

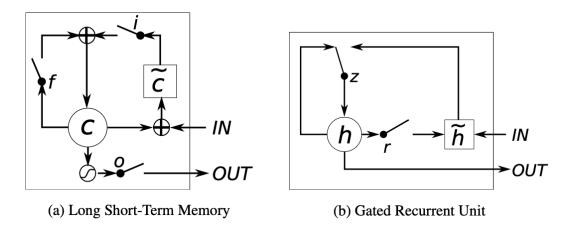
Outline



- □ Sequence Modeling
- □ Transformer
- **□** Experiments
- □ Conclusion



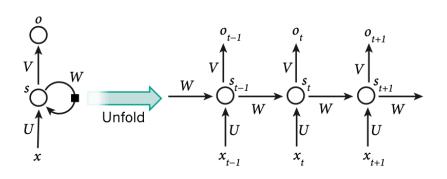
- ☐ What is Sequence Modeling?
 - Sequence modeling refers to the comprehensive modeling of sequential data
 - Recurrent Neural Network (RNN), Long Short-Term Memory (LSTM), and Gated Recurrent Units (GRU) are dominant models for processing sequential data

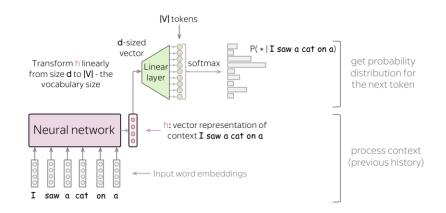




Language Modeling with RNN

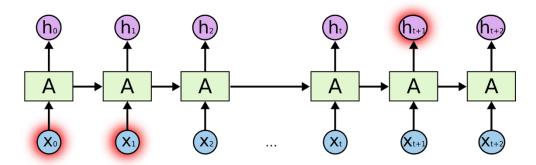
- RNN processes input sequences one step at a time, **accumulating information** in the hidden state
- The final hidden state of an RNN contains the representation of the entire sentence







- Challenge of Conventional Sequence Modeling
 - As the sentence gets longer, RNN becomes **less capable of learning long-range dependencies** between distant words
 - The nature of sequential modeling prevents parallelization within a training example
 - ☐ It becomes critical as the sequence length increases because memory constraints limit batching





☐ Using Convolutional Neural Networks

- Treating sentences with CNNs can compute hidden representations in parallel for all input and output positions
 - But still, this makes it difficult to learn dependencies between distant positions

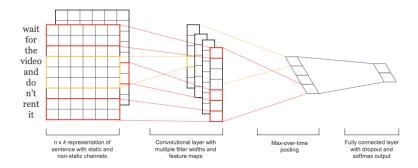


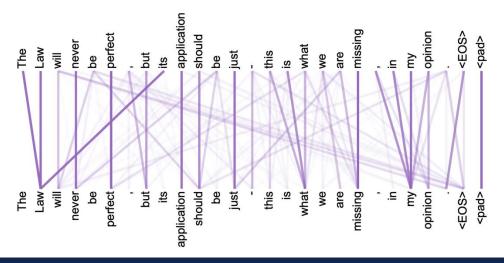
Figure 1: Model architecture with two channels for an example sentence.

Transformer



Self-Attention Mechanism

- Self-attention is an attention mechanism relating different positions of a single sequence in order to compute a representation of the sequence
 - ☐ It enables the model to more effectively capture long-range dependencies than a recurrent model

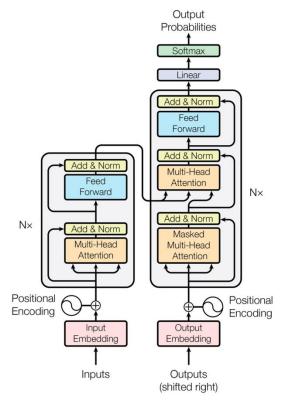


Transformer



What is Transformer?

Transformer is the transduction model that relies entirely on self-attention mechanism to process sequential data, without using recurrence or hidden states

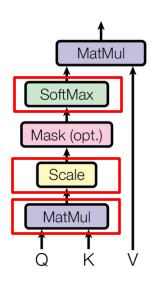




Scaled Dot-Product Attention

- Attention $(Q, K, V) = \operatorname{softmax}(\frac{QK^T}{\sqrt{d_k}})V$
- - ☐ Query represents the target word we want to focus on
 - ☐ Keys represent all the words in the sentence
 - ☐ Values represent the actual meaning or information carried by each Key
- lacksquare QK^T means the similarity between the current Query and all Keys through a dot product

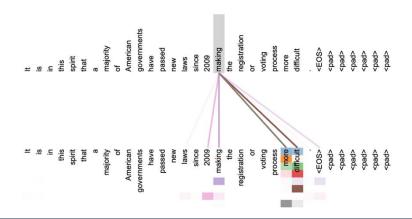
Scaled Dot-Product Attention



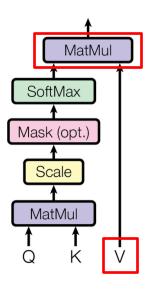


Scaled Dot-Product Attention

- softmax($\frac{QK^T}{\sqrt{d_k}}$)V means aggregating the actual information from other words (Key), weighted by the attention scores
 - ☐ Repeating this process for each word yields a context vector per word, incorporating information from the whole sentence



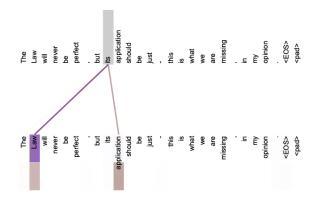
Scaled Dot-Product Attention

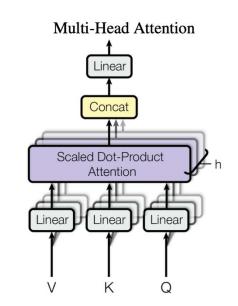




☐ Multi-Head Attention

- Q, K, and V are computed through linear projections and then split into smaller dimensions across multiple heads, where each head performs self-attention independently
 - ☐ Concatenating the outputs of multiple heads produces more generalized representations and improves accuracy





$$\begin{split} \text{MultiHead}(Q,K,V) &= \text{Concat}(\text{head}_1,...,\text{head}_\text{h})W^O \\ \text{where head}_i &= \text{Attention}(QW_i^Q,KW_i^K,VW_i^V) \end{split}$$

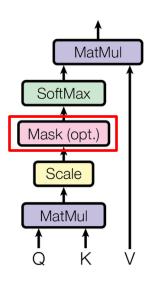


Masked Multi-Head Attention

- The mask in the decoder prevents access to future tokens by setting their attention scores to -inf
- The output is used as the Query to perform attention over the Encoder's output (as the Key and Value)

$$M_{
m causal} = egin{bmatrix} 0 & -\infty & -\infty & \dots & -\infty \ 0 & 0 & -\infty & \dots & -\infty \ 0 & 0 & 0 & \dots & -\infty \ dots & dots & dots & dots & dots \ 0 & 0 & 0 & \dots & 0 \end{bmatrix}$$

Scaled Dot-Product Attention



Other Components



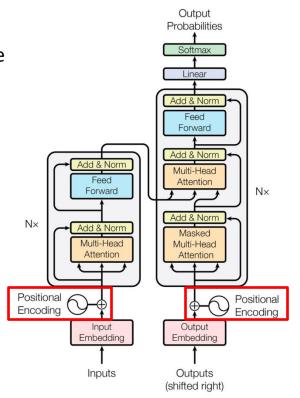
Positional Encoding

Since self-attention operates in parallel without sequence information, positional information must be added for the model to understand token order

$$PE_{(pos,2i)} = sin(pos/10000^{2i/d_{\text{model}}})$$

 $PE_{(pos,2i+1)} = cos(pos/10000^{2i/d_{\text{model}}})$

$$PE_{(pos,2i+1)} = cos(pos/10000^{2i/d_{\text{model}}})$$



Other Components

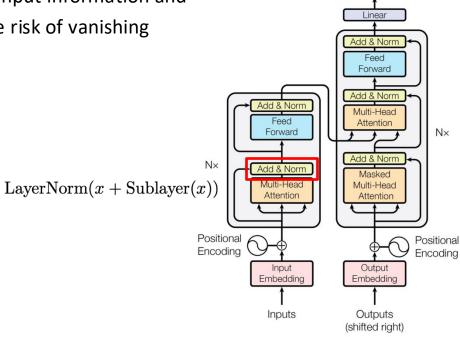


Output
Probabilities

Softmax

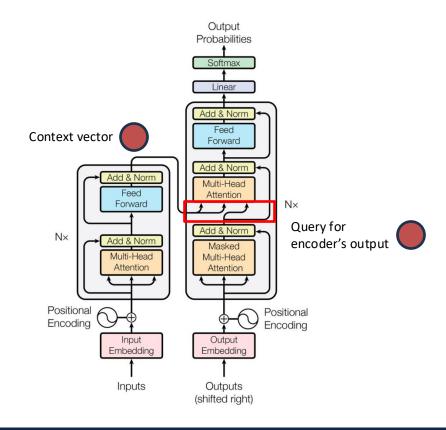
☐ Residual Connection

Residual connection helps preserve input information and improves gradient flow, reducing the risk of vanishing gradients in deep networks



Overall Architecture





Another Example of Transformer



□ News Recommend System with Attention

Q = Information of reader



K = Title of news

Stock market today: Nasdaq notches closing record as Nvidia hits \$4T

Investing: Author Yasin Ebrahim | Stock Markets

China's ETF market is booming, but what comes next?

V = Contents of news

Investing.com-- The Nasdaq closed at record highs Wednesday, shrugging off President Donald Trump's latest tariff blitz as Nvidia rallied to top \$4T in value for the first time, pushing the broader tech sector higher.

At 4:00 pm ET (20:00 GMT), the NASDAQ Composite 100 Futures}} climbed 0.95% to a closing record of 20,611.34, the Dow Jones Industrial Average gained 217 points, or 0.5%, and the S&P 500 index rose 0.6%.

Investing.com -- China's exchange traded fund, or ETF, market has exploded in recent years, with passive funds now outmuscling their active rivals and reshaping the landscape of the world's second-largest equity market. But as the ETF boom accelerates, questions are swirling about what this means for A-share liquidity, volatility, and the future of active management.



□ English-to-German, English-to-French

■ Transformer model outperforms the best previously reported models (including ensembles) by more than 2.0 BLEU, establishing a new state-of-the-art BLEU score of 28.4.

Table 2: The Transformer achieves better BLEU scores than previous state-of-the-art models on the English-to-German and English-to-French newstest2014 tests at a fraction of the training cost.

| Model | BL | EU | Training Cost (FLOPs) | | |
|---------------------------------|-------|-------|-----------------------|---------------------|--|
| Wodel | EN-DE | EN-FR | EN-DE | EN-FR | |
| ByteNet [18] | 23.75 | | | | |
| Deep-Att + PosUnk [39] | | 39.2 | | $1.0\cdot 10^{20}$ | |
| GNMT + RL [38] | 24.6 | 39.92 | $2.3\cdot 10^{19}$ | $1.4\cdot 10^{20}$ | |
| ConvS2S [9] | 25.16 | 40.46 | $9.6\cdot 10^{18}$ | $1.5\cdot 10^{20}$ | |
| MoE [32] | 26.03 | 40.56 | $2.0\cdot 10^{19}$ | $1.2\cdot 10^{20}$ | |
| Deep-Att + PosUnk Ensemble [39] | | 40.4 | | $8.0\cdot 10^{20}$ | |
| GNMT + RL Ensemble [38] | 26.30 | 41.16 | $1.8\cdot 10^{20}$ | $1.1\cdot 10^{21}$ | |
| ConvS2S Ensemble [9] | 26.36 | 41.29 | $7.7\cdot 10^{19}$ | $1.2 \cdot 10^{21}$ | |
| Transformer (base model) | 27.3 | 38.1 | 3.3 · | 10^{18} | |
| Transformer (big) | 28.4 | 41.8 | 2.3 \cdot | 10^{19} | |



□ Variations on the Transformer architecture

| | | | | | | | | | train | PPL | BLEU | params |
|------|---|----------------|-------------|-------|---------|---------|------------|-----------------|-------|-------|-------|---------------|
| | N | $d_{ m model}$ | $d_{ m ff}$ | h | d_k | d_v | P_{drop} | ϵ_{ls} | steps | (dev) | (dev) | $\times 10^6$ |
| base | 6 | 512 | 2048 | 8 | 64 | 64 | 0.1 | 0.1 | 100K | 4.92 | 25.8 | 65 |
| | | | | 1 | 512 | 512 | | | | 5.29 | 24.9 | |
| (4) | | | | 4 | 128 | 128 | | | | 5.00 | 25.5 | |
| (A) | | | | 16 | 32 | 32 | | | | 4.91 | 25.8 | |
| | | | | 32 | 16 | 16 | | | | 5.01 | 25.4 | |
| (D) | | | | | 16 | | | | | 5.16 | 25.1 | 58 |
| (B) | | | | | 32 | | | | | 5.01 | 25.4 | 60 |
| | 2 | | | | | | | | | 6.11 | 23.7 | 36 |
| | 4 | | | | | | | | | 5.19 | 25.3 | 50 |
| | 8 | | | | | | | | | 4.88 | 25.5 | 80 |
| (C) | | 256 | | | 32 | 32 | | | | 5.75 | 24.5 | 28 |
| | | 1024 | | | 128 | 128 | | | | 4.66 | 26.0 | 168 |
| | | | 1024 | | | | | | | 5.12 | 25.4 | 53 |
| | | | 4096 | | | | | | | 4.75 | 26.2 | 90 |
| (D) | | | | | | | 0.0 | | | 5.77 | 24.6 | |
| | | | | | | | 0.2 | | | 4.95 | 25.5 | |
| | | | | | | | | 0.0 | | 4.67 | 25.3 | |
| | | | | | | | | 0.2 | | 5.47 | 25.7 | |
| (E) | | posi | tional er | nbedo | ling in | stead o | f sinusoi | ds | | 4.92 | 25.7 | |
| big | 6 | 1024 | 4096 | 16 | | | 0.3 | | 300K | 4.33 | 26.4 | 213 |



□ English Constituency Parsing

■ The Transformer performs well not only in word prediction but also in more complex tasks such as constituency parsing

Table 4: The Transformer generalizes well to English constituency parsing (Results are on Section 23 of WSJ)

| Parser | Training | WSJ 23 F1 |
|-------------------------------------|--------------------------|-----------|
| Vinyals & Kaiser el al. (2014) [37] | WSJ only, discriminative | 88.3 |
| Petrov et al. (2006) [29] | WSJ only, discriminative | 90.4 |
| Zhu et al. (2013) [40] | WSJ only, discriminative | 90.4 |
| Dyer et al. (2016) [8] | WSJ only, discriminative | 91.7 |
| Transformer (4 layers) | WSJ only, discriminative | 91.3 |
| Zhu et al. (2013) [40] | semi-supervised | 91.3 |
| Huang & Harper (2009) [14] | semi-supervised | 91.3 |
| McClosky et al. (2006) [26] | semi-supervised | 92.1 |
| Vinyals & Kaiser el al. (2014) [37] | semi-supervised | 92.1 |
| Transformer (4 layers) | semi-supervised | 92.7 |
| Luong et al. (2015) [23] | multi-task | 93.0 |
| Dyer et al. (2016) [8] | generative | 93.3 |

Conclusion



□ The Transformer is a sequential modeling architecture that based solely on self-attention without using sequential recurrence
 □ This allows it to learn relationships between tokens regardless of their distance, while enabling parallel computation for faster processing

The model **generalizes well to more complex tasks** beyond simple word prediction



Set Transformer: A Framework for Attention-based Permutation-Invariant Neural Networks

Juho Lee, Yoonho Lee, Jungtaek Kim
ICML 2019

SuYong Jeong

Data Mining And Intelligence System LAB

Outline



- ☐ Set-Input Problem
- □ Set Pooling
- □ Set Transformer
- **□** Experiments
- □ Conclusion

Set-Input Problem



What is Set-Input problem?

- Given a set of instances as an input, the corresponding target is a label for the entire set
 - ☐ Multiple instance learning
 - ☐ 3D shape recognition

Serge's key-chain



Serge **cannot** enter the *Secret Room*

Sanjoy's key-chain



Sanjoy **can** enter the *Secret Room*

Lawrence's key-chain



Lawrence **can** enter the *Secret Room*



Set-Input Problem



- Critical Requirements for Set-Input Problems
 - Stem from the definition of a set
 - ☐ It should be permutation invariant
 - ☐ A model should be able to process input sets of any size

Serge's key-chain



Serge **cannot** enter the *Secret Room*

Sanjoy's key-chain



Sanjoy can enter the Secret Room

Lawrence's key-chain



Lawrence **can** enter the *Secret Room*



They are not easily satisfied in neural-network-based models!

Set Pooling



☐ What is Set Pooling method?

- Set Pooling is neural network architectures which meet both criteria
 - ☐ Each element in a set is independently fed into a feed-forward neural network
 - ☐ Resulting feature-space embeddings are aggregated using a pooling operation
- A permutation-equivariant encoder followed by a permutation-invariant decoder yields a permutation-invariant network

$$net(\lbrace x_1,\ldots,x_n\rbrace) = \rho(pool(\lbrace \phi(x_1),\ldots,\phi(x_n)\rbrace))$$

Set Pooling



☐ What is Set Pooling method?

- Every element in a set is processed independently in a set pooling operation
 - Some information regarding interactions between elements has to be necessarily discarded
 - ☐ This can make some problems unnecessarily difficult to solve

$$net(\lbrace x_1,\ldots,x_n\rbrace) = \rho(pool(\lbrace \phi(x_1),\ldots,\phi(x_n)\rbrace))$$

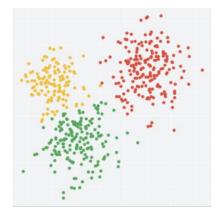
Set Pooling



☐ Amortized Clustering

- Learning a parametric mapping from an input set of points to the centers of clusters
 - ☐ The parametric mapping must assign each point to its corresponding cluster while modelling the explaining away pattern
- Set pooling don't care interactions between elements, making it unsuitable for modeling

relationships or enabling explaining away among cluster centers





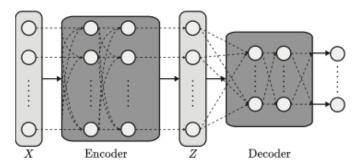
□ Self-attention

- Using Self-attention, we can measure how similar each pair of query and key vectors is
 - The output $\omega(QK^{\top})V$ is a weighted sum of V where a value gets more weight if its corresponding key has larger dot product with the query
 - ☐ We can encode the interactions between elements in the set with self-attention



What is Set Transformer?

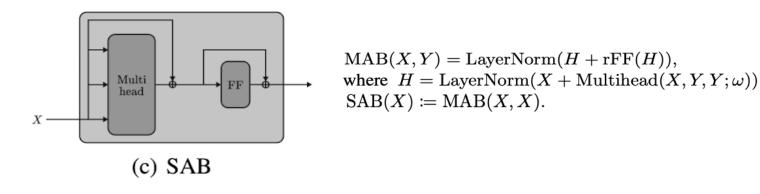
- Set Transformer is an attention-based neural network that is designed to process sets of data
 - ☐ It consists of an encoder followed by a decoder
 - ☐ Each layer in the encoder and decoder attends to their inputs to produce activations
 - ☐ Its aggregating function is parameterized and can adapt to the problem at hand





☐ Set Attention Block

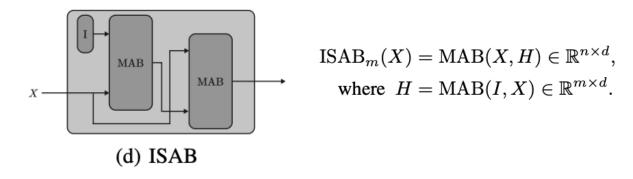
- Set Transformer uses self-attention to concurrently encode the whole set
 - ☐ This gives the Set Transformer the ability to compute pairwise as well as higher-order interactions among instances during the encoding process
 - \square A potential problem with using SABs for set-structured data is the quadratic time complexity $O(n^2)$





□ Induced Set Attention Block

- Along with the set $X \in \mathbb{R}^{n \times d}$, additionally define m d-dimensional vectors $I \in \mathbb{R}^{m \times d}$, which we call inducing points
 - \square Inducing points, I are part of the ISAB itself, and they are trainable parameters
 - \square The learned inducing points are expected to encode some global structure which helps explain the inputs X
 - The time complexity of ISAB_m(X; λ) is O(nm) where m is a hyperparameter





□ Pooling by Multihead Attention

- Features from encoder are aggregated by applying multi-head attention on a learnable set of k seed vectors $S \in \mathbb{R}^{k \times d}$
 - □ We use one seed vector (k= 1) in most cases, but for problems such as amortized clustering which requires k correlated outputs use k seed vectors
 - ☐ Seed vectors enable diverse summarization of the input set and support multi-output prediction by inducing an explaining away effect that prevents redundancy among outputs

$$PMA_k(Z) = MAB(S, rFF(Z)).$$



□ Overall Architecture

- Encoder: $X \mapsto Z \in \mathbb{R}^{n \times d}$ is a stack of SABs or ISABs
 - $\Box \quad \operatorname{Encoder}(X) = \operatorname{SAB}(\operatorname{SAB}(X))$ $\operatorname{Encoder}(X) = \operatorname{ISAB}_m(\operatorname{ISAB}_m(X)).$
 - \square After the encoder transforms data $X \in \mathbb{R}^{n \times d_x}$ into features $Z \in \mathbb{R}^{n \times d_x}$
- lacksquare Decoder: Aggregating Z into a single or a set of vectors to get final outputs
 - $\Box \ \operatorname{Decoder}(Z; \lambda) = \operatorname{rFF}(\operatorname{SAB}(\operatorname{PMA}_k(Z))) \in \mathbb{R}^{k \times d}$ where $\operatorname{PMA}_k(Z) = \operatorname{MAB}(S, \operatorname{rFF}(Z)) \in \mathbb{R}^{k \times d}$,



☐ Maximum Value Regression

Table 1. Mean absolute errors on the max regression task.

| Architecture | MAE |
|--|---|
| rFF + Pooling (mean) rFF + Pooling (sum) rFF + Pooling (max) | 2.133 ± 0.190 1.902 ± 0.137 $\textbf{0.1355} \pm \textbf{0.0074}$ |
| SAB + PMA (ours) | 0.2085 ± 0.0127 |



□ Counting Unique Characters



Table 2. Accuracy on the unique character counting task.

| Architecture | Accuracy | | |
|----------------------|---------------------|--|--|
| rFF + Pooling | 0.4382 ± 0.0072 | | |
| rFFp-mean + Pooling | 0.4617 ± 0.0076 | | |
| rFFp-max + Pooling | 0.4359 ± 0.0077 | | |
| rFF + Dotprod | 0.4471 ± 0.0076 | | |
| rFF + PMA (ours) | 0.4572 ± 0.0076 | | |
| SAB + Pooling (ours) | 0.5659 ± 0.0077 | | |
| SAB + PMA (ours) | 0.6037 ± 0.0075 | | |

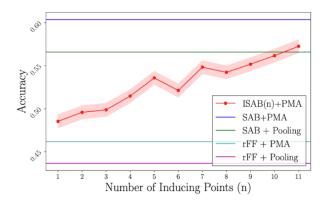


Figure 3. Accuracy of $ISAB_n + PMA$ on the unique character counting task. x-axis is n and y-axis is accuracy.



□ Amortized Clustering

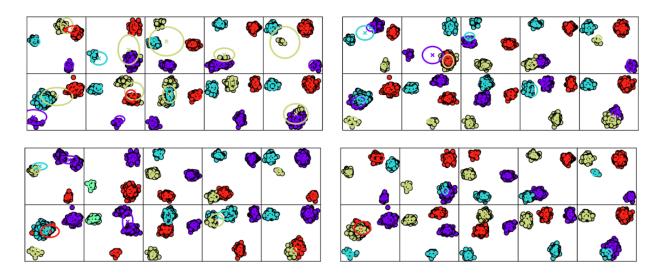
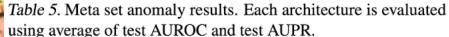


Figure 4. Clustering results for 10 test datasets, along with centers and covariance matrices. rFF+Pooling (top-left), SAB+Pooling (top-right), rFF+PMA (bottom-left), Set Transformer (bottom-right). Best viewed magnified in color.



Set Anomaly Detection





Test AUROC

0.5

 0.5643 ± 0.0139

 0.5687 ± 0.0061

 0.5717 ± 0.0117

 0.5671 ± 0.0139

 0.5757 ± 0.0143

 0.5756 ± 0.0130

 0.5941 ± 0.0170

Black hair & catee

)val face &

lyeglasses &

Austache

Vearing earrings



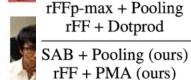














Architecture

Random guess

rFF + Pooling

rFFp-mean + Pooling









Test AUPR

0.125

 0.4126 ± 0.0108

 0.4125 ± 0.0127

 0.4135 ± 0.0162

 0.4155 ± 0.0115

 0.4189 ± 0.0167

 0.4227 ± 0.0127

 0.4386 ± 0.0089



Mustache & Mouth slightly open





□ Point Cloud Classification



Table 4. Test accuracy for the point cloud classification task using 100, 1000, 5000 points.

| Architecture | 100 pts | 1000 pts | 5000 pts |
|---|---|---|---|
| rFF + Pooling (Zaheer et al., 2017) rFFp-max + Pooling (Zaheer et al., 2017) | 0.82 ± 0.02 | $0.83 \pm 0.01 \\ 0.87 \pm 0.01$ | 0.90 ± 0.003 |
| rFF + Pooling | 0.7951 ± 0.0166 | 0.8551 ± 0.0142 | 0.8933 ± 0.0156 |
| rFF + PMA (ours) ISAB (16) + Pooling (ours) ISAB (16) + PMA (ours) | 0.8076 ± 0.0160 0.8273 ± 0.0159 0.8454 ± 0.0144 | 0.8534 ± 0.0152 0.8915 ± 0.0144 0.8662 ± 0.0149 | 0.8628 ± 0.0136 0.9040 ± 0.0173 0.8779 ± 0.0122 |

Conclusion



☐ The Set Transformer is an attention-based set-input neural network architecture

☐ It can model complicated interactions among elements of a set, using attention mechanisms for both encoding and aggregating features

☐ With inducing point method for self-attention, it can be scalable to large sets



Thank you