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# END SEMESTER EXAMINATION, NOVEMBER-2018

Semester : 1st

Subject Code : Sc-102

## MATHEMATICS-I

Full Marks – 70

Time – Three hours

The figures in the margin indicate full marks  
for the questions.

### Instructions :

1. All questions of PART – A are compulsory.
2. Answer any five questions from PART – B.

### PART – A

Marks – 25

1. Fill in the blanks :  $1 \times 10 = 10$

(a) Express  $-\frac{1}{2}$  in the  $a + ib$  form \_\_\_\_\_.

(b) What is the value of  $i^{87}$ ? \_\_\_\_\_.

[Turn over

(c) Equation of a straight line perpendicular to a given line  $Ax + By + C = 0$  is \_\_\_\_\_.

(d) If  ${}^n P_3 = 336$ , then,  ${}^n C_3 =$  \_\_\_\_\_.

(e) If  $A = \begin{bmatrix} 1 & -1 \\ 2 & 5 \end{bmatrix}$ , then  $5A$  is \_\_\_\_\_.

(f) The value of  $\cot 15^\circ$  is \_\_\_\_\_.

(g) The number of ways in which 6 students can be arranged in a circle is \_\_\_\_\_.

(h) If  $A$  is a skew symmetric matrix, then  $A^T$  is equal to \_\_\_\_\_.

(i) The lateral surface area of a cylinder is \_\_\_\_\_.

(j) The value of  $\log_5 25$  is \_\_\_\_\_.

2. Write true or false :  $1 \times 10 = 10$

(a) To convert from Cartesian to polar coordinate we use  $r = \sqrt{x^2 + y^2}$  and  $\theta = \tan^{-1} \frac{X}{Y}$ .

(b) Slope of line passing through  $(7, 2)$  and  $(7, -5)$  is not defined.

- (c) The x-intercept of  $3x + 4y + 5 = 0$  is 4.

(d) If  $x = 1 - i$ , then the value of  $x^2 - 2x + 2 = 0$ .

(e) In any triangle ABC, we have  $c = b \cos B + c \cos C$

(f) General term for  $(x - a)^n$  is  $(-1)^n {}^nC_r x^{n-r} a^r$ .

(g) The equation of the line which is perpendicular to the line  $x + 2y + 1 = 0$  is  $2x - y + 2 = 0$ .

(h) In a matrix multiplication, for any two square matrices A and B,  $AB = BA$ .

(i) The value of  $\left(\omega^4 + \omega^5 + \frac{1}{\omega^7} + \frac{1}{\omega^8}\right)$  is -2, where  $\omega$  is the cube root of unity.

(j) The area of the  $\Delta ABC$ , where  $b = 5$ ,  $c = 3$  and  $A = 30^\circ$  is 13 sq. units.

**3. Choose the correct answer :                           $1 \times 5 = 5$**

- (a) Value of  $\omega^{46}$  is

(b) Cofactor of  $a_{31}$  in  $\begin{vmatrix} 2 & -1 & 0 \\ 1 & -2 & 1 \\ 4 & 3 & -1 \end{vmatrix}$  is

(i)  $\begin{vmatrix} -1 & 0 \\ -2 & 1 \end{vmatrix}$

(ii)  $\begin{vmatrix} -2 & 1 \\ 3 & -1 \end{vmatrix}$

(iii)  $\begin{vmatrix} 2 & -1 \\ 1 & -2 \end{vmatrix}$

(iv)  $\begin{vmatrix} 1 & -2 \\ 4 & 3 \end{vmatrix}$

(c) The sum of the first 8 terms of the series  
2, 6, 18, 54 ..... is

(i) 2320

(ii) 6560

(iii) 4320

(iv) 5670

(d) The curved surface area of cylindrical pillar  
is  $264\text{m}^2$  and its volume is  $924\text{m}^3$ . The ratio  
of its diameter to its height is

(i) 3 : 7

(ii) 7 : 3

(iii) 6 : 7

(iv) 7 : 6

- (e) Equation of the straight line passing through  $(0, -1)$  and parallel to X-axis is
- (i)  $y = 0$       (ii)  $x = 0$   
 (iii)  $y = -1$       (iv)  $x = -1$

### PART – B

Marks – 45

4. Answer the following questions : 3+4+2=9

(a) Find the square root of  $7 - 30\sqrt{-2}$ .

(b) Find the conjugate of  $\frac{3+i}{2+4i}$ . Also find the modulus and amplitude of  $\frac{1+2i}{1-3i}$ .

(c) Find k if  $2k + 1, k, 3k + 2$  are in G.P.

Answer the following questions : 2+3+4=9

(a) Prove that  $(1 + \omega)(1 + \omega^2)(1 + \omega^4)(1 + \omega^8) = 1$ , where  $\omega$  is the imaginary cube root of unity.

(b) Find the term independent of x in  $(2x^2 - \frac{1}{x})^{12}$ .

(c) In how many ways can a term of 11 members from 14 players be formed if

(i) one particular player be always included ?

(ii) one particular player is never included ?

✓ Answer the following questions :  $3+3+3=9$

(a) Simplify  $\log \frac{81}{8} - 2 \log \frac{3}{2} + 3 \log \frac{2}{3} + \log \frac{3}{4}$ .

(b) Without expanding determinant prove that,

$$\begin{vmatrix} 1 & 1 & 1 \\ p & q & r \\ p^2 & q^2 & r^2 \end{vmatrix} = 0$$

(c) Find  $A^2 - 5A + 6I$ , if  $A = \begin{bmatrix} 2 & 0 & 1 \\ 2 & 1 & 3 \\ 1 & -1 & 0 \end{bmatrix}$ .

✓ Answer the following questions :  $3+4+2=9$

(a) Find the coefficient of  $x^{17}$  in the expansion of  $(x - x^2)^{10}$ .

(b) Resolve into partial fractions :  $\frac{x^2 - 3x + 1}{(x-1)^2(x-2)}$ .

(c) Find the value of n if  ${}^n C_2 = 45$ .

8 Answer the following questions : 3+3+3=9

(a) If  $\tan^{-1}x + \tan^{-1}y + \tan^{-1}z = \frac{\pi}{2}$  prove that  $x + y + z = xyz$ .

(b) Prove that  $\frac{\sin A + \sin B}{\cos A + \sin B} = \tan \frac{A+B}{2}$ .

(c) Prove that  $\sin^2 36^\circ + \sin^2 54^\circ = 1$ .

9 Answer the following questions : 3+3+3=9

(a) If  $A = \begin{bmatrix} 3 & 1 \\ 4 & 1 \\ -5 & 2 \end{bmatrix}$  and  $B = \begin{bmatrix} 3 & 1 & 2 \\ -2 & 0 & 4 \end{bmatrix}$  then find the value of AB.

(b) If  $\theta = \frac{a}{b}$ , then find the value of  $b \cos 2\theta + a \sin 2\theta$ .

(c) Find the value of k for which the lines  $5x + 4y - 6 = 0$  and  $2x + ky + 9 = 0$  are parallel.

10. Answer the following questions :      3+3+3=9

- (a) Find the angle between the lines  $2x + y + 3 = 0$  and  $x + 3y + 4 = 0$ .
- (b) The slant height of a frustum of a cone is 4cm and the perimeters (circumference) of its circular ends are 18cm and 6cm. Find the curved surface area of the frustum.
- (c) Calculate the total area of a field with a base of 60m and ordinates 8, 11, 2, 4, 6, 7, 10, 12, 8, 5, 10 respectively.

11. Answer the following questions :      3+3+3=9

- (a) Solve the system of equations by Cramer's rule  
 $5x - y = 9$ ,  $3x + y = 7$  and  $x + y + z = 4$ .
- (b) Find the equation of the straight line, which passes through the point (1, 2) and which is parallel to the straight line  $2x + 3y + 6 = 0$ .
- (c) If  $\cos^2 \alpha - \sin^2 \alpha = \tan^2 \beta$ , then show that  $\cos^2 \beta - \sin^2 \beta = \tan^2 \alpha$ .

12. Answer the following questions :       $3+3+3=9$

- (a) Prove that  $3\tan^{-1}x = \tan^{-1}\left(\frac{3x-x^3}{1-3x^2}\right)$ .
- (b) Prove that  $\cos(60^\circ - A)\cos(30^\circ - B) - \sin(60^\circ - A)\sin(30^\circ - B) = \sin(A+B)$ .
- (c) Find the value of  $\cos\left[\frac{\pi}{6} - \cos^{-1}\left(\frac{1}{2}\right)\right]$ .



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