# HKN CS61A Midterm 2 Review Session

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#### **Disclaimer**

We're not officially affiliated with the course and we don't know what's on your midterm.

This is our best guess based on the lectures, homeworks, past exams, etc.

Always go with the lecture/class material if you feel there is a discrepancy.

Thanks!

### **Agenda**

- Generators and Comprehensions
- OOP
- Abstraction
- Recursion

#### Not covered:

- Basic usage of built-in types (tuples, strings, dicts, etc)
- Implementation Details

```
def llamas(f):
  func = lambda x: x
                                                          What does running each of the following tests
  it = [(1, 2), (2, 3), (3, 4), (4, 5)]
                                                          output?
                                                          def test1():
  def hats(x):
                                                             return llamas("carl")
     return x == 42
                                                          >>> test1()
  def faces(f):
     nonlocal func
     func2 = lambda x: x*2
                                                          def test2():
     it2 = [5, 6, 7, 8]
                                                             return llamas("paul")
                                                          >>> test2()
     if f == "carl":
        func = func2
        it = it2
                                                          def test3():
  if (f == "carl" or f == "paul"):
                                                             return llamas("I like hats")
     faces(f)
                                                          >>> test3()
     return [func(item) for item in it]
  else:
     return tuple((func(item) for item in it if hats(item)))
```

```
def llamas(f):
  func = lambda x: x
                                                          What does running each of the following tests
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                                                          >>> test2()
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     faces(f)
                                                          >>> test3()
     return [func(item) for item in it]
  else:
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```
def llamas(f):
  func = lambda x: x
                                                           What does running each of the following tests
  it = [(1, 2), (2, 3), (3, 4), (4, 5)]
                                                           output?
                                                           def test1():
  def hats(x):
                                                              return llamas("carl")
     return x == 42
                                                           >>> test1()
                                                           [(1, 2, 1, 2), (2, 3, 2, 3), (3, 4, 3, 4), (4, 5, 4, 5)]
  def faces(f):
     nonlocal func
     func2 = lambda x: x*2
                                                           def test2():
     it2 = [5, 6, 7, 8]
                                                              return llamas("paul")
                                                           >>> test2()
     if f == "carl":
        func = func2
        it = it2
                                                           def test3():
  if (f == "carl" or f == "paul"):
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     faces(f)
                                                           >>> test3()
     return [func(item) for item in it]
  else:
     return tuple((func(item) for item in it if hats(item)))
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```
def llamas(f):
  func = lambda x: x
                                                           What does running each of the following tests
  it = [(1, 2), (2, 3), (3, 4), (4, 5)]
                                                           output?
                                                           def test1():
  def hats(x):
                                                              return llamas("carl")
     return x == 42
                                                           >>> test1()
  def faces(f):
                                                           [(1, 2, 1, 2), (2, 3, 2, 3), (3, 4, 3, 4), (4, 5, 4, 5)]
     nonlocal func
     func2 = lambda x: x*2
                                                           def test2():
     it2 = [5, 6, 7, 8]
                                                              return llamas("paul")
                                                           >>> test2()
     if f == "carl":
                                                           [(1, 2), (2, 3), (3, 4), (4, 5)]
        func = func2
        it = it2
                                                           def test3():
  if (f == "carl" or f == "paul"):
                                                              return llamas("I like hats")
     faces(f)
                                                           >>> test3()
     return [func(item) for item in it]
  else:
     return tuple((func(item) for item in it if hats(item)))
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```
def llamas(f):
  func = lambda x: x
                                                           What does running each of the following tests
  it = [(1, 2), (2, 3), (3, 4), (4, 5)]
                                                           output?
                                                           def test1():
  def hats(x):
                                                              return llamas("carl")
     return x == 42
                                                           >>> test1()
  def faces(f):
                                                           [(1, 2, 1, 2), (2, 3, 2, 3), (3, 4, 3, 4), (4, 5, 4, 5)]
     nonlocal func
     func2 = lambda x: x*2
                                                           def test2():
     it2 = [5, 6, 7, 8]
                                                              return llamas("paul")
                                                           >>> test2()
     if f == "carl":
                                                           [(1, 2), (2, 3), (3, 4), (4, 5)]
        func = func2
        it = it2
                                                           def test3():
  if (f == "carl" or f == "paul"):
                                                              return llamas("I like hats")
     faces(f)
                                                           >>> test3()
     return [func(item) for item in it]
  else:
     return tuple((func(item) for item in it if hats(item)))
```

## **Mutability**

```
def llamas(f):
    func = lambda x: x
    it = [(1, 2), (2, 3), (3, 4), (4, 5)]

    def hands(h):
        feet = h
        feet[0] = (99, 99)

if (f == "random man"):
        hands(it)
        return [func(item) for item in it]
```

```
def test4():
    return llamas("random man")
>>> test4()
```

## Mutability

```
def llamas(f):
    func = lambda x: x
    it = [(1, 2), (2, 3), (3, 4), (4, 5)]

    def hands(h):
        feet = h
        feet[0] = (99, 99)

if (f == "random man"):
        hands(it)
        return [func(item) for item in it]
```

```
def test4():
    return llamas("random man")
>>> test4()
[(99, 99), (2, 3), (3, 4), (4, 5)]
```

```
from functools import reduce
>>>line = "raw faces are just gross"
>>>censorlist = ["raw"]
```

- Reverses line
   'ssorg tsuj era secaf war'
- 2) Removes words from line that are in the censorlist 'faces are just gross '
- 3) Doubles each letter then appends "cats" to the front 'cats rraaww ffaacceess aarree jjuusstt ggrroossss'

```
from functools import reduce
>>>line = "raw faces are just gross"
>>>censorlist = ["raw"]
```

- 1) Reverses line
- >>>str(reduce(lambda x, y: y + x, line))
- 2) Removes words from line that are in the censorlist
- 3) Doubles each letter then appends "cats" to the front

```
from functools import reduce
>>>line = "raw faces are just gross"
>>>censorlist = ["raw"]
```

- 1) Reverses line
- >>>str(reduce(lambda x, y: y + x, line))
- 2) Removes words from line that are in the censorlist
- >>>str(reduce(lambda x, y: x + y, map(lambda x: x + " ", filter(lambda x: x not in censorlist, line.split(" ")))))
- 3) Doubles each letter then appends "cats" to the front

```
from functools import reduce

>>>line = "raw faces are just gross"

>>>censorlist = ["raw"]

1) Reverses line

>>>str(reduce(lambda x, y: y + x, line))

2) Removes words from line that are in the censorlist

>>>str(reduce(lambda x, y: x + y, map(lambda x: x + " ", filter(lambda x: x not in censorlist, line.split(" ")))))

3) Doubles each letter then appends "cats" to the front

>>>str(reduce(lambda x, y: x + y, map(lambda x: x + x, line), "cats "))
```

The class **Pokemon** has an attribute modifiers:

A new class, **PoisonType**, inherits from **Pokemon** but has a few different modifiers (shown on the left)

We want to implement part of the **PoisonType** class such that it has these new modifiers instead of the ones from **Pokemon**.



Select all of the following that give PoisonType the correct modifiers attribute:

```
>>> PoisonType.modifiers["Bug"]
                                          >>> Pokemon.modifiers["Bug"]
                                          1.0
   0.5
class PoisonType(Pokemon):
    poison_modifiers = {"Bug":0.5,"Fighting":0.5,"Poison":0.5,"Grass":0.5,
    "Ground":2,"Psychic":2}
    # (a)
    modifiers = Pokemon.modifiers.update(poison modifiers)
   # (b)
    modifiers = dict(list(Pokemon.modifiers) + list(poison_modifiers))
   # (c)
    modifiers = Pokemon.modifiers.copy()
    modifiers.update(poison_modifiers)
    \# (d)
    def modifiers(self, type):
        if type in poison_modifiers.keys():
            return poison_modifiers[type]
        else:
            return modifiers[type]
```

```
class PoisonType(Pokemon):
    poison_modifiers = {"Bug":0.5,"Fighting":0.5,"Poison":0.5,"Grass":0.5,
    "Ground":2,"Psychic":2}
    # (a)
    modifiers = Pokemon.modifiers.update(poison_modifiers)
```

```
class PoisonType(Pokemon):
    poison_modifiers = {"Bug":0.5,"Fighting":0.5,"Poison":0.5,"Grass":0.5,
    "Ground":2,"Psychic":2}
    # (a)
    modifiers = Pokemon.modifiers.update(poison_modifiers)
    >>> modifiers
```

```
class PoisonType(Pokemon):
    poison_modifiers = {"Bug":0.5,"Fighting":0.5,"Poison":0.5,"Grass":0.5,
    "Ground":2,"Psychic":2}
    # (a)
    modifiers = Pokemon.modifiers.update(poison_modifiers)
    >>> modifiers
```

```
class PoisonType(Pokemon):
    poison_modifiers = {"Bug":0.5,"Fighting":0.5,"Poison":0.5,"Grass":0.5,
    "Ground":2,"Psychic":2}
    # (a)
    modifiers = Pokemon.modifiers.update(poison_modifiers)
    >>> modifiers
    *crickets*
update() doesn't return anything, it just modifies the dict
```

```
class PoisonType(Pokemon):
    poison_modifiers = {"Bug":0.5,"Fighting":0.5,"Poison":0.5,"Grass":0.5,
    "Ground":2,"Psychic":2}
    # (b)
    modifiers = dict( list( Pokemon.modifiers ) + list( poison_modifiers )
    )
```

```
class PoisonType(Pokemon):
    poison_modifiers = {"Bug":0.5,"Fighting":0.5,"Poison":0.5,"Grass":0.5,
        "Ground":2,"Psychic":2}
    # (b)
    modifiers = dict( list( Pokemon.modifiers ) + list( poison_modifiers )
    )
```

```
class PoisonType(Pokemon):
    poison_modifiers = {"Bug":0.5,"Fighting":0.5,"Poison":0.5,"Grass":0.5,
    "Ground":2,"Psychic":2}
    # (b)
    modifiers = dict( list( Pokemon.modifiers ) + list( poison_modifiers )
    )
    >>> list( Pokemon.modifiers )
    ["Fire", "Water", "Grass", ...]
```

```
class PoisonType(Pokemon):
    poison_modifiers = {"Bug":0.5,"Fighting":0.5,"Poison":0.5,"Grass":0.5,
    "Ground":2,"Psychic":2}
    # (d)
    @property
    def modifiers(self, type):
        if type in poison_modifiers.keys():
            return poison_modifiers[type]
        else:
            return modifiers[type]
```

Possible Solutions (?)

```
class PoisonType(Pokemon):
    poison_modifiers = {"Bug":0.5,"Fighting":0.5,"Poison":0.5,"Grass":0.5,
    "Ground":2,"Psychic":2}
# (d)
@property
def modifiers(self, type):
    if type in poison_modifiers.keys():
        return poison_modifiers[type]
    else:
        return modifiers[type]

>>> PoisonType.modifiers["Grass"]
```

Square brackets call the <u>getitem</u> () special function,

```
class PoisonType(Pokemon):
    poison_modifiers = {"Bug":0.5,"Fighting":0.5,"Poison":0.5,"Grass":0.5,
    "Ground":2,"Psychic":2}
    # (c)
    modifiers = Pokemon.modifiers.copy()
    modifiers.update(poison_modifiers)
```

Possible Solutions (?)

```
class PoisonType(Pokemon):
    poison_modifiers = {"Bug":0.5,"Fighting":0.5,"Poison":0.5,"Grass":0.5,
    "Ground":2,"Psychic":2}
    # (c)
    modifiers = Pokemon.modifiers.copy()
    modifiers.update(poison_modifiers)
```

THIS VERSION WORKS!

Assume we have the following classes implemented:

```
class GrassType(Pokemon):
                                    class PoisonType(Pokemon):
   modifiers =
                                        modifiers =
       Pokemon.modifiers.copy()
                                            Pokemon.modifiers.copy()
   modifiers.update(
                                        modifiers.update(
        { "Electric": 0.5,
                                            { "Bug": 0.5,
         "Grass": 0.5,
                                              "Fighting": 0.5,
                                              "Poison": 0.5,
         "Ground": 0.5,
         "Water": 0.5,
                                              "Grass": 0.5,
                                              "Ground": 2,
         "Bug": 2,
                                              "Psychic": 2})
         "Flying": 2,
         "Fire": 2,
         "Ice": 2,
          "Poison": 2} )
```

Bulbasaur is a Grass/Poison type pokemon. Suppose we have a new class, **Bulbasaur**, that inherits from these two as follows:

```
class Bulbasaur(GrassType, PoisonType):
```

```
class GrassType(Pokemon):
                                     What do the following statements evaluate to?
    modifiers =
         Pokemon.modifiers.copy()
    modifiers.update(
                                     >>> Bulbasaur.modifiers["Grass"]
         { "Electric":
                       0.5,
           "Grass": 0.5.
           "Ground": 0.5.
           "Water":
                       0.5,
          "Bug":
                       2,
          "Flying":
                                     >>> Bulbasaur.modifiers["Bug"]
          "Fire":
           "Ice":
           "Poison":
                       2} )
class PoisonType(Pokemon):
    modifiers =
                                     >>> Bulbasaur.modifiers["Psychic"]
         Pokemon.modifiers.copy()
    modifiers.update(
         { "Bug":
                     0.5,
           "Fighting": 0.5,
           "Poison": 0.5.
           "Grass": 0.5,
                                     >>> Bulbasaur.modifiers["Dragon"]
           "Ground": 2,
           "Psvchic": 2})
```

```
class GrassType(Pokemon):
                                     What do the following statements evaluate to?
    modifiers =
         Pokemon.modifiers.copy()
    modifiers.update(
                                     >>> Bulbasaur.modifiers["Grass"]
         { "Electric":
                       0.5,
                                     0.5
           "Grass": 0.5.
          "Ground": 0.5.
           "Water":
                       0.5,
          "Bug":
                       2,
          "Flying":
                                     >>> Bulbasaur.modifiers["Bug"]
           "Fire":
           "Ice":
           "Poison":
                       2} )
class PoisonType(Pokemon):
    modifiers =
                                     >>> Bulbasaur.modifiers["Psychic"]
         Pokemon.modifiers.copy()
    modifiers.update(
         { "Bug":
                     0.5,
           "Fighting": 0.5,
           "Poison": 0.5.
           "Grass": 0.5,
                                     >>> Bulbasaur.modifiers["Dragon"]
           "Ground": 2,
           "Psvchic": 2})
```

```
class GrassType(Pokemon):
                                     What do the following statements evaluate to?
    modifiers =
         Pokemon.modifiers.copy()
    modifiers.update(
                                     >>> Bulbasaur.modifiers["Grass"]
         { "Electric":
                       0.5,
                                     0.5
           "Grass": 0.5.
           "Ground": 0.5.
           "Water":
                       0.5,
          "Bug":
                       2,
          "Flying":
                                     >>> Bulbasaur.modifiers["Bug"]
           "Fire":
                                     2.0
           "Ice":
           "Poison":
                       2} )
class PoisonType(Pokemon):
    modifiers =
                                     >>> Bulbasaur.modifiers["Psychic"]
         Pokemon.modifiers.copy()
    modifiers.update(
         { "Bug":
                     0.5,
           "Fighting": 0.5,
           "Poison": 0.5.
           "Grass": 0.5,
                                     >>> Bulbasaur.modifiers["Dragon"]
           "Ground": 2,
           "Psvchic": 2})
```

```
class GrassType(Pokemon):
                                     What do the following statements evaluate to?
    modifiers =
         Pokemon.modifiers.copy()
    modifiers.update(
                                     >>> Bulbasaur.modifiers["Grass"]
         { "Electric":
                       0.5,
                                     0.5
           "Grass": 0.5.
           "Ground": 0.5.
           "Water":
                       0.5,
           "Bug":
                       2,
          "Flying":
                                     >>> Bulbasaur.modifiers["Bug"]
           "Fire":
                                     2.0
           "Ice":
           "Poison":
                       2} )
class PoisonType(Pokemon):
    modifiers =
                                     >>> Bulbasaur.modifiers["Psychic"]
         Pokemon.modifiers.copy()
    modifiers.update(
                                     1.0
         { "Bug":
                     0.5.
           "Fighting": 0.5,
           "Poison": 0.5,
           "Grass": 0.5,
                                     >>> Bulbasaur.modifiers["Dragon"]
           "Ground": 2,
           "Psvchic": 2})
```

```
class GrassType(Pokemon):
                                     What do the following statements evaluate to?
    modifiers =
         Pokemon.modifiers.copy()
    modifiers.update(
                                     >>> Bulbasaur.modifiers["Grass"]
         { "Electric":
                       0.5,
                                     0.5
           "Grass": 0.5.
           "Ground": 0.5.
           "Water":
                       0.5,
           "Bug":
                        2,
           "Flying":
                                     >>> Bulbasaur.modifiers["Bug"]
           "Fire":
                                     2.0
           "Ice":
           "Poison":
                        2} )
class PoisonType(Pokemon):
    modifiers =
                                     >>> Bulbasaur.modifiers["Psychic"]
         Pokemon.modifiers.copy()
    modifiers.update(
                                     1.0
         { "Bug":
                      0.5.
           "Fighting": 0.5,
           "Poison": 0.5,
           "Grass": 0.5,
                                     >>> Bulbasaur.modifiers["Dragon"]
           "Ground": 2,
           "Psvchic": 2})
                                     1.0
class Bulbasaur(GrassType, PoisonType):
```

PROBLEM - Bulbasaur's actual type modifiers don't match *either* type!



SOLUTION - Multiply the modifiers for each type to get the combined modifier for that type.

Write a function that takes two Pokemon types to generate new modifiers.

```
Bulbasaur
 GrassType
                  PoisonType
"Grass": 0.5, "Grass": 0.5,
                                  "Grass": 0.25,
 "Ground": 0.5, "Ground": 2.0,
                                  "Ground":
                                           1.0,
 "Water": 0.5, "Water": 1.0,
                                  "Water":
                                           0.5,
 "Bug": 2.0,
                "Bug": 0.5,
                                  "Bug":
                                           1.0,
 "Flying": 2.0,
                 "Flying": 1.0,
                                  "Flying":
                                           2.0,
                                  "Fire":
 "Fire": 2.0,
                 "Fire":
                          1.0,
                                           2.0,
 "Ice": 2.0,
                                  "Ice":
                 "Ice":
                          1.0,
                                           2.0,
 "Poison": 2.0,
                 "Poison": 0.5,
                                  "Poison": 1.0,
 "Fighting": 1.0,
                 "Fighting": 0.5,
                                  "Fighting": 0.5,
 "Psychic": 1.0,
             "Psychic": 2.0,
                                  "Psychic": 2.0,
 ... }
                 ...}
                                  ...}
```

```
def combine_types( TypeA, TypeB ):
    """Combines two different types to form a new type dictionary of modifiers
    >>> Bulbasaur.modifiers = combine_types(GrassType, PoisonType)
    >>> GrassType.modifiers["Bug"]
    2.0
    >>> PoisonType.modifiers["Bug"]
    0.5
    >>> Bulbasaur.modifiers["Bug"]
    1.0
    >>> Bulbasaur.modifiers["Flying"]
    2.0
    >>> Bulbasaur.modifiers["Grass"]
    0.25
    11 11 11
```

# **BONUS:**

```
def combine_types( TypeA, TypeB ):
    """Combines two different types to form a new type dictionary of modifiers
    >>> Bulbasaur.modifiers = combine_types(GrassType, PoisonType)
    >>> GrassType.modifiers["Bug"]
    2.0
    >>> PoisonType.modifiers["Bug"]
    0.5
    >>> Bulbasaur.modifiers["Bug"]
    1.0
    >>> Bulbasaur.modifiers["Flying"]
    2.0
    >>> Bulbasaur.modifiers["Grass"]
    0.25
    11 11 11
```

# **BONUS:**

#### **OOP Problems**

Do it in one line

```
def combine types( TypeA, TypeB ):
    """Combines two different types to form a new type dictionary of modifiers
    >>> Bulbasaur.modifiers = combine_types(GrassType, PoisonType)
    >>> GrassType.modifiers["Bug"]
    2.0
    >>> PoisonType.modifiers["Bug"]
    0.5
    >>> Bulbasaur.modifiers["Bug"]
    1.0
    >>> Bulbasaur.modifiers["Flying"]
    2.0
    >>> Bulbasaur.modifiers["Grass"]
    0.25
    11 11 11
```

```
def combine_types( TypeA, TypeB ):
    """Combines two different types to form a new type dictionary of modifiers
    """
```

```
def combine_types( TypeA, TypeB ):
    """Combines two different types to form a new type dictionary of modifiers
    """
    new_modifiers = {}
```

```
def combine_types( TypeA, TypeB ):
    """Combines two different types to form a new type dictionary of modifiers
    """
    new_modifiers = {}
    for type in TypeA.modifiers.keys():
```

```
def combine_types( TypeA, TypeB ):
    """Combines two different types to form a new type dictionary of modifiers
    """
    new_modifiers = {}
    for type in TypeA.modifiers.keys():
        new_modifiers[type] = TypeA.modifiers[type] * TypeB.modifiers[type]
```

```
def combine_types( TypeA, TypeB ):
    """Combines two different types to form a new type dictionary of modifiers
    """
    new_modifiers = {}
    for type in TypeA.modifiers.keys():
        new_modifiers[type] = TypeA.modifiers[type] * TypeB.modifiers[type]
    return new_modifiers
```

# **BONUS:**

## **OOP Problems**

Do it in one line

```
def combine_types( TypeA, TypeB ):
    """Combines two different types to form a new type dictionary of modifiers
"""
```

# **BONUS:**

#### **OOP Problems**

Do it in one line

```
class RList(object):
       class EmptyList(object):
 3
           def len (self):
              return 0
      empty = EmptyList()
 6
      def init (self, first, rest=empty):
           self.first = first
           self.rest = rest
      def len (self):
           return 1 + len(self.rest)
  blah = RList(1,RList(2,RList(3)))
  def mystery(rlist):
      if (len(rlist) == 0):
           return
18
      mystery(rlist.rest)
20
      print(rlist.first)
22 mystery(blah)
```

Given this mystery function and the corresponding RList object, what does this mystery function do?

What would Python print after calling mystery on blah?

```
class RList(object):
      class EmptyList(object):
3
          def len (self):
              return 🛭
      empty = EmptyList()
6
      def init (self, first, rest=empty):
          self.first = first
          self.rest = rest
      def len (self):
          return 1 + len(self.rest)
  blah = RList(1,RList(2,RList(3)))
  def mystery(rlist):
      if (len(rlist) == 0):
          return
18
      mystery(rlist.rest)
20
      print(rlist.first)
22 mystery(blah)
```

Given this mystery function and the corresponding RList object, what does this mystery function do?

Print out what's contained in the RList backwards.

What would Python print after calling mystery on blah?

3

2

1

Given a list of integers, without using any for or while loops, write a function to count the instances of odd numbers.

Given a list of integers, without using any for or while loops, write a function to count the instances of odd numbers.

```
def factorial(n):
       if (n == 0):
39
40
           return 1
       return n * factorial(n-1)
41
42
   def sum_factorial(n):
44
       sum = 0
       for i in range(0,n+1):
45
           sum += factorial(i)
46
       return sum
```

Given this factorial function what is the Big O of the sum\_factorial function?

```
def factorial(n):
       if (n == 0):
39
40
           return 1
       return n * factorial(n-1)
41
42
   def sum_factorial(n):
44
       sum = 0
       for i in range(0,n+1):
45
           sum += factorial(i)
46
       return sum
```

Given this function, what is the Big O of this function?

$$O(n) = n^2$$

```
def factorial(n):
       if (n == 0):
39
40
           return 1
       return n * factorial(n-1)
41
42
   def sum_factorial(n):
44
       sum = 0
       for i in range(0,n+1):
45
           sum += factorial(i)
46
       return sum
```

Using this original function, implement the memoized function that was implemented in class. After implementing it, figure out the Big O of the memoized sum factorial.

```
29 def memo(f):
30
       cache = \{\}
31
       def memoized(n):
32
           if n not in cache:
33
                cache[n] = f(n)
34
           return cache[n]
       return memoized
35
36
   @me mo
   def factorial(n):
39
       if (n == 0):
40
           return 1
       return n * factorial(n-1)
41
42
48 def sum factorial(n):
44
       sum = A
45
       for i in range(0,n+1):
46
           sum += factorial(i)
47
       return sum
```

The way to memoize is on the left.

Big O is now

$$O(n) = n$$

Since, you only have to calculate each factorial once, and if you only add one more, its constant time.

```
class Tree(object):
    def __init__(self, value, left = None, right = None):
        self.value = value
        self.left = left
        self.right = right
```

Given the class tree object that is shown on the left. Write a function that will sum all the values that are within this tree.

```
def sumValues(tree):
if (tree == None):
return 0
return tree.value + sumValues(tree.left) + sumValues(tree.right)
```

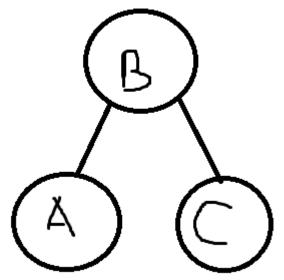
```
def sumValues(tree):
if (tree == None):
return 0
return tree.value + sumValues(tree.left) + sumValues(tree.right)
```

What is the Big O of this function, given that n is number of nodes?

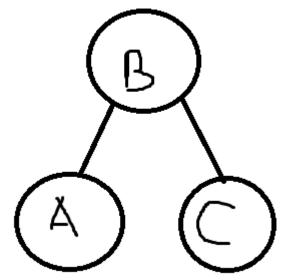
```
def sumValues(tree):
if (tree == None):
return 0
return tree.value + sumValues(tree.left) + sumValues(tree.right)
```

What is the Big O of this function, given that n is number of nodes?

$$O(n) = n$$



This is the function for an inorder traversal of a tree, what would this function print given this tree?



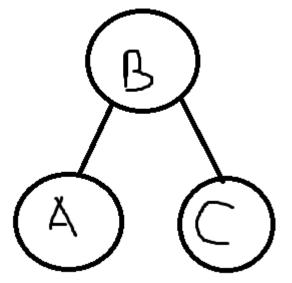
64 def inorder(tree):
65 if(tree == None):
66 return
67 inorder(tree.left)
68 print(tree.value)
69 inorder(tree.right)
70

This is the function for an inorder traversal of a tree, what would this function print given this tree?

А

В

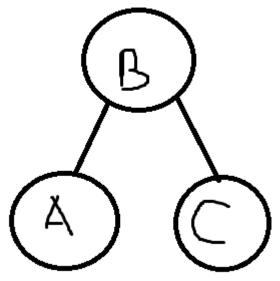
 $\mathsf{C}$ 



```
64 def inorder(tree):
65    if(tree == None):
66     return
67    inorder(tree.left)
68    print(tree.value)
69    inorder(tree.right)
70
```

Now you know how an inorder traversal works, write the Preorder Traversal and the Postorder Traversal.

Preorder:B, A, C Postorder:A, C, B



```
64 def inorder(tree):
65    if(tree == None):
66       return
67    inorder(tree.left)
68    print(tree.value)
69    inorder(tree.right)
70
```

```
def preorder(tree):
72
       if(tree == None):
73
            return
74
       print (tree.value)
75
       preorder(tree.left)
76
       preorder(tree.riqht)
77
78
   def postorder(tree)
79
       if(tree == None):
80
            return
81
       postorder(tree.left)
82
       postorder(tree.right)
83
       print(tree.value)
```

#### **Tree**

```
def inorder(tree):
65
        if(tree == None):
66
            return
67
        inorder(tree.left)
68
        print(tree.value)
69
        inorder(tree.right)
70
71 def preorder(tree):
       if(tree == None):
72
73
           return
74
       print (tree.value)
75
       preorder(tree.left)
       preorder(tree.right)
76
77
   def postorder(tree)
       if(tree == None):
79
80
           return
81
       postorder(tree.left)
82
       postorder(tree.riqht)
       print(tree.value)
83
```

Now that we have these functions, lets build a tree using what you know from here.

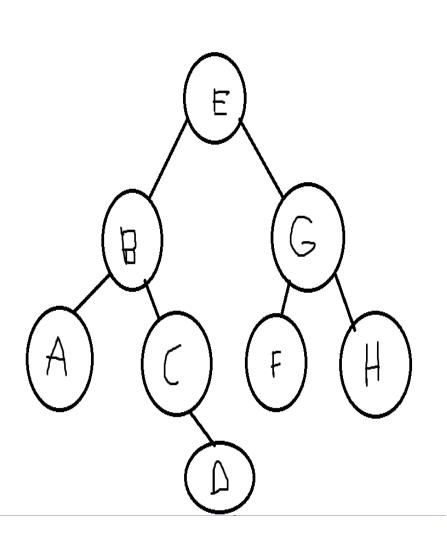
Inorder:

A, B, C, D, E, F, G, H Preorder:

E, B, A, C, D, G, F, H Postorder:

A, D, C, B, F, H, G, E

#### **Tree**



Now that we have these functions, lets build a tree using what you know from here.

Inorder:

A, B, C, D, E, F, G, H Preorder:

E, B, A, C, D, G, F, H Postorder:

A, D, C, B, F, H, G, E

## **Interfaces**

catchable2.catch(owner1)

An interface describes a set of messages and their meaning. Let's define the "catchable" interface as these methods: catch(self, owner): assigns the owner of this catchable to be "owner", but only if original owner is "None" if the owner isn't "None", call the owner's block pokeball() release(self): assigns the owner of this catchable to be "None" owner(self): returns the owner of this catchable in particular, we want any "catchable" pokemon to be able to work with something like: def trade(catchable1, catchable2): owner1 = catchable1.owner() owner2 = catchable2.owner() catchable1.release() catchable1.catch(owner2) catchable2.release()

## **Interfaces**

Does this class correctly implement "catchable"? class Missingno(Pokemon): < ... other class attributes, methods, etc > def catch(self, owner): if self. owner != None: self.\_\_owner.block\_pokeball() elif owner != None: self. owner = owner self. owner.corrupt save data() def release(self): if self. owner != None: self.\_owner.corrupt\_save\_data() else: self. owner = None def owner(self): return self. owner

#### catch(self, owner):

assigns the owner of this catchable to be "owner", but only if old owner is "None" if the owner isn't "None", call the owner's block pokeball()

#### release(self):

assigns the owner of this catchable to be "None"

#### owner(self):

returns the owner of this catchable

## **Interfaces**

```
Does this class correctly implement "catchable"?
class Missingno(Pokemon):
  < ... other class attributes, methods, etc >
  def catch(self, owner):
    if self. owner != None:
      self.__owner.block_pokeball()
    elif owner != None:
      self. owner = owner
      self. owner.corrupt save data()
  def release(self):
    if self._owner != None:
      self._owner.corrupt_save_data()
    else:
      self. owner = None
  def owner(self):
    return self. owner
```

#### catch(self, owner):

assigns the owner of this catchable to be "owner", but only if old owner is "None" if the owner isn't "None", call the owner's block pokeball()

#### release(self):

assigns the owner of this catchable to be "None"

#### owner(self):

returns the owner of this catchable

No.

#### Obvious reason:

release() fails to set owner to None if it isn't already

#### Less obvious:

corrupt\_save\_data() might have side effects that don't fit the interface, but it depends on what corrupt\_save\_data() does and what the interface intends/allows.

# \_\_repr\_\_ and \_\_str\_\_

- A common Python interface for getting a string representation.
- \_repr\_ should produce something legible to the interpreter and unambiguous to the identity of the object.
- \_str\_ should produce something a human can read and understand.

# **Multiple Representations**

Data can be represented in many different forms

```
you've seen strings, tuples, lists, ... even functions
```

That one company is designing a contacts system for the Pokegear/Pokenav/Poketech/C-Gear/Xtransciever. Specifically, they want an Entry type which stores an id, name, and number.

Here's an implementation that does it all using strings (terrible choice).

No id/name/number ever contains a tab character.

```
class Entry:
    def __init__(self, id, name, number):
        self.__data = str(id) + '\t' + str(name) + '\t' + str(number)
    def get(self, key):
        if key is 'id':
            return int(self.__data.split('\t')[0])
        elif key is 'name':
            return str(self.__data.split('\t')[1])
        elif key is 'number':
            return int(self.__data.split('\t')[2])
```

Using a different representation of the data, implement Entry (ours is 5 lines total).

# **Multiple Representations**

Using a different representation of the data, implement Entry (ours is 5 lines total).

```
class Entry:
    def __init__(self, id, name, number):
        self.__data = {'id':id, 'name':name, 'number':number}
    def get(self, key):
        return self.__data[key]
```

Other ways include: store as fields, store in a list, store in a tuple ...

# Type dispatching and Data-directed Programming

#### Type dispatching:

- We can use a different function for each possible combination of types on an operator and using the correct function for a provided combination of types.
- In lecture, you explored tag-based table method.

#### Data-directed Programming:

 a dispatching function performs table lookups with the operator and types to apply the correct function.

# **Type Coercion**

Sometimes, it makes sense to do an operation dispatched between different types by converting one of the types into another.

The way to do this is obvious with many numeric types (an integer can be coerced to a rational number can be coerced to a real number).

It is not always the case that one type is a subset of the other.

We have count\_legendaries(ls), a function which takes in a list and outputs the number of legendaries in the list. For example:

```
>>> count_legendaries(['Unown', 'Geodude', 'Mewtwo'])
1
```

Make a coercion so that we can count the legendaries in comma-separated strings, such as 'Bulbasaur,Charmander,Squirtle' using count\_legendaries.

```
def cs_to_ls(comma_separated_string):
    return _____
```

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>>> count_legendaries(['Unown', 'Geodude', 'Mewtwo'])
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Make a coercion so that we can count the legendaries in comma-separated strings, such as 'Bulbasaur, Charmander, Squirtle' using count\_legendaries.

```
def cs_to_ls(comma_separated_string):
    return comma_separated_string.split(',')
```