

Towards a Theory of Co-evolutive Networked Territorial Systems: Insights from Transportation Governance Modeling in Pearl River Delta, China

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Complex Urban Systems

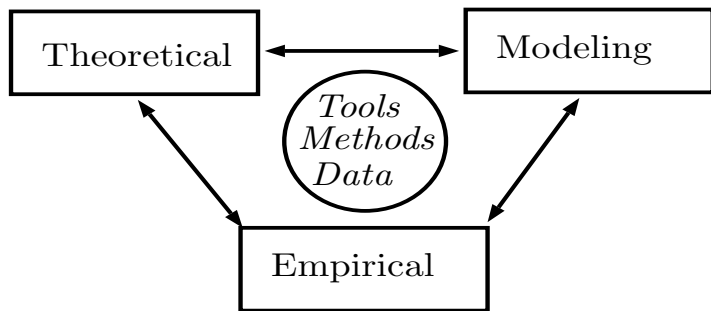
Source : Wikipedia

Complex Systems Approaches in Science

- Failure of reductionism already highlighted by Anderson in 1972 [Anderson, 1972]
- Yet few domains with Integrative Theories
- Even physics begins to realize the potential of this “New Kind of Science [Wolfram, 2002] : Quantum coherence paradox solved through computational complexity [] ; Very recent theory of emergent gravity solves Dark Matter issue

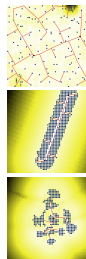
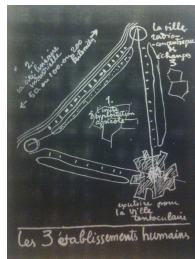
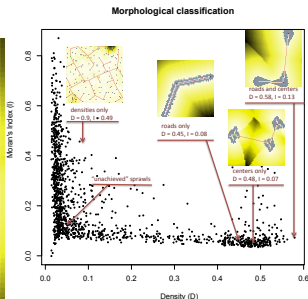
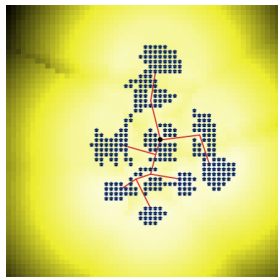
Theoretical and Quantitative Geography

Extended framework for TQG [Livet et al., 2010]



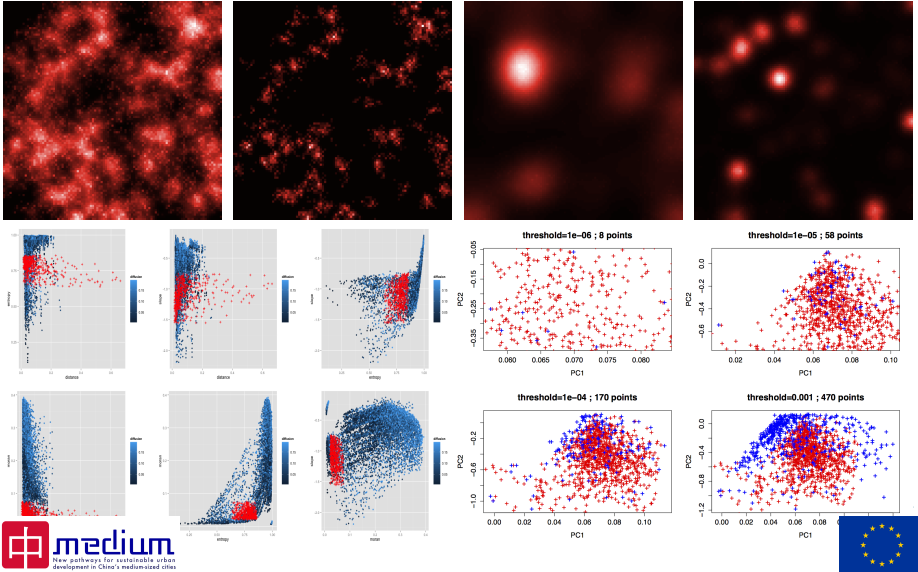
Meso-scale Coupled Growth

Simple co-evolutionary dynamics produce stylized urban forms at a mesoscopic scale [Raimbault et al., 2014]



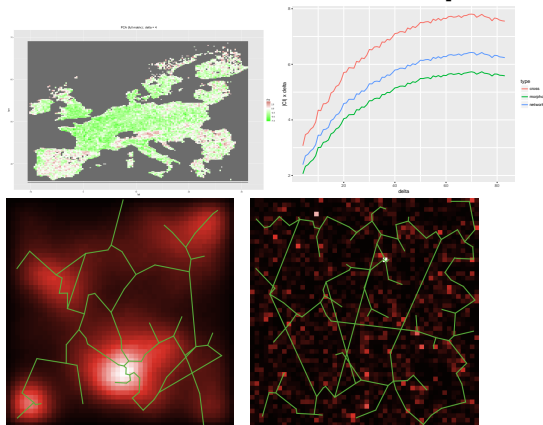
Aggregation-diffusion Urban Growth

Evidence of autonomous Morphogenetic processes : morphological calibration of an Aggregation-diffusion growth model



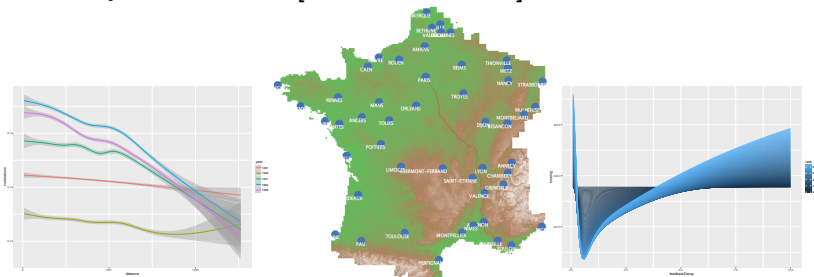
Coupled Growth and Correlations

Spatial non-stationarity of correlation matrix between urban morphology and network topology [Raimbault, 2016a] ; coupled growth model yield a large range of potential correlations [Raimbault, 2016b]



Macro-scale Growth and Network Necessity

Macro-scale population growth model reveals physical network effects in French System of Cities [Raimbault, 2016c]



Theory : Pillars

- ① *Networked Human Territories* → Raffestin approach to territory combined with Dupuy theory of networks.
- ② *Evolutionary Urban Theory* → City Systems as complex Adaptive systems, applied to human settlements in general and thus territorial systems.
- ③ *Urban Morphogenesis* → Morphogenesis as autonomous rules to explain growth of urban form. Used as the provider of modular decompositions.
- ④ *Boundaries and Co-evolution* → Co-evolution as the existence of *niche*, consequence of boundary patterns.

Theory : Specification

- Previous def. of territorial systems
- Modular decomposition and stationarity : existence of scales
- Feedback loops between and inside scales yield weak emergence, thus complexity
- Morphogenesis gives modular decomposition and co-evolution
- **Main assumption.** Necessity of Networks : networks are necessary component of co-evolutive niches.

The LUTETIA Model : Rationale

The LUTETIA Model : Structure

Governance Modeling

Matrix of actors utilities, depending on respective choices

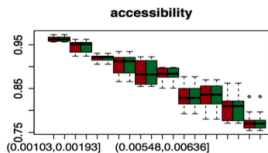
| 1 2 | C | A |
|-------|---|---|
| C | $U_i = \kappa \cdot \Delta X_i(Z_C^*) - I - \frac{\delta I}{2}$ | $\begin{cases} U_1 = \kappa \cdot \Delta X_1(Z_1^*) - I \\ U_2 = \kappa \cdot \Delta X_2(Z_2^*) - I - \frac{\delta I}{2} \end{cases}$ |
| A | $\begin{cases} U_1 = \kappa \cdot \Delta X_1(Z_1^*) - I - \frac{\delta I}{2} \\ U_2 = \kappa \cdot \Delta X_2(Z_2^*) - I \end{cases}$ | $U_i = \kappa \cdot \Delta X_i(Z_i^*) - I$ |

Two types of games implemented :

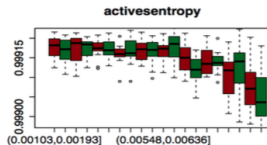
- Mixed Nash equilibrium, where actors compete
- One Rational Discrete Choice equilibrium

Model Output : Examples

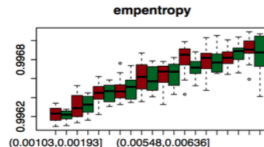
Model Exploration : Examples



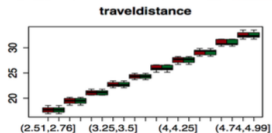
Lambda Accessibility



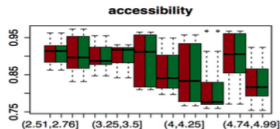
Lambda Accessibility



Lambda Accessibility



Network speed



Network speed

Application to Delta Pearl River Mega-city Region

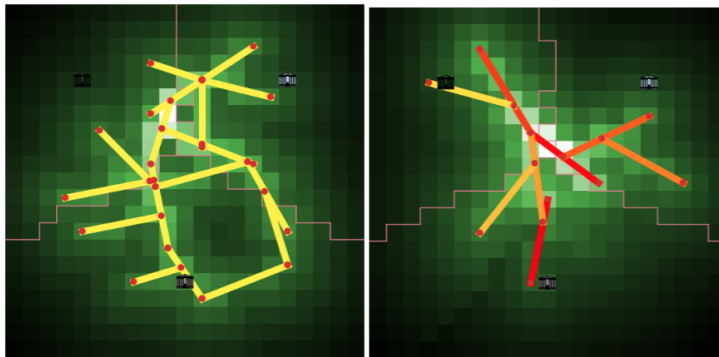
Application to DPR

Conclusion

- All code and data available at <https://github.com/JusteRaimbault/CityNetwork/tree/master/Models> in general ;

Reserve Slides

Long Time Limits for Transportation Networks



Governance Game Specification

Mixed Nash equilibrium probability :

$$p_i = \frac{J}{\Delta X_{\bar{i}} Z_C^* - \Delta X_{\bar{i}} Z_{\bar{i}}^*}$$

Discrete Choice model :

$$U_i(C) - U_i(NC) = p_{\bar{i}}(\Delta X_i Z_C^* - \Delta X_i Z_{\bar{i}}^*) - J$$

then

$$p_i = \frac{1}{1 + \exp \left(-\beta_{DC} \cdot \left(\frac{\Delta X_i Z_C^* - \Delta X_i Z_{\bar{i}}^*}{1 + \exp \left(-\beta_{DC} (p_{\bar{i}}(\Delta X_{\bar{i}} Z_C^* - \Delta X_{\bar{i}} Z_{\bar{i}}^*) - J) \right)} - J \right) \right)}$$

Lutetia : default parameter values

$$A_{max} = E_{max} = 500; r_A = 1; r_E = 0.8; \gamma_E = 0.9; \gamma_A = 0.65; \beta_I = 1.8; \lambda = 0.005; r_0 = 2$$

$$N_{expl} = 25; I = 0.001; J = 0.0001; v = 5; E_{ext}(t_0) = 3E_{max}; t_f = 4$$

Lutetia : Land-use Initialization

Initial distribution of Actives and Employments around governance centers at positions \vec{x}_i by

$$A(\vec{x}) = A_{max} \cdot \exp\left(\frac{\|\vec{x} - \vec{x}_i\|}{r_A}\right); E(\vec{x}) = E_{max} \cdot \exp\left(\frac{\|\vec{x} - \vec{x}_i\|}{r_E}\right)$$

Lutetia : Transportation

Transportation module : computation of flows ϕ_{ij} by solving on p_i, q_j by a fixed point method (Furness algorithm), the system of gravital flows

$$\begin{cases} \phi_{ij} = p_i q_j A_i E_j \exp(-\lambda_{tr} d_{ij}) \\ \sum_k \phi_{kj} = E_j; \sum_k \phi_{ik} = A_i \\ p_i = \frac{1}{\sum_k q_k E_k \exp(-\lambda_{tr} d_{ik})}; q_j = \frac{1}{\sum_k p_k A_k \exp(-\lambda_{tr} d_{kj})} \end{cases}$$

Trajectories then attributed by effective shortest path, and corresponding congestion c obtained (no Wardrop equilibrium).

Speed of network given by BPR function $v(c) = v_0 \left(1 - \frac{c}{\kappa}\right)^{\gamma_c}$. Congestion not used in current studies (infinite capacity κ).

Lutetia : Land-use Evolution

Land-Use module : we assume that residential/employments relocations are at equilibrium at the time scale of a tick, that corresponds to transportation infrastructure evolution time scale which is much larger (Bretagnolle, 2009).

We take a Cobb-douglas function for utilities of actives/employments at a given cell

$$U_i(A) = X_i(A)^{\gamma_A} \cdot F_i(A)^{1-\gamma_A}; F_i(A) = \frac{1}{A_i E_i}$$

$$U_j(E) = X_j(E)^{\gamma_E} \cdot F_j(E)^{1-\gamma_E}; F_j(E) = 1$$

where $X_i(A) = A_i \cdot \sum_j E_j \exp(-\lambda \cdot d_{ij})$ and $X_j(E) = E_j \cdot \sum_i A_i \exp(-\lambda \cdot d_{ij})$. Relocations are then done deterministically following a discrete choice model :

$$A_i(t+1) = \sum_i A_i(t) \cdot \frac{\exp(\beta U_i(A))}{\sum_i \exp(\beta U_i(A))}$$

$$E_j(t+1) = \sum_j E_j(t) \cdot \frac{\exp(\beta U_j(E))}{\sum_j \exp(\beta U_j(E))}$$

Lutetia : Network Distance Computation

Effective distances computation

- Euclidian distance matrix $d(i,j)$ computed analytically
- Network shortest paths between network intersections (rasterized network) updated in a dynamic way (addition of new paths and update/change of old paths if needed when a link is added), correspondance between network patches and closest intersection also updated dynamically ; $O(N_{inters}^3)$
- Weak component clusters and distance between clusters updated ; $O(N_{nw}^2)$
- Network distances between network patches updated, through the heuristic of only minimal connexions between clusters ; $O(N_{nw}^2)$
- Effective distances (taking paces/congestion into account) updated as minimum between euclidian time and $\min_{C,C'} d(i,C) + d_{nw}(p_C(i), p'_C(j)) + d(C',j)$; $O(N_{clusters}^2 \cdot N^2)$
[Approximated with \min_C only in the implementation, consistent within the interaction ranges ~ 5 patches taken in the model]

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