#### Introduction to Algorithms, Fall, 2023 Programming Homework 6

# Problem B Shortest Paths with Negative Weights

Time limit: 1 second

Memory limit: 2048 megabytes

#### **Problem Description**

You are given a directed graph with n vertices and m directed edges, where the vertices are numbered from 1 to n. Each edge in the graph is associated with a weight  $w_i$ .

Your objective is to compute the total sum of the shortest path lengths between all pairs of vertices such that the second vertex is reachable from the first one. To clarify, let dist(u, v) represent the shortest distance between vertices labeled u and v if v is reachable from u, and dist(u, v) = 0 otherwise. Your program needs to output the sum of these distances computed over all vertex pairs:  $\sum_{i=1}^{n} \sum_{j=1}^{n} dist(u, v)$ . Your program also has to detect negative-weight cycles if there is any.

#### **Input Format**

The first line of the input contains two integers n and m. Each of the following m lines contains three integers  $u_i$ ,  $v_i$  and  $w_i$ , where the i-th line denotes that there is a directed edge from vertex  $u_i$  to  $v_i$  in the graph.

### **Output Format**

Output the sum  $\sum_{i=1}^{n} \sum_{j=1}^{n} dist(u, v)$  in one line. If there is at least one negative-weight cycle uin the graph, print Negative-weight cycle found.

# **Technical Specification**

- $1 \le n \le 3000$
- $0 \le m \le 3000$
- $1 \le u_i, v_i \le n$  and  $u_i \ne v_i$  for  $i = 1, 2, \dots, m$
- $-10^8 \le w_i \le 10^8 \text{ for } i = 1, 2, \dots, m$

#### Scoring

- 1. (40 points)  $w_i > 0$  for i = 1, 2, ..., m.
- 2. (40 points)  $n \le 300$ .
- 3. (20 points) No additional constraints.

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#### Sample Output 1

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# Sample Input 2

```
3 3
1 2 -1
2 3 -2
3 1 -3
```

# Sample Output 2

Negative-weight cycle found

# Sample Input 3

3000 0

# Sample Output 3

0

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# Sample Input 4

5	6														
1	3	-4	4												
3	5	-6	6												
2	4	-1	1												
4	5	-2	2												
4	5	-3	3												
1	2	-2	2												

# Sample Output 4

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