

# A Theory of co-evolutive networked territorial systems : Exemplification of Network Necessity

## *Working Paper*

JUSTE RAIMBAULT

Date

### **Abstract**

Second part of theoretical paper developing a theory of co-evolutive networked territorial systems : application to simple models of urban growth for systems of cities.

## **1 Context and Objective**

### **1.1 Literature review**

[Bretagnolle et al., 2000] already propose a spatial extension of the Gibrat model (*detail*)  
[Favaro and Pumain, 2011] is a more refined extension with economic cycles

### **1.2 Exemplifying Network Necessity**

## **2 Model Description**

### **2.1 From Gibrat to Marius : the dilemma of formulation**

### **2.2 Model description**

## **3 Results**

### **3.1 Implementation**

### **3.2 Model Exploration**

### **3.3 Model Calibration**

## **4 Discussion**

## **5 Supplementary Materials**

### **5.1 Integrating Gibrat**

Analytical resolution is possible for some aspects of the Gibrat model. We detail here the computation for some.

**Expectancies** If working with expectancies, it makes no sense to proceed to Monte Carlo simulation as a direct resolution gives a deterministic recurrence relation on expectancies. Let  $\mu_t = \mathbb{E}[P(t)]$

**Covariance**

**Distribution**

## **5.2 A Bayesian iterative approach**

## **References**

- [Bretagnolle et al., 2000] Bretagnolle, A., Mathian, H., Pumain, D., and Rozenblat, C. (2000). Long-term dynamics of european towns and cities: towards a spatial model of urban growth. Cybergeo: European Journal of Geography.
- [Favaro and Pumain, 2011] Favaro, J.-M. and Pumain, D. (2011). Gibrat revisited: An urban growth model incorporating spatial interaction and innovation cycles. Geographical Analysis, 43(3):261–286.