1.3

Black Magic

Contents

13

14 }

```
1 #include <bits/stdc++.h>
 1 Basic
                                       #include <ext/pb_ds/assoc_container.hpp>
  1.1 Run .
                                       #include <ext/pb_ds/tree_policy.hpp>
                                      4
                                       #include <ext/pb_ds/priority_queue.hpp>
   using namespace std;
  using namespace __gnu_pbds;
 2 Data Structure
                                       using set_t =
  2.1 Disjoint Set
           tree<int, null_type, less<int>, rb_tree_tag,
  tree_order_statistics_node_update>;
                                       using map_t =
                                         tree<int, int, less<int>, rb_tree_tag,
 3 Graph
  12
                                          tree_order_statistics_node_update>;
                                     3
                                      13
                                       using heap t =
  14
                                         __gnu_pbds::priority_queue<int>;
                                       using ht_t =
  gp_hash_table<int, int>;
                                      17
                                       int main() {
  //set-----
                                      18
 4 Flow & Matching
                                      19
                                         set t st:
   st.insert(5); st.insert(6);
   21
                                         st.insert(3); st.insert(1);
  22
  5
                                         // the smallest is (0), biggest is (n-1), kth small
                                            is (k-1)
 5 String
                                     7
                                         int num = *st.find_by_order(0);
                                      24
                                         cout << num << '\n'; // print 1
  25
   26
  num = *st.find_by_order(st.size() - 1);
                                      27
                                         cout << num << '\n'; // print 6
                                      28
  29
  30
                                         // find the index
                                         int index = st.order_of_key(6);
                                         cout << index << '\n'; // print 3</pre>
                                      32
  33
   // check if there exists x
                                      34
  8
                                         int x = 5;
                                      35
  7.5 Chinese Remainder Thm \dots \dots \dots \dots \dots \dots \dots
                                     8
                                      36
                                         int check = st.erase(x);
  if (check == 0) printf("st not contain 5\n");
                                      37
   else if (check == 1) printf("st contain 5\n");
                                      40
                                         //tree policy like set
  st.insert(5); st.insert(5);
  41
                                    9 42
                                         cout << st.size() << '\n'; // print 4</pre>
  10
                                      43
                                         //map-----
                                      44
                                      45
                                         map_t mp;
                                      46
                                         mp[1] = 2;
    Basic
                                      47
                                         cout << mp[1] << '\n';
                                      48
                                         auto tmp = *mp.find_by_order(0); // pair
                                         cout << tmp.first << " " << tmp.second << ' \setminus n';
 1.1
     Run
                                      49
                                      50
                                         //heap------
                                      51
1 #use -> sh run.sh {name}
                                         heap_t h1, h2;
                                      52
2 g++ -02 -std=c++14 -Wall -Wextra -Wshadow -o $1 $1.cpp
                                      53
                                         h1.push(1); h1.push(3);
3 | ./$1 < t.in > t.out
                                         h2.push(2); h2.push(4);
                                      54
                                      55
                                         h1.join(h2);
                                         cout << h1.size() << h2.size() << h1.top() << '\n';</pre>
                                      56
                                      57
 1.2 Default
                                      58
                                         //hash-table-----
                                      59
                                         ht_t ht;
                                      60
1 #include <bits/stdc++.h>
                                         ht[85] = 5:
                                      61
2 using namespace std;
                                      62
                                         ht[89975] = 234;
3 using LL = long long;
                                         for (auto i : ht) {
4 #define IOS ios_base::sync_with_stdio(0); cin.tie(0);
                                          cout << i.first << " " << i.second << '\n';</pre>
                                      64
5 #define pb push_back
                                      65
6 #define eb emplace_back
                                      66 }
7 const int INF = 1e9;
8 \mid const \mid int \mid MOD = 1e9 + 7;
9 const double EPS = 1e-6;
10 const int MAXN = 0;
                                       1.4 Binary Search
12 int main() {
                                      1 lower_bound(a, a + n, k);
                                                           //最左邊 ≥ k 的位置
```

2 upper_bound(a, a + n, k);

3 | upper_bound(a, a + n, k) - 1; //最右邊 ≤ k 的位置

//最左邊 > k 的位置

```
4 | lower_bound(a, a + n, k) - 1; //最右邊 < k 的位置</td>5 | [lower_bound, upper_bound)//等於 k 的範圍6 | equal_range(a, a + n, k);
```

2 Data Structure

2.1 Disjoint Set

```
1 // 0-base
2 const int MAXN = 1000;
3 int boss[MAXN];
4 void init(int n) {
    for (int i = 0; i < n; i++) {</pre>
       boss[i] = -1;
    }
7
8 }
9 int find(int x) {
10
   if (boss[x] < 0) {
11
      return x;
12
13
    return boss[x] = find(boss[x]);
14 }
15 bool uni(int a, int b) {
16
    a = find(a);
17
    b = find(b);
18
    if (a == b) {
       return false;
19
20
21
     if (boss[a] > boss[b]) {
22
       swap(a, b);
23
24
     boss[a] += boss[b];
25
     boss[b] = a;
26
     return true;
27 }
```

2.2 BIT RARSQ

```
1 // 1-base
2 #define lowbit(k) (k & -k)
3
4 int n;
5 vector<int> B1, B2;
7 void add(vector<int> &tr, int id, int val) {
    for (; id <= n; id += lowbit(id)) {</pre>
9
      tr[id] += val;
    }
10
11 | }
12 void range_add(int 1, int r, int val) {
13
    add(B1, 1, val);
    add(B1, r + 1, -val);
14
    add(B2, 1, val * (1 - 1));
15
16
    add(B2, r + 1, -val * r);
17 }
18 int sum(vector<int> &tr, int id) {
19
    int ret = 0:
    for (; id >= 1; id -= lowbit(id)) {
20
21
      ret += tr[id];
    }
22
23
    return ret;
24 }
25 int prefix_sum(int id) {
    return sum(B1, id) * id - sum(B2, id);
27 }
28 int range_sum(int 1, int r) {
    return prefix_sum(r) - prefix_sum(l - 1);
29
```

2.3 zkw RMQ

```
1 // 0-base
  const int INF = 1e9;
  const int MAXN = ;
  int n;
 6 int a[MAXN], tr[MAXN << 1];</pre>
  // !!! remember to call this function
9 void build() {
10
    for (int i = 0; i < n; i++) {
11
      tr[i + n] = a[i];
12
13
     for (int i = n - 1; i > 0; i--) {
14
       tr[i] = max(tr[i << 1], tr[i << 1 | 1]);
15
16 }
17 void update(int id, int val) {
18
    for (tr[id += n] = val; id > 1; id >>= 1) {
      tr[id >> 1] = max(tr[id], tr[id ^ 1]);
19
20
21 }
22
  int query(int 1, int r) { // [1, r)
    int ret = -INF;
23
     for (1 += n, r += n; 1 < r; 1 >>= 1, r >>= 1) {
24
25
       if (1 & 1) {
26
        ret = max(ret, tr[1++]);
27
       if (r & 1) {
28
29
         ret = max(ret, tr[--r]);
30
31
    }
32
     return ret;
33 }
```

3 Graph

3.1 Dijkstra

```
1 // 0-base
  const LL INF = 1e18;
  const int MAXN = ;
3
  struct Edge {
    int to:
    LL cost;
     Edge(int v, LL c) : to(v), cost(c) {}
 7
     bool operator < (const Edge &other) const {</pre>
9
      return cost > other.cost;
10
11 };
12
13 int n;
14 LL dis[MAXN];
15 vector < Edge > G[MAXN];
16
17 void init() {
18
    for (int i = 0; i < n; i++) {
19
      G[i].clear();
20
       dis[i] = INF;
21
    }
22 }
23
  void Dijkstra(int st, int ed = -1) {
    priority_queue < Edge > pq;
24
     pq.emplace(st, 0);
26
     dis[st] = 0;
27
     while (!pq.empty()) {
       auto now = pq.top();
28
       pq.pop();
29
       if (now.to == ed) {
30
31
         return;
32
33
       if (now.cost > dis[now.to]) {
34
         continue:
```

3.2 SPFA(negative cycle)

```
1 // 0-base
2 const LL INF = 1e18;
3 const int MAXN = ;
4 struct Edge {
    int to;
    LL cost:
     Edge(int v, LL c) : to(v), cost(c) {}
8 };
9
10 int n;
11 LL dis[MAXN];
12 vector < Edge > G[MAXN];
13
14 void init() {
     for (int i = 0; i < n; i++) {</pre>
15
16
       G[i].clear();
17
       dis[i] = INF;
18
     }
19 }
20 bool SPFA(int st) {
     vector<int> cnt(n, 0);
21
22
     vector<bool> inq(n, false);
     queue<int> q;
23
24
     q.push(st);
25
     dis[st] = 0;
26
27
     inq[st] = true;
28
     while (!q.empty()) {
29
       int now = q.front();
30
       q.pop();
       inq[now] = false;
31
32
       for (auto &e : G[now]) {
33
         if (dis[e.to] > dis[now] + e.cost) {
34
           dis[e.to] = dis[now] + e.cost;
35
           if (!inq[e.to]) {
36
              cnt[e.to]++;
              if (cnt[e.to] > n) {
37
                // negative cycle
38
39
                return false;
40
41
              inq[e.to] = true;
42
              q.push(e.to);
43
44
45
       }
46
     }
47
     return true;
```

3.3 Floyd Warshall

```
11
        for (int j = 0; j < n; j++) {
          G[i][j] = INF;
12
13
        G[i][i] = 0;
14
15
16 }
17
   void floyd() {
18
     for (int k = 0; k < n; k++) {
        for (int i = 0; i < n; i++) {
19
          for (int j = 0; j < n; j++) {
  if (G[i][k] != INF && G[k][j] != INF) {</pre>
20
21
               G[i][j] = min(G[i][j], G[i][k] + G[k][j]);
22
23
24
          }
25
     }
26
27 }
```

3.4 Topological Sort

```
1 // 0-base
  // if ret.size < n -> cycle
  int n;
  vector<vector<int>> G;
6
  vector<int> topoSort() {
     vector<int> indeg(n), ret;
7
     for (auto &li : G) {
 9
       for (int x : li) {
10
         ++indeg[x];
11
     }
12
     // use priority queue for lexic. largest ans
13
14
     queue < int > q;
     for (int i = 0; i < n; i++) {</pre>
15
16
       if (!indeg[i]) {
17
         q.push(i);
18
19
     }
20
     while (!q.empty()) {
21
      int u = q.front();
       q.pop();
22
23
       ret.pb(u);
       for (int v : G[u]) {
24
25
         if (--indeg[v] == 0) {
           q.push(v);
26
27
28
29
     }
30
     return ret;
31 }
```

3.5 Kosaraju SCC

```
1 // 0-base
2 int n;
  vector<vector<int>> G, G2; // G2 = G rev
  vector<bool> vis;
  vector<int> s, color;
6 int sccCnt;
7
  void dfs1(int u) {
    vis[u] = true;
    for (int v : G[u]) {
10
      if (!vis[v]) {
         dfs1(v);
11
12
      }
    }
13
    s.pb(u);
14
15 }
16 void dfs2(int u) {
17
    color[u] = sccCnt;
18
    for (int v : G2[u]) {
      if (!color[v]) {
```

19

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72 73

74 75

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92

93

94

return ret;

```
20
          dfs2(v);
       }
21
22
     }
23 }
24 void Kosaraju() {
     sccCnt = 0;
25
     for (int i = 0; i < n; i++) {
26
27
       if (!vis[i]) {
         dfs1(i);
28
29
30
     }
     for (int i = n - 1; i \ge 0; i - -) {
31
32
       if (!color[s[i]]) {
33
          ++sccCnt:
34
          dfs2(s[i]);
       }
35
     }
36
37 }
```

3.6 Tree Diameter

```
1 // 0-base;
2 const int MAXN = ;
3
4 struct Edge {
    int to;
6
    int cost;
    Edge(int v, int c) : to(v), cost(c) {}
8 };
9
10 | int n, d = 0;
11 int d1[MAXN], d2[MAXN];
12 vector < Edge > G[MAXN];
13 // dfs(0, -1);
14 void dfs(int u, int from) {
     d1[u] = d2[u] = 0;
15
     for (auto e : G[u]) {
16
       if (e.to == from) {
17
18
         continue;
19
20
       dfs(e.to, u);
       int t = d1[e.to] + e.cost;
21
       if (t > d1[u]) {
22
23
         d2[u] = d1[u];
         d1[u] = t;
24
25
       } else if (t > d2[u]) {
         d2[u] = t;
26
27
    }
28
29
     d = max(d, d1[u] + d2[u]);
30 }
```

3.7 Directed MST

```
1 // 0-base
2 const LL INF = 1e18;
  const int MAXN = ;
3
5 struct Edge {
6
    int from;
7
     int to;
8
     LL cost;
     Edge(int u, int v, LL c) : from(u), to(v), cost(c)
9
         {}
10 };
11
12 struct DMST {
13
    int n;
     int vis[MAXN], pre[MAXN], id[MAXN];
14
    LL in[MAXN];
15
16
     vector < Edge > edges;
17
     void init(int _n) {
18
      n = _n;
```

```
edges.clear();
void add_edge(int from, int to, LL cost) {
  edges.eb(from, to, cost);
LL run(int root) {
 LL ret = 0;
  while (true) {
    for (int i = 0; i < n; i++) {</pre>
      in[i] = INF;
    // find in edge
    for (auto &e : edges) {
      if (e.cost < in[e.to] && e.from != e.to) {</pre>
        pre[e.to] = e.from;
        in[e.to] = e.cost;
      }
    }
    // check in edge
    for (int i = 0; i < n; i++) {
      if (i == root) {
        continue;
     if (in[i] == INF) {
        return -1;
      }
    int nodenum = 0;
    memset(id, -1, sizeof(id));
    memset(vis, -1, sizeof(vis));
    in[root] = 0;
    // find cycles
    for (int i = 0; i < n; i++) {
      ret += in[i];
      int v = i;
      while (vis[v] != i && id[v] == -1 && v !=
          root) {
        vis[v] = i;
        v = pre[v];
      if (id[v] == -1 && v != root) {
        for (int j = pre[v]; j != v; j = pre[j]) {
          id[j] = nodenum;
        id[v] = nodenum++;
      }
    }
    // no cycle
    if (nodenum == 0) {
     break;
    for (int i = 0; i < n; i++) {
      if (id[i] == -1) {
        id[i] = nodenum++;
      }
    }
    // grouping the vertices
    for (auto &e : edges) {
      int to = e.to;
      e.from = id[e.from];
      e.to = id[e.to];
      if (e.from != e.to) {
        e.cost -= in[to]; //!!!
      }
    }
    n = nodenum:
    root = id[root];
 }
```

4

```
96 };
```

95 }

4.1 Relation

```
1 | 1. 一般圖
2 | 1最大匹配| + |最小邊覆蓋| = |V|
3 | 1最大獨立集| + |最小點覆蓋| = |V|
4 | 1最大圖| = |補圖的最大獨立集|
5 | 2. 二分圖
6 | 1最大匹配| = |最小點覆蓋|
7 | 1最大獨立集| = |最小邊覆蓋|
8 | 1最大獨立集| = |V| - |最大匹配|
9 | 1最大圖| = |補圖的最大獨立集|
```

Flow & Matching

4.2 Bipartite Matching

```
1 // 0-base
2 const int MAXN = ;
3 int n;
4 vector<int> G[MAXN];
5 int vy[MAXN], my[MAXN];
7 bool match(int u) {
8
    for (int v : G[u]) {
9
       if (vy[v]) {
10
         continue;
11
       vy[v] = true;
12
       if (my[v] == -1 || match(my[v])) {
13
         my[v] = u;
14
15
         return true;
       }
16
17
    }
    return false;
18
19 }
20 int sol() {
    int cnt = 0;
21
     memset(my, -1, sizeof(my));
22
     for (int i = 0; i < n; i++) {
23
       memset(vy, 0, sizeof(vy));
24
25
       if (match(i)) {
26
         cnt++:
27
       }
    }
28
29
     return cnt;
30 }
```

4.3 KM

```
1 const int INF = 1e9;
2 const int MAXN = ;
3 struct KM { //1-base
     int n, G[MAXN][MAXN];
    int lx[MAXN], ly[MAXN], my[MAXN];
6
     bool vx[MAXN], vy[MAXN];
     void init(int _n) {
7
       n = _n;
       for (int i = 1; i <= n; i++) {</pre>
9
10
         for (int j = 1; j <= n; j++) {</pre>
11
           G[i][j] = 0;
12
13
      }
14
15
     bool match(int i) {
16
       vx[i] = true;
17
       for (int j = 1; j \le n; j++) {
```

```
18
         if (1x[i] + 1y[j] == G[i][j] && !vy[j]) {
            vy[j] = true;
19
20
            if (!my[j] || match(my[j])) {
21
              my[j] = i;
              return true;
22
           }
23
24
         }
25
       }
26
       return false;
27
28
     void update() {
       int delta = INF;
29
30
       for (int i = 1; i <= n; i++) {
         if (vx[i]) {
31
32
            for (int j = 1; j <= n; j++) {
              if (!vy[j]) {
33
                delta = min(delta, lx[i] + ly[j] -
34
                     G[i][j]);
35
           }
36
         }
37
38
       for (int i = 1; i <= n; i++) {
39
40
         if (vx[i]) {
41
           lx[i] -= delta;
42
         if (vy[i]) {
43
44
           ly[i] += delta;
45
46
       }
     }
47
48
     int run() {
       for (int i = 1; i <= n; i++) {</pre>
49
50
         lx[i] = ly[i] = my[i] = 0;
51
         for (int j = 1; j <= n; j++) {
52
           lx[i] = max(lx[i], G[i][j]);
53
         }
54
55
       for (int i = 1; i <= n; i++) {</pre>
56
         while (true) {
            for (int i = 1; i <= n; i++) {</pre>
57
58
              vx[i] = vy[i] = 0;
59
            if (match(i)) {
60
61
              break;
62
            } else {
63
              update();
            }
64
65
         }
66
67
       int ans = 0;
       for (int i = 1; i <= n; i++) {
68
69
         ans += lx[i] + ly[i];
70
71
       return ans;
72
73 };
```

4.4 Dinic

```
1 #define eb emplace_back
2 const LL INF = 1e18;
3 const int MAXN = ;
  struct Edge {
    int to;
    LL cap;
    int rev;
    Edge(int v, LL c, int r) : to(v), cap(c), rev(r) {}
8
9 };
10
  struct Dinic {
    int n;
11
12
    int level[MAXN], now[MAXN];
13
    vector<Edge> G[MAXN];
14
    void init(int _n) {
15
      n = _n;
      for (int i = 0; i <= n; i++) {</pre>
16
```

```
17
         G[i].clear();
                                                                     vector<int> G[MAXN];
       }
18
                                                                15
                                                                     vector<Edge> edges;
19
     }
                                                                16
                                                                     void init(int _n) {
     void add_edge(int u, int v, LL c) {
20
                                                                17
                                                                        n = _n;
21
       G[u].eb(v, c, G[v].size());
                                                                18
                                                                        edges.clear();
                                                                        for (int i = 0; i < n; i++) {</pre>
22
       // directed graph
                                                                19
       G[v].eb(u, 0, G[u].size() - 1);
                                                                20
                                                                          G[i].clear();
23
24
       // undirected graph
                                                                21
                                                                        }
       // G[v].eb(u, c, G[u].size() - 1);
25
                                                                22
26
                                                                23
                                                                     void add_edge(int u, int v, LL c, LL cap) {
27
     bool bfs(int st, int ed) {
                                                                24
                                                                        // directed
                                                                       G[u].pb(edges.size());
       fill(level, level + n + 1, -1);
                                                                25
28
29
       queue<int> q;
                                                                26
                                                                        edges.eb(u, v, c, cap);
                                                                27
       q.push(st);
                                                                       G[v].pb(edges.size());
30
31
       level[st] = 0;
                                                                28
                                                                        edges.eb(v, u, -c, 0);
       while (!q.empty()) {
32
                                                                29
         int u = q.front();
                                                                30
                                                                     bool SPFA(int st, int ed) {
33
34
         q.pop();
                                                                31
                                                                        for (int i = 0; i < n; i++) {</pre>
         for (const auto &e : G[u]) {
                                                                          pre[i] = -1;
                                                                32
35
           if (e.cap > 0 && level[e.to] == -1) {
                                                                33
                                                                          dis[i] = INF;
36
             level[e.to] = level[u] + 1;
                                                                          cnt[i] = 0;
37
                                                                34
             q.push(e.to);
                                                                35
                                                                          inq[i] = false;
38
           }
                                                                       }
39
                                                                36
         }
                                                                37
                                                                        queue < int > q;
40
41
       }
                                                                38
                                                                       bool negcycle = false;
42
       return level[ed] != -1;
                                                                39
43
                                                                40
                                                                       dis[st] = 0;
44
     LL dfs(int u, int ed, LL limit) {
                                                                41
                                                                        cnt[st] = 1;
45
       if (u == ed) {
                                                                42
                                                                        inq[st] = true;
46
         return limit;
                                                                43
                                                                        q.push(st);
47
                                                                44
48
       LL ret = 0;
                                                                45
                                                                        while (!q.empty() && !negcycle) {
49
       for (int &i = now[u]; i < G[u].size(); i++) {</pre>
                                                                46
                                                                          int u = q.front();
50
         auto &e = G[u][i];
                                                                47
                                                                          q.pop();
         if (e.cap > 0 && level[e.to] == level[u] + 1) {
51
                                                                48
                                                                          inq[u] = false;
52
           LL f = dfs(e.to, ed, min(limit, e.cap));
                                                                49
                                                                          for (int i : G[u]) {
53
           ret += f;
                                                                50
                                                                            int v = edges[i].v;
           limit -= f;
                                                                51
                                                                            LL cost = edges[i].cost;
54
           e.cap -= f;
                                                                            LL cap = edges[i].cap;
55
                                                                52
           G[e.to][e.rev].cap += f;
56
                                                                53
57
           if (!limit) {
                                                                54
                                                                            if (dis[v] > dis[u] + cost && cap > 0) {
58
                                                                55
                                                                              dis[v] = dis[u] + cost;
             return ret;
                                                                56
                                                                              pre[v] = i;
59
           }
         }
                                                                57
                                                                              if (!inq[v]) {
60
61
                                                                58
                                                                                q.push(v);
       if (!ret) {
                                                                59
                                                                                cnt[v]++;
62
63
         level[u] = -1;
                                                                60
                                                                                inq[v] = true;
                                                                61
64
65
       return ret;
                                                                62
                                                                                if (cnt[v] == n + 2) {
                                                                                   negcycle = true;
66
                                                                63
67
     LL flow(int st, int ed) {
                                                                64
                                                                                  break;
68
       LL ret = 0;
                                                                65
69
       while (bfs(st, ed)) {
                                                                66
                                                                              }
70
         fill(now, now + n + 1, 0);
                                                                67
                                                                            }
         ret += dfs(st, ed, INF);
                                                                         }
71
                                                                68
       }
                                                                       }
72
                                                                69
73
       return ret;
                                                                70
74
                                                                71
                                                                        return dis[ed] != INF;
75 };
                                                                72
                                                                     LL sendFlow(int v, LL curFlow) {
                                                                73
                                                                74
                                                                        if (pre[v] == -1) {
                                                                75
                                                                         return curflow;
  4.5 MCMF
                                                                76
                                                                77
                                                                       int i = pre[v];
1 // 0-base
                                                                       int u = edges[i].u;
                                                                78
2 const LL INF = 1e18;
                                                                79
                                                                       LL cost = edges[i].cost;
3
  const int MAXN = ;
                                                                80
4 struct Edge {
                                                                        LL f = sendFlow(u, min(curFlow, edges[i].cap));
                                                                81
    int u, v;
                                                                82
6
     LL cost;
                                                                83
                                                                        ans_cost += f * cost;
7
     LL cap:
                                                                84
                                                                        edges[i].cap -= f;
8
     Edge(int _u, int _v, LL _c, LL _cap) : u(_u),
                                                                85
                                                                        edges[i ^ 1].cap += f;
         v(_v), cost(_c), cap(_cap) {}
                                                                86
                                                                        return f;
9 };
                                                                87
10 struct MCMF {
                     // inq times
                                                                88
                                                                     pair<LL, LL> run(int st, int ed) {
     int n, pre[MAXN], cnt[MAXN];
11
                                                                89
                                                                        ans_flow = ans_cost = 0;
```

while (SPFA(st, ed)) {

90

12

13

LL ans_flow, ans_cost, dis[MAXN];

bool inq[MAXN];

```
91     ans_flow += sendFlow(ed, INF);
92     }
93     return make_pair(ans_flow, ans_cost);
94     }
95 };
```

5 String

5.1 Manacher

```
1 int p[2 * MAXN];
2 int Manacher(const string &s) {
     string st = "@#";
3
    for (char c : s) {
       st += c;
       st += '#';
6
7
    st += '$';
8
    int id = 0, mx = 0, ans = 0;
    for (int i = 1; i < st.length() - 1; i++) {</pre>
10
       p[i] = (mx > i ? min(p[2 * id - i], mx - i) : 1);
11
       for (; st[i - p[i]] == st[i + p[i]]; p[i]++);
12
       if (mx < i + p[i]) {</pre>
13
14
         mx = i + p[i];
15
         id = i;
16
17
       ans = max(ans, p[i] - 1);
18
19
    return ans;
20 }
```

5.2 Trie

```
1 const int MAXL = ;
2 const int MAXC = ;
3 struct Trie {
     int nex[MAXL][MAXC];
    int len[MAXL];
     int sz;
7
     void init() {
       memset(nex, 0, sizeof(nex));
8
9
       memset(len, 0, sizeof(len));
       sz = 0:
10
11
     void insert(const string &str) {
12
13
       int p = 0;
14
       for (char c : str) {
         int id = c - 'a';
15
         if (!nex[p][id]) {
16
17
           nex[p][id] = ++sz;
18
19
         p = nex[p][id];
20
21
       len[p] = str.length();
22
     }
     vector<int> find(const string &str, int i) {
23
24
       int p = 0;
       vector<int> ans;
25
26
       for (; i < str.length(); i++) {</pre>
         int id = str[i] - 'a';
27
28
         if (!nex[p][id]) {
29
           return ans;
30
31
         p = nex[p][id];
         if (len[p]) {
32
33
           ans.pb(len[p]);
34
       }
35
36
       return ans;
37
38 };
```

5.3 Z-value

```
1 // 0-base
2 // 對於個長度為 n 的字串 s
3 // 定義函數 z[i] 表示 s 和 s[i, n - 1]
4|// (即以 s[i] 開頭的後綴)的最長公共前綴 (LCP)的長度
  // z[0] = 0 \circ
5
  vector<int> z_function(string s) {
6
    int n = (int)s.length();
    vector<int> z(n);
9
    for (int i = 1, l = 0, r = 0; i < n; ++i) {
      if (i <= r && z[i - 1] < r - i + 1) {</pre>
10
11
        z[i] = z[i - 1];
12
      } else {
        z[i] = max(0, r - i + 1);
13
        while (i + z[i] < n \&\& s[z[i]] == s[i + z[i]])
14
            ++z[i]:
15
      if (i + z[i] - 1 > r) l = i, r = i + z[i] - 1;
16
17
    }
18
    return z;
19 }
```

6 DP

6.1 LIS

```
1 int LIS(vector<int> &a) {
    vector<int> s;
     for (int i = 0; i < a.size(); i++) {</pre>
       if (s.empty() || s.back() < a[i]) {</pre>
         s.push_back(a[i]);
5
       } else {
7
         *lower_bound(s.begin(), s.end(), a[i],
8
           [](int x, int y) {return x < y;}) = a[i];
9
    }
10
11
     return s.size();
12 }
```

6.2 LCS

```
1 int LCS(string s1, string s2) {
    int n1 = s1.size(), n2 = s2.size();
     vector<vector<int>> dp(n1 + 1, vector<int>(n2 + 1,
3
         0));
     for (int i = 1; i <= n1; i++) {</pre>
      for (int j = 1; j <= n2; j++) {</pre>
5
         if (s1[i - 1] == s2[j - 1]) {
7
           dp[i][j] = dp[i - 1][j - 1] + 1;
8
         } else {
9
           dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]);
10
11
      }
    }
12
13
    return dp[n1][n2];
14 }
```

7 Math

7.1 Extended GCD

```
1 // ax + by = c
2 int extgcd(int a, int b, int c, int &x, int &y) {
3    if (b == 0) {
4         x = c / a;
5         y = 0;
6    return a;
```

7.2 Gaussian Elimination

```
1 const double EPS = 1e-6;
2 double Gauss(vector<vector<double>> &d) {
     int n = d.size(), m = d[0].size();
     double det = 1;
     for (int i = 0; i < m; i++) {
       int p = -1;
       for (int j = i; j < n; j++) {
7
         if (fabs(d[j][i]) < EPS) {</pre>
8
           continue;
9
10
11
         if (p == -1 || fabs(d[j][i]) > fabs(d[p][i])) {
12
13
       }
14
15
       if (p == -1) {
16
         continue;
17
18
       if (p != i) {
         det *= -1;
19
20
21
       for (int j = 0; j < m; j++) {
22
         swap(d[p][j], d[i][j]);
23
       for (int j = 0; j < n; j++) {
24
25
         if (i == j) {
26
           continue;
27
28
         double z = d[j][i] / d[i][i];
         for (int k = 0; k < m; k++) {
29
           d[j][k] -= z * d[i][k];
30
31
32
33
     for (int i = 0; i < n; i++) {
34
35
       det *= d[i][i];
36
37
     return det;
38 }
```

7.3 Prime Table

```
1 | vector<int> p;
2
  bitset<MAXN> is_notp;
3 void PrimeTable(int n) {
    is_notp.reset();
    is_notp[0] = is_notp[1] = 1;
    for (int i = 2; i <= n; ++i) {
7
       if (!is_notp[i]) {
        p.push_back(i);
8
       for (int j = 0; j < (int)p.size(); ++j) {</pre>
10
         if (i * p[j] > n) {
11
12
           break;
13
         is_notp[i * p[j]] = 1;
14
15
         if (i % p[j] == 0) {
16
           break;
17
       }
18
19
    }
20 }
```

7.4 Phi Table

```
· 歐拉函數計算對於一個整數 N,小於等於 N 的正整數中,有幾個和 N 互質
```

```
1 void phi_table(int n) {
    phi[1] = 1;
    for (int i = 2; i <= n; i++) {
       if (phi[i]) {
         continue;
6
7
      for (int j = i; j < n; j += i) {
         if (!phi[j]) {
8
          phi[j] = j;
10
11
         phi[j] = phi[j] / i * (i - 1);
12
    }
13
14 }
```

・ 如果 $gcd(p,q) = 1, \Phi(p) \cdot \Phi(q) = \Phi(p \cdot q)$

• $\Phi(p^k) = p^{k-1} \times (p-1)$

7.5 Chinese Remainder Thm

```
1 / / 参数可为负数的扩展欧几里德定理
void exOJLD(int a, int b, int& x, int& y) {
    //根据欧几里德定理
3
    if (b == 0) { //任意数与0的最大公约数为其本身。
      x = 1;
6
      y = 0;
7
    } else {
      int x1, y1;
8
      exOJLD(b, a % b, x1, y1);
      if (a * b < 0) { //异号取反
10
11
        x = -y1;
        y = a / b * y1 - x1;
12
      } else { //同号
13
       x = y1;
14
15
        y = x1 - a / b * y1;
16
17
    }
18 }
  //剩余定理
19
20 int calSYDL(int a[], int m[], int k) {
               //这个可以刪除
    int N[k]:
    int mm = 1; //最小公倍数
    int result = 0;
    for (int i = 0; i < k; i++) {
24
25
      mm *= m[i];
26
27
    for (int j = 0; j < k; j++) {
28
      int L, J;
      exOJLD(mm / m[j], -m[j], L, J);
29
      N[j] = m[j] * J + 1; // 1

N[j] = mm / m[j] * L; // 2
30
31
          1和2这两个值应该是相等的。
      result += N[j] * a[j];
32
33
    }
34
    return (result % mm + mm) % mm;
35
        mm)之间,这么写是为了防止result初始为负数,本例中不可能为
    //写成: return result%mm;即可。
36
37 }
38
39
  int main() {
40
    int a[3] = {2, 3, 6}; // a[i]=n%m[i]
    int m[3] = {3, 5, 7};
41
42
    cout << calSYDL(a, m, 3) << endl;</pre>
    //輸出為滿足兩條陣列的最小n,第3參數為陣列長度
43
    //所有滿足答案的數字集合為n+gcd(m0, m1, m2...)*k,
44
        k為正數
45
    return 0;
46 }
```

7.6 Josephus

7.7 Catalan

```
C_0 = 1 \quad \text{and} \quad C_{n+1} = \frac{2(2n+1)}{n+2} C_n
1 long long f[N] = {1}, i, t, p;
2 int main() {
     for (int i = 1; i <= 100; i++) {</pre>
3
       f[i] = f[i - 1] * (4 * i - 2) % mod;
        for (t = i + 1, p = mod - 2; p; t = (t * t) %
5
            mod, p >>= 1LL) {
          if (p & 1) {
7
            f[i] *= t;
            f[i] %= mod;
8
9
10
       }
11
     }
12 }
```

8 Geometry

8.1 Point

```
1 // notice point type!!!
2 using dvt = int;
3 const double EPS = 1e-6;
4 const double PI = acos(-1);
6 struct Pt {
7
   dvt x;
8
   dvt y;
10 bool operator < (const Pt &a, const Pt &b) {
   return a.x == b.x ? a.y < b.y : a.x < b.x;</pre>
11
12 }
13 bool operator == (const Pt &a, const Pt &b) {
14
   return a.x == b.x && a.y == b.y;
15 }
16 Pt operator + (const Pt &a, const Pt &b) {
17
    return {a.x + b.x, a.y + b.y};
18 }
19 Pt operator - (const Pt &a, const Pt &b) {
20
   return {a.x - b.x, a.y - b.y};
21 }
22 // multiply constant
23 Pt operator * (const Pt &a, const dvt c) {
24 return {a.x * c, a.y * c};
25 }
26 Pt operator / (const Pt &a, const dvt c) {
27
   return {a.x / c, a.y / c};
28 }
29 // |a| \times |b| \times cos(x)
30 dvt iproduct(const Pt &a, const Pt &b) {
31
    return a.x * b.x + a.y * b.y;
32 }
33 // |a| \times |b| \times \sin(x)
34 dvt cross(const Pt &a, const Pt &b) {
   return a.x * b.y - a.y * b.x;
35
36 }
37 dvt dis_pp(const Pt &a, const Pt, &b) {
dvt dx = a.x - b.x;
39
    dvt dy = a.y - b.y;
    return sqrt(dx * dx, dy * dy);
40
41 }
```

8.2 Line

```
1 struct Line {
    Pt st;
    Pt ed;
3
4 };
5 // return point side
  // left, on line, right -> 1, 0, -1
7 int side(Line 1, Pt a) {
    dvt cross_val = cross(a - 1.st, 1.ed - 1.st);
    if (cross_val > EPS) {
10
      return 1:
    } else if (cross_val < -EPS) {</pre>
11
12
      return -1;
13
    } else {
14
       return 0;
    }
15
16 }
17 // AB infinity, CD segment
18 bool has_intersection(Line AB, Line CD) {
19
    int c = side(AB, CD.st);
    int d = side(AB, CD.ed);
20
21
    if (c == 0 || d == 0) {
22
      return true;
23
    } else {
      // different side
24
25
       return c == -d;
    }
26
27 }
  // find intersection point, two line, not seg
29 pair<int, Pt> intersection(Line a, Line b) {
    Pt A = a.ed - a.st;
31
    Pt B = b.ed - b.st;
    Pt C = b.st - a.st;
32
33
    dvt mom = cross(A, B);
    dvt son = cross(C, B);
34
    if (std::abs(mom) <= EPS) {</pre>
35
      if (std::abs(son) <= EPS) {</pre>
36
37
        return {1, {}}; // same line
38
       } else {
39
        return {2, {}}; // parallel
40
                          // ok
41
    } else {
       return {0, a.st + A * (son / mom)};
42
43
44 }
45 // line to point distance
46 dvt dis_lp(Line 1, Pt a) {
    return area3x2(1.st, l.ed, a) / dis_pp(l.st, l.ed);
47
48 }
                      d(P,L) = \frac{|ax_0 + by_0 + c|}{\underline{\qquad}}
```

8.3 Area

```
1 // triangle
2 dvt area3(Pt a, Pt b, Pt c) {
   return std::abs(cross(b - a, c - a) / 2);
3
4 }
5 dvt area3x2(Pt a, Pt b, Pt c) { // for integer
   return std::abs(cross(b - a, c - a));
7 }
  // simple convex area(can in)
8
9
  dvt area(vector<Pt> &a) {
10
  dvt ret = 0:
    for (int i = 0, sz = a.size(); i < sz; i++) {</pre>
      ret += cross(a[i], a[(i + 1) % sz]);
12
13
14
    return std::abs(ret) / 2;
15 }
16 // check point in/out a convex
17 int io_convex(vector<Pt> convex, Pt q) {
18
    // convex is Counterclockwise
    for (int i = 0, sz = convex.size(); i < sz; i++) {
19
     Pt cur = convex[i] - q;
```

```
Pt nex = convex[(i + 1) % sz] - q;
21
       dvt cross_val = cross(cur, nex);
22
23
       if (std::abs(cross_val) <= EPS) {</pre>
        return 0; // on edge
24
25
       if (cross_val < 0) {</pre>
26
27
         return -1; // outside
28
29
     }
     return 1;
30
                     // inside
31 }
```

8.4 Convex Hull

```
1 vector < Pt > convex_hull(vector < Pt > &a) {
    sort(a.begin(), a.end());
3
    a.erase(unique(a.begin(), a.end());
    int sz = a.size(), m = 0;
    vector<Pt> ret(sz + 5); // safe 1 up
    for (int i = 0; i < sz; i++) {</pre>
6
7
      while (m > 1 &&
         cross(ret[m - 1] - ret[m - 2], a[i] - ret[m -
8
           2]) <= EPS) {
9
      }
10
11
      ret[m++] = a[i];
    }
12
    int k = m;
13
    for (int i = sz - 2; i >= 0; i--) {
14
      while (m > k &&
15
16
         cross(ret[m - 1] - ret[m - 2], a[i] - ret[m -
            2]) <= EPS) {
17
      }
18
19
      ret[m++] = a[i];
20
21
    if (sz > 1) {
22
      m - - ;
23
24
    ret.resize(m);
25
    return ret;
26 }
```