

Computational Analysis of Big Data

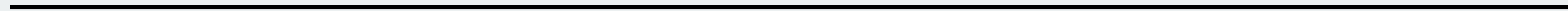
Week 2

A Data Scientist's most fundamental tools

Data visualization

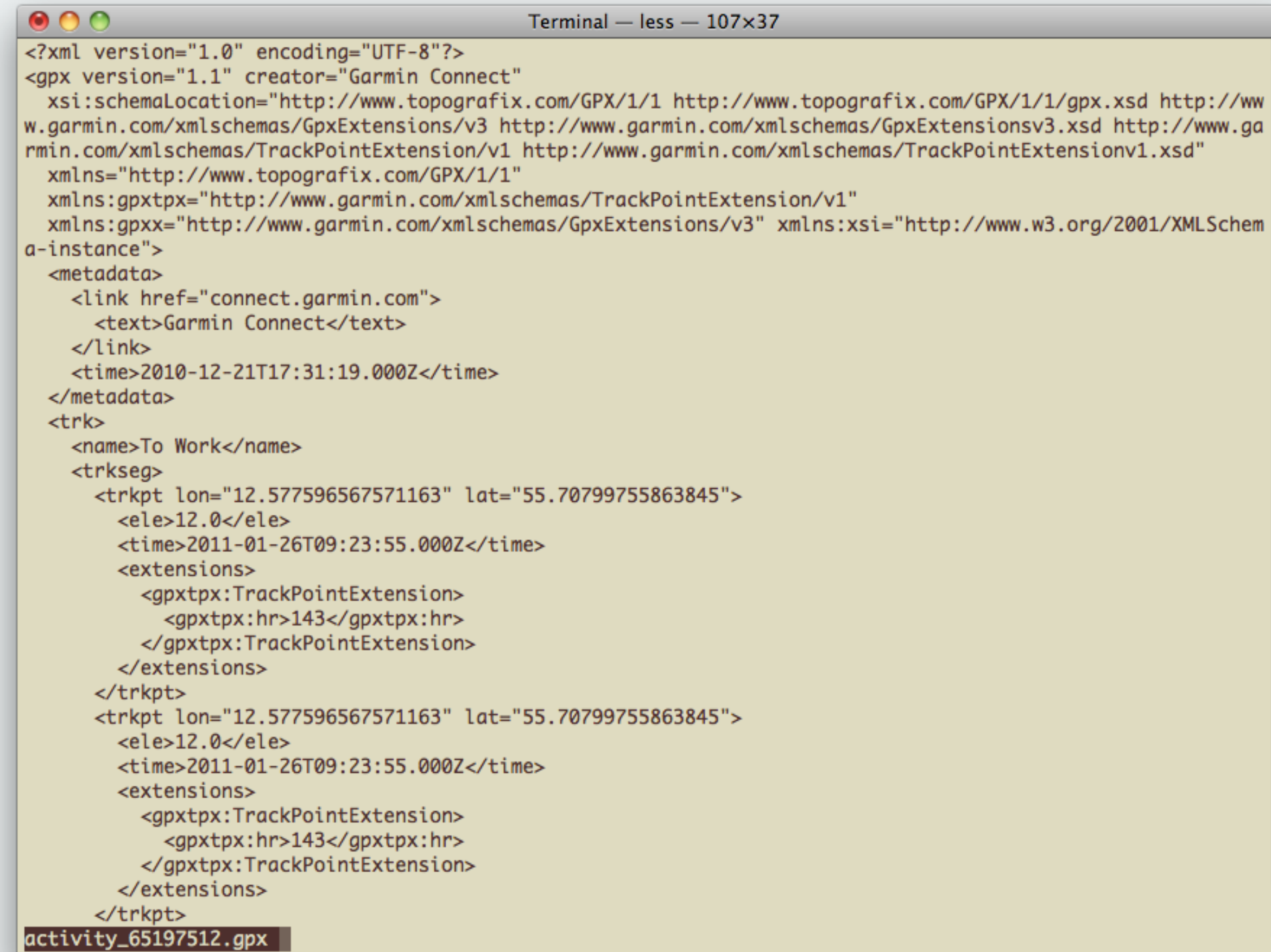
1
1000

1
1000
.



This is data

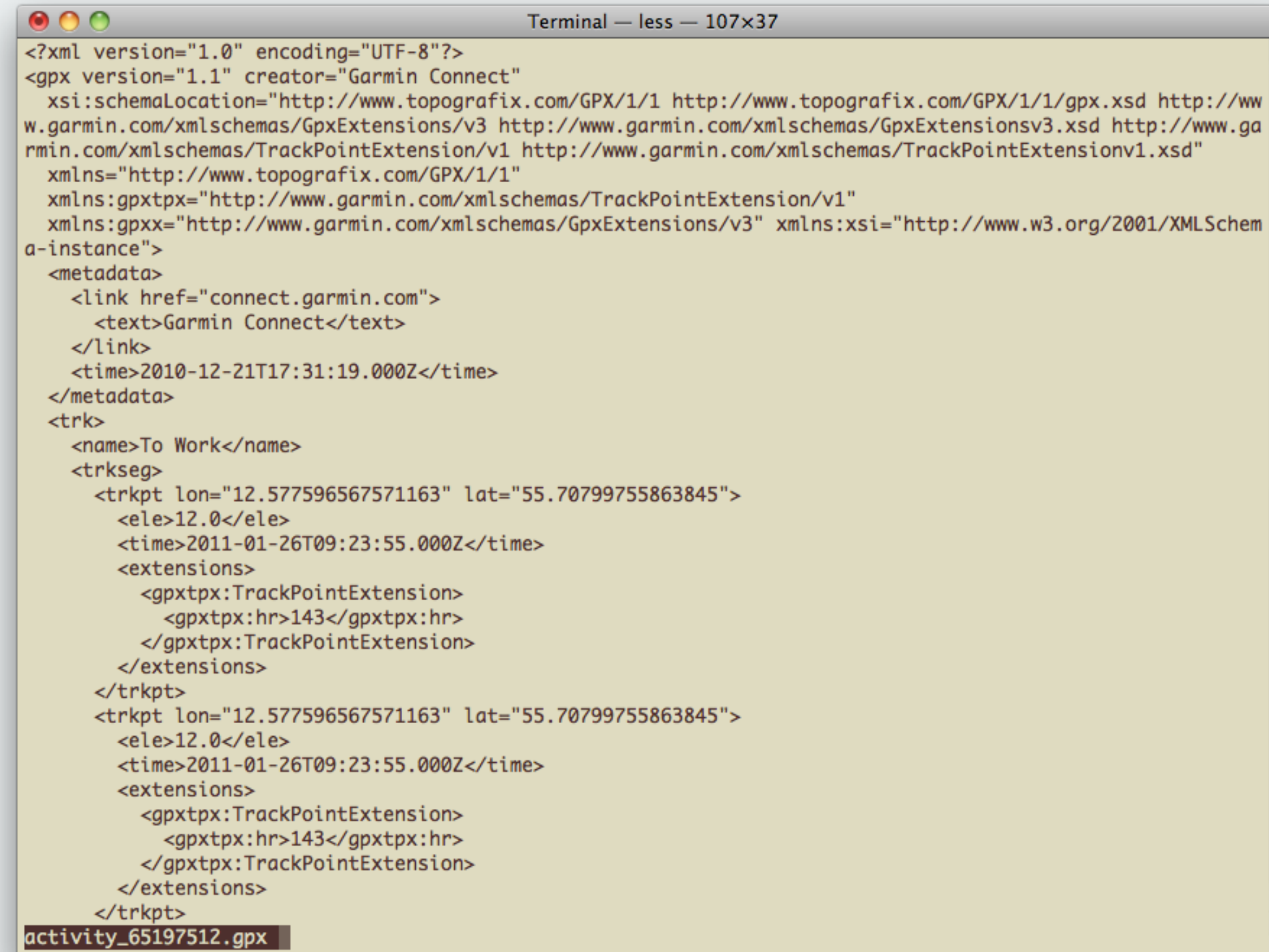
It's usually some
(large) file full of
text and numbers

A terminal window titled "Terminal — less — 107x37" displays the XML content of a GPX file named "activity_65197512.gpx". The XML is a GPX 1.1 file created by "Garmin Connect". It includes a metadata section with a link to "connect.garmin.com" and a timestamp of "2010-12-21T17:31:19.000Z". The main track section contains two track segments, each with a track point. The first track point has a longitude of "12.577596567571163", a latitude of "55.70799755863845", an elevation of "12.0", and a timestamp of "2011-01-26T09:23:55.000Z". It also includes an extension for "TrackPointExtension" with a heart rate of "143". The second track point is identical. The terminal window has a yellow background and a blue scrollbar on the right.

```
<?xml version="1.0" encoding="UTF-8"?>
<gpx version="1.1" creator="Garmin Connect"
  xsi:schemaLocation="http://www.topografix.com/GPX/1/1 http://www.topografix.com/GPX/1/1/gpx.xsd http://www.garmin.com/xmlschemas/GpxExtensions/v3 http://www.garmin.com/xmlschemas/GpxExtensionsv3.xsd http://www.garmin.com/xmlschemas/TrackPointExtension/v1 http://www.garmin.com/xmlschemas/TrackPointExtensionv1.xsd"
  xmlns="http://www.topografix.com/GPX/1/1"
  xmlns:gpstpx="http://www.garmin.com/xmlschemas/TrackPointExtension/v1"
  xmlns:gpxx="http://www.garmin.com/xmlschemas/GpxExtensions/v3" xmlns:xsi="http://www.w3.org/2001/XMLSchema-instance">
  <metadata>
    <link href="connect.garmin.com">
      <text>Garmin Connect</text>
    </link>
    <time>2010-12-21T17:31:19.000Z</time>
  </metadata>
  <trk>
    <name>To Work</name>
    <trkseg>
      <trkpt lon="12.577596567571163" lat="55.70799755863845">
        <ele>12.0</ele>
        <time>2011-01-26T09:23:55.000Z</time>
        <extensions>
          <gpstpx:TrackPointExtension>
            <gpstpx:hr>143</gpstpx:hr>
          </gpstpx:TrackPointExtension>
        </extensions>
      </trkpt>
      <trkpt lon="12.577596567571163" lat="55.70799755863845">
        <ele>12.0</ele>
        <time>2011-01-26T09:23:55.000Z</time>
        <extensions>
          <gpstpx:TrackPointExtension>
            <gpstpx:hr>143</gpstpx:hr>
          </gpstpx:TrackPointExtension>
        </extensions>
      </trkpt>
    </trkseg>
  </trk>
</gpx>
```

This is location data

It's usually some (large) file full of text and numbers

A terminal window titled "Terminal — less — 107x37" displays the XML content of a GPX file named "activity_65197512.gpx". The XML is a GPX 1.1 file created by "Garmin Connect". It includes a metadata section with a link to "connect.garmin.com" and a timestamp of "2010-12-21T17:31:19.000Z". The main track section contains two track segments, each with a track point. The first track point has a longitude of "12.577596567571163", a latitude of "55.70799755863845", an elevation of "12.0", and a timestamp of "2011-01-26T09:23:55.000Z". It also includes an extension for "TrackPointExtension" with a heart rate value of "143". The second track point is identical. The terminal window has a yellow background and a blue scrollbar on the right.

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<?xml version="1.0" encoding="UTF-8"?>
<gpx version="1.1" creator="Garmin Connect"
  xsi:schemaLocation="http://www.topografix.com/GPX/1/1 http://www.topografix.com/GPX/1/1/gpx.xsd http://www.garmin.com/xmlschemas/GpxExtensions/v3 http://www.garmin.com/xmlschemas/GpxExtensionsv3.xsd http://www.garmin.com/xmlschemas/TrackPointExtension/v1 http://www.garmin.com/xmlschemas/TrackPointExtensionv1.xsd"
  xmlns="http://www.topografix.com/GPX/1/1"
  xmlns:gpstpx="http://www.garmin.com/xmlschemas/TrackPointExtension/v1"
  xmlns:gpxx="http://www.garmin.com/xmlschemas/GpxExtensions/v3" xmlns:xsi="http://www.w3.org/2001/XMLSchema-instance">
  <metadata>
    <link href="connect.garmin.com">
      <text>Garmin Connect</text>
    </link>
    <time>2010-12-21T17:31:19.000Z</time>
  </metadata>
  <trk>
    <name>To Work</name>
    <trkseg>
      <trkpt lon="12.577596567571163" lat="55.70799755863845">
        <ele>12.0</ele>
        <time>2011-01-26T09:23:55.000Z</time>
        <extensions>
          <gpstpx:TrackPointExtension>
            <gpstpx:hr>143</gpstpx:hr>
          </gpstpx:TrackPointExtension>
        </extensions>
      </trkpt>
      <trkpt lon="12.577596567571163" lat="55.70799755863845">
        <ele>12.0</ele>
        <time>2011-01-26T09:23:55.000Z</time>
        <extensions>
          <gpstpx:TrackPointExtension>
            <gpstpx:hr>143</gpstpx:hr>
          </gpstpx:TrackPointExtension>
        </extensions>
      </trkpt>
    </trkseg>
  </trk>
</gpx>
```

And if you're lucky there is also some kind of `<markup>`

Most raw data is incomprehensible to humans

We have:

- Narrow spectrum of data that we can process and understand
- Limited memory for processing new information
- Limited attention for undertaking focussed tasks



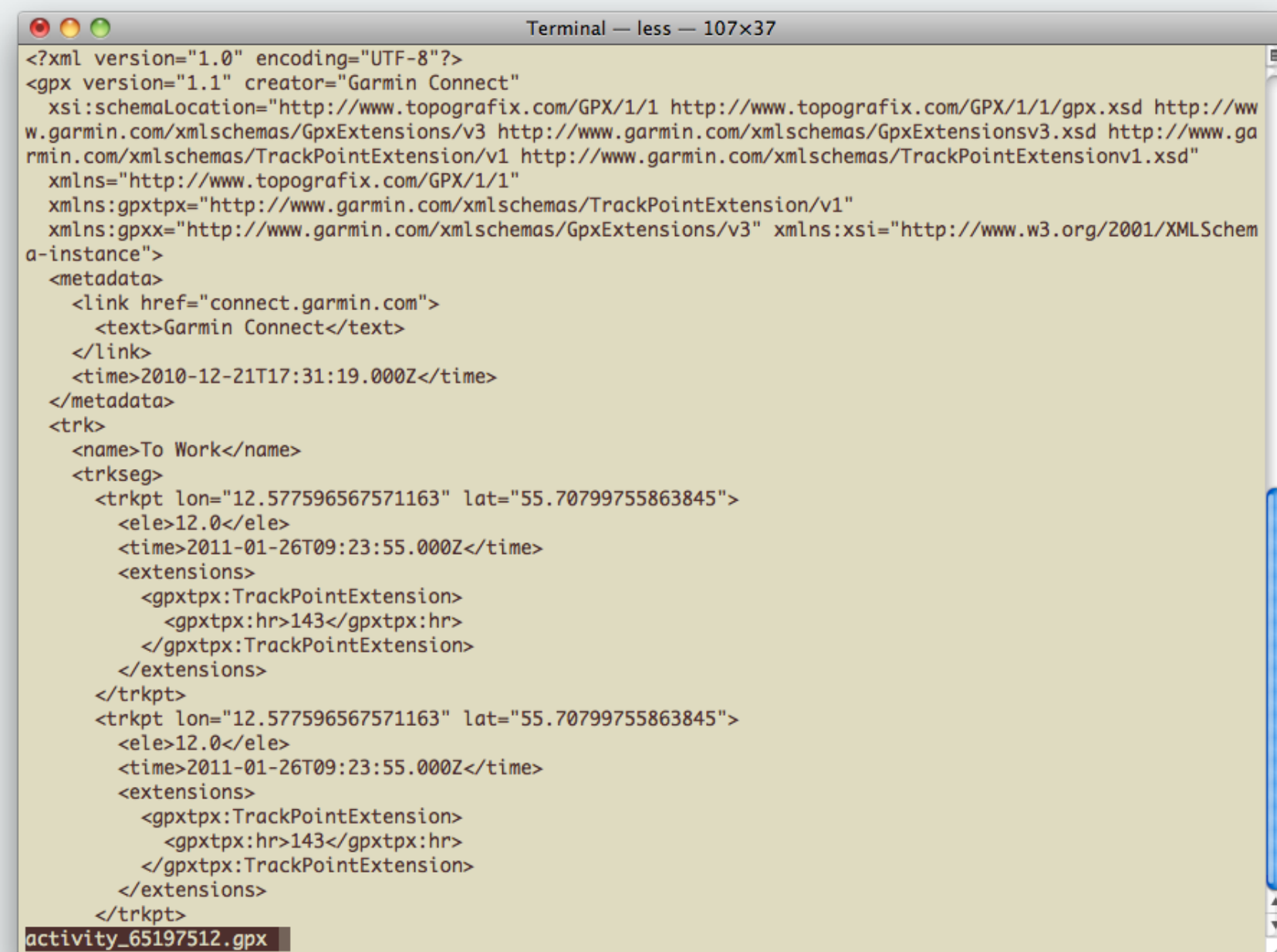
The human eye is made for advanced pattern recognition

It can:

- Immediately recognize a pattern in a highly complex image
- Quickly spot things that deviate from patterns (outlier detection)
- Process streams of images and recognize patterns over time



Data must be rendered in human-friendly format



Terminal — less — 107x37

```
<?xml version="1.0" encoding="UTF-8"?>
<gpx version="1.1" creator="Garmin Connect"
  xsi:schemaLocation="http://www.topografix.com/GPX/1/1 http://www.topografix.com/GPX/1/1/gpx.xsd http://www.garmin.com/xmlschemas/GpxExtensions/v3 http://www.garmin.com/xmlschemas/GpxExtensionsv3.xsd http://www.garmin.com/xmlschemas/TrackPointExtension/v1 http://www.garmin.com/xmlschemas/TrackPointExtensionv1.xsd"
  xmlns="http://www.topografix.com/GPX/1/1"
  xmlns:gpxtpx="http://www.garmin.com/xmlschemas/TrackPointExtension/v1"
  xmlns:gpxx="http://www.garmin.com/xmlschemas/GpxExtensions/v3" xmlns:xsi="http://www.w3.org/2001/XMLSchema-instance">
  <metadata>
    <link href="connect.garmin.com">
      <text>Garmin Connect</text>
    </link>
    <time>2010-12-21T17:31:19.000Z</time>
  </metadata>
  <trk>
    <name>To Work</name>
    <trkseg>
      <trkpt lon="12.577596567571163" lat="55.70799755863845">
        <ele>12.0</ele>
        <time>2011-01-26T09:23:55.000Z</time>
        <extensions>
          <gpxtpx:TrackPointExtension>
            <gpxtpx:hr>143</gpxtpx:hr>
          </gpxtpx:TrackPointExtension>
        </extensions>
      </trkpt>
      <trkpt lon="12.577596567571163" lat="55.70799755863845">
        <ele>12.0</ele>
        <time>2011-01-26T09:23:55.000Z</time>
        <extensions>
          <gpxtpx:TrackPointExtension>
            <gpxtpx:hr>143</gpxtpx:hr>
          </gpxtpx:TrackPointExtension>
        </extensions>
      </trkpt>
    </trkseg>
  </trk>
</gpx>
```

activity_65197512.gpx



?

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```
Terminal — less — 107x37
<?xml version="1.0" encoding="UTF-8"?>
<gpx version="1.1" creator="Garmin Connect"
  xsi:schemaLocation="http://www.topografix.com/GPX/1/1 http://www.topografix.com/GPX/1/1/gpx.xsd http://www.garmin.com/xmlschemas/GpxExtensions/v3 http://www.garmin.com/xmlschemas/GpxExtensionsv3.xsd http://www.garmin.com/xmlschemas/TrackPointExtension/v1 http://www.garmin.com/xmlschemas/TrackPointExtensionv1.xsd"
  xmlns="http://www.topografix.com/GPX/1/1"
  xmlns:gpstpx="http://www.garmin.com/xmlschemas/TrackPointExtension/v1"
  xmlns:gpss="http://www.garmin.com/xmlschemas/GpxExtensions/v3" xmlns:xsi="http://www.w3.org/2001/XMLSchema-instance">
  <metadata>
    <link href="connect.garmin.com">
      <text>Garmin Connect</text>
    </link>
    <time>2010-12-21T17:31:19.000Z</time>
  </metadata>
  <trk>
    <name>To Work</name>
    <trkseg>
      <trkpt lon="12.577596567571163" lat="55.70799755863845">
        <ele>12.0</ele>
        <time>2011-01-26T09:23:55.000Z</time>
        <extensions>
          <gpstpx:TrackPointExtension>
            <gpstpx:hr>143</gpstpx:hr>
          </gpstpx:TrackPointExtension>
        </extensions>
      </trkpt>
      <trkpt lon="12.577596567571163" lat="55.70799755863845">
        <ele>12.0</ele>
        <time>2011-01-26T09:23:55.000Z</time>
        <extensions>
          <gpstpx:TrackPointExtension>
            <gpstpx:hr>143</gpstpx:hr>
          </gpstpx:TrackPointExtension>
        </extensions>
      </trkpt>
    </trkseg>
  </trk>
</gpx>
activity_65197512.gpx
```



	lat	lon
0	55.784332	12.525468
1	55.784437	12.525030
2	55.784435	12.525043
3	55.784224	12.525565
4	55.784437	12.525031
5	55.784411	12.525055
6	55.784397	12.525070
7	55.784215	12.525537
8	55.784416	12.525059
9	55.784147	12.525530
10	55.784417	12.525063
11	55.784222	12.525535
12	55.784415	12.525052
13	55.784152	12.525590
14	55.784411	12.525054
15	55.784387	12.525093
16	55.784255	12.525532
17	55.784406	12.525060
18	55.784402	12.525065
19	55.784353	12.525407
20	55.784414	12.525059
21	55.784220	12.525534
22	55.784410	12.525083
23	55.784192	12.525557
24	55.784406	12.525053
25	55.784411	12.525060
26	55.784243	12.525500
27	55.784400	12.525066
28	55.784408	12.525056
29	55.784168	12.525580
...

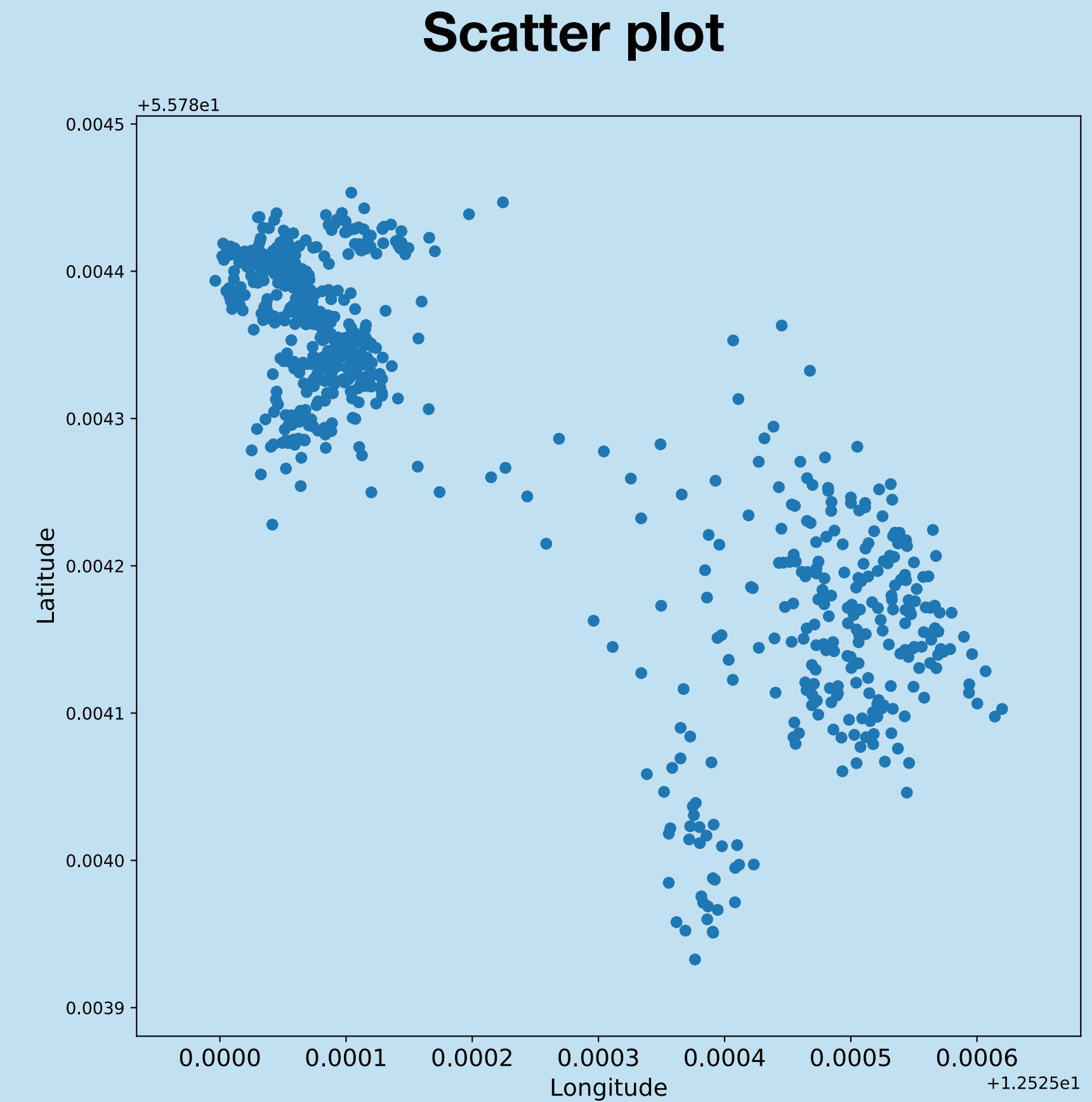


?

Data must be rendered in human-friendly format

```
Terminal — less — 107×37
<?xml version="1.0" encoding="UTF-8"?>
<gpx version="1.1" creator="Garmin Connect"
  xsi:schemaLocation="http://www.topografix.com/GPX/1/1 http://www.topografix.com/GPX/1/1/gpx.xsd http://www.
w.garmin.com/xmlschemas/GpxExtensions/v3 http://www.garmin.com/xmlschemas/GpxExtensionsv3.xsd http://www.ga
rmin.com/xmlschemas/TrackPointExtension/v1 http://www.garmin.com/xmlschemas/TrackPointExtensionv1.xsd"
  xmlns="http://www.topografix.com/GPX/1/1"
  xmlns:gpxtpx="http://www.garmin.com/xmlschemas/TrackPointExtension/v1"
  xmlns:gxpx="http://www.garmin.com/xmlschemas/GpxExtensions/v3" xmlns:xsi="http://www.w3.org/2001/XMLSchema
a-instance">
  <metadata>
    <link href="connect.garmin.com">
      <text>Garmin Connect</text>
    </link>
    <time>2010-12-21T17:31:19.000Z</time>
  </metadata>
  <trk>
    <name>To Work</name>
    <trkseg>
      <trkpt lon="12.577596567571163" lat="55.70799755863845">
        <ele>12.0</ele>
        <time>2011-01-26T09:23:55.000Z</time>
        <extensions>
          <gpxtpx:TrackPointExtension>
            <gpxtpx:hr>143</gpxtpx:hr>
          </gpxtpx:TrackPointExtension>
        </extensions>
      </trkpt>
      <trkpt lon="12.577596567571163" lat="55.70799755863845">
        <ele>12.0</ele>
        <time>2011-01-26T09:23:55.000Z</time>
        <extensions>
          <gpxtpx:TrackPointExtension>
            <gpxtpx:hr>143</gpxtpx:hr>
          </gpxtpx:TrackPointExtension>
        </extensions>
      </trkpt>
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  </trk>
</gpx>
activity_65197512.gpx
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6	55.784397	12.525070
7	55.784215	12.525537
8	55.784416	12.525059
9	55.784147	12.525530
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12	55.784415	12.525052
13	55.784152	12.525590
14	55.784411	12.525054
15	55.784387	12.525093
16	55.784255	12.525532
17	55.784406	12.525060
18	55.784402	12.525065
19	55.784353	12.525407
20	55.784414	12.525059
21	55.784220	12.525534
22	55.784410	12.525083
23	55.784192	12.525557
24	55.784406	12.525053
25	55.784411	12.525060
26	55.784243	12.525500
27	55.784400	12.525066
28	55.784408	12.525056
29	55.784168	12.525580
...



Data must be rendered in human-friendly format

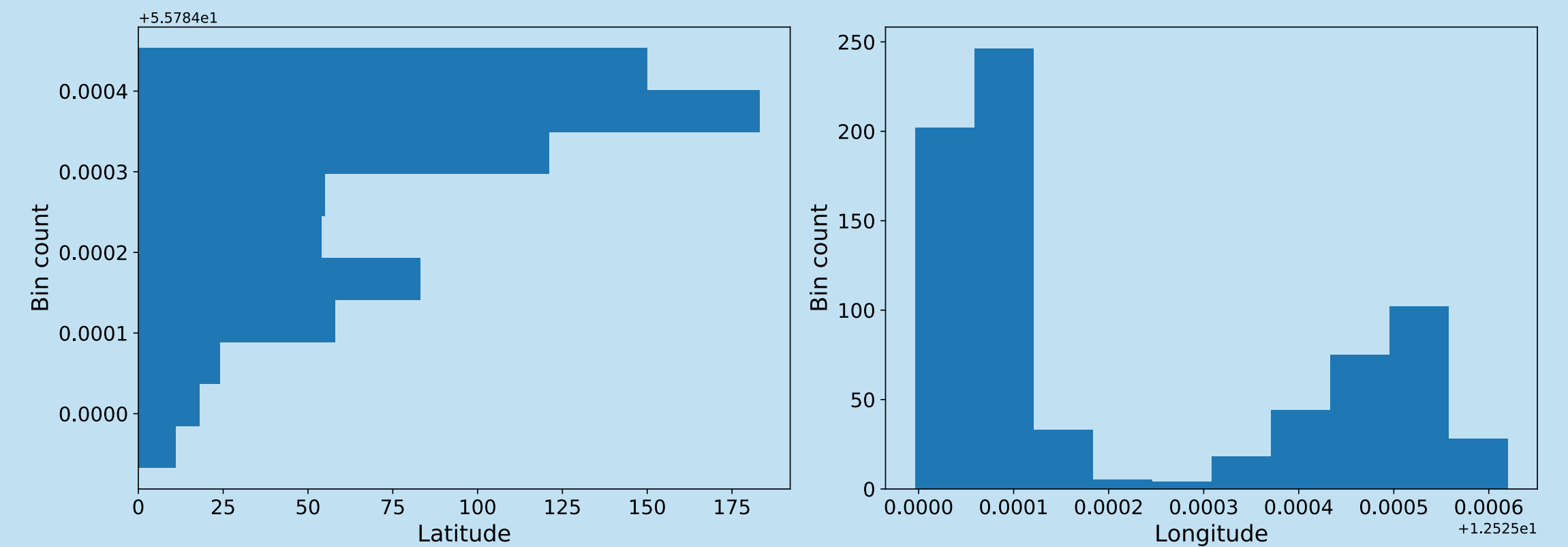
```
Terminal — less — 107x37
<?xml version="1.0" encoding="UTF-8"?>
<gpx version="1.1" creator="Garmin Connect"
  xsi:schemaLocation="http://www.topografix.com/GPX/1/1 http://www.topografix.com/GPX/1/1/gpx.xsd http://www.garmin.com/xmlschemas/GpxExtensions/v3 http://www.garmin.com/xmlschemas/GpxExtensionsv3.xsd http://www.garmin.com/xmlschemas/TrackPointExtension/v1 http://www.garmin.com/xmlschemas/TrackPointExtensionv1.xsd"
  xmlns="http://www.topografix.com/GPX/1/1"
  xmlns:gpstpx="http://www.garmin.com/xmlschemas/TrackPointExtension/v1"
  xmlns:gpex="http://www.garmin.com/xmlschemas/GpxExtensions/v3" xmlns:xsi="http://www.w3.org/2001/XMLSchema-instance">
  <metadata>
    <link href="connect.garmin.com">
      <text>Garmin Connect</text>
    </link>
    <time>2010-12-21T17:31:19.000Z</time>
  </metadata>
  <trk>
    <name>To Work</name>
    <trkseg>
      <trkpt lon="12.577596567571163" lat="55.70799755863845">
        <ele>12.0</ele>
        <time>2011-01-26T09:23:55.000Z</time>
        <extensions>
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            <gpstpx:hr>143</gpstpx:hr>
          </gpstpx:TrackPointExtension>
        </extensions>
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      <trkpt lon="12.577596567571163" lat="55.70799755863845">
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        <time>2011-01-26T09:23:55.000Z</time>
        <extensions>
          <gpstpx:TrackPointExtension>
            <gpstpx:hr>143</gpstpx:hr>
          </gpstpx:TrackPointExtension>
        </extensions>
      </trkpt>
    </trkseg>
  </trk>
</gpx>
activity_65197512.gpx
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	lat	lon
0	55.784332	12.525468
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12	55.784415	12.525052
13	55.784152	12.525590
14	55.784411	12.525054
15	55.784387	12.525093
16	55.784255	12.525532
17	55.784406	12.525060
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26	55.784243	12.525500
27	55.784400	12.525066
28	55.784408	12.525056
29	55.784168	12.525580
...



Histogram

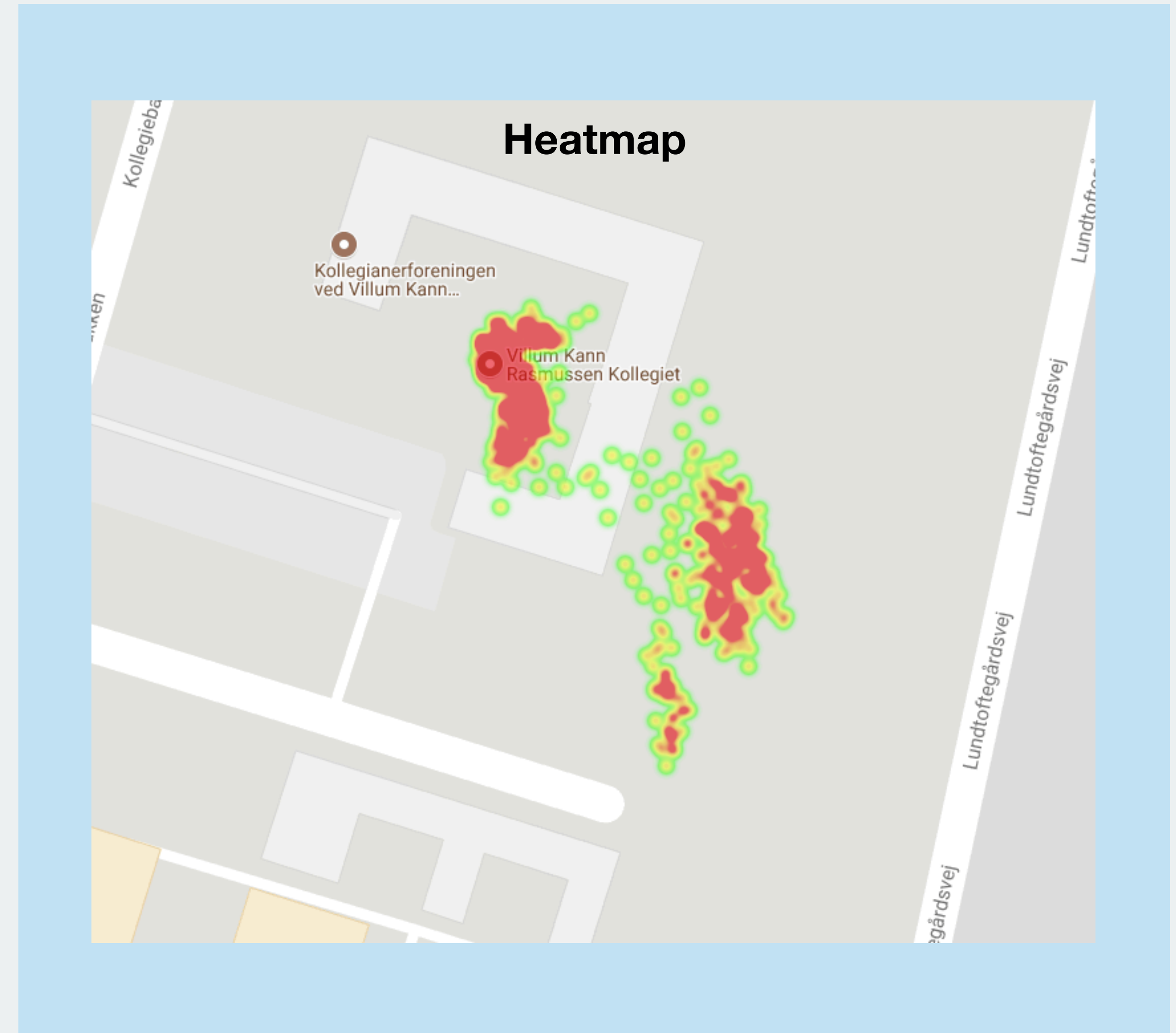


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```
Terminal — less — 107x37
<?xml version="1.0" encoding="UTF-8"?>
<gpx version="1.1" creator="Garmin Connect"
  xsi:schemaLocation="http://www.topografix.com/GPX/1/1 http://www.topografix.com/GPX/1/1/gpx.xsd http://www.garmin.com/xmlschemas/GpxExtensions/v3 http://www.garmin.com/xmlschemas/GpxExtensionsv3.xsd http://www.garmin.com/xmlschemas/TrackPointExtension/v1 http://www.garmin.com/xmlschemas/TrackPointExtensionv1.xsd"
  xmlns="http://www.topografix.com/GPX/1/1"
  xmlns:gpstpx="http://www.garmin.com/xmlschemas/TrackPointExtension/v1"
  xmlns:gpex="http://www.garmin.com/xmlschemas/GpxExtensions/v3" xmlns:xsi="http://www.w3.org/2001/XMLSchema-instance">
  <metadata>
    <link href="connect.garmin.com">
      <text>Garmin Connect</text>
    </link>
    <time>2010-12-21T17:31:19.000Z</time>
  </metadata>
  <trk>
    <name>To Work</name>
    <trkseg>
      <trkpt lon="12.577596567571163" lat="55.70799755863845">
        <ele>12.0</ele>
        <time>2011-01-26T09:23:55.000Z</time>
        <extensions>
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            <gpstpx:hr>143</gpstpx:hr>
          </gpstpx:TrackPointExtension>
        </extensions>
      </trkpt>
      <trkpt lon="12.577596567571163" lat="55.70799755863845">
        <ele>12.0</ele>
        <time>2011-01-26T09:23:55.000Z</time>
        <extensions>
          <gpstpx:TrackPointExtension>
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  </trk>
</gpx>
activity_65197512.gpx
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	lat	lon
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5	55.784411	12.525055
6	55.784397	12.525070
7	55.784215	12.525537
8	55.784416	12.525059
9	55.784147	12.525530
10	55.784417	12.525063
11	55.784222	12.525535
12	55.784415	12.525052
13	55.784152	12.525590
14	55.784411	12.525054
15	55.784387	12.525093
16	55.784255	12.525532
17	55.784406	12.525060
18	55.784402	12.525065
19	55.784353	12.525407
20	55.784414	12.525059
21	55.784220	12.525534
22	55.784410	12.525083
23	55.784192	12.525557
24	55.784406	12.525053
25	55.784411	12.525060
26	55.784243	12.525500
27	55.784400	12.525066
28	55.784408	12.525056
29	55.784168	12.525580
...



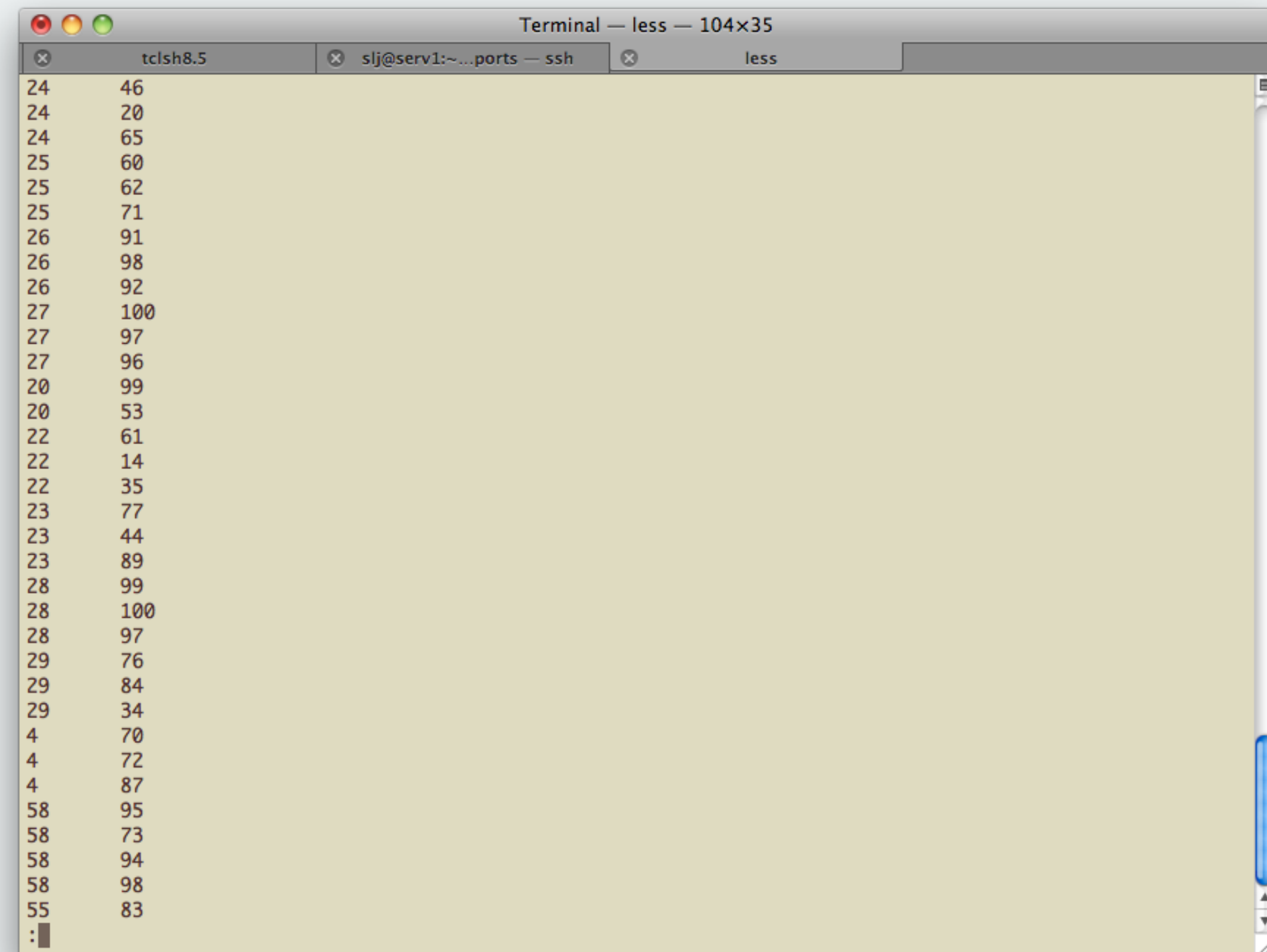
Relational data



A terminal window titled "Terminal — less — 104x35" displays a table of data. The table has two columns of numbers. The first column contains values ranging from 4 to 29, and the second column contains values ranging from 14 to 100. The data is presented in a simple text format with a light yellow background.

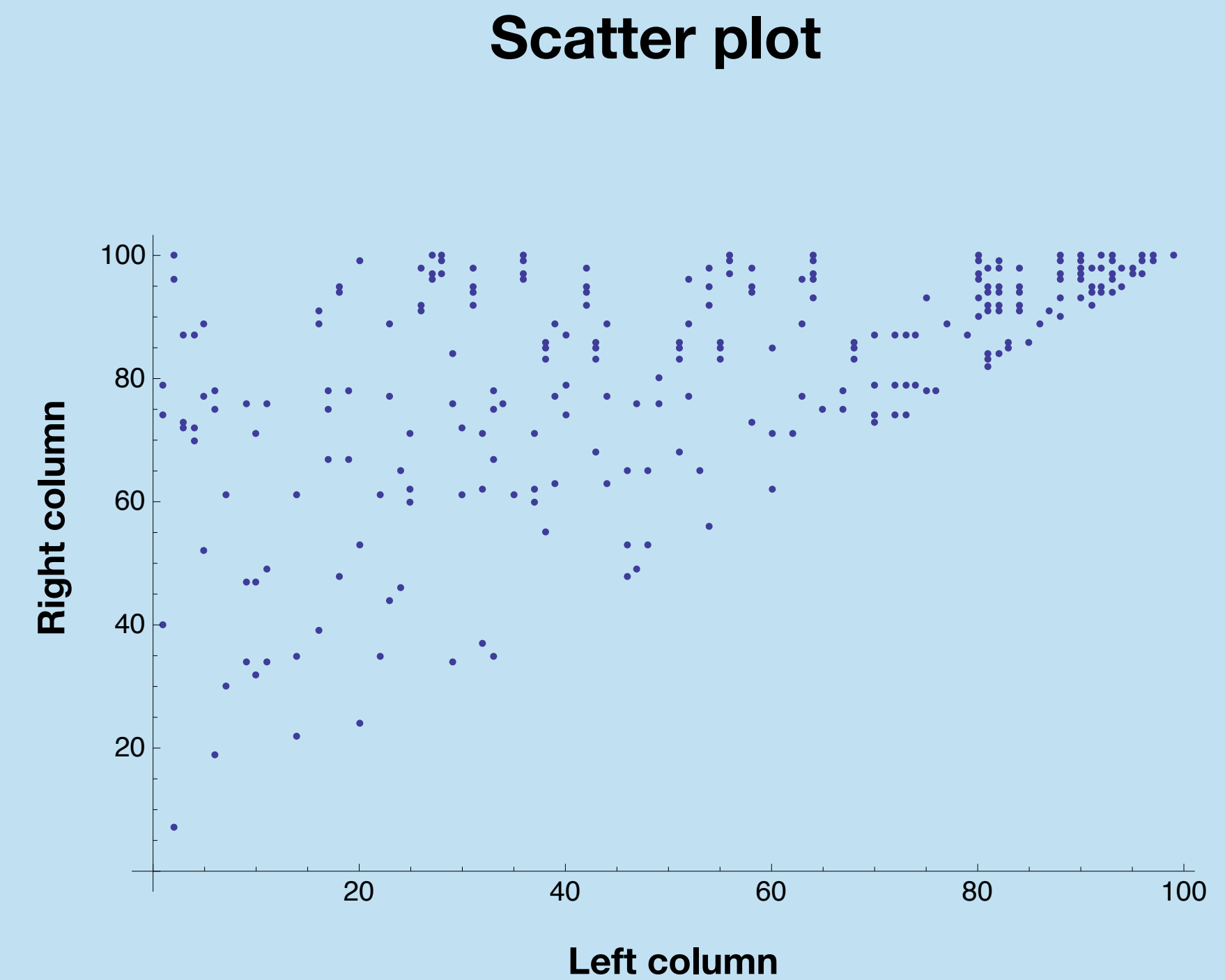
24	46
24	20
24	65
25	60
25	62
25	71
26	91
26	98
26	92
27	100
27	97
27	96
20	99
20	53
22	61
22	14
22	35
23	77
23	44
23	89
28	99
28	100
28	97
29	76
29	84
29	34
4	70
4	72
4	87
58	95
58	73
58	94
58	98
55	83
:	

Relational data

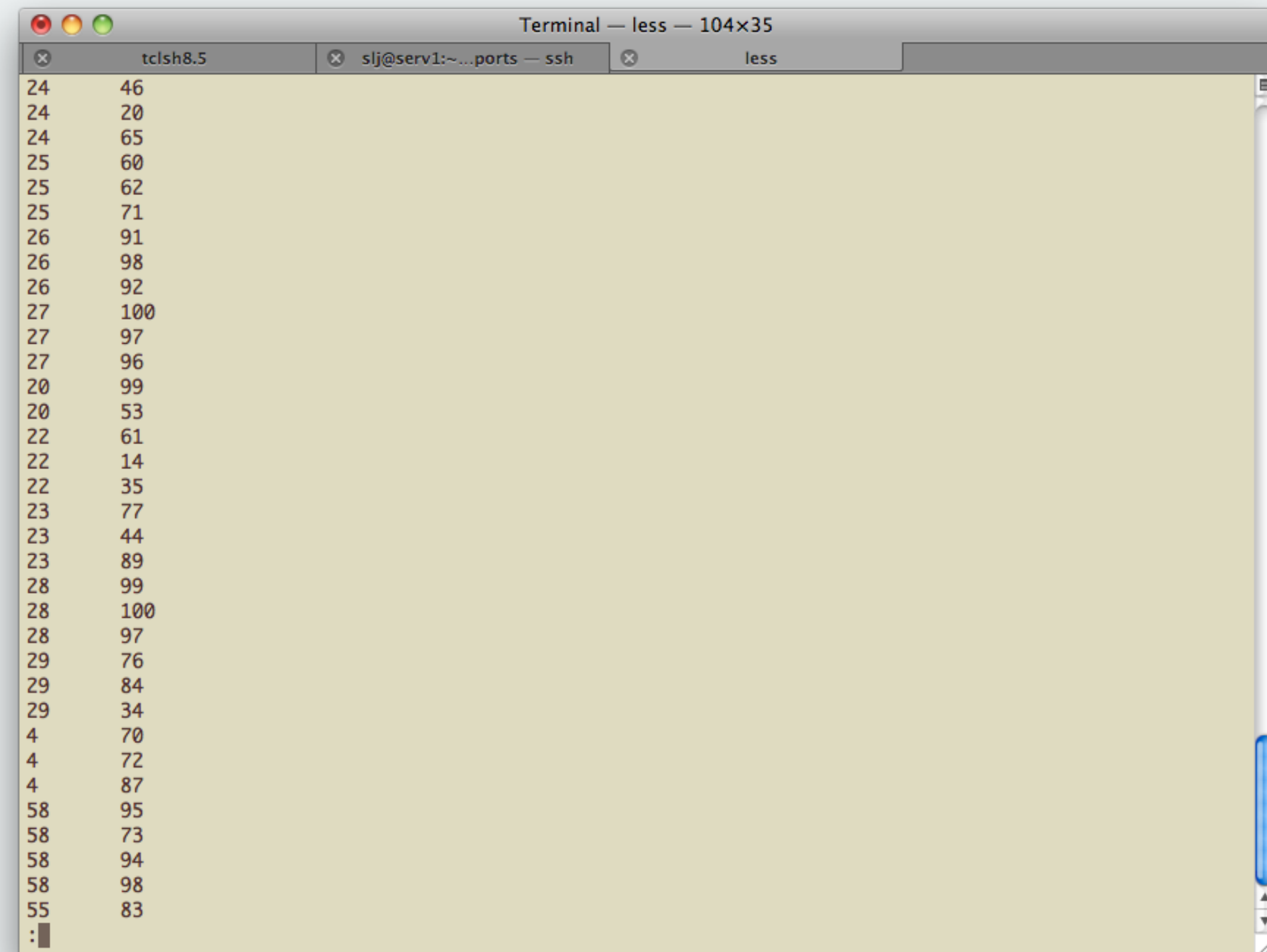


Terminal window showing a table of data. The window title is "Terminal — less — 104x35". The table has two columns of numbers. The first column contains values ranging from 4 to 28, and the second column contains values ranging from 83 to 100. The data is displayed in a less window.

24	46
24	20
24	65
25	60
25	62
25	71
26	91
26	98
26	92
27	100
27	97
27	96
20	99
20	53
22	61
22	14
22	35
23	77
23	44
23	89
28	99
28	100
28	97
29	76
29	84
29	34
4	70
4	72
4	87
58	95
58	73
58	94
58	98
55	83

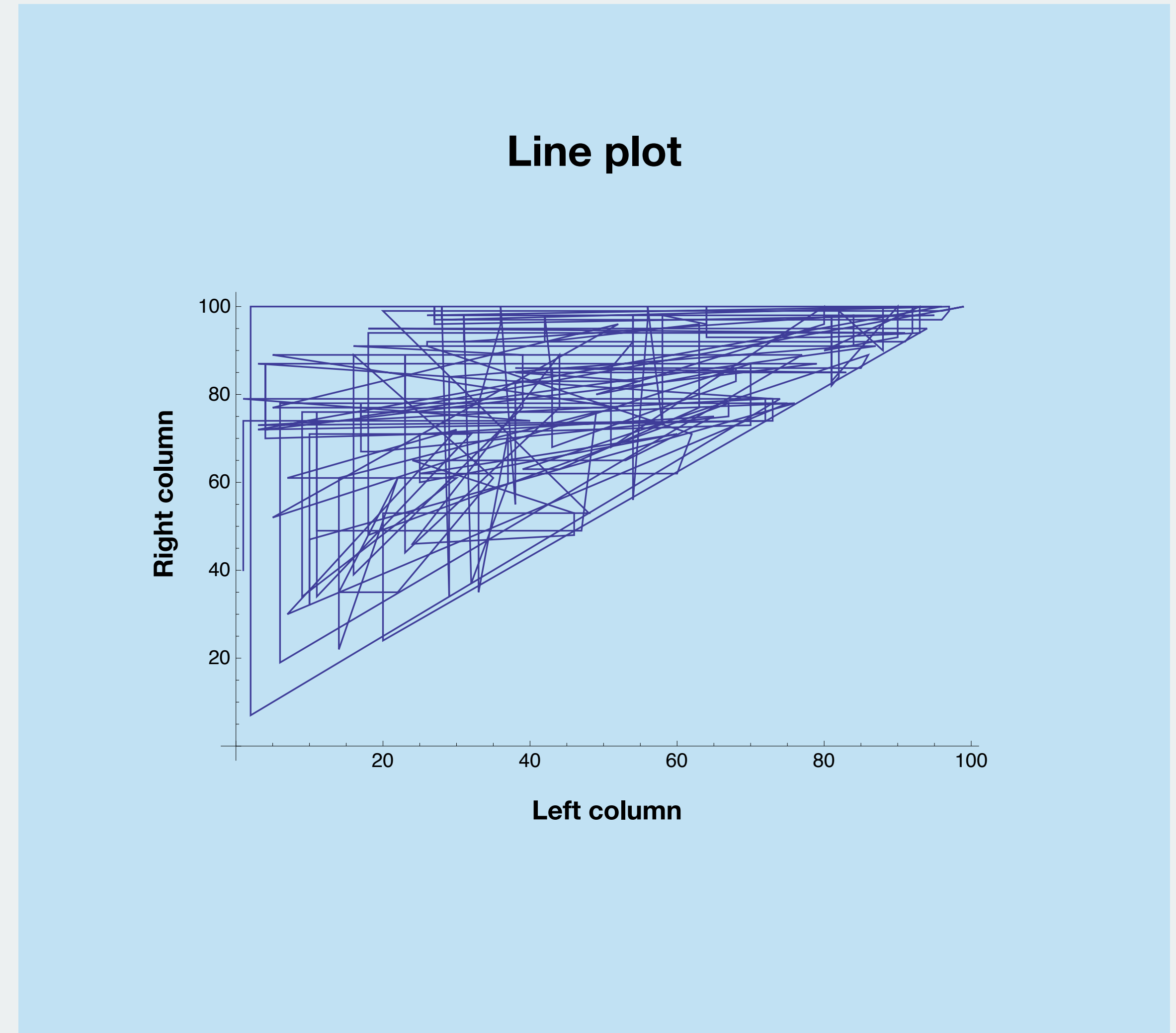


Relational data

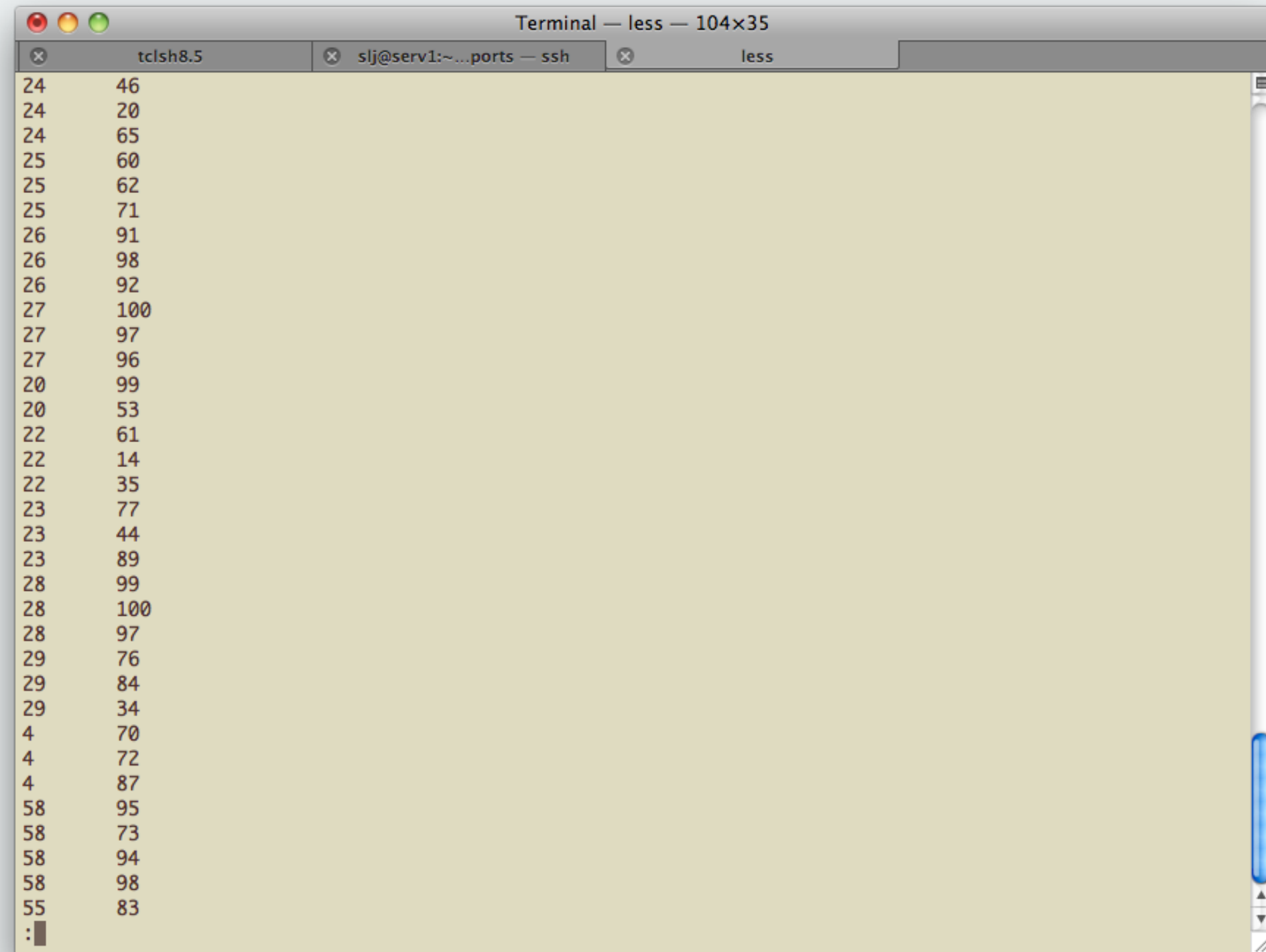


A terminal window titled "Terminal — less — 104x35" displays a table of data. The table has two columns: the first column contains IDs (e.g., 24, 25, 26, 27, 20, 22, 23, 28, 29, 4, 58, 55) and the second column contains values (e.g., 46, 20, 65, 60, 62, 71, 91, 98, 92, 100, 97, 96, 99, 53, 61, 14, 35, 77, 44, 89, 99, 100, 97, 76, 84, 34, 70, 72, 87, 95, 73, 94, 98, 83). The terminal window has a title bar with standard macOS window controls and a tab bar showing "tclsh8.5", "slj@serv1:~...ports — ssh", and "less".

24	46
24	20
24	65
25	60
25	62
25	71
26	91
26	98
26	92
27	100
27	97
27	96
20	99
20	53
22	61
22	14
22	35
23	77
23	44
23	89
28	99
28	100
28	97
29	76
29	84
29	34
4	70
4	72
4	87
58	95
58	73
58	94
58	98
55	83



Relational data

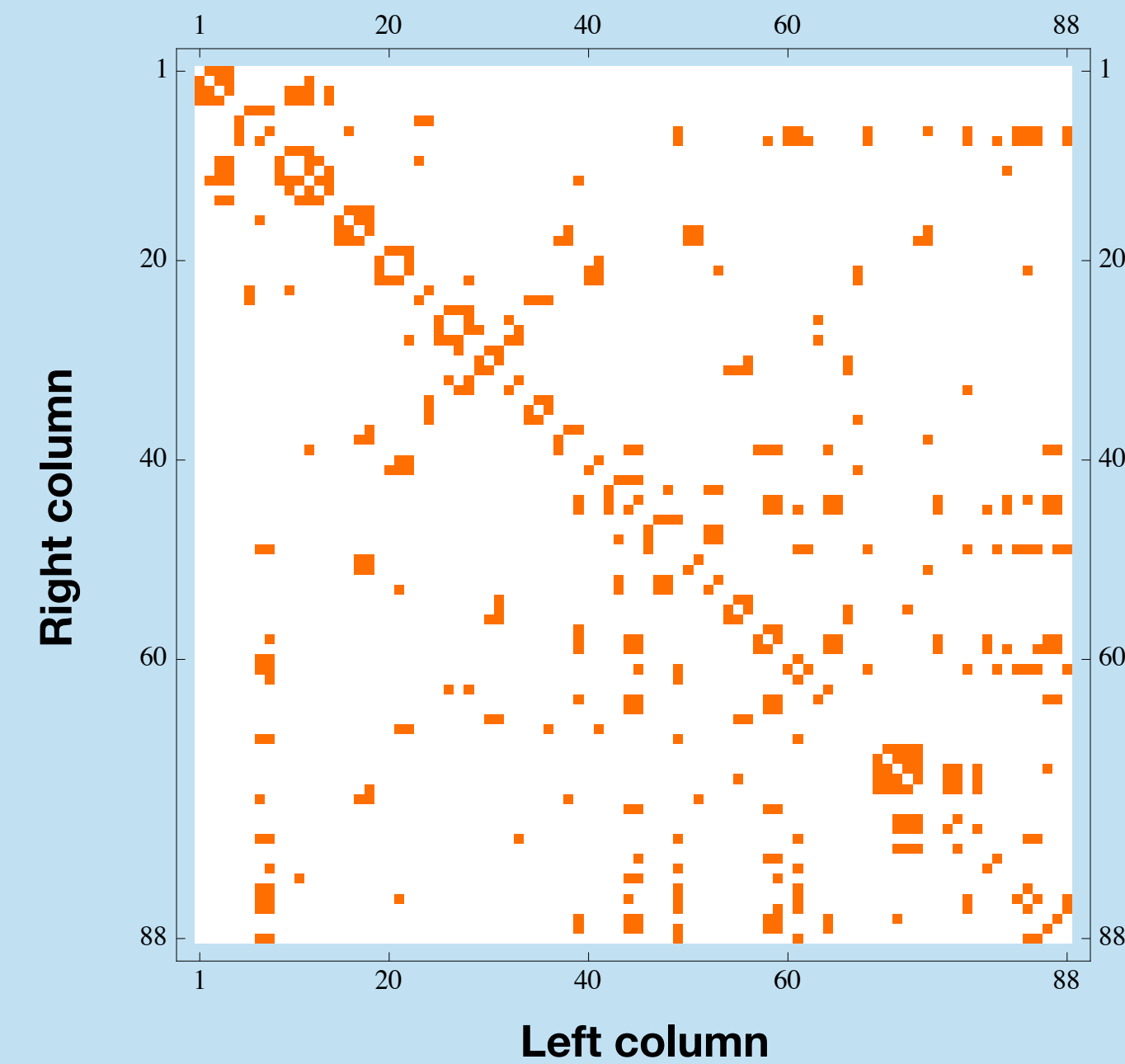


Terminal window showing a list of pairs of numbers, representing relational data. The window title is "Terminal — less — 104x35". The data is displayed in a table format with two columns.

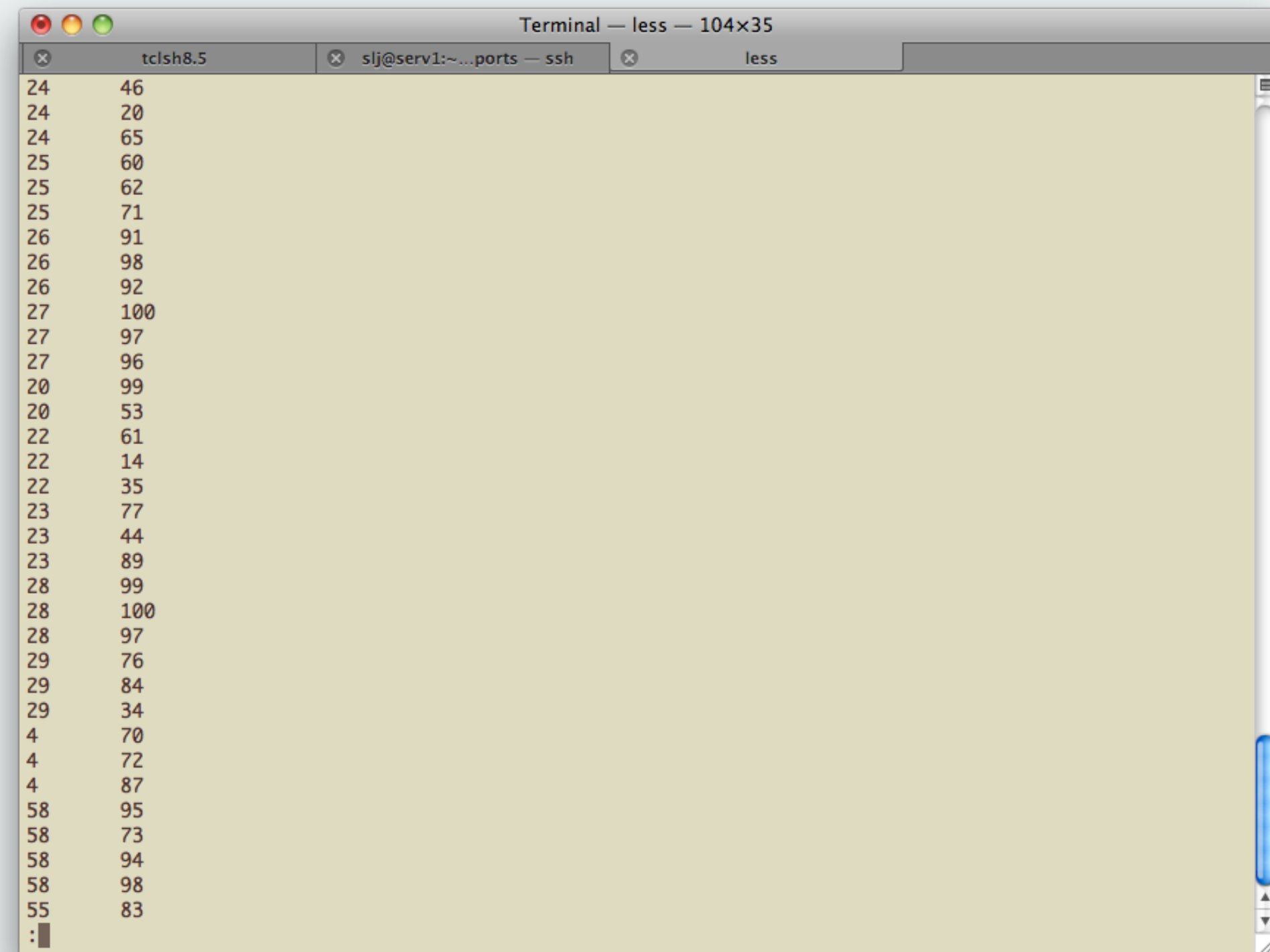
24	46
24	20
24	65
25	60
25	62
25	71
26	91
26	98
26	92
27	100
27	97
27	96
20	99
20	53
22	61
22	14
22	35
23	77
23	44
23	89
28	99
28	100
28	97
29	76
29	84
29	34
4	70
4	72
4	87
58	95
58	73
58	94
58	98
55	83



Row-ordered adjacency matrix



Relational data



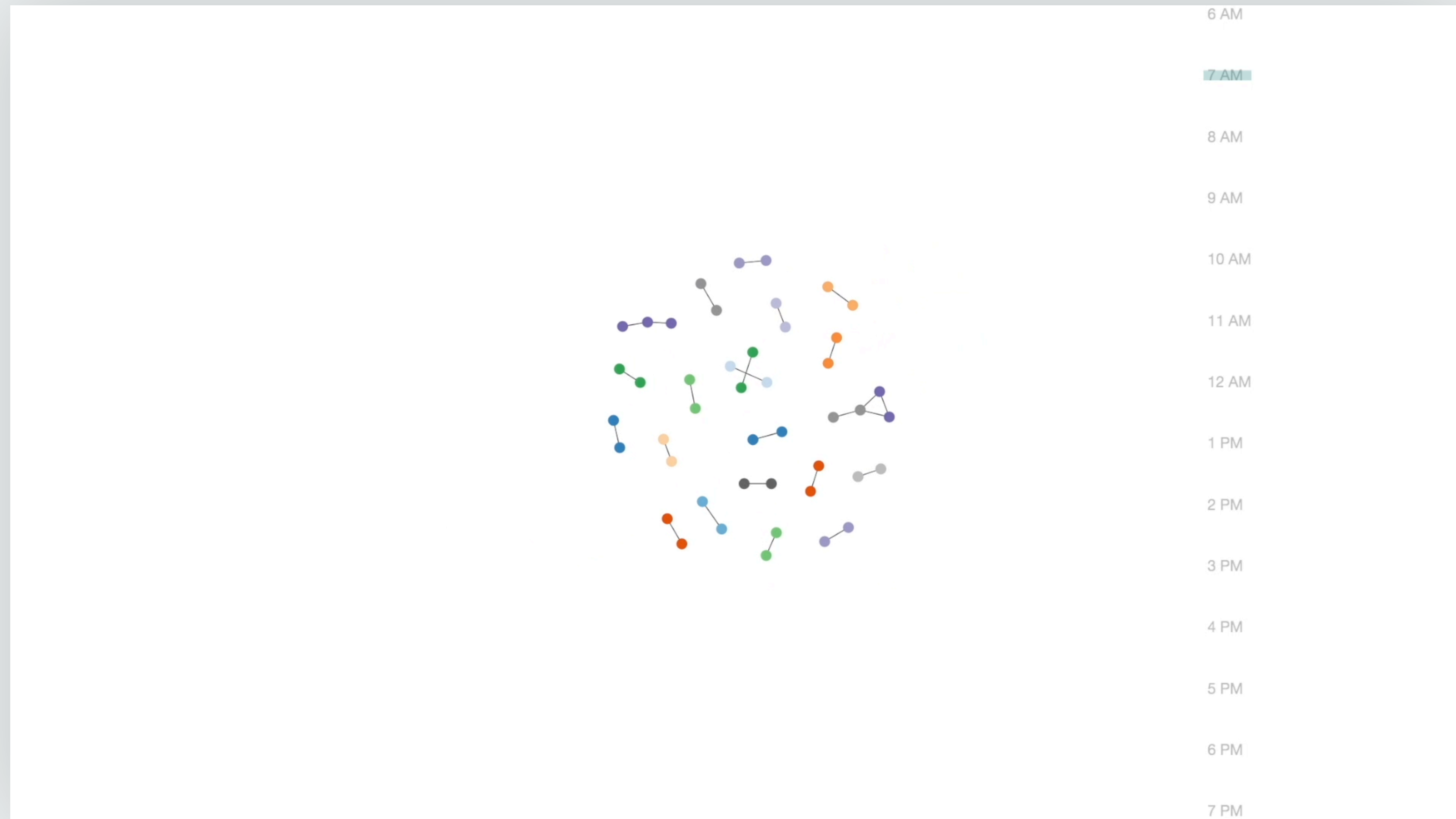
A terminal window titled "Terminal — less — 104x35" displays a list of IP addresses and their associated ports. The window has three tabs: "tclsh8.5", "slj@serv1:~...ports — ssh", and "less". The data is presented in a two-column format, with IP addresses on the left and ports on the right. The list is as follows:

24	46
24	20
24	65
25	60
25	62
25	71
26	91
26	98
26	92
27	100
27	97
27	96
20	99
20	53
22	61
22	14
22	35
23	77
23	44
23	89
28	99
28	100
28	97
29	76
29	84
29	34
4	70
4	72
4	87
58	95
58	73
58	94
58	98
55	83



Network

Very complex data that changes in time!

[link](#)[link](#)

Most fancy visualizations break down to very simple things

**For understanding how
data is distributed**

- Histograms
- Kernel density plots
- Box plots/violin plots
- Heatmaps

Most fancy visualizations break down to very simple things

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**For understanding
how variables in
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- Scatter plots
- Pairs plot
- Time series plot
- Line plot
- Bar plot

Most fancy visualizations break down to very simple things

For understanding how data is distributed

- Histograms
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For understanding how variables in data compare and develop

- Scatter plots
- Pairs plot
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- Bar plot

For understanding interrelations in highly connected data

- Networks

Linear algebra

Linear algebra

A principled and scalable method for manipulating data

Linear algebra **A principled and scalable method for manipulating data**

Objects

- Scalars
- Vectors
- Matrices

**Everything is
a Tensor!**

Linear algebra A principled and scalable method for manipulating data

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**Everything is
a Tensor!**

scalar

0D

```
In [2]: print np.random.randint(1, 100)
Last executed 2018-01-25 11:52:52 in 5ms
82
```


Linear algebra A principled and scalable method for manipulating data

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```
In [2]: print np.random.randint(1, 100)
Last executed 2018-01-25 11:52:52 in 5ms
82
```

vector

1D

```
In [3]: print np.random.randint(1, 100, size=3)
Last executed 2018-01-25 11:53:37 in 5ms
[83 80 84]
```

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```

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Last executed 2018-01-25 11:53:37 in 5ms
[83 80 84]
```

matrix

2D

```
In [4]: print np.random.randint(1, 100, size=(3, 3))
Last executed 2018-01-25 11:54:38 in 4ms
[[99 47 77]
 [15 82  9]
 [59 55 48]]
```

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Last executed 2018-01-25 11:53:37 in 5ms
[83 80 84]
```

matrix

2D

```
In [4]: print np.random.randint(1, 100, size=(3, 3))
Last executed 2018-01-25 11:54:38 in 4ms
[[99 47 77]
 [15 82  9]
 [59 55 48]]
```

3D-tensor

3D

```
In [5]: print np.random.randint(1, 100, size=(3, 3, 3))
Last executed 2018-01-25 11:55:19 in 5ms
[[[45 11 73]
  [84 50 88]
  [13 22 97]]

 [[10  5 12]
  [27 23 76]
  [43 84 53]]

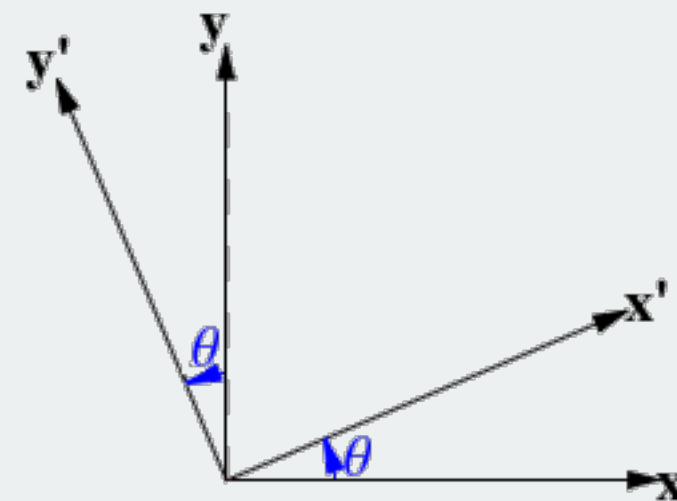
 [[86 58 61]
  [71 95 86]
  [92 19 68]]]
```

Linear algebra A principled and scalable method for manipulating data

Operations

- Products: **dot**, cross
- Elementwise: *addition, subtraction, multiplication, division*
- Mutations: *transpose, inverse/pseudo-inverse, scaling, rotation*

$$\begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} ax + by + cz \\ dx + ey + fz \\ gx + hy + iz \end{bmatrix}$$



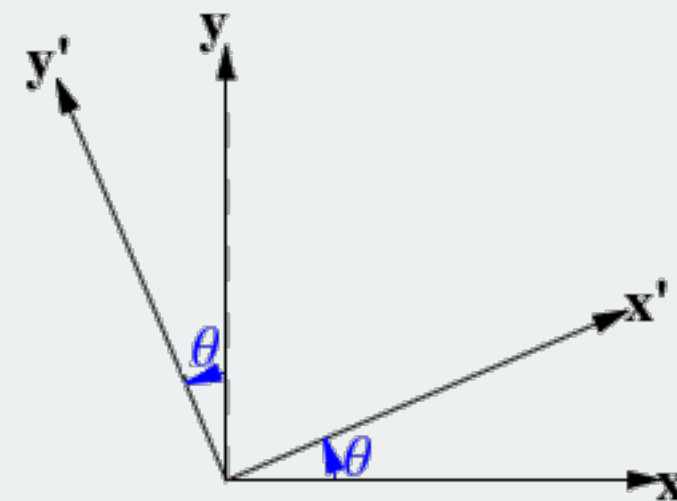
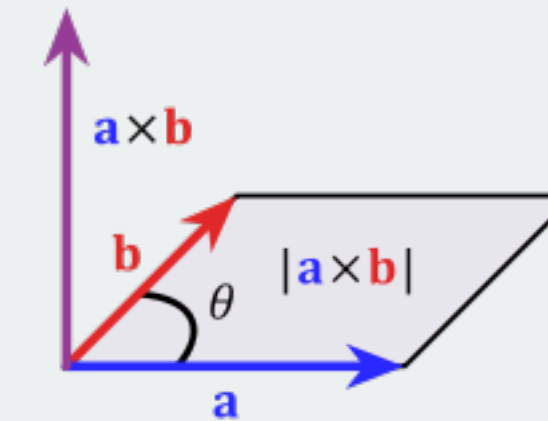
**used frequently for
basis transformation**

Linear algebra A principled and scalable method for manipulating data

Operations

- Products: *dot*, **cross**
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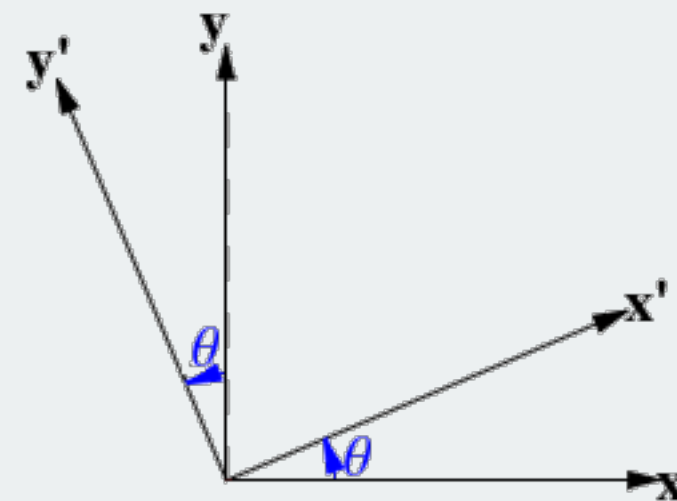
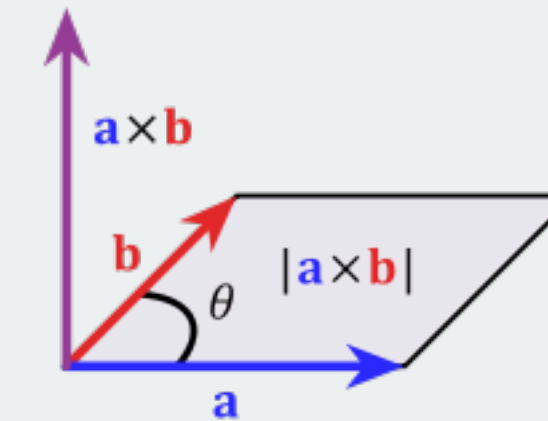
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$$\begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} ax + by + cz \\ dx + ey + fz \\ gx + hy + iz \end{bmatrix}$$



used frequently for
basis transformation

$$\begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix} \quad \text{Original matrix}$$

$$\begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix}^T \Rightarrow \begin{bmatrix} a & d & g \\ b & e & h \\ c & f & i \end{bmatrix}$$

Statistics

Statistics

A set of tools and jargon for describing data

Statistics

A set of tools and jargon for describing data

Vocabulary

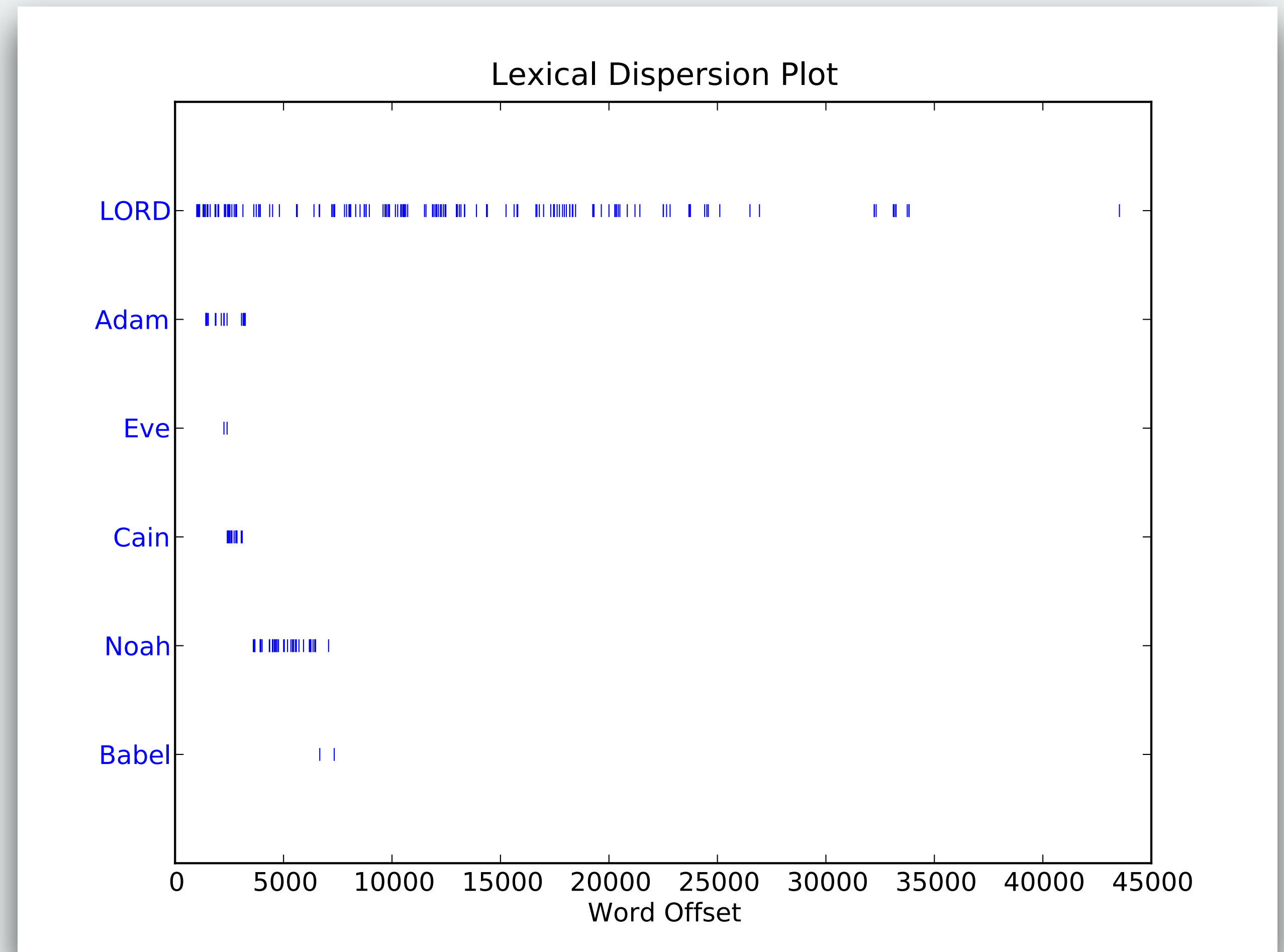
- Mean, median
- Variance, standard deviation, range
- Correlation, covariance

Statistics

A set of tools and jargon for describing data

Vocabulary

- Mean, median
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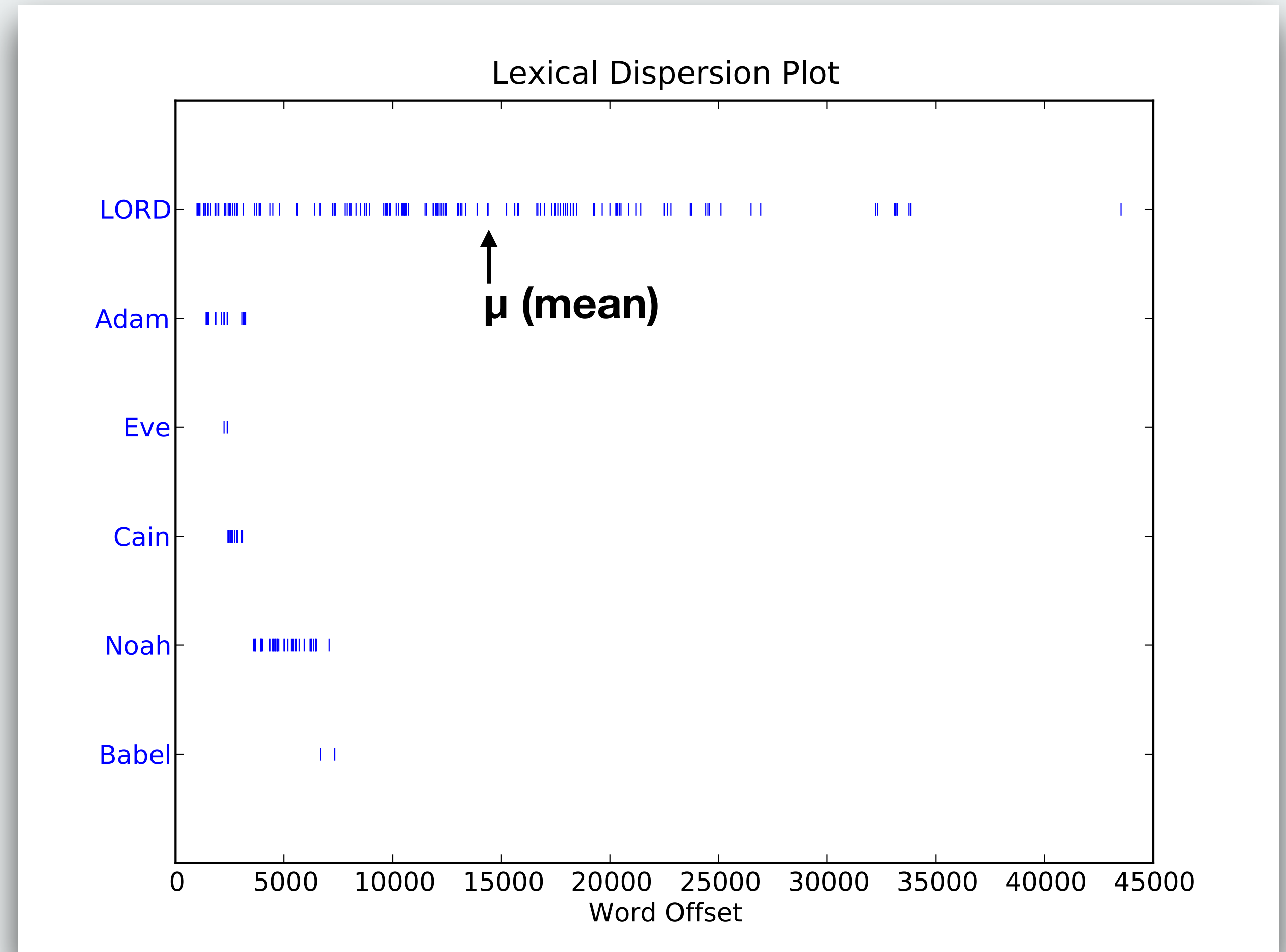
Statistics

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$$\mu = \frac{\text{Sum of values}}{\text{Number of values}}$$



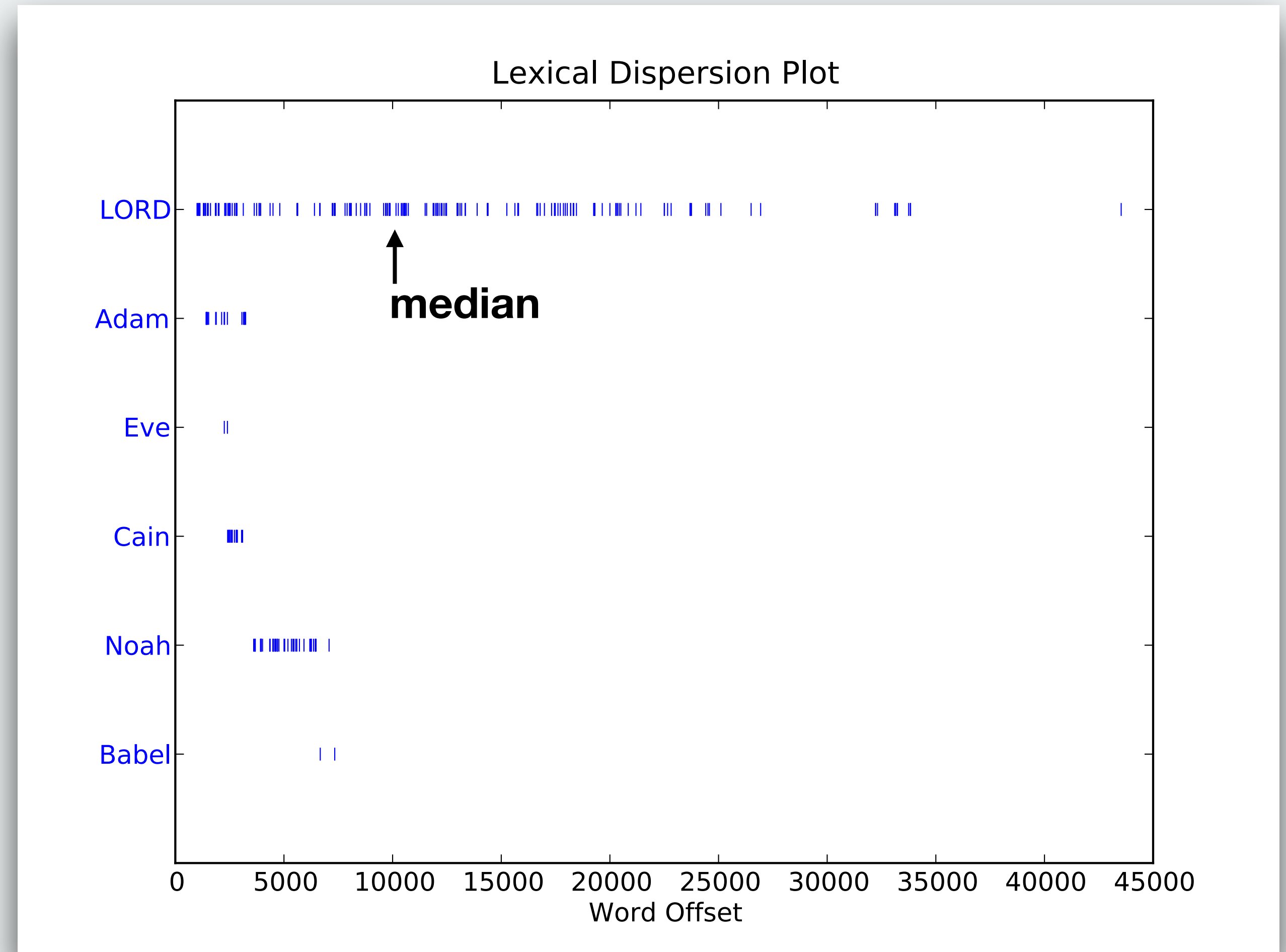
Statistics

A set of tools and jargon for describing data

Vocabulary

- Mean, **median**
- Variance, standard deviation, range
- Correlation, covariance

median = Middle number
in ordered list



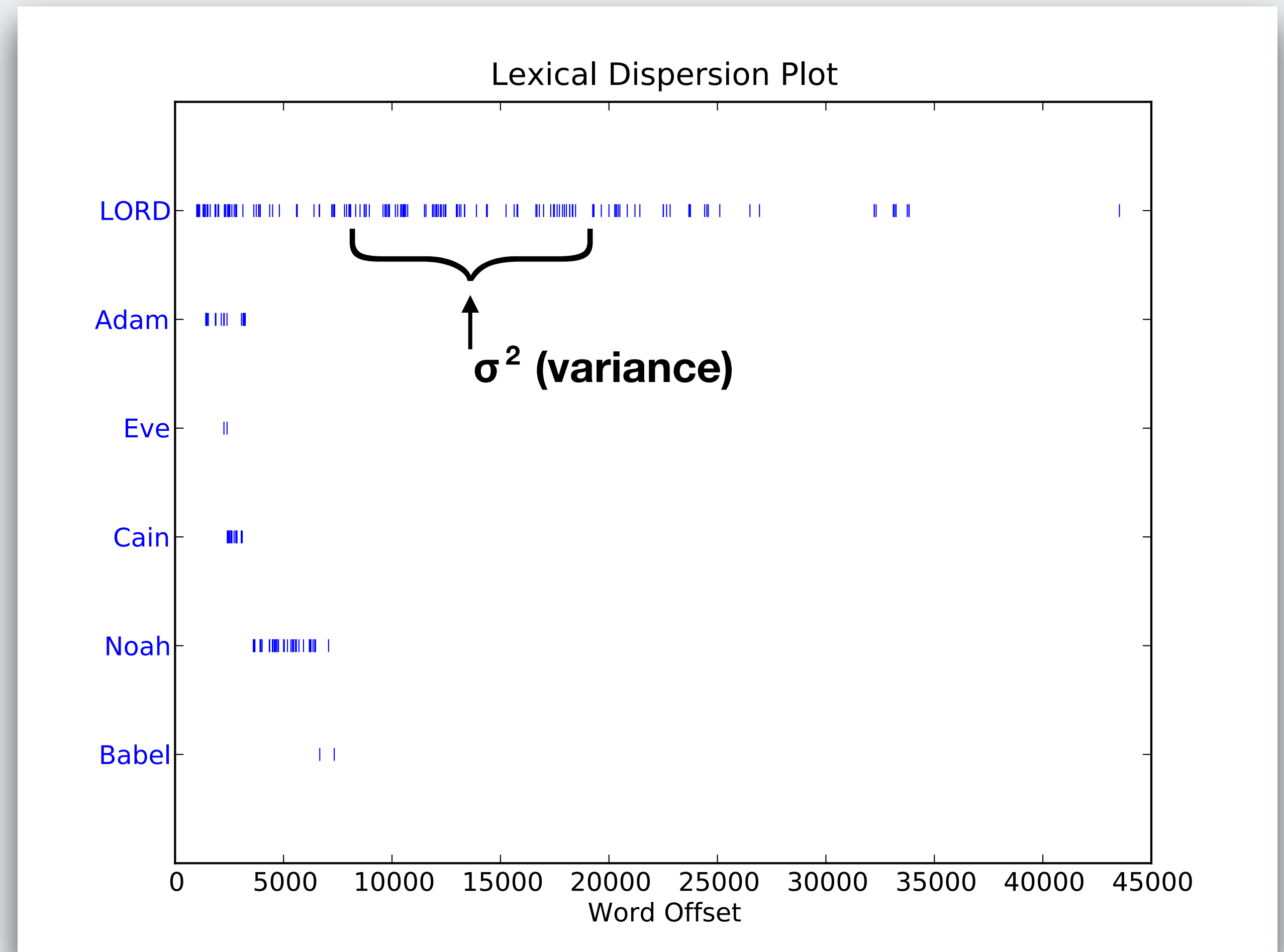
Statistics

A set of tools and jargon for describing data

Vocabulary

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- **Variance**, standard deviation, range
- Correlation, covariance

$$\sigma^2 = \frac{1}{N-1} \sum_{i=1}^n (x_i - \mu)^2$$



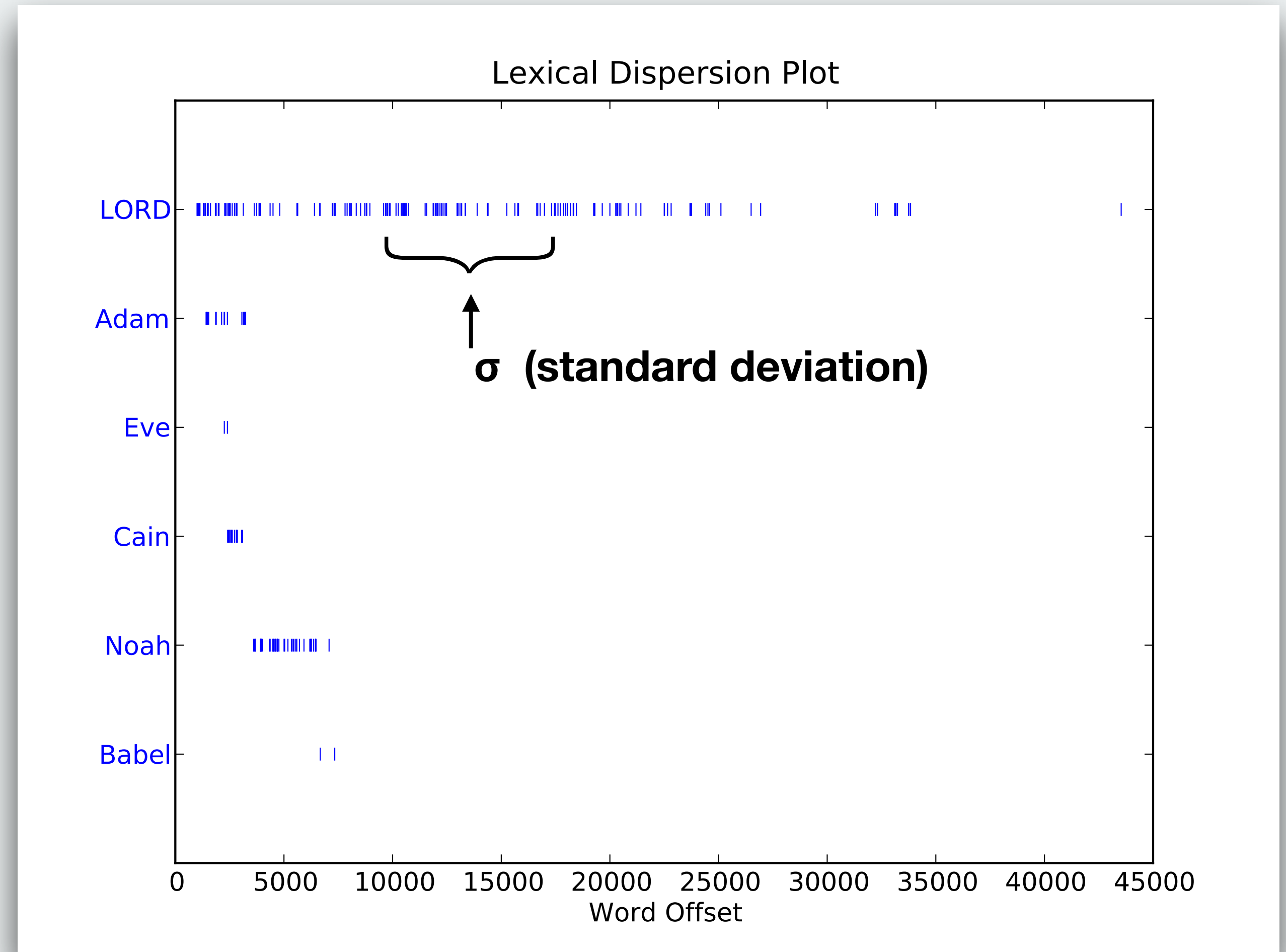
Statistics

A set of tools and jargon for describing data

Vocabulary

- Mean, median
- Variance, **standard deviation**, range
- Correlation, covariance

$$\sigma = \sqrt{\frac{1}{N-1} \sum_{i=1}^n (x_i - \mu)^2}$$



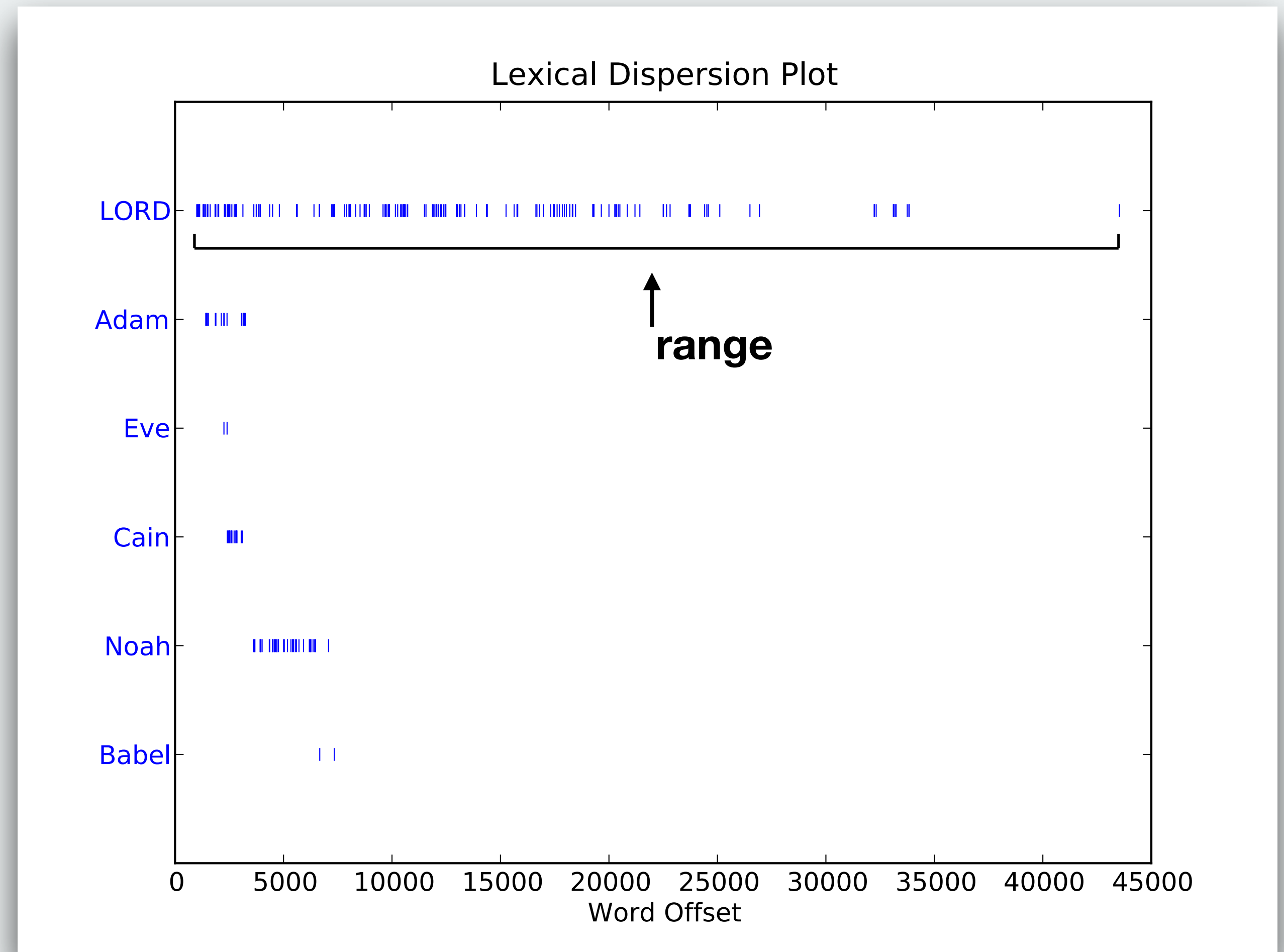
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$$\text{range} = \max(\text{value}) - \min(\text{value})$$



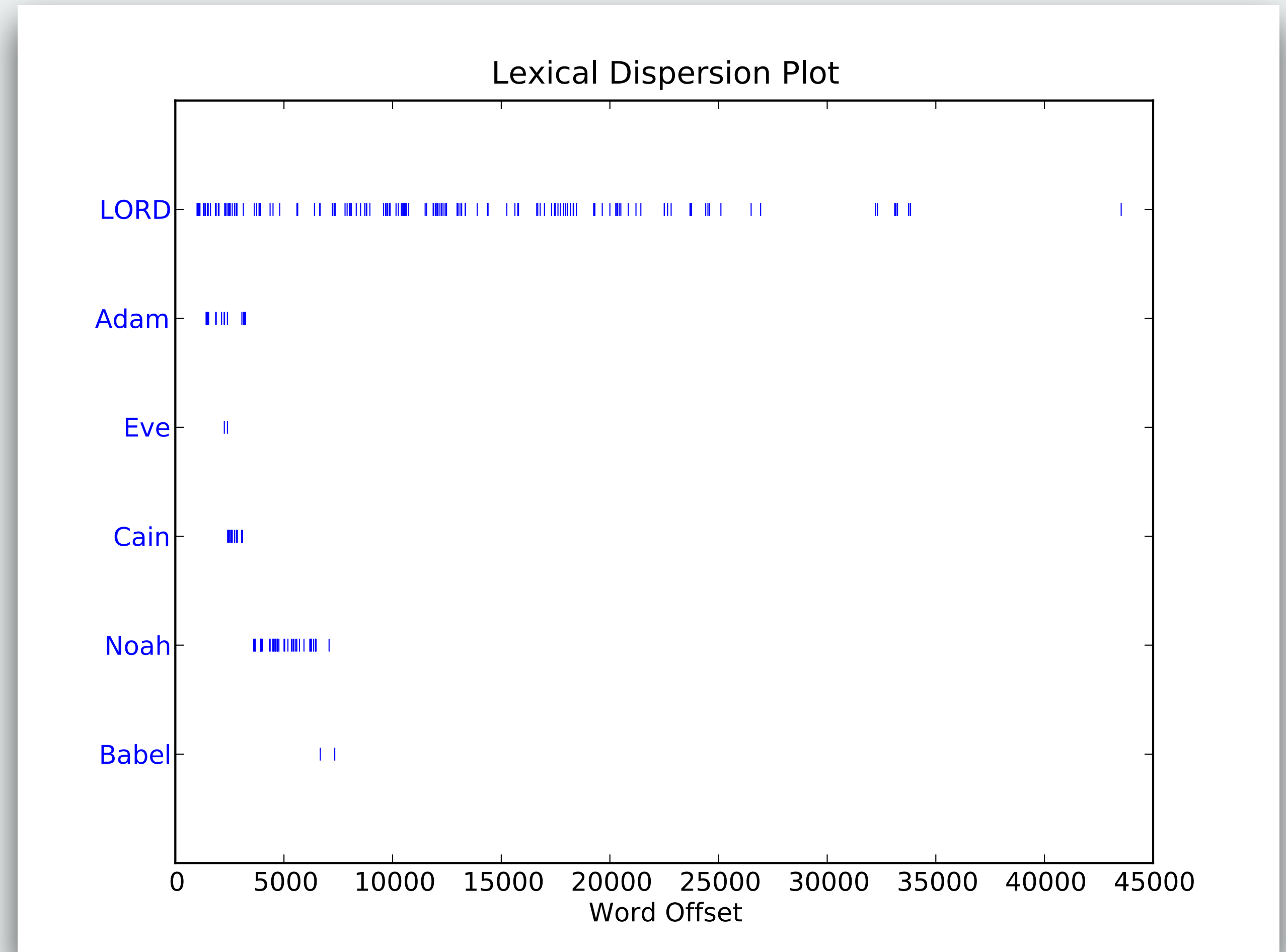
Statistics

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Vocabulary

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- Correlation, **covariance**

$$\text{cov}(\mathbf{X}, \mathbf{Y}) = \frac{1}{n} \sum_{i=1}^n (x_i - \mu_X)(y_i - \mu_Y)$$



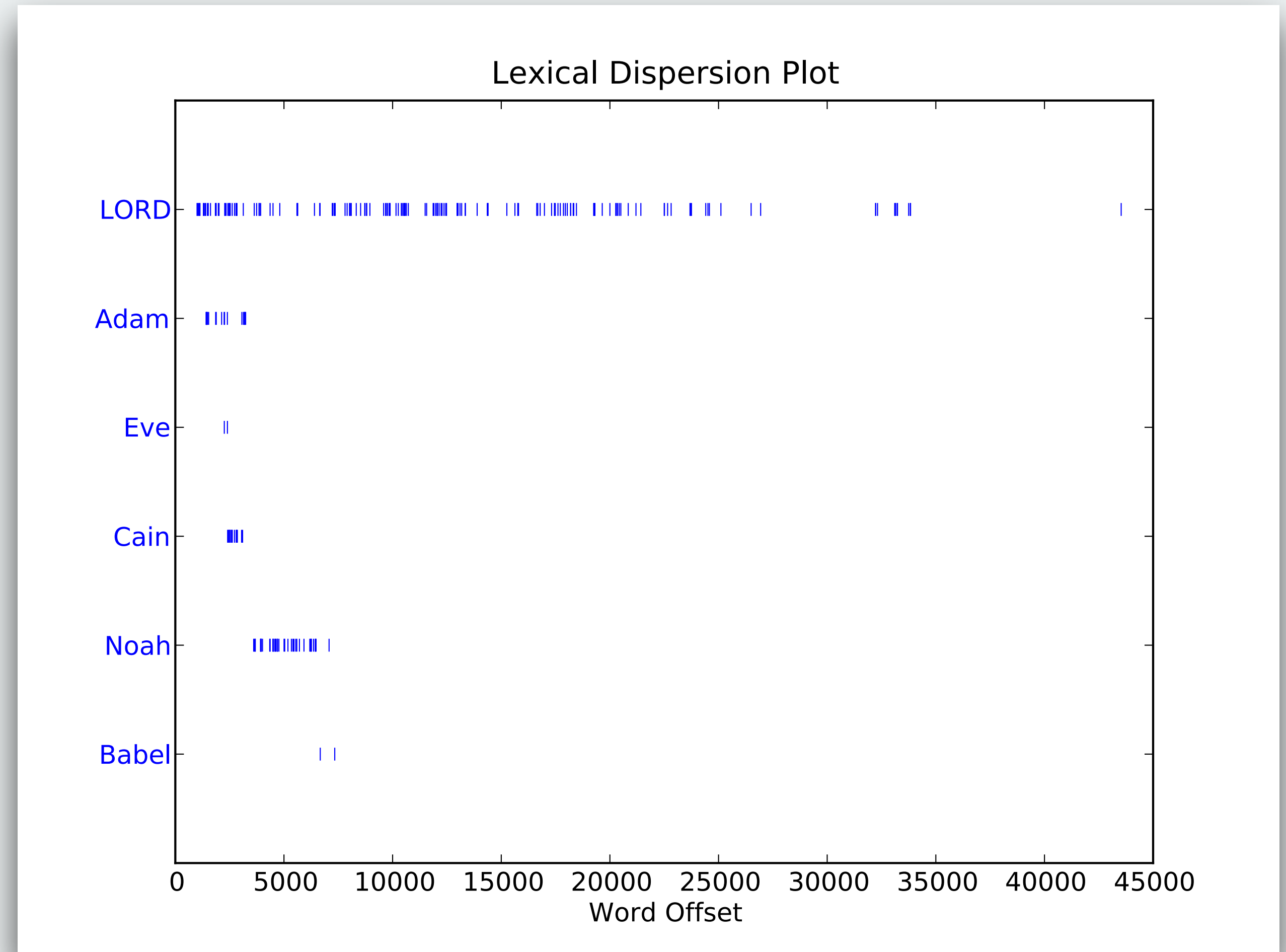
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$$\text{cor}(X, Y) = \frac{\text{cov}(X, Y)}{\sigma_X \sigma_Y}$$



Probability theory

Probability theory

Formalized framework for dealing with randomness

Probability theory

Formalized framework for dealing with randomness

Important concepts

- Discrete vs. continuous
- Distribution and process
- Random and stochastic
- Probability functions
 - Probability *mass* function (pmf)
 - Probability *density* function (pdf)
 - *Cumulative density* function (cdf)

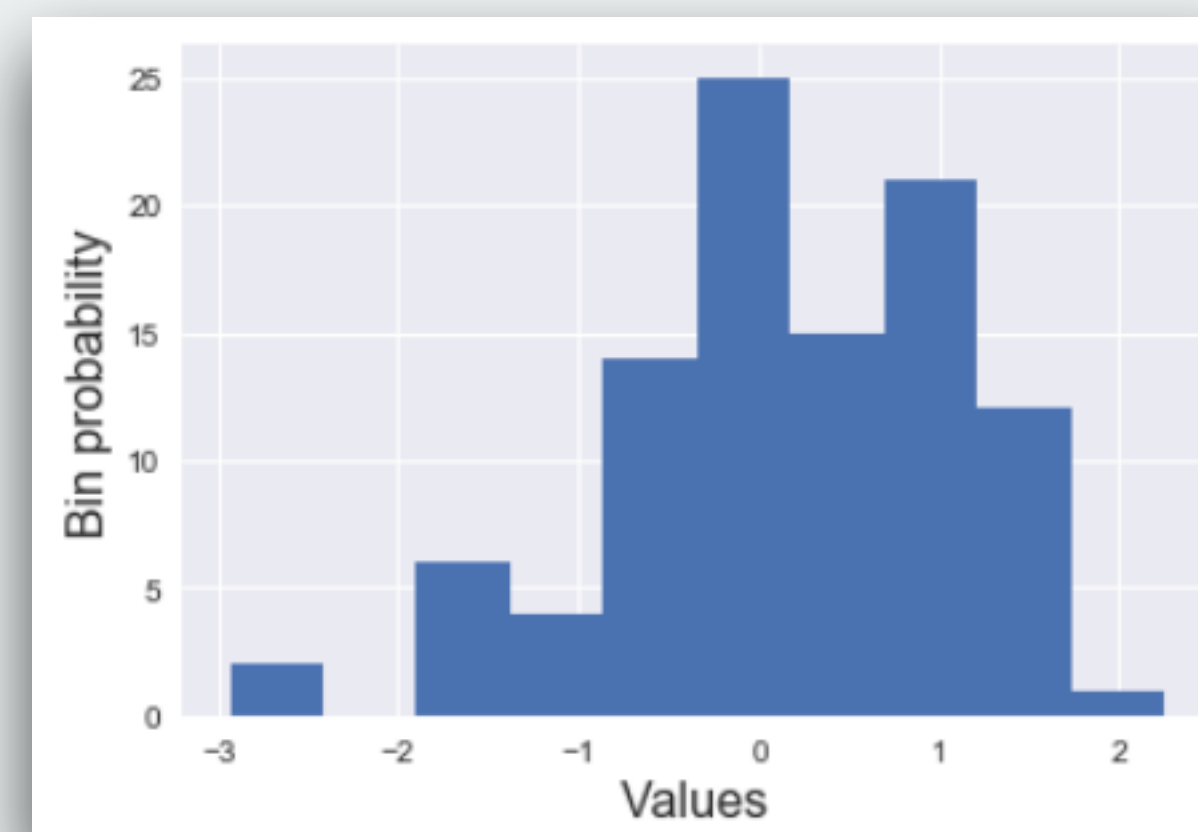
Probability theory

Formalized framework for dealing with randomness

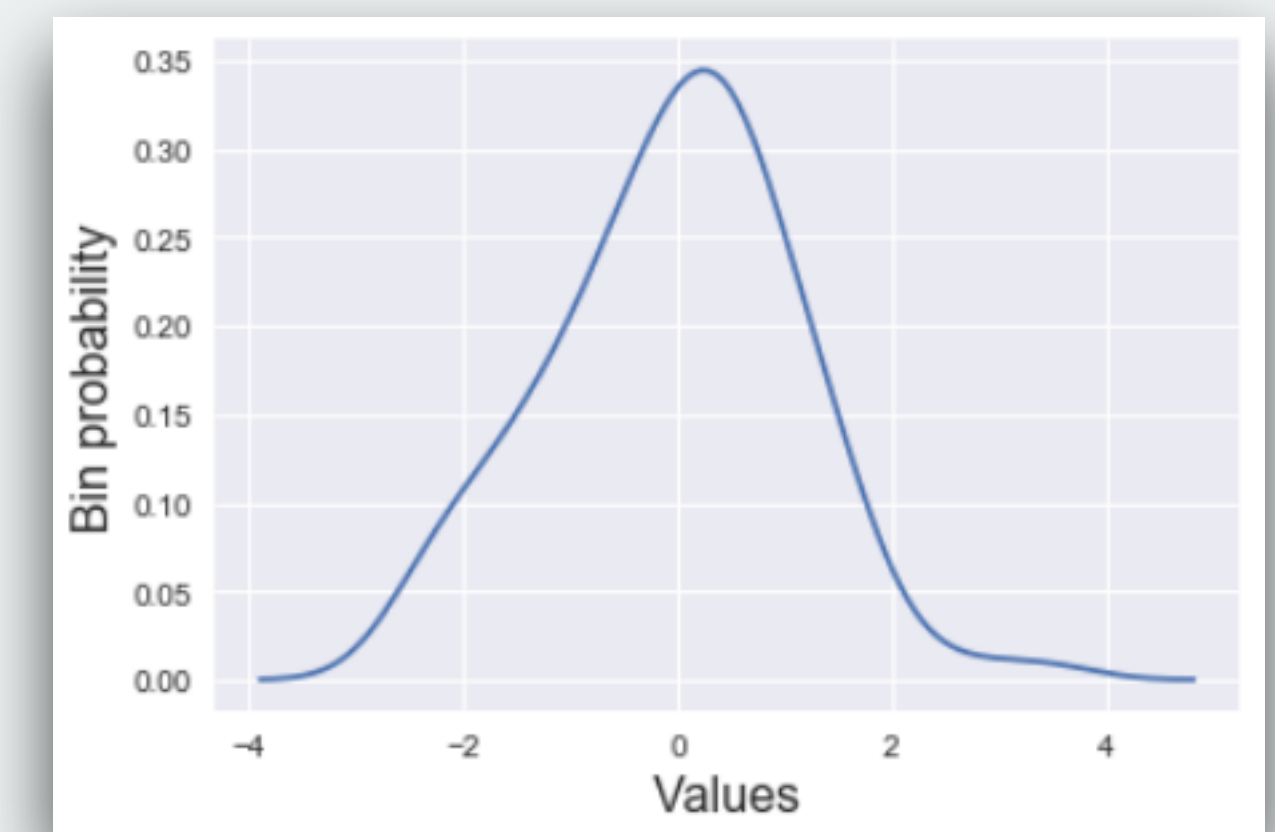
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Discrete



Continuous



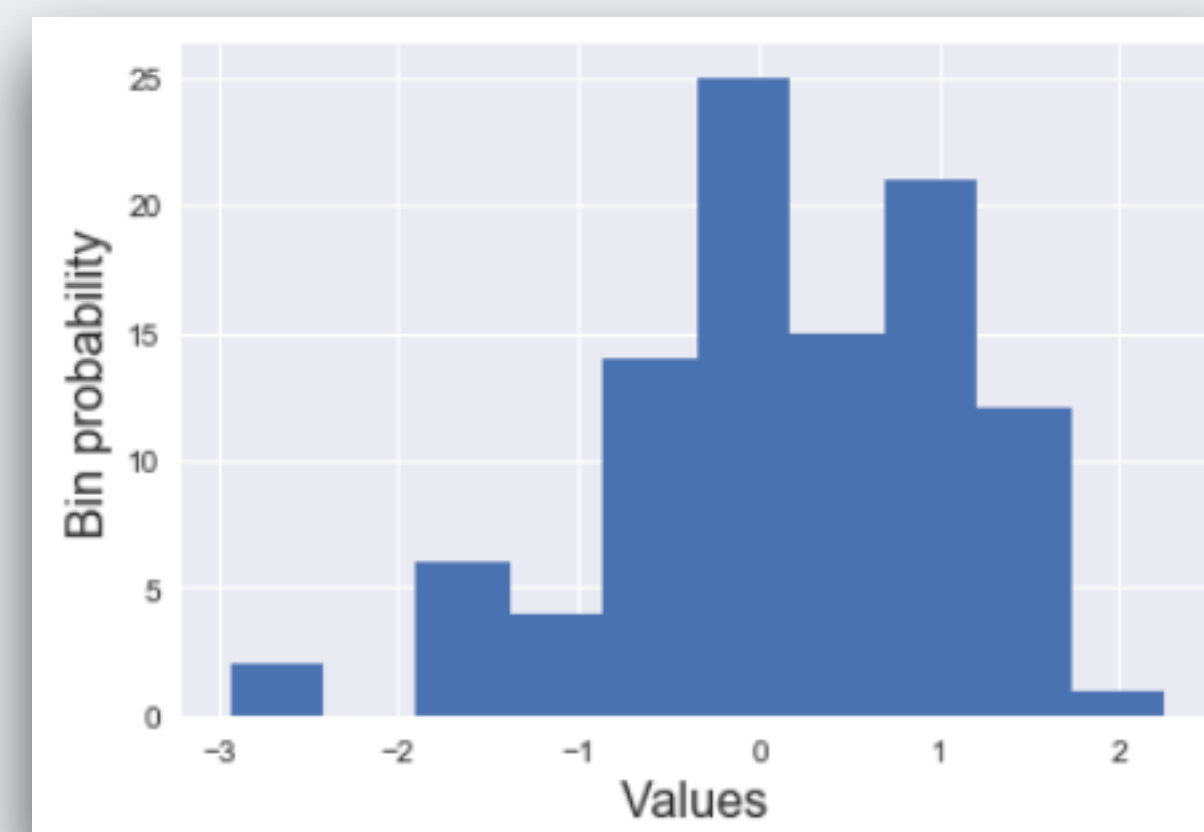
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Distribution



Process



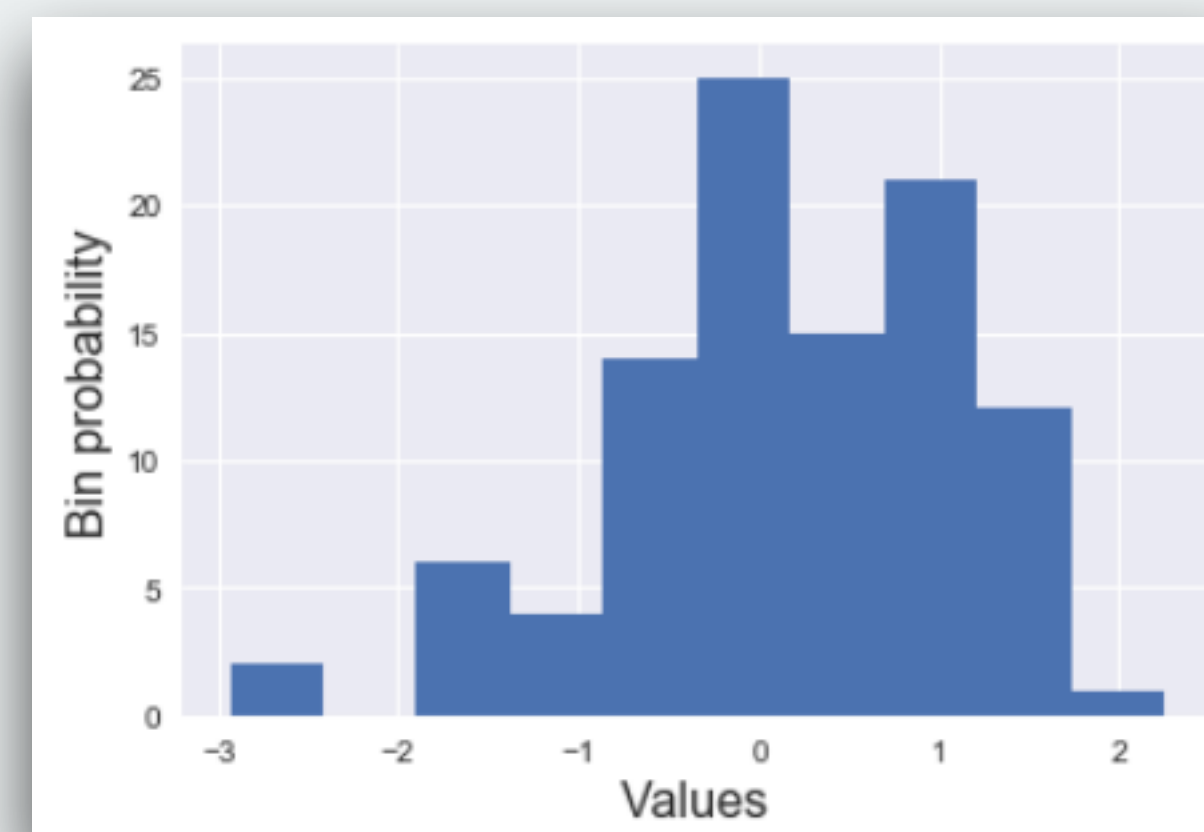
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A **variable** is *random*



A **process** is *stochastic*



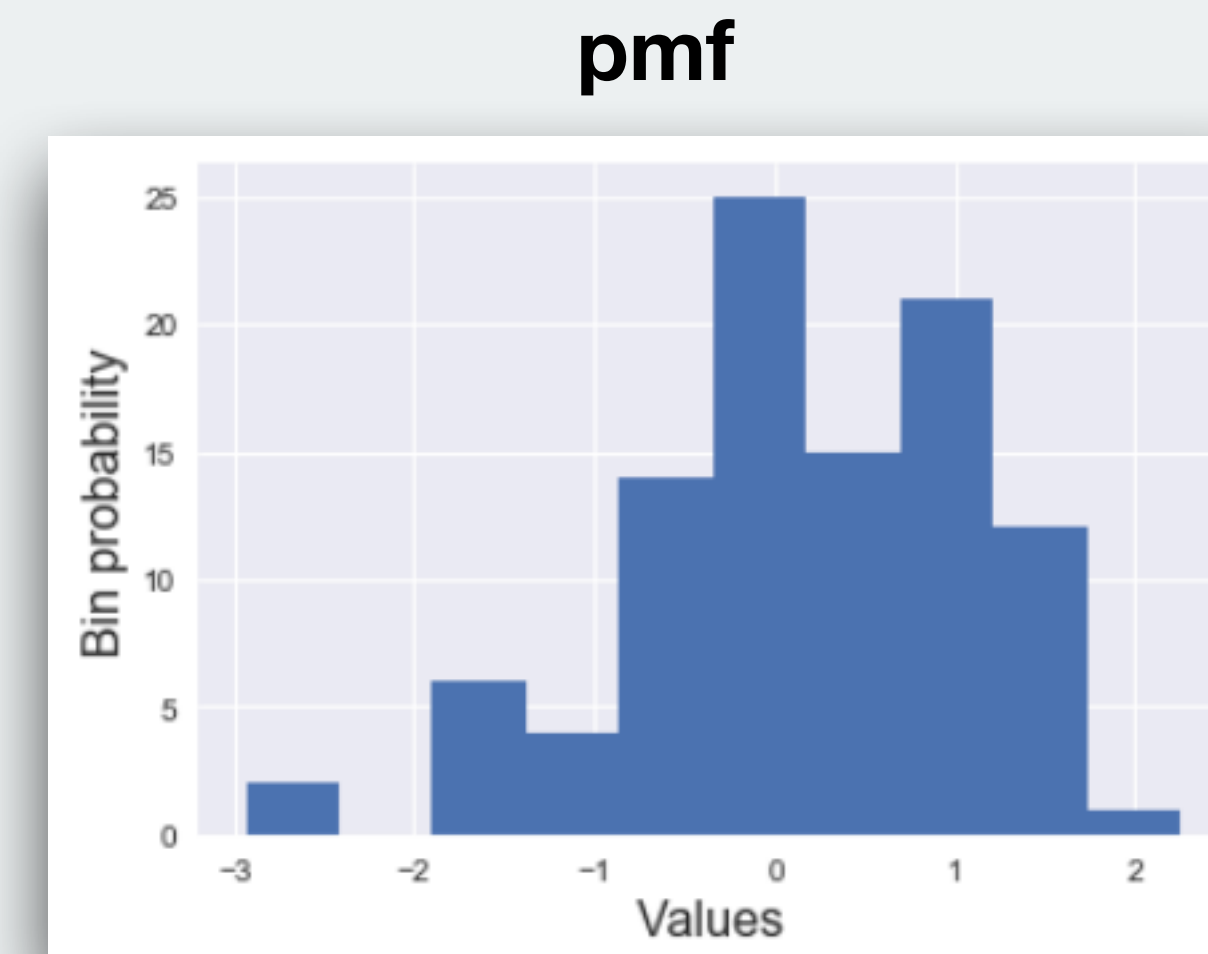
Otherwise the two words mean the same

Probability theory

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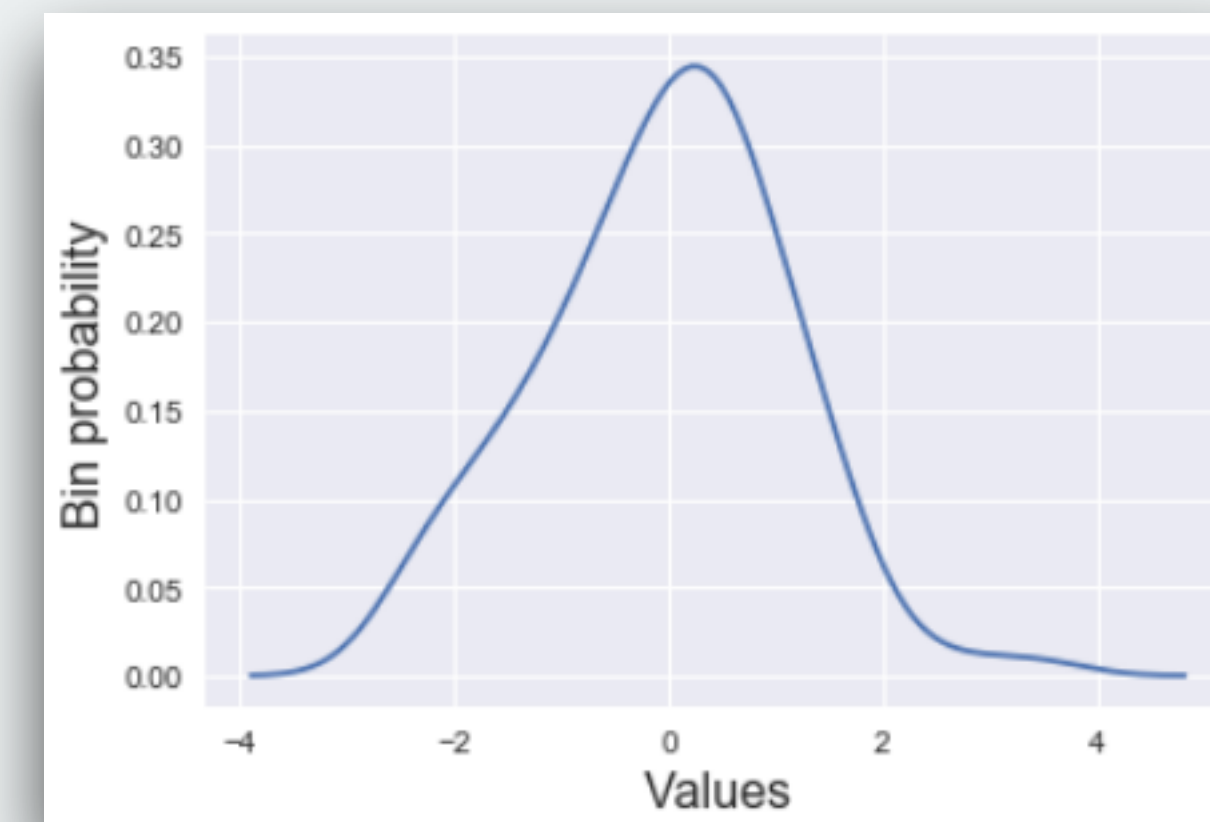
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pdf



Probability theory

Formalized framework for dealing with randomness

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 - **Cumulative density function (cdf)**

cdf

