Han Zhang

Logistics

Observational Studies

Ignorability

Matching

Readings

Today's topics are drawn from:

 Joshua D. Angrist and Jorn-Steffen Pischke. Mostly Harmless Econometrics: An Empiricists Companion. Princeton University Press, 2009. (Chapters 2 - 3)

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- Aronow, Peter M., and Benjamin T. Miller. Foundations of Agnostic Statistics. Cambridge University Press, 2019. (Chapters 6 - 7)

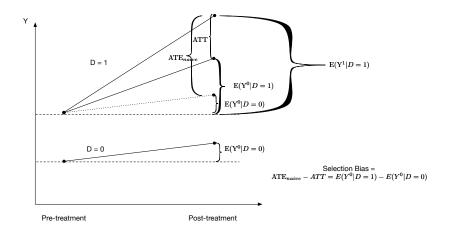


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- Proofs:
 - Imbens, Guido W., and Donald B. Rubin. Causal inference in statistics, social, and biomedical sciences. Cambridge University Press, 2015 (Chapter 6 - 7).



• $ATE_{naive} = E(Y^1|D=1) - E(Y^0|D=0)$, which is the mean differences in "treatment" and "control" outcomes.

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- Rule of thumb: the gold-standard is always randomized controlled experiment

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- The trend is leaning toward design-based causal inference

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 - A non-exhaustive lists include economic growth itself, leadership personality, geospatial conditions, etc.



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 - POLITY Score (democracy scores)



Estimating causal effects in natural experiment

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- We can also use regression estimator: $\hat{\rho}$ estimates ATE

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- There is no substitute for a good research design (here, exogenous shocks)



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 - Another differences from the randomized experiments

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- Be clear what you are comparing with
- In randomized controlled experiments, treatment and control groups were chosen with clear standard so there is no such problem



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- Note that randomized experiments automatically satisfy this assumption

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- or, there is selection bias due to unobservables

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 If ignorability assumption is true, and you assume the effect of treatment is constant on Y, we can use regression to estimate causal effects:

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 - More X increases the possibility that you do not missed anything important confounders

Regression as Imputation

Ignorability 000000000

• If ignorability is true, the regression estimator of ATE is implicitly making counterfactual imputation using linear regression.

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1	?	2	1	1	7
2	5	?	0	8	2
3	?	3	1	9	3
4	?	10	1	3	1
5	?	2	1	5	2
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2	5	$\hat{\beta}_0 + \hat{\beta}_1 \cdot 1 + \hat{\beta}_2 \cdot 8 + \hat{\beta}_3 \cdot 2$	0	8	2	
3	$\hat{\beta}_0 + \hat{\beta}_1 \cdot 0 + \hat{\beta}_2 \cdot 9 + \hat{\beta}_3 \cdot 3$	3	1	9	3	
4	$\hat{\beta}_0 + \hat{\beta}_1 \cdot 0 + \hat{\beta}_2 \cdot 3 + \hat{\beta}_3 \cdot 1$	10	1	3	1	
5	$\hat{\beta}_0 + \hat{\beta}_1 \cdot 0 + \hat{\beta}_2 \cdot 5 + \hat{\beta}_3 \cdot 2$	2	1 ≣	5 ≥ →	2	990

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• Run a regression as $Y = \beta_0 + \beta_1 D_i + \beta_2 X_{[1]i} + \beta_3 X_{[2]i}$, and impute counterfactual outcome using the linear regression:

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- Jens Hainmueller and Dominik Hangartner, Who Gets a Swiss Passport? A Natural Experiment in Immigrant Discrimination, American Political Science Review 107 (2013), no. 01, 159–187

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 - Other unobserved confounders you can think of?

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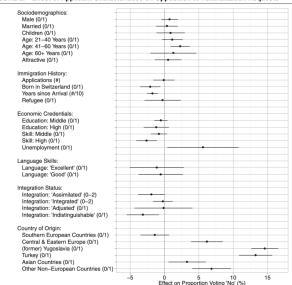
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- These features ensures minimum measurement error, and also ignorability

FIGURE 2. Effect of Applicant Characteristics on Opposition to Naturalization Requests



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- That is, they have private information other than that listed in the leaflets

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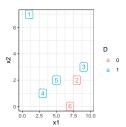
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- Then we can estimate ATE as the the difference between the mean of Y_i^1 and Y_i^0 for all units

Unit	Y_i^0	Y_i^1	D_i	$X_{[1]i}$	$X_{[2]i}$
1	?	2	1	1	7
2	5	?	0	8	2
3	?	3	1	9	3
4	?	10	1	3	1
5	?	2	1	5	2
6	0	?	0	7	0

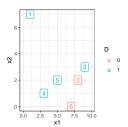
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- Unit 3 is treated; it is closest to unit 2; unit 2 is the matched unit of unit 3
- $Y_3^0 \leftarrow Y_2^0 = 5$

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 - This is usually called propensity score matching



Uni	it Y_i^0	Y_i^1	D_i	$X_{[1]i}$	$X_{[2]i}$	$p(D_i=1 X_i)$	
1	?	2		1	7	0.33	
2	5	?	0	8	2	0.14	
3	?	3	1	10	3	0.73	
4	?	10	1	3	1	0.35	
5	?	2	1	5	2	0.78	
6	0	?	0	7	0	0.70	

	Unit	Y_i^0	Y_i^1	D_i	$X_{[1]i}$	$X_{[2]i}$	$p\left(D_i=1 X_i\right)$	
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• Estimated ATE is 7/6

 Regression estimates of ATE in general will be different from matching estimates of ATE (MHE 3.3)

$$A\hat{T}E_{ols} = \hat{\rho} = \sum_{x} \frac{\omega(x)}{(\sum_{x} \omega(j))} \cdot A\hat{T}E_{x}$$

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 - These are observations whose treatment status cannot be predicted well by X, thus could have omitted variable bias



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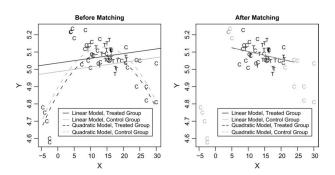
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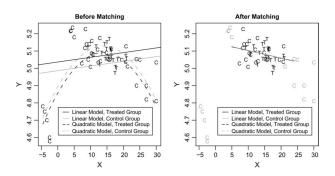


• Why approaching experimental ideal is important?



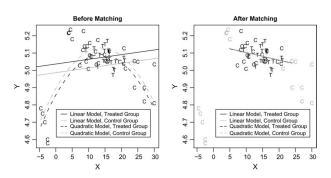


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 - That is, construct a data as (NSW(treated), CPS); CPS replaced NSW control units



What the authors did:

TABLE 2.—SAMPLE CHARACTERISTICS AND ESTIMATED IMPACTS FROM THE NSW AND CPS SAMPLES

Control Sample	No. of Observations	Mean Propensity Score ^A	Age	School	Black	Hispanic	No Degree	Married	RE74	RE75	U74	U75	Treatment Effect (Diff. in Means)	Regression Treatment Effect
NSW	185	0.37	25.82	10.35	0.84	0.06	0.71	0.19	2095	1532	0.29	0.40	1794 ^B	1672°
													(633)	(638)
Full CPS	15992	0.01	33.23	12.03	0.07	0.07	0.30	0.71	14017	13651	0.88	0.89	-8498	1066
		$(0.02)^{D}$	(0.53)	(0.15)	(0.03)	(0.02)	(0.03)	(0.03)	(367)	(248)	(0.03)	(0.04)	(583)E	(554)
Without replacement:														
Random	185	(0.03)	25.26 (0.79)	10.30 (0.23)	(0.04)	0.06 (0.03)	0.65 (0.05)	0.22 (0.04)	2305 (495)	1687 (341)	(0.05)	(0.05)	1559 (733)	1651 (709)

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TABLE 2.—SAMPLE CHARACTERISTICS AND ESTIMATED IMPACTS FROM THE NSW AND CPS SAMPLES

Control Sample	No. of Observations	Mean Propensity Score ^A	Age	School	Black	Hispanic	No Degree	Married	RE74	RE75	U74	U75	Treatment Effect (Diff. in Means)	Regression Treatment Effect
NSW	185	0.37	25.82	10.35	0.84	0.06	0.71	0.19	2095	1532	0.29	0.40	1794 ^B	1672 ^C
													(633)	(638)
Full CPS	15992	0.01	33.23	12.03	0.07	0.07	0.30	0.71	14017	13651	0.88	0.89	-8498	1066
		$(0.02)^{D}$	(0.53)	(0.15)	(0.03)	(0.02)	(0.03)	(0.03)	(367)	(248)	(0.03)	(0.04)	(583)E	(554)
Without replacement:														
Random	185	0.32	25.26	10.30	0.84	0.06	0.65	0.22	2305	1687	0.37	0.51	1559	1651
		(0.03)	(0.79)	(0.23)	(0.04)	(0.03)	(0.05)	(0.04)	(495)	(341)	(0.05)	(0.05)	(733)	(709)

- What the authors did:
 - Experiments: raw ATE vs. regression estimated ATE based on [NSW(treated), NSW(control)]
 - CPS: ATE_{naive} vs. regression adjusted ATE_{naive} based on [NSW(treated), CPS)]
 - Matching: match each unit in NSW treatment group with a control in CPS, then calculate ATE_{naive} and regress adjusted ATE_{naive} based on [NSW(treated), CPS(matched)]

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 - And it will be dangerous to add occupation as a control variable, since occupation may be the result of treatment

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 - Essentially admit that we cannot control everything; there are some unobserved variables we cannot control for

Econometric tools in working with non-ignorability

Fixed effect and diff-in-diff

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- Fixed effect and diff-in-diff
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