# Homework Assignment 1 Total Points: 50

Professor Karem A. Sakallah

EECS 598-002: Formal Verification of Hardware & Software Systems

Assigned: January 16, 2024 Due: January 23, 2024

### Guidelines

- The College of Engineering Honor Code applies to all work in this course.
- The due date is firm. Follow submission instructions (at the end).

### **Objectives**

This assignment involves the basic use of the Colorado University Decision Diagram package (CUDD) through the RePyCUDD Python wrapper.

## 1 [BDD Construction Mechanics] (30 Points)

Write Python scripts to construct BDDs for each of the following functions. Label and order your variables according to  $x_0 < x_1 < x_2 < \cdots$ 

- a. (5 Points)  $f(x_0, x_1, x_2) = x_0 x_1' x_2$ .
- b. (5 Points)  $f(x_0, x_1, x_2)$  is the 3-input majority function.
- c. (10 Points)  $f(x_0, x_1, x_2, x_3)$  is the function that is 1 if exactly 2 of the variables are 1.
- d. (5 Points)  $f(x_0, x_1, x_2, x_3) = x_0 \oplus x_1 \oplus x_2 \oplus x_3$
- e. (5 Points) Reorder the variables in part d to  $x_3 < x_2 < x_1 < x_0$ , and report the change in the number of nodes in the BDD of f compared to part d.

### 2 [Effect of Variable Ordering] (20 Points)

Construct the BDD for the 8-variable function

$$f = x_1 x_2 + x_3 x_4 + x_5 x_6 + x_7 x_8$$

a. (5 Points) Using the variable order  $x_1 < x_2 < x_3 < x_4 < x_5 < x_6 < x_7 < x_8$ .

- b. (5 Points) Using the variable order  $x_1 < x_3 < x_5 < x_7 < x_2 < x_4 < x_6 < x_8$ .
- c. (10 Points) Derive formulas for the BDD size under these two orderings assuming the number of variable is  $n \ge 2$ ).

#### **Submission Instructions**

- 1. Create a directory named <your uniquame>\_hw1
- 2. Place in the directory the following Python files corresponding to each of the problems or problem parts:
  - Problem 1: h2p1.py
  - Problem 2: h2p2b.py, h2p2c.py
- 3. Execute your Python files to produce similarly named dot files.
- 4. Use dot to generate similarly-named pdf files.
- 5. Use your favorite document editor to write the answers to problem 2.c.
- 6. Generate a single pdf file named <your uniquename>\_hw1.pdf that contains the written answers to problems 2.c.
- 7. Zip the entire directory using "zip -r <your uniquename>\_hw1.zip <your uniquename>\_hw1" and upload to Canvas.