

# Thesis Progress Meeting

J. Raimbault<sup>1,2</sup>

<sup>1</sup>Géographie-cités (UMR 8504 CNRS)

<sup>2</sup>LVMT (UMR-T 9403 IFSTTAR)

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# Achieved Work (by projects)

- Cybergeo [1.6w] (ETA 1.5w)
- Gibrat-interaction [1.7w] (ETA 1.5w)
- Spatial Statistics [0.5w]
- Misc (AlgoSR, Scaling, MetaZipf, Lutecia, Chine, SFI prep.) [0.5w]
- Organisation/conference/biblio [0.7w]
- Side projects (Transportation, Ecotoxicology) [0.5w] (ETA 0.5w)

# Model Description

→ Rationale : extend an interaction model for system of cities by including physical network, to investigate its influence on system dynamics

→ Work under Gibrat independence assumptions, i.e.  $\text{Cov}[P_i(t), P_j(t)] = 0$ . If  $\vec{P}(t+1) = \mathbf{R} \cdot \vec{P}(t)$  where  $\mathbf{R}$  is also independent, then  $\mathbb{E}[\vec{P}(t+1)] = \mathbf{R} \cdot \mathbb{E}[\vec{P}(t)]$ . Expectancies only for now (higher moments computable similarly)

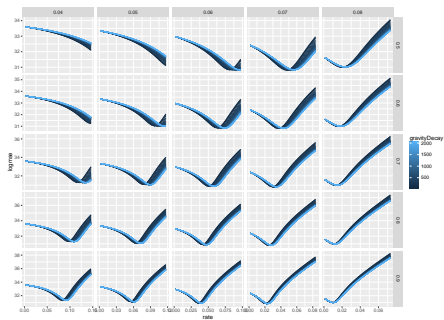
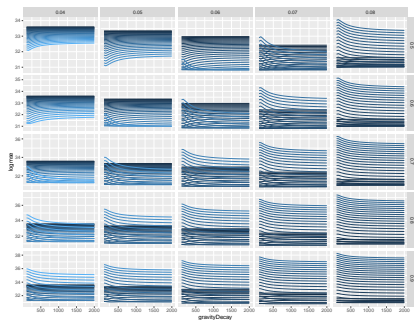
→ With  $\vec{\mu}(t) = \mathbb{E}[\vec{P}(t)]$ , we generalize this approach by taking  $\vec{\mu}(t+1) = f(\vec{\mu}(t))$

→ In our case,  $f(\vec{\mu}) = r_0 \cdot \mathbf{Id} \cdot \vec{\mu} + \mathbf{G} \cdot \mathbf{1} + \mathbf{N} \cdot$  with

- $G_{ij} = w_G \cdot \frac{V_{ij}}{\langle V_{ij} \rangle}$  and  $V_{ij} = \left( \frac{\mu_i \mu_j}{\sum \mu_k^2} \right)^{\gamma_G} \exp(-d_{ij}/d_G)$
- $N_i = w_N \cdot \sum_{kl} \left( \frac{\mu_k \mu_l}{\sum \mu} \right)^{\gamma_N} \exp(-d_{kl,i}/d_N)$  where  $d_{kl,i}$  is distance to shortest path between  $k, l$  computed with slope impedance ( $Z = (1 + \alpha/\alpha_0)^{n_0}$  with  $\alpha_0 \simeq 3$ )

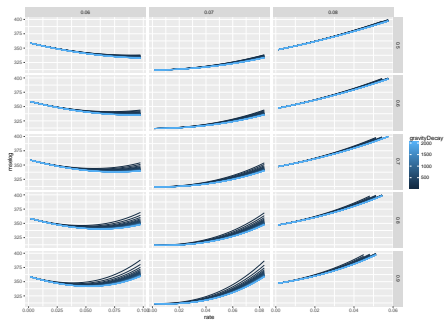
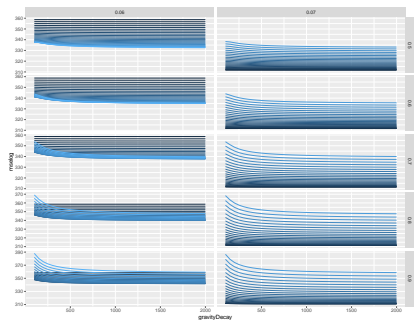
# Exploration : Gravity Only

*logmse : log of mean square error on populations*



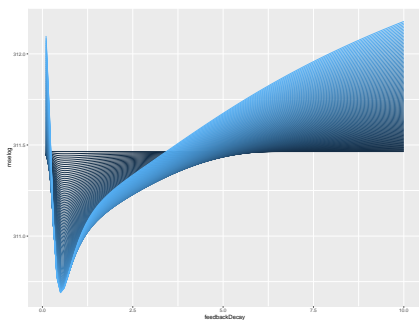
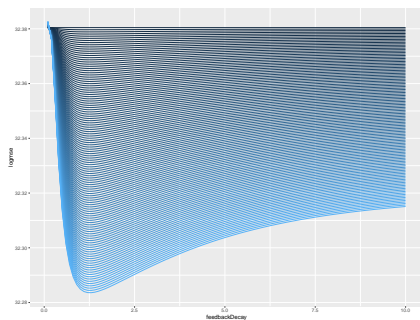
# Exploration : Gravity Only

*mselog* : mean square error on log of populations



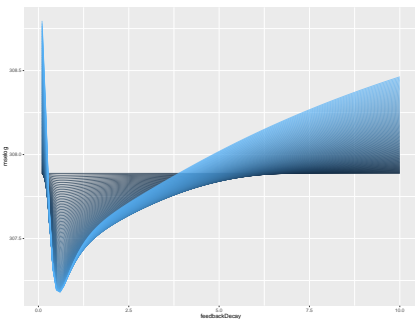
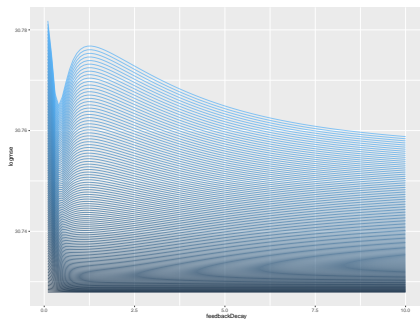
# Exploration

## *Feedback Only*



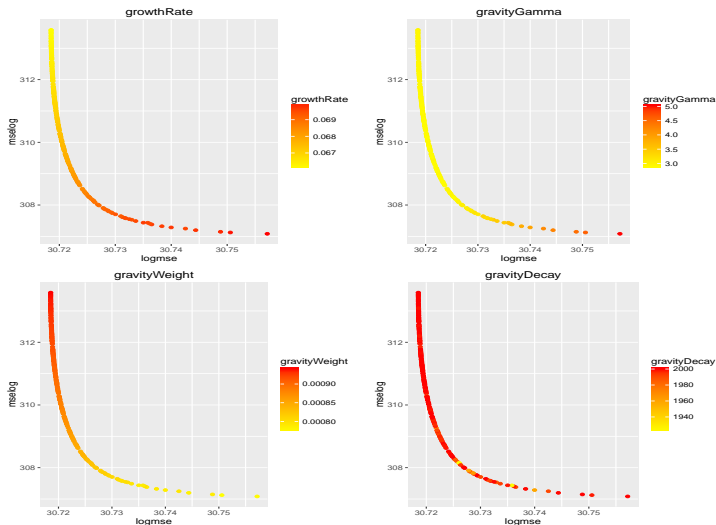
# Exploration

*Feedback with fixed gravity : first evidences of network effects ; confirmed with effect of  $\alpha_0$*



# Calibration

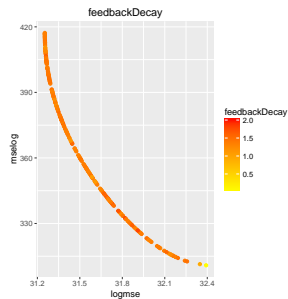
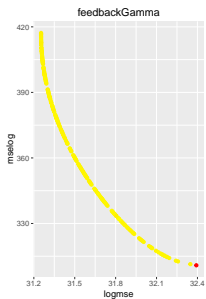
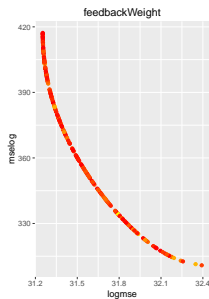
## Gravity only





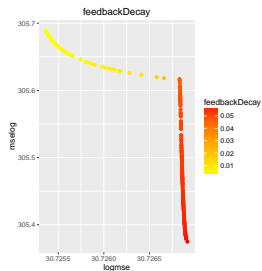
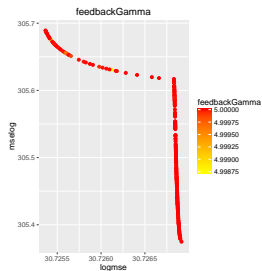
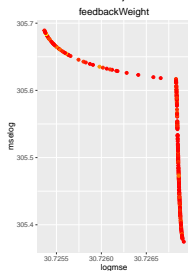
# Calibration

## *Feedback only*



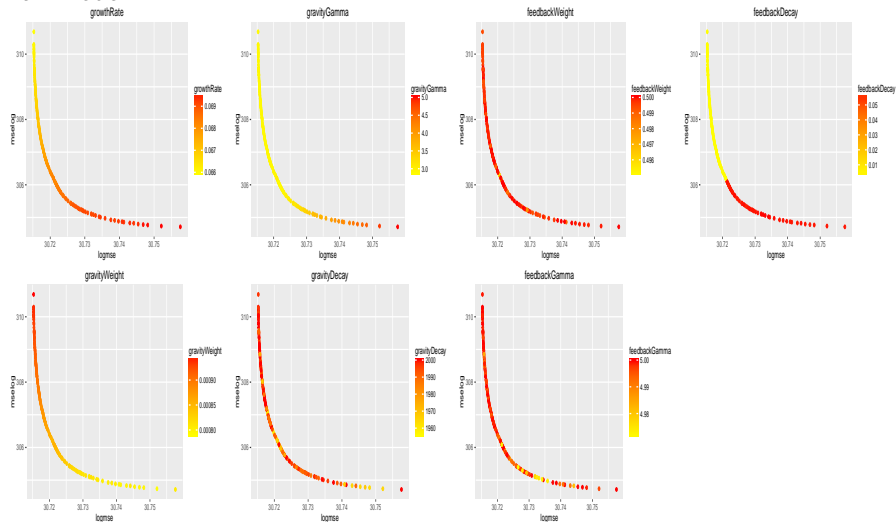
# Calibration

## Full Model, Iterative Calibration



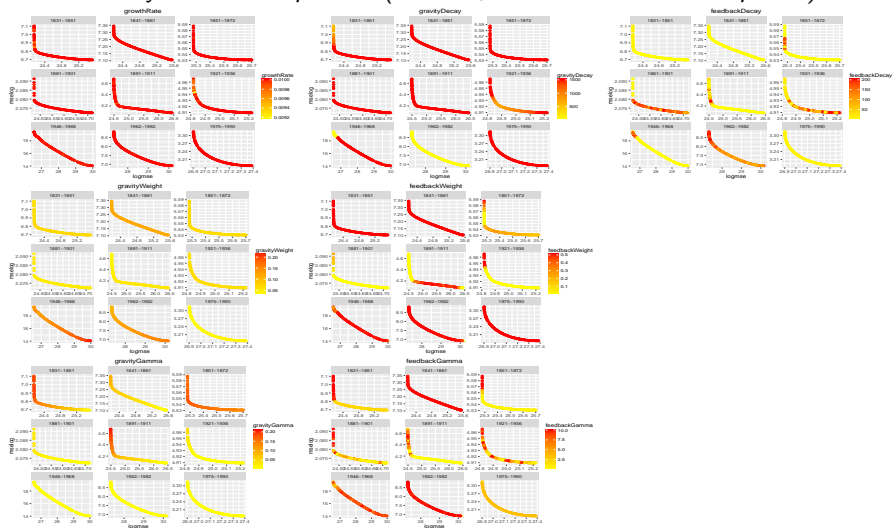
# Calibration

## Full Model



# Temporal moving window

*Calibration by normalized periods (no wars, same number of data points)*

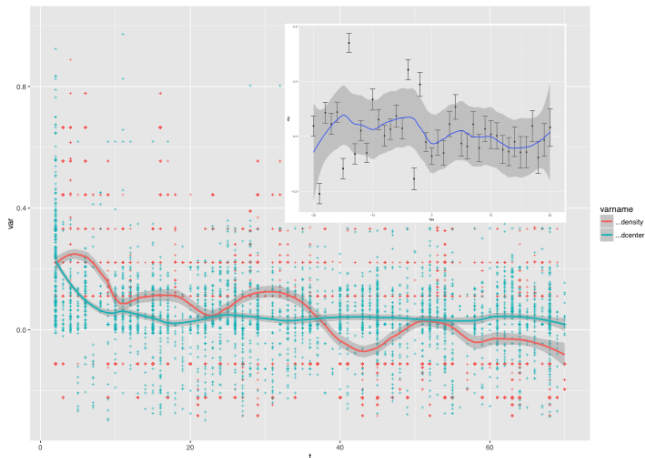


# Next steps

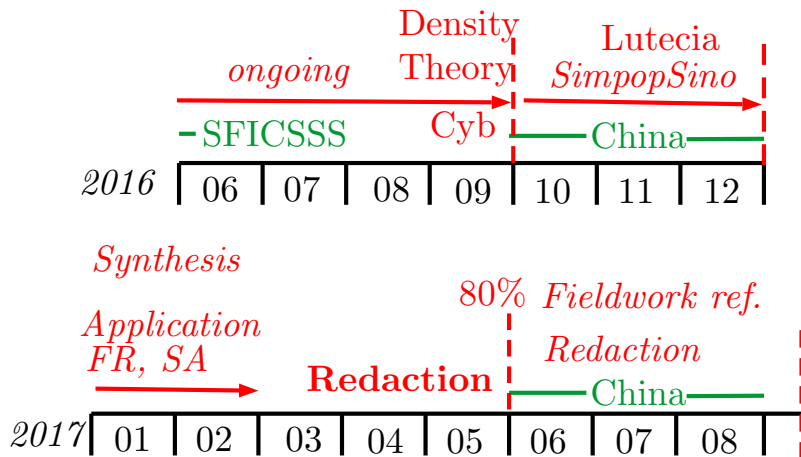
- Compute empirical AIC to check if improvement is worth additional parameters. Various approaches :
  - Via empirical likelihood
  - Via non-linear sparse regression
  - Via behavior space and statistical multimodeling
- Calibration profiles (still running)
- Link with models with covariance : propose a general framework (extending the Simon-Gibrat work)

# Spatial Statistics

*First work on Granger causality for spatial statistics : synthetic data by RBD model*



# Thesis Organisation



# Next steps (until August 30th 2016)

- SFICSSS [4w] (+ holidays [2w])
- Cybergeo Paper [1w]
- Density Paper [1w]
- Theoretical Paper [1w]
- Static Correlations (presentation at RGS conference on 31th) [1w]
- China project [1w]