Problem B Dynamic Graph Queries

Time limit: 1 second

Memory limit: 2048 megabytes

Problem Description

You are given a graph of n vertices, where the vertices are numbered from 1 to n. Each vertex has a color of black or white. There are no edges between the vertices initially.

q queries are given. Each query belongs to one of the following three types:

- 1. 1 $u_i v_i$ —Add an **undirected** edge between vertex u_i and v_i .
- 2. 2 u_i —Find the number of black verticies in the same connected component as u_i .
- 3. $3 u_i$ —Find the nearest distance of a black vertex from vertex u_i . The distance between two vertices is the smallest number of edges in a path between two vertices. If there are no black vertices reachable from vertex u_i , output -1. Note that the number of this type of query is limited to 100 in this problem.

Can you answer all these queries?

Input Format

The first line of the input contains two integers n and q. The second line of the input contains n space-separated integers a_1, a_2, \ldots, a_n . The i-th vertex is black if $a_i = 1$, otherwise it is white. The i-th of the following q lines contains the i-th query in the format as in the problem description.

Output Format

For each query of type 2 and 3, output the answer to the query in one line.

Technical Specification

- $1 \le n, q \le 2 \times 10^5$
- $0 \le a_i \le 1 \text{ for } i = 1, 2, \dots, n$
- $1 \le u_i < v_i \le n$ for $i = 1, 2, \dots, q$ of query type 1
- $1 \le u_i \le n$ for i = 1, 2, ..., q of query type 2 and 3
- It is guaranteed that the number of queries of type 3 is at most 100. Note that there is no limitation on query of type 2.
- It is guaranteed that there is at least one query of type 2 or 3 in the input.

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Scoring

- 1. (40 points) Only queries of type 1 and 2 appear in the input.
- 2. (40 points) Only queries of type 1 and 3 appear in the input.
- 3. (20 points) No additional constraints.

Sample Input 1

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      5
      8

      1
      0
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      2
      4
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      1
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Sample Output 1

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-1
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```

Sample Input 2

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      5
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Sample Output 2



Sample Input 3

```
      5
      7

      0
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      1

      1
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```

Sample Output 3

-1		
0		
1		
0		
0		

Hint

Use a disjoint set data structure to handle queries of type 2. You also need to run BFS to handle queries of type 3.