

MH1200 Quiz 2

September 15, 2016

Problem 1. Let

$$A = \begin{bmatrix} 1 & 1 & 1 \\ 0 & 1 & 3 \\ 0 & 2 & 4 \end{bmatrix}.$$

Give an elementary matrix E such that EA is upper triangular.

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & -2 & 1 \end{bmatrix}$$

Problem 2. Determine the values of b for which the system of linear equations

$$\begin{bmatrix} 1 & 1 & 1 \\ 1 & 3 & 5 \\ 2 & 0 & -2 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} 1 \\ b \\ 2 \end{bmatrix}$$

has a solution.

$$\begin{array}{cccc} 1 & 1 & 1 & 1 \\ 0 & 2 & 4 & b-1 \\ 0 & -2 & -4 & 0 \end{array} \rightarrow \begin{array}{cccc} 1 & 1 & 1 & 1 \\ 0 & 2 & 4 & b-1 \\ 0 & 0 & 0 & b-1 \end{array}$$

The system will have infinitely many solutions if b is equal to 1