#x從角度轉弧度
26 math.gamma(x)#x的gamma函數
27 math.pi#常數
28 math.e#常數
29 math.inf
30
31 ### ascii
32 ord(x)#char to asc
33 chr(x)#asc to char
35 x.encode().hex()#string to hex
36 ### reverse string
37 string = "abc"
38 string_reverse = string[::-1]
```

1.5 Binary Search

1.6 Ternary Search

```
const double EPS = 1e-6;
// target function
double f(double x) { return x * x; }
double ternarySearch() {
```

2 Data Structure

2.1 Disjoint Set

```
1 // 0-base
2 const int MAXN = 1000;
3 int boss[MAXN];
  void init(int n) {
    for (int i = 0; i < n; i++) {</pre>
       boss[i] = -1;
    }
7
8 }
9
  int find(int x) {
10
    if (boss[x] < 0) {
11
      return x;
12
13
     return boss[x] = find(boss[x]);
  }
14
15
  bool uni(int a, int b) {
    a = find(a);
16
     b = find(b);
17
     if (a == b) {
18
19
      return false;
20
     if (boss[a] > boss[b]) {
21
22
       swap(a, b);
23
24
     boss[a] += boss[b];
25
     boss[b] = a;
26
     return true;
27 }
```

2.2 BIT RARSQ

```
1 // 1-base
  #define lowbit(k) (k & -k)
4
  int n;
5
  vector<int> B1, B2;
  void add(vector<int> &tr, int id, int val) {
    for (; id <= n; id += lowbit(id)) {</pre>
8
9
      tr[id] += val;
    }
10
11 }
12 void range_add(int 1, int r, int val) {
    add(B1, 1, val);
13
14
    add(B1, r + 1, -val);
    add(B2, 1, val * (1 - 1));
15
16
    add(B2, r + 1, -val * r);
17 }
18 int sum(vector<int> &tr, int id) {
19
    int ret = 0;
    for (; id >= 1; id -= lowbit(id)) {
20
21
      ret += tr[id];
    }
22
23
    return ret;
24 }
25 int prefix_sum(int id) {
```

```
26     return sum(B1, id) * id - sum(B2, id);
27     }
28     int range_sum(int 1, int r) {
29         return prefix_sum(r) - prefix_sum(1 - 1);
30     }

2.3     zkw RMQ
```

```
1 // 0-base
2 const int INF = 1e9;
3 const int MAXN = ;
5 int n;
6 int a[MAXN], tr[MAXN << 1];</pre>
8 // !!! remember to call this function
  void build() {
    for (int i = 0; i < n; i++) {</pre>
10
11
      tr[i + n] = a[i];
12
    for (int i = n - 1; i > 0; i--) {
13
      tr[i] = max(tr[i << 1], tr[i << 1 | 1]);
14
15
16 }
17 void update(int id, int val) {
    for (tr[id += n] = val; id > 1; id >>= 1) {
18
19
      tr[id >> 1] = max(tr[id], tr[id ^ 1]);
    }
20
21 }
22 int query(int 1, int r) { // [1, r)
    int ret = -INF;
23
24
     for (1 += n, r += n; 1 < r; 1 >>= 1, r >>= 1) {
      if (1 & 1) {
25
26
         ret = max(ret, tr[1++]);
      }
27
28
      if (r & 1) {
29
         ret = max(ret, tr[--r]);
30
31
    }
32
     return ret;
```

2.4 Segment Tree RARMQ

33 }

```
1 struct Node {
2
     int val, tag;
3
    Node *lc, *rc;
     Node() : lc(nullptr), rc(nullptr), tag(0) {}
     void pull() {
       if (!1c) {
6
7
         val = rc->val;
       } else if (!rc) {
8
         val = lc->val;
9
       } else {
10
11
         val = max(lc->val, rc->val);
       }
12
13
    }
14
     void push() {
15
       if (lc) {
16
         lc->tag += tag;
17
         lc->val += tag;
18
19
       if (rc) {
         rc->tag += tag;
20
21
         rc->val += tag;
       }
22
23
       tag = 0;
24
    }
25 }:
26 struct SegmentTree {
27
     Node *root;
28
     SegmentTree() : root(nullptr) {}
29
     void build(Node* &T, int 1, int r, const
         vector<int> &o) {
```

```
30
       T = new Node();
       if (1 == r) {
31
         T->val = o[1];
32
         return;
33
34
35
       int mid = (1 + r) / 2;
       build(T->lc, l, mid, o);
36
37
       build(T->rc, mid + 1, r, o);
38
       T->pull();
39
40
     void update(Node* &T, int 1, int r, int q1, int qr,
         int v) {
41
       if (ql <= 1 && r <= qr) {</pre>
         T->val += v;
42
43
         T->tag += v;
44
         return;
45
       }
46
       T->push();
47
       int mid = (1 + r) / 2;
       if (qr <= mid) {
48
         update(T->lc, 1, mid, ql, qr, v);
49
50
       } else if (mid < ql) {</pre>
51
         update(T->rc, mid + 1, r, ql, qr, v);
52
       } else {
53
         update(T->lc, 1, mid, ql, mid, v);
         update(T->rc, mid + 1, r, mid + 1, qr, v);
54
55
       T->pull();
56
57
58
     int query(Node* &T, int 1, int r, int q1, int qr) {
       if (ql <= 1 && r <= qr) {</pre>
59
60
         return T->val;
61
62
       T->push();
63
       int mid = (1 + r) / 2;
64
       if (qr <= mid) {
65
         return query(T->lc, 1, mid, ql, qr);
       } else if (mid < ql) {</pre>
66
67
         return query(T->rc, mid + 1, r, ql, qr);
68
       } else {
69
         return max(query(T->lc, 1, mid, ql, mid),
70
              query(T->rc, mid + 1, r, mid + 1, qr));
71
72
    }
73 };
```

3 Graph

3.1 Dijkstra

```
1 // 0-base
  const LL INF = 1e18;
   const int MAXN = ;
 4
   struct Edge {
    int to;
    LL cost;
     Edge(int \ v, \ LL \ c) \ : \ to(v), \ cost(c) \ \{\}
     bool operator < (const Edge &other) const {</pre>
9
       return cost > other.cost;
10
    }
11 \ \ \ ;
12
13
   int n;
14 LL dis[MAXN];
15 vector < Edge > G[MAXN];
16
17
   void init() {
     for (int i = 0; i < n; i++) {
18
       G[i].clear();
19
       dis[i] = INF;
20
21
    }
22
23
   void Dijkstra(int st, int ed = -1) {
   priority_queue < Edge > pq;
```

```
25
     pq.emplace(st, 0);
     dis[st] = 0:
26
27
     while (!pq.empty()) {
28
       auto now = pq.top();
29
       pq.pop();
30
       if (now.to == ed) {
31
         return:
32
       if (now.cost > dis[now.to]) {
33
34
         continue;
35
       for (auto &e : G[now.to]) {
36
37
         if (dis[e.to] > now.cost + e.cost) {
           dis[e.to] = now.cost + e.cost;
38
39
           pq.emplace(e.to, dis[e.to]);
40
41
       }
42
    }
43 }
```

3.2 SPFA(negative cycle)

```
1 // 0-base
2 const LL INF = 1e18;
3 const int MAXN = ;
 4 struct Edge {
    int to;
6
    LL cost;
7
     Edge(int v, LL c) : to(v), cost(c) {}
8 };
10 int n;
11 LL dis[MAXN];
12 vector < Edge > G[MAXN];
13
14 void init() {
    for (int i = 0; i < n; i++) {</pre>
15
16
       G[i].clear();
       dis[i] = INF;
17
18
    }
19 }
20 bool SPFA(int st) {
21
    vector<int> cnt(n, 0);
     vector < bool > inq(n, false);
22
23
     queue < int > q;
24
     q.push(st);
25
     dis[st] = 0;
26
     inq[st] = true;
27
     while (!q.empty()) {
28
29
       int now = q.front();
30
       q.pop();
       inq[now] = false;
31
       for (auto &e : G[now]) {
32
         if (dis[e.to] > dis[now] + e.cost) {
33
34
            dis[e.to] = dis[now] + e.cost;
           if (!inq[e.to]) {
35
36
              cnt[e.to]++;
37
              if (cnt[e.to] > n) {
38
                // negative cycle
39
                return false;
40
41
              inq[e.to] = true;
              q.push(e.to);
42
43
           }
         }
44
45
       }
     }
46
47
     return true;
48 }
```

3.3 Floyd Warshall

```
1 // 0-base
  // G[i][i] < 0 -> negative cycle
  const LL INF = 1e18;
  const int MAXN = ;
 6
  int n;
7
  LL G[MAXN][MAXN];
  void init() {
9
    for (int i = 0; i < n; i++) {</pre>
10
11
       for (int j = 0; j < n; j++) {
         G[i][j] = INF;
12
13
       }
       G[i][i] = 0;
14
15
    }
16 }
17
  void floyd() {
18
     for (int k = 0; k < n; k++) {
       for (int i = 0; i < n; i++) {</pre>
19
20
         for (int j = 0; j < n; j++) {
           if (G[i][k] != INF && G[k][j] != INF) {
21
22
             G[i][j] = min(G[i][j], G[i][k] + G[k][j]);
           }
23
24
         }
25
    }
26
27 }
```

3.4 Topological Sort

```
// 0-base
  // if ret.size < n -> cycle
  int n;
  vector<vector<int>> G;
  vector<int> topoSort() {
 6
     vector<int> indeg(n), ret;
7
     for (auto &li : G) {
9
       for (int x : li) {
10
         ++indeg[x];
11
       }
    }
12
13
     // use priority queue for lexic. largest ans
14
     queue<int> q;
15
     for (int i = 0; i < n; i++) {
16
       if (!indeg[i]) {
17
         q.push(i);
18
       }
     }
19
20
     while (!q.empty()) {
21
       int u = q.front();
       q.pop();
22
23
       ret.pb(u);
       for (int v : G[u]) {
24
25
         if (--indeg[v] == 0) {
26
           q.push(v);
27
28
       }
    }
29
30
     return ret;
31 }
```

3.5 Tree Diameter

```
1 // 0-base;
2 const int MAXN = ;
3
4 struct Edge {
5   int to;
6   int cost;
7   Edge(int v, int c) : to(v), cost(c) {}
8 };
9
```

```
10 | int n, d = 0;
                                                                 52
                                                                          in[root] = 0;
11 int d1[MAXN], d2[MAXN];
                                                                 53
12 vector < Edge > G[MAXN];
                                                                          // find cycles
                                                                 54
13 // dfs(0, -1);
                                                                 55
                                                                          for (int i = 0; i < n; i++) {</pre>
14 void dfs(int u, int from) {
                                                                 56
                                                                            ret += in[i];
15
     d1[u] = d2[u] = 0;
                                                                 57
                                                                             int v = i;
     for (auto e : G[u]) {
                                                                             while (vis[v] != i && id[v] == -1 && v !=
16
                                                                 58
17
       if (e.to == from) {
                                                                                 root) {
                                                                               vis[v] = i;
18
         continue;
                                                                 59
19
                                                                 60
                                                                               v = pre[v];
20
       dfs(e.to, u);
                                                                 61
       int t = d1[e.to] + e.cost;
                                                                            if (id[v] == -1 && v != root) {
21
                                                                 62
22
       if (t > d1[u]) {
                                                                 63
                                                                               for (int j = pre[v]; j != v; j = pre[j]) {
                                                                                id[j] = nodenum;
23
         d2[u] = d1[u];
                                                                 64
24
         d1[u] = t;
                                                                 65
       } else if (t > d2[u]) {
                                                                              id[v] = nodenum++;
25
                                                                 66
         d2[u] = t;
                                                                 67
                                                                            }
26
                                                                          }
27
                                                                 68
     }
                                                                 69
28
29
     d = max(d, d1[u] + d2[u]);
                                                                 70
                                                                          // no cycle
                                                                          if (nodenum == 0) {
30 }
                                                                 71
                                                                 72
                                                                            break;
                                                                 73
                                                                 74
  3.6 Directed MST
                                                                 75
                                                                          for (int i = 0; i < n; i++) {</pre>
                                                                            if (id[i] == -1) {
                                                                 76
1 // 0-base
                                                                 77
                                                                              id[i] = nodenum++;
2 const LL INF = 1e18;
                                                                            }
                                                                 78
3 const int MAXN = ;
                                                                 79
                                                                 80
5 struct Edge {
                                                                          // grouping the vertices
                                                                 81
    int from;
6
                                                                 82
                                                                          for (auto &e : edges) {
     int to;
                                                                            int to = e.to;
                                                                 83
     LL cost:
8
                                                                 84
                                                                            e.from = id[e.from];
9
     Edge(int u, int v, LL c) : from(u), to(v), cost(c)
                                                                             e.to = id[e.to];
                                                                 85
         {}
                                                                 86
                                                                            if (e.from != e.to) {
10 }:
                                                                 87
                                                                              e.cost -= in[to]; //!!!
11
                                                                            }
                                                                 88
12 struct DMST {
                                                                 89
13
    int n;
                                                                 90
     int vis[MAXN], pre[MAXN], id[MAXN];
14
                                                                          n = nodenum;
15
     LL in[MAXN]:
                                                                 92
                                                                          root = id[root];
16
     vector < Edge > edges;
                                                                 93
     void init(int _n) {
17
                                                                 94
                                                                        return ret;
       n = _n;
18
                                                                     }
                                                                 95
19
       edges.clear();
                                                                 96 };
20
21
     void add_edge(int from, int to, LL cost) {
22
       edges.eb(from, to, cost);
23
                                                                    3.7 LCA
     LL run(int root) {
24
25
       LL ret = 0;
       while (true) {
                                                                  1 const int LOG = 20;
26
         for (int i = 0; i < n; i++) {</pre>
                                                                 2 vector<int> tin(MAXN), tout(MAXN), depth(MAXN);
27
28
           in[i] = INF;
                                                                  3 int par[MAXN][LOG];
                                                                    int timer = 0;
29
30
                                                                    vector<int> G[MAXN];
         // find in edge
31
         for (auto &e : edges) {
                                                                    void dfs(int u, int f) {
32
33
           if (e.cost < in[e.to] && e.from != e.to) {</pre>
                                                                  8
                                                                      tin[u] = ++timer;
                                                                      par[u][0] = f;
34
              pre[e.to] = e.from;
                                                                 9
35
              in[e.to] = e.cost;
                                                                 10
                                                                      for (int v : G[u]) {
                                                                        if (v != f) {
           }
36
                                                                 11
37
                                                                 12
                                                                          depth[v] = depth[u] + 1;
38
                                                                 13
                                                                          dfs(v, u);
         // check in edge
                                                                 14
39
40
         for (int i = 0; i < n; i++) {</pre>
                                                                 15
           if (i == root) {
41
                                                                 16
                                                                      tout[u] = ++timer;
42
             continue;
                                                                 17 }
           }
43
                                                                 18
           if (in[i] == INF) {
                                                                 19
                                                                    void Doubling(int n) {
44
45
              return -1;
                                                                 20
                                                                      for (int j = 1; j < LOG; ++j) {
                                                                        for (int i = 1; i <= n; ++i) {</pre>
                                                                 21
46
47
         }
                                                                 22
                                                                          par[i][j] = par[par[i][j - 1]][j - 1];
48
                                                                 23
49
         int nodenum = 0;
                                                                 24
```

25 }

26

memset(id, -1, sizeof(id));

memset(vis, -1, sizeof(vis));

50

51

```
H2J
                                                              FJCU
27 bool anc(int u, int v) { return tin[u] <= tin[v] &&
                                                               25
       tout[v] <= tout[u]; }</pre>
                                                                     void dfs(int v) {
                                                               26
                                                               27
28
29 int LCA(int u, int v) {
                                                               28
30
    if (depth[u] > depth[v]) {
                                                               29
31
       swap(u, v);
                                                               30
                                                                           dfs(i.second);
32
                                                               31
33
    if (anc(u, v)) {
                                                               32
                                                                         }
       return u;
                                                               33
34
                                                                      }
                                                                    }
35
                                                               34
36
    for (int j = LOG - 1; j >= 0; --j) {
                                                               35
       if (!anc(par[u][j], v)) u = par[u][j];
37
                                                               36
                                                               37
                                                                       edges.PB(true);
38
39
    return par[u][0];
                                                               38
40 }
                                                               39
41
                                                               40
42 int dis(int u, int v) {
                                                               41
43
    int lca = LCA(u, v);
                                                               42
                                                                       chk[from]++;
    return depth[u] + depth[v] - 2 * depth[lca];
                                                               43
                                                                      chk[to]++;
44
45 }
                                                               44
46
                                                               45
47 /*
                                                                46
48 dfs(root, root);
                                                               47
                                                                       // check[from]++;
49 Doubling(n);
                                                               48
                                                               49
50 */
                                                                    bool eular_path() {
                                                               50
                                                                      int st = -1;
                                                               52
  3.8 Euler Circuit
                                                                53
                                                                           st = i;
  七橋問題根據起點與終點是否相同,分成 Euler path(不同)及 Euler circuit(相
                                                                           break;
                                                                55
                                                                         }
                                                               57
                                                                      }
     • 判斷法
                                                               58
                                                                       if (st == -1) {
     · 無向圖部分,將點分成奇點(度數為奇數)和偶點(度數為偶數)。
                                                               59
                                                                         return false;
                                                               60
          - Euler path: 奇點數為 0 或 2
                                                               61
                                                                       dfs(st);
          - Euler circuit:沒有奇點
                                                               62
                                                                       return true;
```

- · 有向圖部分,將點分成出點(出度 入度 = 1)和入點(入度 出度 = 1)還 有平衡點(出度 = 入度)。
 - Euler path:出點和入點個數同時為 0 或 1。
 - Euler circuit:只有平衡點。
- 求出一組解
- 用 DFS 遍歷整張圖,設 S 為離開的順序,無向圖的答案為 S ,有向圖的答案 為反向的 s 。
- · DFS 起點選定:
 - Euler path:無向圖選擇任意一個奇點,有向圖選擇出點。
 - Euler circuit:任意一點。

```
1 // Code from Eric
2 #define ll long long
3 #define PB push_back
4 #define EB emplace_back
5 #define PII pair<int, int>
6 #define MP make_pair
7 #define all(x) x.begin(), x.end()
8 #define maxn 50000+5
10 //structure
11 struct Eular {
    vector<PII> adj[maxn];
12
13
    vector<bool> edges;
    vector < PII > path;
14
15
    int chk[maxn];
16
    int n;
17
18
    void init(int _n) {
19
      n = n:
       for (int i = 0; i <= n; i++) adj[i].clear();</pre>
20
       edges.clear();
21
22
       path.clear();
23
       memset(chk, 0, sizeof(chk));
24
```

30 }

```
for (auto i : adj[v]) {
        if (edges[i.first] == true) {
           edges[i.first] = false;
           path.EB(MP(i.second, v));
    void add_Edge(int from, int to) {
       // for bi-directed graph
      adj[from].PB(MP(edges.size() - 1, to));
      adj[to].PB(MP(edges.size() - 1, from));
       // for directed graph
      // adj[from].PB(MP(edges.size()-1, to));
      for (int i = 1; i <= n; i++) {
        if (chk[i] % 2 == 1) {
63
64
    void print_path(void) {
65
      for (auto i : path) {
66
        printf("%d %d\n", i.first, i.second);
67
68
    }
69
70 };
1 // Code from allen(lexicographic order)
2 #include <bits/stdc++.h>
  using namespace std;
  const int ALP = 30;
  const int MXN = 1005;
  int n;
  int din[ALP], dout[ALP];
  int par[ALP];
  vector<string> vs[MXN], ans;
9
10
  bitset<MXN> vis, used[ALP];
11
  void djsInit() {
12
    for (int i = 0; i != ALP; ++i) {
13
      par[i] = i;
14
15
16 }
17
18
  int Find(int x) { return (x == par[x] ? (x) : (par[x]
       = Find(par[x])); }
19
20 void init() {
    djsInit();
    memset(din, 0, sizeof(din));
22
23
    memset(dout, 0, sizeof(dout));
    vis.reset();
24
    for (int i = 0; i != ALP; ++i) {
25
       vs[i].clear();
26
27
      used[i].reset();
28
29
    return;
```

6

```
31
   void dfs(int u) {
32
     for (int i = 0; i != (int)vs[u].size(); ++i) {
34
       if (used[u][i]) {
35
         continue;
36
       used[u][i] = 1;
37
38
       string s = vs[u][i];
       int v = s[s.size() - 1] - 'a';
39
40
       dfs(v);
41
       ans.push_back(s);
    }
42
43 }
44
45 bool solve() {
    int cnt = 1;
46
47
     for (int i = 0; i != n; ++i) {
48
       string s;
       cin >> s;
49
       int from = s[0] - 'a', to = s.back() - 'a';
50
51
       ++din[to];
52
       ++dout[from];
53
       vs[from].push_back(s);
       vis[from] = vis[to] = true;
54
55
       if ((from = Find(from)) != (to = Find(to))) {
         par[from] = to;
56
57
         ++cnt;
       }
58
59
     }
60
     if ((int)vis.count() != cnt) {
       return false;
61
62
     int root, st, pin = 0, pout = 0;
63
     for (int i = ALP - 1; i >= 0; --i) {
64
65
       sort(vs[i].begin(), vs[i].end());
       if (vs[i].size()) root = i;
66
67
       int d = dout[i] - din[i];
       if (d == 1) {
68
69
         ++pout;
70
         st = i;
71
       } else if (d == -1) {
72
         ++pin;
       } else if (d != 0) {
73
74
         return false;
75
76
77
     if (pin != pout || pin > 1) {
       return false;
78
79
80
     ans.clear();
81
     dfs((pin ? st : root));
82
     return true;
83 }
84
85 int main() {
86
    int t;
87
     cin >> t;
88
     while (t--) {
89
       cin >> n;
       init():
90
91
       if (!solve()) {
         cout << "***\n";
92
93
         continue;
94
95
       for (int i = ans.size() - 1; i >= 0; --i) {
96
         cout << ans[i] << ".\n"[i == 0];
97
98
99 }
```

4 Connectivity

4.1 Kosaraju SCC

```
1 // 0-base
 2 int n:
  vector<vector<int>> G, G2; // G2 = G rev
  vector<bool> vis;
  vector<int> s, color;
  int sccCnt;
  void dfs1(int u) {
     vis[u] = true;
     for (int v : G[u]) {
9
10
      if (!vis[v]) {
11
         dfs1(v);
       }
12
13
    }
14
     s.pb(u);
15 }
16 void dfs2(int u) {
17
     color[u] = sccCnt;
18
     for (int v : G2[u]) {
19
      if (!color[v]) {
20
         dfs2(v);
       }
21
22
    }
23 }
24
  void Kosaraju() {
25
     sccCnt = 0;
26
     for (int i = 0; i < n; i++) {
       if (!vis[i]) {
27
28
         dfs1(i);
29
30
     for (int i = n - 1; i >= 0; i--) {
31
32
       if (!color[s[i]]) {
33
         ++sccCnt;
34
         dfs2(s[i]);
35
36
    }
37 }
```

4.2 BCC

```
1 typedef pair<int, int> PII;
2 int low[MXV], depth[MXV];
 3 bool is_cut_vertex[MXV], visit[MXV];
  vector<int> G[MXV];
  vector < PII > BCC[MXV];
  int bcc_cnt = 0;
  stack<PII> st;
  vector<pair<int, int>> my_cut_edge;
9
10
  void dfs(int now, int cur_depth, int f) {
11
     visit[now] = true;
12
     depth[now] = low[now] = cur_depth;
13
     int cut_son = 0;
14
15
     for (auto i : G[now]) {
       if (i == f) continue;
16
17
       if (visit[i]) { // ancestor
         if (depth[i] < depth[now]) { // #</pre>
18
           low[now] = min(low[now], depth[i]);
19
20
           st.push({now, i});
21
22
       } else { // offspring
23
         st.push({now, i});
         dfs(i, cur_depth + 1, now);
24
25
         cut_son += 1;
         low[now] = min(low[now], low[i]);
26
27
         if (low[i] >= depth[now]) {
28
           is_cut_vertex[now] = true;
29
           auto t = st.top();
           st.pop();
30
           while (t != make_pair(now, i)) {
31
             BCC[bcc_cnt].push_back(t);
32
33
             t = st.top();
34
             st.pop();
35
           BCC[bcc_cnt].push_back(t);
36
```

```
37
           ++bcc_cnt;
         }
38
         // ###
39
         if (low[i] > depth[now])
40
41
           my_cut_edge.push_bach({now, i});
42
    }
43
44
     if (cur_depth == 0)
45
       is_cut_vertex[now] = (cut_son != 1);
46
     return;
47 }
48
49 bool is_2_edge_connected(int n) {
     memset(visit, 0, sizeof(visit));
50
51
     dfs(1, 0, -1);
    return my_cut_edge.size() == 0;
52
53 }
```

4.3 Articulation Point

1 // from aizu

```
2 typedef long long int 11;
3 typedef unsigned long long int ull;
4 #define BIG_SIZE 2000000000
5 #define MOD 1000000007
6 #define EPS 0.000000001
7 using namespace std;
9 #define SIZE 100000
10
11 vector<int> G[SIZE];
12 int N;
13 bool visited[SIZE];
14 int visited_order[SIZE], parent[SIZE], lowest[SIZE],
16 void dfs(int cur, int pre_node) {
     visited_order[cur] = lowest[cur] = number;
17
18
    number++;
19
20
     visited[cur] = true;
21
22
23
24
     for (int i = 0; i < G[cur].size(); i++) {</pre>
25
       next = G[cur][i];
       if (!visited[next]) {
26
27
         parent[next] = cur;
28
         dfs(next, cur);
29
         lowest[cur] = min(lowest[cur], lowest[next]);
       } else if (visited[next] == true && next !=
30
           pre_node) {
         lowest[cur] = min(lowest[cur],
31
              visited_order[next]);
32
33
    }
34 }
35
36 void art_points() {
37
     for (int i = 0; i < N; i++) visited[i] = false;</pre>
38
39
     number = 1;
40
     dfs(0, -1);
41
42
     int tmp_parent, root_num = 0;
43
     vector<int> V;
45
46
     for (int i = 1; i < N; i++) {</pre>
47
       tmp_parent = parent[i];
       if (tmp_parent == 0) {
48
49
         root_num++;
50
       } else if (visited_order[tmp_parent] <=</pre>
           lowest[i]) {
51
         V.push_back(tmp_parent);
52
```

```
53
     if (root num >= 2) {
54
55
       V.push_back(0);
    }
56
57
     sort(V.begin(), V.end());
58
     V.erase(unique(V.begin(), V.end()), V.end());
59
60
     for (int i = 0; i < V.size(); i++) {</pre>
       printf("%d\n", V[i]);
61
62
63 }
64
65 int main() {
66
     int E;
67
     scanf("%d %d", &N, &E);
     int from, to;
68
69
     for (int i = 0; i < E; i++) {
       scanf("%d %d", &from, &to);
70
71
       G[from].push_back(to);
72
       G[to].push_back(from);
    }
73
74
     art_points();
75 }
```

4.4 Bridges

```
1 // from aizu
2 typedef long long int 11;
  typedef unsigned long long int ull;
  #define BIG_NUM 200000000
  #define MOD 1000000007
  #define EPS 0.00000001
  using namespace std;
  struct Edge {
9
    bool operator<(const struct Edge &arg) const {</pre>
10
       if (s != arg.s) {
11
12
         return s < arg.s;</pre>
       } else {
13
14
         return t < arg.t;</pre>
15
    }
16
17
    int s, t;
18 };
19
  struct Info {
20
    Info(int arg_to, int arg_edge_id) {
21
       to = arg to:
22
       edge_id = arg_edge_id;
    }
23
24
    int to, edge_id;
25 };
26
  int V, E, number;
  int order[100000], lowlink[100000];
28
29
  bool visited[100000];
30
  Edge edge[100000];
  vector < Info > G[100000];
32
  void recursive(int cur) {
33
    order[cur] = number++;
34
35
    lowlink[cur] = order[cur];
36
37
    int next;
38
39
     for (int i = 0; i < G[cur].size(); i++) {</pre>
       next = G[cur][i].to;
40
41
       if (order[next] == -1) {
42
43
         visited[G[cur][i].edge_id] = true;
44
         recursive(next);
45
         lowlink[cur] = min(lowlink[cur], lowlink[next]);
46
47
       } else if (visited[G[cur][i].edge_id] == false) {
48
         lowlink[cur] = min(lowlink[cur], order[next]);
49
    }
50
```

```
51 }
52
53 int main() {
     scanf("%d %d", &V, &E);
55
     for (int i = 0; i < E; i++) {
       scanf("%d %d", &edge[i].s, &edge[i].t);
56
       if (edge[i].s > edge[i].t) {
57
58
         swap(edge[i].s, edge[i].t);
59
60
       G[edge[i].s].push_back(Info(edge[i].t, i));
61
       G[edge[i].t].push_back(Info(edge[i].s, i));
62
63
     sort(edge, edge + E);
64
65
     number = 0;
66
67
     for (int i = 0; i < V; i++) {
68
       order[i] = -1;
69
       lowlink[i] = -1;
70
     for (int i = 0; i < E; i++) {</pre>
71
72
       visited[i] = false;
73
74
75
     recursive(0);
76
77
     int from, to;
78
     for (int i = 0; i < E; i++) {
       from = edge[i].s;
79
80
       to = edge[i].t;
       if (order[edge[i].s] > order[edge[i].t]) {
81
82
         swap(from, to);
83
84
       if (order[from] < lowlink[to]) {</pre>
         printf("%d %d\n", edge[i].s, edge[i].t);
85
86
87
     }
88
     return 0;
89 }
```

5 Flow & Matching

5.1 Relation

```
1 | 1. 一般圖
2 | 1最大匹配 | + 1最小邊覆蓋 | = |V|
3 | 1最大獨立集 | + 1最小點覆蓋 | = |V|
4 | 1最大圖 | = |補圖的最大獨立集 |
5 | 2. 二分圖
6 | 1最大匹配 | = |最小點覆蓋 |
7 | 1最大獨立集 | = |日小邊覆蓋 |
8 | 1最大獨立集 | = |V| - |最大匹配 |
9 | 1最大圖 | = |補圖的最大獨立集 |
```

5.2 Bipartite Matching

```
1 // 0-base
2 const int MAXN = ;
3 int n;
4 vector<int> G[MAXN];
5 int vy[MAXN], my[MAXN];
7 bool match(int u) {
8
    for (int v : G[u]) {
9
      if (vy[v]) {
10
         continue;
11
12
      vy[v] = true;
13
       if (my[v] == -1 || match(my[v])) {
14
         my[v] = u;
         return true;
15
```

```
16
    }
17
     return false;
18
19 }
20 int sol() {
21
    int cnt = 0;
    memset(my, -1, sizeof(my));
22
23
     for (int i = 0; i < n; i++) {
      memset(vy, 0, sizeof(vy));
24
       if (match(i)) {
25
26
         cnt++;
27
28
    }
29
     return cnt;
30 }
```

9

5.3 KM

```
1 const int INF = 1e9;
  const int MAXN = ;
  struct KM { //1-base
     int n, G[MAXN][MAXN];
     int lx[MAXN], ly[MAXN], my[MAXN];
     bool vx[MAXN], vy[MAXN];
 7
     void init(int _n) {
 8
       n = _n;
       for (int i = 1; i <= n; i++) {</pre>
9
         for (int j = 1; j <= n; j++) {</pre>
10
11
           G[i][j] = 0;
12
         }
       }
13
14
15
     bool match(int i) {
16
       vx[i] = true;
17
       for (int j = 1; j <= n; j++) {
         if (lx[i] + ly[j] == G[i][j] && !vy[j]) {
18
            vy[j] = true;
19
20
            if (!my[j] || match(my[j])) {
21
              my[j] = i;
22
              return true;
23
         }
24
25
       }
26
       return false;
27
28
     void update() {
       int delta = INF;
29
30
       for (int i = 1; i <= n; i++) {
         if (vx[i]) {
31
           for (int j = 1; j <= n; j++) {</pre>
32
33
              if (!vy[j]) {
                delta = min(delta, lx[i] + ly[j] -
34
                    G[i][j]);
35
36
           }
         }
37
38
39
       for (int i = 1; i <= n; i++) {
40
         if (vx[i]) {
41
           lx[i] -= delta;
42
43
         if (vy[i]) {
44
           ly[i] += delta;
45
46
     }
47
48
     int run() {
       for (int i = 1; i <= n; i++) {
49
50
         lx[i] = ly[i] = my[i] = 0;
51
         for (int j = 1; j <= n; j++) {
52
           lx[i] = max(lx[i], G[i][j]);
53
         }
54
55
       for (int i = 1; i <= n; i++) {
56
         while (true) {
           for (int i = 1; i <= n; i++) {</pre>
```

```
58
               vx[i] = vy[i] = 0;
                                                                         58
59
                                                                         59
             if (match(i)) {
                                                                         60
60
61
               break;
                                                                         61
62
             } else {
                                                                         62
63
               update();
                                                                         63
64
                                                                         64
65
          }
                                                                         65
        }
66
                                                                         66
        int ans = 0;
67
                                                                         67
68
        for (int i = 1; i <= n; i++) {</pre>
                                                                         68
          ans += lx[i] + ly[i];
                                                                         69
69
70
                                                                         70
71
                                                                         71
        return ans;
72
                                                                         72
73 };
                                                                         73
                                                                         74
                                                                         75 };
```

5.4 Dinic

5.5 MCMF

}

return ret;

}

if (!ret) {

return ret;

LL ret = 0;

return ret;

level[u] = -1;

LL flow(int st, int ed) {

while (bfs(st, ed)) {

fill(now, now + n + 1, 0);

ret += dfs(st, ed, INF);

}

}

```
1 #define eb emplace_back
2 const LL INF = 1e18;
3 const int MAXN = ;
 4 struct Edge {
    int to;
6
    LL cap;
7
     int rev:
    Edge(int v, LL c, int r) : to(v), cap(c), rev(r) {}
8
9 };
10 struct Dinic {
11
    int n;
     int level[MAXN], now[MAXN];
12
     vector < Edge > G[MAXN];
13
     void init(int _n) {
14
15
       n = _n;
       for (int i = 0; i <= n; i++) {</pre>
16
17
         G[i].clear();
       }
18
19
     void add_edge(int u, int v, LL c) {
20
       G[u].eb(v, c, G[v].size());
21
22
       // directed graph
       G[v].eb(u, 0, G[u].size() - 1);
23
       // undirected graph
24
25
       // G[v].eb(u, c, G[u].size() - 1);
26
27
     bool bfs(int st, int ed) {
       fill(level, level + n + 1, -1);
28
29
       queue < int > q;
30
       q.push(st);
31
       level[st] = 0;
32
       while (!q.empty()) {
         int u = q.front();
33
         q.pop();
34
         for (const auto &e : G[u]) {
35
36
           if (e.cap > 0 && level[e.to] == -1) {
             level[e.to] = level[u] + 1;
37
             q.push(e.to);
38
39
           }
         }
40
41
       }
42
       return level[ed] != -1;
43
44
     LL dfs(int u, int ed, LL limit) {
45
       if (u == ed) {
46
         return limit;
47
48
       LL ret = 0;
       for (int &i = now[u]; i < G[u].size(); i++) {</pre>
49
50
         auto &e = G[u][i];
51
         if (e.cap > 0 && level[e.to] == level[u] + 1) {
           LL f = dfs(e.to, ed, min(limit, e.cap));
52
           ret += f;
53
54
           limit -= f;
55
           e.cap -= f;
56
           G[e.to][e.rev].cap += f;
           if (!limit) {
57
```

```
1 // 0-base
 2 const LL INF = 1e18;
  const int MAXN = ;
  struct Edge {
    int u, v;
    LL cost;
     LL cap;
     Edge(int _u, int _v, LL _c, LL _cap) : u(_u),
         v(_v), cost(_c), cap(_cap) {}
 9
  };
  struct MCMF {
                     // inq times
10
    int n, pre[MAXN], cnt[MAXN];
11
12
     LL ans_flow, ans_cost, dis[MAXN];
13
     bool inq[MAXN];
     vector<int> G[MAXN];
14
15
     vector<Edge> edges;
16
     void init(int _n) {
17
       n = _n;
18
       edges.clear():
19
       for (int i = 0; i < n; i++) {
         G[i].clear();
20
       }
21
22
23
     void add_edge(int u, int v, LL c, LL cap) {
24
       // directed
25
       G[u].pb(edges.size());
26
       edges.eb(u, v, c, cap);
       G[v].pb(edges.size());
27
28
       edges.eb(v, u, -c, 0);
29
     bool SPFA(int st, int ed) {
30
31
       for (int i = 0; i < n; i++) {</pre>
         pre[i] = -1;
32
         dis[i] = INF;
33
34
         cnt[i] = 0;
35
         inq[i] = false;
       }
36
37
       queue < int > q;
38
       bool negcycle = false;
39
40
       dis[st] = 0;
41
       cnt[st] = 1;
42
       inq[st] = true;
43
       q.push(st);
44
45
       while (!q.empty() && !negcycle) {
46
         int u = q.front();
47
         q.pop();
48
         inq[u] = false;
         for (int i : G[u]) {
49
           int v = edges[i].v;
50
51
           LL cost = edges[i].cost;
           LL cap = edges[i].cap;
52
53
           if (dis[v] > dis[u] + cost && cap > 0) {
54
```

```
55
              dis[v] = dis[u] + cost;
              pre[v] = i;
56
57
              if (!inq[v]) {
58
                q.push(v);
59
                cnt[v]++;
60
                inq[v] = true;
61
62
                if (cnt[v] == n + 2) {
                  negcycle = true;
63
64
                  break;
65
             }
66
67
           }
         }
68
69
70
71
       return dis[ed] != INF;
72
     }
73
     LL sendFlow(int v, LL curFlow) {
74
       if (pre[v] == -1) {
75
         return curFlow;
76
77
       int i = pre[v];
78
       int u = edges[i].u;
79
       LL cost = edges[i].cost;
80
       LL f = sendFlow(u, min(curFlow, edges[i].cap));
81
82
       ans_cost += f * cost;
83
       edges[i].cap -= f;
84
       edges[i ^ 1].cap += f;
85
86
       return f;
87
     }
88
     pair<LL, LL> run(int st, int ed) {
89
       ans_flow = ans_cost = 0;
       while (SPFA(st, ed)) {
90
91
         ans_flow += sendFlow(ed, INF);
92
93
       return make_pair(ans_flow, ans_cost);
94
95 };
```

5.6 Stable Matching

```
1 int t, n, b[N][N], bi[N], g[N][N], bg[N], gb[N];
2
3 void sol() {
     deque<int> dq;
     memset(gb, 0, sizeof(gb));
     memset(bi, 0, sizeof(bi));
     for (int i = 1; i <= n; i++) dq.push_back(i);</pre>
7
     while (!dq.empty()) {
8
9
       int x = dq.front();
       dq.pop_front();
10
11
       int y = b[x][++bi[x]];
       if (!gb[y]) {
12
         gb[y] = x;
13
14
         bg[x] = y;
       } else if (g[y][x] < g[y][gb[y]]) {</pre>
15
16
         dq.push_back(gb[y]);
17
         gb[y] = x;
         bg[x] = y;
18
19
       } else {
20
          dq.push_back(x);
21
22
23
     for (int i = 1; i <= n; i++) {</pre>
       cout << bg[i] << '\n';</pre>
24
25
26 }
27
28 int main() {
29
    int x;
30
     cin >> t;
     for (int i = 0; i < t; i++) {</pre>
31
       cin >> n;
32
```

```
33
        for (int i = 1; i <= n; i++) {
          for (int j = 1; j <= n; j++) {</pre>
34
35
            cin >> b[i][j];
          }
36
37
       for (int i = 1; i <= n; i++) {</pre>
38
39
          for (int j = 1; j <= n; j++) {</pre>
            cin >> x;
40
41
            g[i][x] = j;
42
43
       3
       if (i) cout << '\n';
44
45
       sol();
46
     }
47 }
```

6 String

6.1 Manacher

```
1 int p[2 * MAXN];
  int Manacher(const string &s) {
    string st = "@#";
    for (char c : s) {
       st += c;
6
       st += '#';
    }
7
    st += '$';
8
     int id = 0, mx = 0, ans = 0;
10
     for (int i = 1; i < st.length() - 1; i++) {</pre>
       p[i] = (mx > i ? min(p[2 * id - i], mx - i) : 1);
11
12
       for (; st[i - p[i]] == st[i + p[i]]; p[i]++);
       if (mx < i + p[i]) {</pre>
13
         mx = i + p[i];
14
15
         id = i;
16
       }
17
       ans = max(ans, p[i] - 1);
    }
18
19
    return ans;
20 }
```

6.2 Trie

```
1 const int MAXL = ;
  const int MAXC = ;
 2
  struct Trie {
     int nex[MAXL][MAXC];
    int len[MAXL];
     int sz;
 7
     void init() {
 8
       memset(nex, 0, sizeof(nex));
       memset(len, 0, sizeof(len));
9
10
       sz = 0;
     }
11
     void insert(const string &str) {
12
13
       int p = 0;
14
       for (char c : str) {
15
         int id = c - 'a';
16
         if (!nex[p][id]) {
17
           nex[p][id] = ++sz;
18
         p = nex[p][id];
19
20
21
       len[p] = str.length();
22
23
     vector<int> find(const string &str, int i) {
24
       int p = 0;
25
       vector<int> ans;
26
       for (; i < str.length(); i++) {</pre>
         int id = str[i] - 'a';
27
28
         if (!nex[p][id]) {
           return ans:
```

6.3 Z-value

```
1 // 0-base
2 // 對於個長度為 n 的字串 s
3 // 定義函數 z[i] 表示 s 和 s[i, n - 1]
4|//(即以 s[i] 開頭的後綴)的最長公共前綴(LCP)的長度
5 // z[0] = 0 \circ
6 vector<int> z_function(string s) {
    int n = (int)s.length();
    vector<int> z(n);
    for (int i = 1, l = 0, r = 0; i < n; ++i) {
      if (i <= r && z[i - 1] < r - i + 1) {</pre>
10
11
        z[i] = z[i - 1];
12
      } else {
13
        z[i] = max(0, r - i + 1);
        while (i + z[i] < n \&\& s[z[i]] == s[i + z[i]])
14
            ++z[i]:
15
16
      if (i + z[i] - 1 > r) l = i, r = i + z[i] - 1;
17
    }
18
    return z;
19 }
```

7 DP

7.1 LIS

```
1 int LIS(vector<int> &a) {
    vector<int> s;
2
     for (int i = 0; i < a.size(); i++) {</pre>
       if (s.empty() || s.back() < a[i]) {</pre>
5
         s.push_back(a[i]);
       } else {
         *lower_bound(s.begin(), s.end(), a[i],
7
           [](int x, int y) {return x < y;}) = a[i];
9
10
    }
11
     return s.size();
12 }
```

7.2 LCS

```
1 int LCS(string s1, string s2) {
2
    int n1 = s1.size(), n2 = s2.size();
3
    vector<vector<int>> dp(n1 + 1, vector<int>(n2 + 1,
         0));
     for (int i = 1; i <= n1; i++) {</pre>
       for (int j = 1; j \le n2; j++) {
         if (s1[i - 1] == s2[j - 1]) {
7
           dp[i][j] = dp[i - 1][j - 1] + 1;
8
         } else {
           dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]);
9
10
11
      }
12
    }
13
     return dp[n1][n2];
14 }
```

7.3 Huge Knapsack

```
1 // from aizu
2 #include <bits/stdc++.h>
3 typedef long long int 11;
4 typedef unsigned long long int ull;
  #define BIG_NUM 2000000000
  #define MOD 1000000007
  #define EPS 0.000000001
  using namespace std;
10
11
  #define SIZE 25
12
13
  struct Info {
14
    Info() { value = 0, weight = 0; }
15
    Info(ll arg_value, ll arg_weight) {
16
      value = arg_value;
      weight = arg_weight;
17
18
    bool operator<(const struct Info &arg) const {</pre>
19
         return weight < arg.weight; }</pre>
20
21
    11 value, weight;
22 };
23
  11 N, W;
25 11 POW[SIZE];
26 ll table_B[1 << 21];
27
  Info info[45];
28
29
  int main() {
30
    POW[0] = 1;
31
     for (int i = 1; i < SIZE; i++) {</pre>
32
      POW[i] = POW[i - 1] * 2;
33
34
    scanf("%11d %11d", &N, &W);
35
36
    for (int i = 0; i < N; i++) {
37
38
       scanf("%11d %11d", &info[i].value,
           &info[i].weight);
39
40
41
    if (N == 1) {
42
      if (info[0].weight <= W) {</pre>
43
         printf("%11d\n", info[0].value);
      } else {
44
45
         printf("0 \ n");
      }
46
47
48
       return 0;
49
50
51
     vector<int> A, B;
52
     for (int i = 0; i < N / 2; i++) {
53
       A.push_back(i);
54
55
     for (int i = N / 2; i < N; i++) {
56
      B.push_back(i);
57
58
59
     vector<Info> vec_A, vec_B;
60
     for (int state = 0; state < POW[A.size()]; state++)</pre>
61
       11 \text{ sum\_w} = 0;
      11 sum_value = 0;
62
63
       for (int loop = 0; loop < A.size(); loop++) {</pre>
         if (state & POW[loop]) {
64
65
           sum_w += info[A[loop]].weight;
           sum_value += info[A[loop]].value;
66
         }
67
68
69
       vec_A.push_back(Info(sum_value, sum_w));
70
71
     sort(vec_A.begin(), vec_A.end());
72
```

```
73
     for (int state = 0; state < POW[B.size()]; state++)</pre>
       11 \text{ sum\_w} = 0;
74
75
       11 sum_value = 0;
76
       for (int loop = 0; loop < B.size(); loop++) {</pre>
77
          if (state & POW[loop]) {
            sum_w += info[B[loop]].weight;
78
79
            sum_value += info[B[loop]].value;
80
81
82
       vec_B.push_back(Info(sum_value, sum_w));
83
     sort(vec_B.begin(), vec_B.end());
84
85
86
     table_B[0] = vec_B[0].value;
     for (int i = 1; i < vec_B.size(); i++) {</pre>
87
       //ある重さ以下の最大価値を求める
88
89
       table_B[i] = max(table_B[i - 1], vec_B[i].value);
90
91
     int tail = vec_B.size() - 1;
92
     ll ans = 0;
93
      for (int i = 0; i < vec_A.size(); i++) {</pre>
94
       while (tail >= 0 && vec_A[i].weight +
95
            vec_B[tail].weight > W) tail--;
       if (tail < 0) break;</pre>
96
97
       ans = max(ans, vec_A[i].value + table_B[tail]);
98
99
100
101
     printf("%11d\n", ans);
102
     return 0;
103 }
```

7.4 Coin Change

```
1 // from aizu
2 int main() {
     int n, m, min, tmp;
     scanf("%d", &n);
     int minimum[n + 1];
     scanf("%d", &m);
6
     int coin[m];
8
     for (int i = 0; i < m; i++) scanf("%d", &coin[i]);</pre>
9
10
     minimum[0] = 0;
     minimum[1] = 1;
11
12
     for (int i = 2; i <= n; i++) {
       min = n + 1;
13
       for (int k = 0; k < m; k++) {
14
         if (coin[k] <= i) {</pre>
15
16
           tmp = 1 + minimum[i - coin[k]];
           min = (min <= tmp) ? min : tmp;</pre>
17
18
         }
19
       }
20
       minimum[i] = min;
21
22
23
     printf("%d\n", minimum[n]);
24
25
     return 0;
26 }
```

7.5 Edit Distance

```
1 // from aizu
2 typedef long long int 11;
3 typedef unsigned long long int ull;
4 #define BIG_NUM 2000000000
5 #define MOD 1000000007
6 #define EPS 0.000000001
8 int main() {
```

```
char A[1001], B[1001];
     int len_A, len_B;
10
     scanf("%s %s", A, B);
11
12
13
     for (len_A = 0; A[len_A] != '\0'; len_A++);
     for (len_B = 0; B[len_B] != '\0'; len_B++);
14
15
16
     int** dp = new int*[len_B + 1];
17
18
     for (int row = 0; row <= len_B; row++) {</pre>
19
       dp[row] = new int[len_A + 1];
20
21
     for (int col = 0; col <= len_A; col++) {</pre>
22
23
       dp[0][col] = col;
24
25
26
     for (int row = 1; row <= len_B; row++) {</pre>
27
       dp[row][0] = row;
28
29
30
     int cost;
31
32
     for (int row = 1; row <= len_B; row++) {</pre>
33
       for (int col = 1; col <= len_A; col++) {</pre>
         if (A[col - 1] == B[row - 1]) {
34
35
           cost = 0;
36
         } else {
37
           cost = 1:
38
         dp[row][col] = min(dp[row - 1][col - 1] + cost,
39
40
           min(dp[row - 1][col] + 1, dp[row][col - 1] +
                1)):
41
       }
    }
42
43
44
     printf("%d\n", dp[len_B][len_A]);
45 }
```

Math

8.1 Number Theory

```
· Inversion:
   aa^{-1}\equiv 1\ (\mathrm{mod}\ m).\ a^{-1}\ \mathrm{exists}\ \mathrm{iff}\ \gcd(a,m)=1.
· Linear inversion:
   a^{-1} \equiv (m - \lfloor \frac{m}{a} \rfloor) \times (m \mod a)^{-1} \pmod{m}
• Fermat's little theorem:
   a^p \equiv a \pmod{p} if p is prime.
• Euler function:
   \phi(n) = n \prod_{p \mid n} \frac{p-1}{p}
. Euler theorem: a^{\phi(n)} \equiv 1 \pmod{n} \text{ if } \gcd(a,n) = 1.

    Extended Euclidean algorithm:

    ax + by = \gcd(a, b) = \gcd(b, a \mod b) = \gcd(b, a - \lfloor \frac{a}{b} \rfloor b) = bx_1 + (a - \lfloor \frac{a}{b} \rfloor b)
    \lfloor \frac{a}{b} \rfloor b) y_1 = a y_1 + b (x_1 - \lfloor \frac{a}{b} \rfloor y_1)
• Divisor function:
   \sigma_x(n) = \sum_{d|n} d^x. n = \prod_{i=1}^r p_i^{a_i}.
   \sigma_x(n) = \prod_{i=1}^r \frac{p_i^{(a_i+1)x} - 1}{p_i^x - 1} \text{ if } x \neq 0. \quad \sigma_0(n) = \prod_{i=1}^r (a_i + 1).
· Chinese remainder theorem:
    x \equiv a_i \pmod{m_i}.
    M = \prod m_i. M_i = M/m_i. t_i = M_i^{-1}.
    x = kM + \sum a_i t_i M_i, k \in \mathbb{Z}.
```

8.2 Extended GCD

```
1 // ax + by = c
2 int extgcd(int a, int b, int c, int &x, int &y) {
 if (b == 0) {
```

8.3 Gaussian Elimination + det

```
1 const double EPS = 1e-6;
2 double Gauss(vector<vector<double>> &d) {
     int n = d.size(), m = d[0].size();
3
     double det = 1;
     for (int i = 0; i < m; i++) {
       int p = -1;
       for (int j = i; j < n; j++) {</pre>
7
         if (fabs(d[j][i]) < EPS) {</pre>
8
9
           continue;
10
         if (p == -1 || fabs(d[j][i]) > fabs(d[p][i])) {
11
12
13
14
       if (p == -1) {
15
         continue;
16
17
       if (p != i) {
18
19
         det *= -1;
20
21
       for (int j = 0; j < m; j++) {
         swap(d[p][j], d[i][j]);
22
23
       for (int j = 0; j < n; j++) {
24
         if (i == j) {
25
           continue;
26
         }
27
28
         double z = d[j][i] / d[i][i];
         for (int k = 0; k < m; k++) {
29
           d[j][k] -= z * d[i][k];
30
31
32
      }
33
     for (int i = 0; i < n; i++) {
34
35
       det *= d[i][i];
36
    }
37
     return det;
38 }
39 // new
40 const int MAXN = 300;
41 const double EPS = 1e-8;
42 int n:
43 double A[MAXN][MAXN];
44 void Gauss() {
     for (int i = 0; i < n; i++) {</pre>
45
       bool ok = 0;
46
47
       for (int j = i; j < n; j++) {</pre>
48
         if (fabs(A[j][i]) > EPS) {
           swap(A[j], A[i]);
49
50
           ok = 1;
51
           break;
         }
52
53
       if (!ok) continue;
54
55
       double fs = A[i][i];
       for (int j = i + 1; j < n; j++) {
56
57
         double r = A[j][i] / fs;
         for (int k = i; k < n; k++) {
58
           A[j][k] -= A[i][k] * r;
59
60
61
       }
62
    }
63 }
```

8.4 Prime Table

```
1 vector < int > p;
2 bitset < MAXN > is_notp;
3
  void PrimeTable(int n) {
     is_notp.reset();
     is_notp[0] = is_notp[1] = 1;
     for (int i = 2; i <= n; ++i) {
 7
       if (!is_notp[i]) {
 8
         p.push_back(i);
9
10
       for (int j = 0; j < (int)p.size(); ++j) {</pre>
11
         if (i * p[j] > n) {
12
           break;
13
         is_notp[i * p[j]] = 1;
14
15
         if (i % p[j] == 0) {
16
           break;
17
18
    }
19
20 }
```

8.5 Phi

- · 歐拉函數計算對於一個整數 N,小於等於 N 的正整數中,有幾個和 N 互質
- ・ 如果 $gcd(p,q) = 1, \Phi(p) \cdot \Phi(q) = \Phi(p \cdot q)$
- $\Phi(p^k) = p^{k-1} \times (p-1)$

```
1 void phi_table(int n) {
     phi[1] = 1;
     for (int i = 2; i <= n; i++) {</pre>
3
      if (phi[i]) {
5
         continue;
6
7
       for (int j = i; j < n; j += i) {
8
         if (!phi[j]) {
           phi[j] = j;
10
11
         phi[j] = phi[j] / i * (i - 1);
12
    }
13
14 }
```

8.6 Chinese Remainder Thm

```
1 / / 参数可为负数的扩展欧几里德定理
2 void exOJLD(int a, int b, int& x, int& y) {
    //根据欧几里德定理
   if (b == 0) { //任意数与0的最大公约数为其本身。
      x = 1;
5
6
      y = 0;
    } else {
7
      int x1, y1;
9
      exOJLD(b, a % b, x1, y1);
10
      if (a * b < 0) { //异号取反
11
        x = -y1;
12
        y = a / b * y1 - x1;
      } else { //同号
13
14
       x = y1;
15
        y = x1 - a / b * y1;
16
      }
   }
17
18 }
19 //剩余定理
20 int calSYDL(int a[], int m[], int k) {
   int N[k]; //这个可以删除
21
    int mm = 1; //最小公倍数
22
    int result = 0;
23
    for (int i = 0; i < k; i++) {
24
25
     mm *= m[i];
```

```
26
    }
    for (int j = 0; j < k; j++) {
27
28
      int L, J;
      \verb|exOJLD(mm / m[j], -m[j], L, J); \\
29
      N[j] = m[j] * J + 1; // 1

N[j] = mm / m[j] * L; // 2
30
31
          1和2这两个值应该是相等的。
      result += N[j] * a[j];
32
    }
33
34
    return (result % mm + mm) % mm;
    //落在(0, mm)之间,这么写是为了防止result初始为负数
35
    //本例中不可能为负可以直接
36
    //写成: return result%mm;即可。
37
38 }
39
40 int main() {
41
    int a[3] = {2, 3, 6}; // a[i]=n%m[i]
42
    int m[3] = \{3, 5, 7\};
    cout << calSYDL(a, m, 3) << endl;</pre>
43
    //輸出為滿足兩條陣列的最小n,第3參數為陣列長度
    //所有滿足答案的數字集合為n+gcd(m0,m1,m2...)*k,
        k為 正數
    return 0;
46
```

8.7 Josephus

```
1 int josephus(int n, int k) { // 有 n個人 圍成一圈, 每 k個一次 2 return n > 1 ? (josephus(n - 1, k) + k) % n : 0; 3 } // 回傳最後一人的編號, 0 index
```

8.8 Catalan

```
C_0 = 1 \quad \text{and} \quad C_{n+1} = \frac{2(2n+1)}{n+2} C_n
1 long long f[N] = {1}, i, t, p;
2 int main() {
     for (int i = 1; i <= 100; i++) {</pre>
3
        f[i] = f[i - 1] * (4 * i - 2) % mod;
        for (t = i + 1, p = mod - 2; p; t = (t * t) %
5
            mod, p >>= 1LL) {
          if (p & 1) {
7
            f[i] *= t;
            f[i] %= mod;
9
          }
       }
10
11
     }
12 }
```

8.9 Matrix Multiplication

```
1 struct Matrix {
    int row, col;
    vector<vector<int>> v;
    Matrix() : row(0), col(0) {}
    Matrix(int r, int c) : row(r), col(c) {
      v = vector<vector<int>>(r, vector<int>(c, 0));
6
7
8 };
9 Matrix operator * (Matrix &a, Matrix &b) {
    assert(a.col == b.row);
10
11
    Matrix ret(a.row, b.col);
12
    for (int i = 0; i < a.row; i++) {</pre>
      for (int j = 0; j < b.col; j++) {</pre>
13
         for (int k = 0; k < a.col; k++) {</pre>
15
           ret.v[i][j] += a.v[i][k] * b.v[k][j];
16
17
      }
18
```

```
19
    return ret;
20 }
21 Matrix mPow(Matrix a, int n) {
22
    assert(a.row == a.col);
23
    Matrix ret(a.row, a.col);
    ret.v[0][0] = ret.v[1][1] = 1;
    while (n > 0) {
25
26
      if (n & 1) {
27
        ret = ret * a;
29
       a = a * a;
       n >>= 1;
30
31
    }
32
    return ret;
33 }
```

8.10 Fibonacci

```
 \begin{bmatrix} f(n) \\ f(n-1) \end{bmatrix} = \begin{bmatrix} 1 & 1 \\ 1 & 0 \end{bmatrix}^{(n-1)} \begin{bmatrix} 1 \\ 0 \end{bmatrix}
                                           O(logn)
 1 LL fib(int n) {
      if (n <= 1) {
          return n;
      }
 5
      Matrix a(2, 2), b(2, 1);
 6
      a.v[0][0] = a.v[0][1] = a.v[1][0] = 1;
 7
       b.v[0][0] = 1;
 8
      auto t = mPow(a, n - 1);
      t = t * b;
9
10
       return t.v[0][0];
11 }
```

f(n) = f(n-1) + f(n-2)

9 Geometry

9.1 Point

```
1 // notice point type!!!
  using dvt = int;
  const double EPS = 1e-6;
  const double PI = acos(-1);
6
  struct Pt {
7
    dvt x;
   dvt y;
8
9 };
10 bool operator < (const Pt &a, const Pt &b) {
11
   return a.x == b.x ? a.y < b.y : a.x < b.x;
12 }
13 bool operator == (const Pt &a, const Pt &b) {
14
  return a.x == b.x && a.y == b.y;
15 }
16 Pt operator + (const Pt &a, const Pt &b) {
17
   return {a.x + b.x, a.y + b.y};
18 }
19 Pt operator - (const Pt &a, const Pt &b) {
20
   return {a.x - b.x, a.y - b.y};
21 }
  // multiply constant
22
23 Pt operator * (const Pt &a, const dvt c) {
24
  return {a.x * c, a.y * c};
25 }
26 Pt operator / (const Pt &a, const dvt c) {
27
  return {a.x / c, a.y / c};
28 }
29 // |a| \times |b| \times cos(x)
  dvt iproduct(const Pt &a, const Pt &b) {
   return a.x * b.x + a.y * b.y;
```

```
Pt st;
3
    Pt ed;
4 };
  // return point side
6 // left, on line, right -> 1, 0, -1
7 int side(Line 1, Pt a) {
     dvt cross_val = cross(a - 1.st, 1.ed - 1.st);
9
    if (cross_val > EPS) {
10
       return 1;
    } else if (cross_val < -EPS) {</pre>
11
       return -1;
12
13
    } else {
14
       return 0:
15
16 }
17 // AB infinity, CD segment
18 bool has_intersection(Line AB, Line CD) {
    int c = side(AB, CD.st);
19
20
     int d = side(AB, CD.ed);
     if (c == 0 || d == 0) {
21
22
       return true;
23
    } else {
24
       // different side
       return c == -d;
25
26
    }
27 }
28 // find intersection point, two line, not seg
29 pair<int, Pt> intersection(Line a, Line b) {
    Pt A = a.ed - a.st;
30
    Pt B = b.ed - b.st;
31
32
     Pt C = b.st - a.st;
    dvt mom = cross(A, B);
33
34
     dvt son = cross(C, B);
    if (std::abs(mom) <= EPS) {</pre>
35
      if (std::abs(son) <= EPS) {</pre>
36
37
         return {1, {}}; // same line
38
       } else {
39
         return {2, {}}; // parallel
      }
40
41
    } else {
42
       return {0, a.st + A * (son / mom)};
43
44 }
45 // line to point distance
46 dvt dis_lp(Line 1, Pt a) {
    return area3x2(1.st, 1.ed, a) / dis_pp(1.st, 1.ed);
47
```

9.3 Area

```
1  // triangle
2  dvt area3(Pt a, Pt b, Pt c) {
3    return std::abs(cross(b - a, c - a) / 2);
4  }
5  dvt area3x2(Pt a, Pt b, Pt c) { // for integer
6    return std::abs(cross(b - a, c - a));
7  }
8  // simple convex area(can in)
```

```
9 dvt area(vector<Pt> &a) {
     dvt ret = 0:
10
     for (int i = 0, sz = a.size(); i < sz; i++) {</pre>
      ret += cross(a[i], a[(i + 1) % sz]);
12
13
14
     return std::abs(ret) / 2;
15 }
16
  // check point in/out a convex
  int io_convex(vector<Pt> convex, Pt q) {
17
18
     // convex is Counterclockwise
19
     for (int i = 0, sz = convex.size(); i < sz; i++) {
       Pt cur = convex[i] - q;
20
21
       Pt nex = convex[(i + 1) % sz] - q;
       dvt cross_val = cross(cur, nex);
22
23
       if (std::abs(cross_val) <= EPS) {</pre>
24
         return 0; // on edge
25
26
       if (cross_val < 0) {</pre>
27
         return -1; // outside
28
    }
29
30
     return 1;
                     // inside
31 }
```

9.4 Convex Hull

```
1 vector < Pt > convex_hull(vector < Pt > &a) {
    sort(a.begin(), a.end());
 3
     a.erase(unique(a.begin(), a.end()), a.end());
     int sz = a.size(), m = 0;
     vector<Pt> ret(sz + 5); // safe 1 up
 6
     for (int i = 0; i < sz; i++) {
 7
       while (m > 1 &&
 8
         cross(ret[m - 1] - ret[m - 2], a[i] - ret[m -
            2]) <= EPS) {
 9
       }
10
11
       ret[m++] = a[i];
12
    }
     int k = m;
13
14
     for (int i = sz - 2; i >= 0; i--) {
       while (m > k &&
15
         cross(ret[m - 1] - ret[m - 2], a[i] - ret[m -
16
             2]) <= EPS) {
17
18
       }
19
       ret[m++] = a[i];
20
     if (sz > 1) {
21
22
      m - -;
23
    }
24
     ret.resize(m):
25
     return ret;
26 }
```