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DMAIS

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## DeepPath: A Reinforcement Learning Method for Knowledge Graph Reasoning

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EMNLP 2017

## Relational Message Passing for Knowledge Graph Completion

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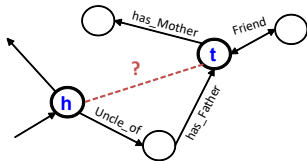
KDD 2021



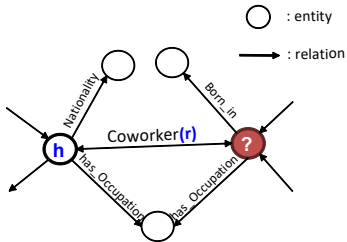
- **Main interest**
  
- **DeepPath**
  - Problem with previous models
  - Architecture
  - Experiments
  
- **Conclusion**
  
- **PathCon**
  - Problem with previous models
  - Architecture
  - Experiments
  
- **Conclusion**

## Knowledge Graph Completion(KGC)

- Find ? for  $(h,r,?)$  or  $(?,r,t)$  or  $(h,?,t)$



▲ relation prediction

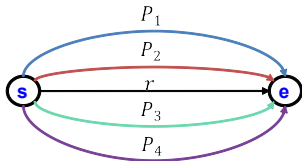


▲ link prediction

# Problem with previous models(DeepPath)

## ■ Problem of PRA

- PRA(2011a), a very impactful random walk based research on KGC
- However, operates in a fully discrete space limiting the ability to score and compare results

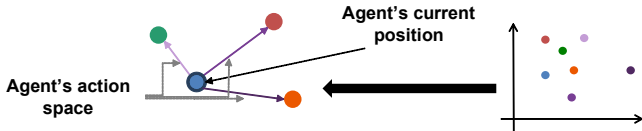


$$score(e; s) = \sum_{P \in \mathbf{P}_\ell} h_{s,P}(e) \theta_P$$

# Architecture(DeepPath)

## >> Preview of DeepPath

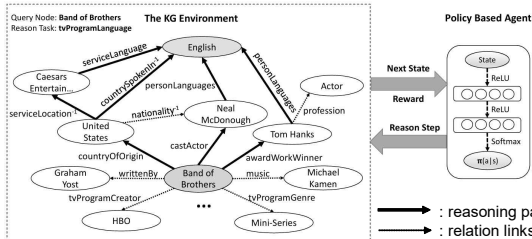
- Reinforcement learning(RL) based model
  - Trains a policy-based RL agent to find promising reasoning paths
- Incorporates translation based KG embedding method
  - Agent uses embeddings to navigate the path in a continuous space



# Architecture(DeepPath)

$$\langle S, A, P, R \rangle$$

Markov decision process(MDP) = environment

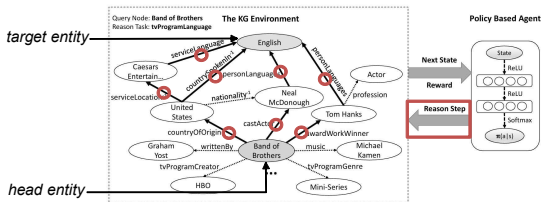


# Architecture(DeepPath)

## Components of RL environment $\langle S, A, P, R \rangle$

Given tuple  $(h, r, t)$ , we want the agent to find the most informative paths linking the target nodes

- **Action** : Agent uses policy network to pick the most promising relation to extend the path



# Architecture(DeepPath)

## Components of RL environment $\langle S, A, P, R \rangle$

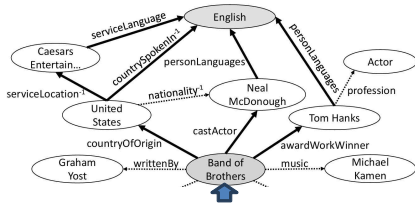
- States : Help define the current circumstance the agent is facing

$e$  : entity embedding generated from TransE

$$s_t = e_t \oplus (e_{\text{target}} - e_t)$$

equivalent to the sum of  
relation embeddings of a  
path which can connect  
 $e_{\text{target}}$  to  $e_t$

since TransE is able to model composition!!





- **Components of RL environment<S,A,P,R>**

- **Rewards** : 3 segments contribute to enhance the quality of paths found by the agent

- 1. Global **accuracy**

$$r_{\text{GLOBAL}} = \begin{cases} +1, & \text{if the path reaches } e_{\text{target}} \\ -1, & \text{otherwise} \end{cases}$$

- 2. Path **efficiency**

$$r_{\text{EFFICIENCY}} = \frac{1}{\text{length}(p)}$$

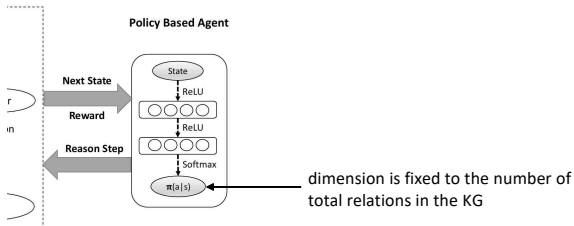
- 3. Path **diversity**

$$r_{\text{DIVERSITY}} = -\frac{1}{|F|} \sum_{i=1}^{|F|} \cos(\mathbf{p}, \mathbf{p}_i)$$

# Architecture(DeepPath)

- Components of RL environment  $\langle S, A, P, R \rangle$

- Policy network** : neural network that maps state vector to probability distribution of all possible actions



# Architecture(DeepPath)

- Supervised policy learning inspired by *AlphaGo(2016)*

- Large action space of KG results in poor convergence with naive trial and error approaches
- To tackle this problem, **feed paths that connect positive sample first** to better guide the agent (after that, we retrain the model on trial and error)

<expected total rewards for one episode>  <supervised version of reward gradient>

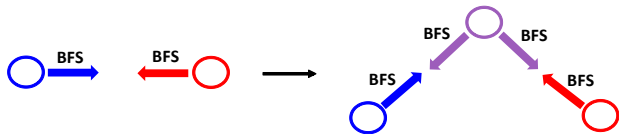
$$\begin{aligned} J(\theta) &= \mathbb{E}_{a \sim \pi(a|s;\theta)} \left( \sum_t R_{s_t, a_t} \right) \\ &= \sum_t \sum_{a \in \mathcal{A}} \pi(a|s_t; \theta) R_{s_t, a_t} \end{aligned}$$

$$\begin{aligned} \nabla_{\theta} J(\theta) &= \sum_t \sum_{a \in \mathcal{A}} \pi(a|s_t; \theta) \nabla_{\theta} \log \pi(a|s_t; \theta) \\ &\approx \nabla_{\theta} \sum_t \log \pi(a = r_t | s_t; \theta) \end{aligned}$$

- $r_t$  belongs to the supervised path  $p$
- it assumes that all the actions are done with 100% certainty

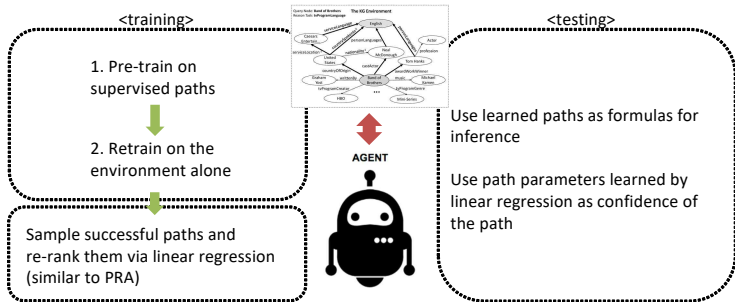
# Architecture(DeepPath)

- Traditional two-side BFS is not enough
  - Supervised paths are sampled by picking a subset of positive tuples  $(e_{source}, e_{target})$  and conducting BFS from each entity until they meet
  - However, BFS is biased to **short paths** which may hinder generality in retraining process
  - To tackle this, randomly sample a intermediate node and conduct two two-side BFS



# Architecture(DeepPath)

## Review of DeepPath schema



## ■ Settings

☐ **Metric** : MAP(Mean Average Precision)

☐ **Dataset** : FB15k-237, NELL-995(Tasks refer to relations that we will observe in this section)

Dataset	# Ent.	# R.	# Triples	# Tasks
FB15K-237	14,505	237	310,116	20
NELL-995	75,492	200	154,213	12

## ■ Experiments

☐ Entity prediction and fact prediction

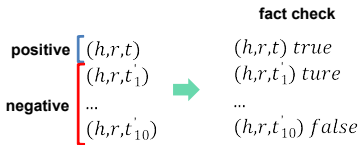
# Experiments(DeepPath)

## ■ Link prediction and # of collected reasoning paths

FB15K-237					NELL-995					# of Reasoning Paths		
Tasks	PRA	RL	TransE	TransR	Tasks	PRA	RL	TransE	TransR	Tasks	PRA	RL
teamSports	<b>0.987</b>	0.955	0.896	0.784	athletePlaysForTeam	0.547	<b>0.750</b>	0.627	0.673	worksFor	247	25
birthPlace	0.441	<b>0.531</b>	0.403	0.417	athletePlaysInLeague	0.841	<b>0.960</b>	0.773	0.912	teamPlaySports	113	27
personNationality	<b>0.846</b>	0.823	0.641	0.720	athleteHomeStadium	0.859	<b>0.890</b>	0.718	0.722	teamPlaysInLeague	69	21
filmDirector	0.349	<b>0.441</b>	0.386	0.399	athletePlaysSport	0.474	0.957	0.876	<b>0.963</b>	athlethomestadium	37	11
filmWrittenBy	0.601	0.457	0.563	<b>0.605</b>	teamPlaySports	0.791	0.738	0.761	<b>0.814</b>	organizationHiredPerson	244	9
filmLanguage	0.663	<b>0.670</b>	0.642	0.641	orgHeadquaterCity	<b>0.811</b>	0.790	0.620	0.657	...		
tvLanguage	0.960	<b>0.969</b>	0.804	0.906	worksFor	0.681	<b>0.711</b>	0.677	0.692	Average #	137.2	20.3
capitalOf	<b>0.829</b>	0.783	0.554	0.493	bornLocation	0.668	0.757	0.712	<b>0.812</b>			
organizationFounded	0.281	0.309	<b>0.390</b>	0.339	personLeadsOrg	0.700	<b>0.795</b>	0.751	0.772			
musicianOrigin	0.426	<b>0.514</b>	0.361	0.379	orgHiredPerson	0.599	<b>0.742</b>	0.719	0.737			
...					...							
Overall	0.541	<b>0.572</b>	0.532	0.540		0.675	<b>0.796</b>	0.737	0.789			

## Fact prediction

- Generate 10 negative triples(fake a certain entity, e.g.  $(h', r, t)$ ) for each positive
- Rank all the positive and negative triples(PRA is not able to process fact prediction)



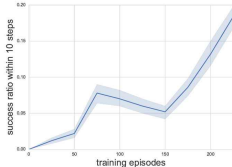
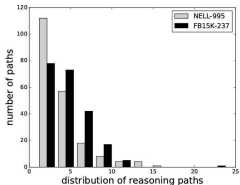
Methods	Fact Prediction Results	
	FB15K-237	NELL-995
RL	<b>0.311</b>	<b>0.493</b>
TransE	0.277	0.383
TransH	0.309	0.389
TransR	0.302	0.406
TransD	0.303	0.413



# Experiments(DeepPath)

## Other analysis

Relation	Reasoning Path
filmCountry	filmReleaseRegion
	featureFilmLocation $\rightarrow$ locationContains $^{-1}$
	actorFilm $^{-1} \rightarrow$ personNationality
personNationality	placeOfBirth $\rightarrow$ locationContains $^{-1}$
	peoplePlaceLived $\rightarrow$ locationContains $^{-1}$
	peopleMarriage $\rightarrow$ locationOfCeremony $\rightarrow$ locationContains $^{-1}$
tvProgramLanguage	tvCountryOfOrigin $\rightarrow$ countryOfficialLanguage
	tvCountryOfOrigin $\rightarrow$ filmReleaseRegion $^{-1} \rightarrow$ filmLanguage
	tvCastActor $\rightarrow$ filmLanguage
personBornInLocation	personBornInCity
	graduatedUniversity $\rightarrow$ graduatedSchool $^{-1} \rightarrow$ personBornInCity
	personBornInCity $\rightarrow$ atLocation $^{-1} \rightarrow$ atLocation
athletePlaysForTeam	athleteHomeStadium $\rightarrow$ teamHomeStadium $^{-1}$
	athletePlaysSport $\rightarrow$ teamPlaysSport $^{-1}$
	athleteLedSportsTeam
personLeadsOrganization	worksFor
	organizationTerminatedPerson $^{-1}$
	mutualProxyFor $^{-1}$



# Conclusion(DeepPath)

- DeepPath for knowledge graph completion

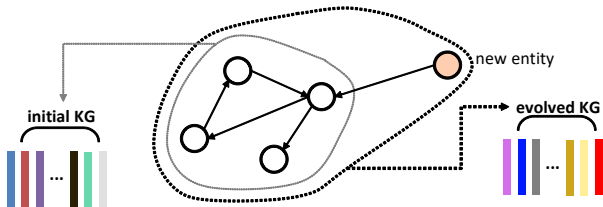
- First reinforcement learning based KGC model
- Complex reward function to explore more informative paths
- Adopted embeddings to define states on a continuous space

- Limitations of DeepPath

- Sparse reward and large action space is still a problem
- Supervised policy learning is not safe from bias (on the other hand, AlphaGo Zero(2017))
- Transductive nature because of the need to create embeddings for all entities and relations.

# Problem with previous models(PathCon)

- Translation based embedding models's transductive nature
  - Embedding based models can't scale to evolving KGs



# Architecture(PathCon)

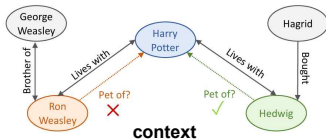
- Considering context and path for link prediction

- Entity type(inferred from surrounding relations) = **Context**

- Relational paths between target nodes = **Path**

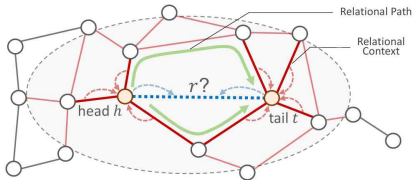


Link prediction model  
**PathCon**



## ■ Preview of PathCon

- Context obtained by **relational message passing**, detect target entity's **TYPE**
- Paths detect target nodes **relative positions**



## Problem formulation

link probability distribution  $\longrightarrow p(r|h, t) \propto \underbrace{p(h, t|r)} \cdot p(r)$

$\underbrace{p(h, t|r)} = \frac{1}{2} \left( \underbrace{p(h|r)} \cdot \underbrace{p(t|h, r)} + \underbrace{p(t|r)} \cdot \underbrace{p(h|t, r)} \right)$

$p(C(h)|r) \quad p(C(t)|r)$   
subgraph of entity = **context**

how  $t(h)$  can be reached from  $h(t)$  = **path**

regularization term

The diagram illustrates the problem formulation for the PathCon architecture. It starts with the link probability distribution  $p(r|h, t)$ , which is proportional to the product of the joint probability  $p(h, t|r)$  and the regularization term  $p(r)$ . The joint probability  $p(h, t|r)$  is then decomposed into two terms:  $p(h|r) \cdot p(t|h, r)$  and  $p(t|r) \cdot p(h|t, r)$ . The first term,  $p(h|r)$ , is associated with the context  $p(C(h)|r)$ , which is the subgraph of entity  $h$ . The second term,  $p(t|h, r)$ , is associated with the path  $p(C(t)|r)$ , which represents how  $t(h)$  can be reached from  $h(t)$ . The regularization term  $p(r)$  is also shown, with a dashed arrow indicating its role in the overall formulation.

# Architecture(PathCon)

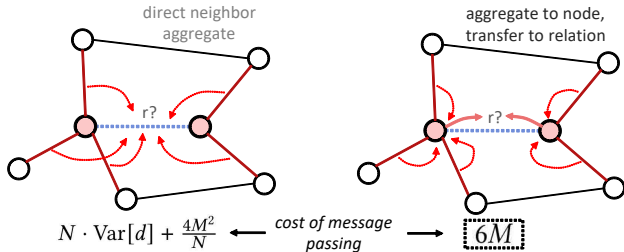
- Relational message passing(context)

$N$  : #nodes

$M$  : #edges

$\text{Var}[d]$  : variance of node degree

- Message aggregation between neighbor relations for entity context



- Relational message passing(context)

- Overview of relational message passing for relational context

$$m_v^i = A_1 \left( \{s_e^i\}_{e \in N(v)} \right), \quad // \text{node aggregate}$$

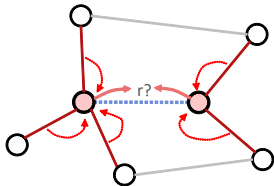
$$m_e^i = A_2 \left( m_v^i, m_u^i \right), \quad v, u \in N(e), \quad // \text{aggregate to edge}$$

$$s_e^{i+1} = U \left( s_e^i, m_e^i \right). \quad // \text{update edge state}$$

---

$$m_v^i = \sum_{e \in N(v)} s_e^i, \quad // A_1, A_2$$

$$s_e^{i+1} = \sigma \left( [m_v^i, m_u^i, s_e^i] \cdot W^i + b^i \right), \quad v, u \in N(e), \quad // U$$





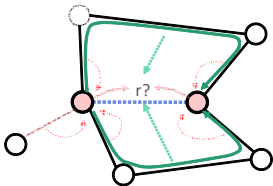
# Architecture(PathCon)

- Relational paths(**path**)

- Represents relative position between h and t
- Specify embeddings for all possible path combination

$|R|^k, k \text{ hop paths}$  ← isn't this too much?

“only 3.2% of all possible paths of length 2 occur in the FB15K dataset”



- Combining relational **context** and **path**

- Context score vector, path attention and path score vector(K iterations)

$$s_{(h,t)} = \sigma \left( \left[ m_h^{K-1}, m_t^{K-1} \right] \cdot W^{K-1} + b^{K-1} \right) \quad \alpha_P = \frac{\exp \left( s_P^\top s_{(h,t)} \right)}{\sum_{P \in \mathcal{P}_{h \rightarrow t}} \exp \left( s_P^\top s_{(h,t)} \right)} \quad s_{h \rightarrow t} = \sum_{P \in \mathcal{P}_{h \rightarrow t}} \alpha_P s_P$$

- Optimization process

$$p(r|h, t) = \text{SOFTMAX} \left( s_{(h,t)} + s_{h \rightarrow t} \right)$$

$$\min \mathcal{L} = \sum_{(h,r,t) \in \mathcal{D}} J(p(r|h, t), r)$$

The output dimension must match the number of total relations in the KG

## ■ Datasets

- FB15k, FB15k-237, WN18, WN18RR, NELL995, DDB14(DDB14 proposed in this paper)

	FB15K	FB15K-237	WN18	WN18RR	NELL995	DDB14
#nodes	14,951	14,541	40,943	40,943	63,917	9,203
#relations	1,345	237	18	11	198	14
#training	483,142	272,115	141,442	86,835	137,465	36,561
#validation	50,000	17,535	5,000	3,034	5,000	4,000
#test	59,071	20,466	5,000	3,134	5,000	4,000
$\mathbb{E}[d]$	64.6	37.4	6.9	4.2	4.3	7.9
$\text{Var}[d]$	32,441.8	12,336.0	236.4	64.3	750.6	978.8

## ■ Metrics

- MRR, Hit@1, 3

## ■ Link prediction

Method	TransE	ComplEx	DisMult	RotatE	Simple	QuatE	PATHCON
#param.	3.7M	7.4M	3.7M	7.4M	7.4M	14.7M	0.06M

	FB15K			FB15K-237			WN18			WN18RR			NELL995			DDB14		
	MRR	Hit@1	Hit@3	MRR	Hit@1	Hit@3	MRR	Hit@1	Hit@3	MRR	Hit@1	Hit@3	MRR	Hit@1	Hit@3	MRR	Hit@1	Hit@3
TransE	0.962	0.940	0.982	0.966	0.946	0.984	0.971	0.955	0.984	0.784	0.669	0.870	<u>0.841</u>	<u>0.781</u>	<u>0.889</u>	<u>0.966</u>	<u>0.948</u>	0.980
ComplEx	0.901	0.844	0.952	0.924	0.879	0.970	<u>0.985</u>	<u>0.979</u>	<u>0.991</u>	0.840	0.777	0.880	0.703	0.625	0.765	0.953	0.931	0.968
DistMult	0.661	0.439	0.868	0.875	0.806	0.936	0.786	0.584	0.987	0.847	<u>0.787</u>	0.891	0.634	0.524	0.720	0.927	0.886	0.961
RotatE	0.979	0.967	0.986	0.970	0.951	0.980	0.984	<u>0.979</u>	0.986	0.799	0.735	0.823	0.729	0.691	0.756	0.953	0.934	0.964
Simple	<u>0.983</u>	<u>0.972</u>	<u>0.991</u>	0.971	0.955	0.987	0.972	<u>0.964</u>	0.976	0.730	0.659	0.755	0.716	0.671	0.748	0.924	0.892	0.948
QuatE	<u>0.983</u>	<u>0.972</u>	<u>0.991</u>	<u>0.974</u>	<u>0.958</u>	<u>0.988</u>	0.981	0.975	0.983	0.823	0.767	0.852	0.752	0.706	0.783	0.946	0.922	0.962
DRUM	0.945	0.945	0.978	0.959	0.905	0.958	0.969	0.956	0.980	<u>0.854</u>	0.778	<u>0.912</u>	0.715	0.640	0.740	0.958	0.930	<u>0.987</u>
CON	0.962 ± 0.000	0.934 ± 0.000	0.988 ± 0.000	0.978 ± 0.000	0.961 ± 0.001	<b>0.995</b> ± 0.000	0.960 ± 0.002	0.927 ± 0.005	0.992 ± 0.001	0.943 ± 0.002	0.894 ± 0.004	0.993 ± 0.003	0.875 ± 0.003	0.815 ± 0.004	0.928 ± 0.003	0.977 ± 0.000	0.961 ± 0.001	0.994 ± 0.001
PATH	0.937 ± 0.001	0.918 ± 0.001	0.951 ± 0.001	0.972 ± 0.001	0.957 ± 0.001	0.986 ± 0.001	0.981 ± 0.000	0.971 ± 0.005	0.989 ± 0.001	0.933 ± 0.000	0.897 ± 0.001	0.961 ± 0.001	0.737 ± 0.001	0.685 ± 0.002	0.764 ± 0.002	0.969 ± 0.000	0.948 ± 0.001	0.991 ± 0.000
PATHCON	<b>0.984</b> ± 0.001	<b>0.974</b> ± 0.002	<b>0.995</b> ± 0.001	<b>0.979</b> ± 0.000	<b>0.964</b> ± 0.001	0.994 ± 0.001	<b>0.993</b> ± 0.001	<b>0.988</b> ± 0.001	<b>0.998</b> ± 0.000	<b>0.974</b> ± 0.001	<b>0.954</b> ± 0.002	<b>0.994</b> ± 0.000	<b>0.896</b> ± 0.001	<b>0.844</b> ± 0.004	<b>0.941</b> ± 0.004	<b>0.980</b> ± 0.000	<b>0.966</b> ± 0.001	<b>0.995</b> ± 0.000

# Experiments(PathCon)

## Model variant study(context aggregator)

### Concat aggregator

$$s_e^{i+1} = \sigma \left( [m_v^i, m_u^i, s_e^i] \cdot W^i + b^i \right), v, u \in \mathcal{N}(e)$$

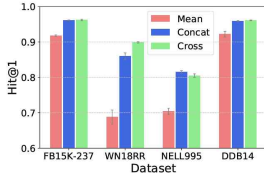
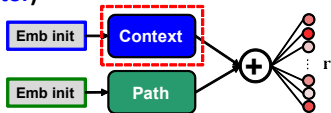
### Mean aggregator

$$s_e^{i+1} = \sigma \left( \frac{1}{3} (m_v^i + m_u^i + s_e^i) W + b \right), v, u \in \mathcal{N}(e)$$

### Cross context aggregator

$$m_v^i m_u^{i\top} = \begin{bmatrix} m_v^{i(1)} m_u^{i(1)} & \dots & m_v^{i(1)} m_u^{i(d)} \\ \dots & \dots & \dots \\ m_v^{i(d)} m_u^{i(1)} & \dots & m_v^{i(d)} m_u^{i(d)} \end{bmatrix}$$

$$s_e^{i+1} = \sigma \left( \text{flatten}(m_v^i m_u^{i\top}) W_1^i + s_e^i W_2^i + b^i \right), v, u \in \mathcal{N}(e)$$



# Experiments(PathCon)

## Model variant study(path representation, path aggregator)

- Independent random initialization
- Learning path representation via RNN

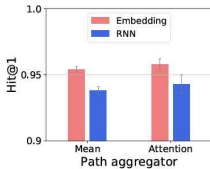
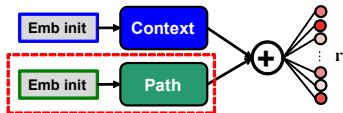
$$s_P = \text{RNN}(r_1, r_2, \dots)$$

- Attention aggregator

$$s_{h \rightarrow t} = \sum_{P \in \mathcal{P}_{h \rightarrow t}} \alpha_P s_P$$

- Mean aggregator

$$s_{h \rightarrow t} = \sum_{P \in \mathcal{P}_{h \rightarrow t}} s_P$$



# Experiments(PathCon)

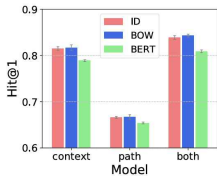
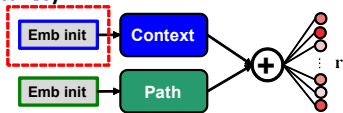
## Model variant study(initial edge features)

□ Identity(one-hot)

□ BOW(Bag Of Words)

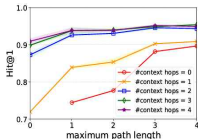
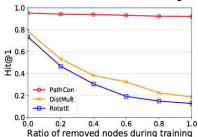
□ BERT(Bidirectional Encoder Representations from Transformers)

Input of BOW, BERT are individual relation's english name



# Experiments(PathCon)

## Other analysis



## relations of DDB14

0: belong(s) to the category of  
1: is a category subset of  
2: may cause  
3: is a subtype of  
4: is a risk factor for  
5: is associated with  
6: may contraindicate

7: interacts with  
8: belongs to the drug family of  
9: belongs to drug super-family  
10: is a vector for  
11: may be allelic with  
12: see also  
13: is an ingredient of

transformation matrix of path(▼) and context(►)

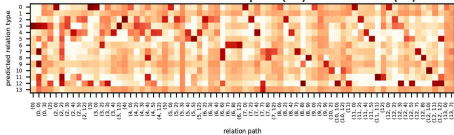


Figure 8: The learned correlation between all relational paths with length  $\leq 2$  and the predicted relations on DDB14.

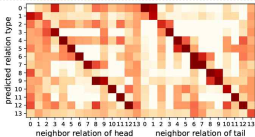


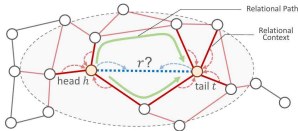
Figure 9: The learned correlation between the contextual relations of head/tail and the predicted relations on DDB14.



# Conclusion(PathCon)

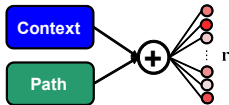
## ■ Message passing based KGC model

- Novel architecture of **relational message passing**
- **Entity-independent** inductive model
- Combined **context**(message passing) and **path** for link prediction



## ■ More stuff to discuss about

- Is it okay to neglect direction attributes of relations?
- Why did BERT perform worst in initial edge features?
- What happens if new paths are created by new entities?
- Need harder negative than random sampling(e.g.  $(h, r', t)$ ), such as using GAN
- Path dependent to context problem



*Thank You!*



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