**Longitudinal data, trajectories and telemonitoring: how to analyze them?**

**Example of sleep data**

**Title for CHEST (50 characters): How to analyze longitudinal data? Sleep modeling**

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**Abbreviations**

ANOVA, analysis of variance; ARIMA, autoregression integrated moving average; CPAP, continuous positive airway pressure; ESS, Epworth sleepiness scale; GBTM, group-based trajectory modelling; GMM, growth mixture modelling; LCA, latent class analysis; LTA, latent transition analysis

**Keywords**

Longitudinal data; statistical approaches; description; classification; modeling; forecasting

# Abstract (word count)

Background

Aims

Methods

Results

Conclusion

# Introduction

Traditionally, data is measured at a specific point in time, making it impossible to analyze changes and evolutions over time1. One approach to overcoming this limitation is to repeatedly measure the same variable of interest in a consistent population over a given period. This repeated measurement data is known as longitudinal data. In models with longitudinal data, individuals are affected by a treatment or other risk factors over a number of time points separated by specific intervals.

Similarly, with longitudinal data, the study of trajectories is emerging2. Numerous positioning technologies and remote sensors enable the analysis of a vast data set, namely trajectory data. Thanks to this, patient monitoring and predictive analytics are progressively more efficient.

Another category of longitudinal data is the time series, which consist of a sequence of numerical values representing the evolution of a specific quantity over time. These developments of random variables can be analyzed to study their past evolution and future behavior.

However, working with longitudinal data presents some challenges, such as missing or extreme values, correlations between repeated measurements and variations in measurement intervals1. The quality and quantity of data over time could influence the accuracy and the reliability of the statistical model used to analyze these data. Moreover, an inadequate choice of statistical method could add bias in parameter estimates and outcome predictions1.

Consequently, advanced models and methods have been developed, resulting in a need for a guide in selecting and applying statistical techniques for longitudinal data analysis.

# What is the source of the data?

The type of data may depend on the data source, and may have an impact on the choice of statistical method. Data can be broadly classified into numerical and categorical types (Figure 1). Numerical data can further be divided into discrete data – representing distinct and separate values, such as the number of hospitalization or of arousals per night - and continuous data, which consist of ordered measurements with equal intervals. Continuous data can be categorized into ratio and interval data. Ratio data have a true zero, allowing for operations such as addition, subtraction, multiplication, and division (e.g. height, weight, or blood pressure measurements). In contrast, interval data lack a true zero, meaning that multiplication and division are not meaningful (e.g., temperature).

The method of data collection impacts both data type and data quality (Figure 2). Consequently, variations in data quality and quantity require different statistical approaches. For example:

* Medical records (history or follow-up visits) can provide ordinal, nominal, continuous and discrete data with a good quality and quantity.
* Case Report Form (CRF) or self-administered questionnaires provide ordinal, nominal, discrete and continuous data but their quality and quantity are moderate, often affected by missing data or reporting errors. Moreover, data collected through specific questions may limit the scope of the analysis.
* Interviews generate similar data types with high quality but moderate quantity, as responses are mandatory and the data volume depends on the time of interview.
* Connected devices primarily collect continuous or discrete data with high quality, though the quantity tends to decline over time due to user compliance issues or device limitations.

Careful consideration of the study’s context, including its objectives, population included, data type and source, and research questions enhances model selection and ensures robust and meaningful analysis.

# Which statistical method to use?

Selecting the appropriate statistical method requires consideration of several key questions:

*What is the purpose of the study and what are its objectives?*

Depending on the research question, the statistical method may differ (Figure 3). The methods also vary in complexity (Figure 4), ranging from relatively simple descriptive analyses to more advanced modeling and forecasting approaches.

Descriptive methods, such as ANOVA or χ², were among the simplest statistical models. They are mostly used to analyze repeated measurements, particularly categorical variables derived from medical records, questionnaires or interviews. Then, the classifications methods, such as LCA on repeated measurements, K-means clustering and LTA for longitudinal data were less complex. Finally, methods used for modeling or forecasting were the most complex statistical approaches, such as GMM, mixed or GBTM methods using longitudinal data; ARIMA and Cross-correlation methods for time series or Joint and Hidden Markov models with mixed data.

In terms of data type and data source, longitudinal data methods incorporate both categorical and numerical data, derived from medical records, questionnaires, connected device or interviews. Time series methods mostly rely on numerical data from medical records or connected device. Mixed data approaches handle both continuous and categorical variables, allowing for diverse data sources.

*Is the chosen statistical method correct?*

Once the type and source of data, as well as the study objectives are clearly defined, it is necessary to verify that the selected statistical method is appropriate. Before conducting the analysis, the goal, advantages and limitations of the chosen method should be carefully assessed to ensure its suitability. To illustrate the application of different statistical methods, an example of sleep data analysis was carried out. A dataset was simulated using R, consisting of 50 patients with 1000 time points, representing CPAP adherence and ESS score. The CPAP adherence followed a normal distribution (with negative values replaced by 0; μ = 4, σ = 1.5), while the ESS score was a discrete variable ranging from 0 to 24. For certain methods that only accept categorical variables, both variables were transformed into categorical data: non-adherent ([0h; 2h[) vs. almost adherent ([2h; 4h[) vs. adherent (≥4h) for CPAP adherence; with excessive sleepiness (≥10) vs. without (<10) for the ESS score.

First, descriptive methods were applied to compare the population characteristics, providing an initial overview of the data distribution and trends.

1. ANOVA model3

*Objective* - Assess whether there is a statistically significant interaction effect between 2 and 3 within-subjects factors in explaining a continuous outcome.

*Strengths* – Allows comparison between more than 2 groups.

*Limits* - If the null hypothesis is rejected, it indicates that at least one group differs, but does not specify which group(s), although some post hoc tests are available to counter this limitation; assumes normal distribution, metric scale and equal variance across groups; susceptible to outliers, which can affect the model’s reliability.

*Example* – ANOVA was used to analyze continuous data on CPAP adherence over time, including all time points and all patients. The p-value was 0.09, indicating no statistically significant difference in CPAP adherence across time.

1. χ² method

*Objective* - Evaluate independence and assess differences between variables across a series of contingency tables; assess whether the proportions of the binary variable vary over time.

*Advantages* - Different models are available based on the number of measurements, as Mc Nemar’s test for 2 measurements or Mantel-Haenszel for more than 2 measurements; simple and computationally efficient model.

*Limits* - All theoretical numbers must be greater than 5; assumes that all individuals transition between states (no dropouts); the sample must be random; does not account for covariates.

*Example* - The χ² Mantel-Haenszel method was applied, assuming that 2 nominal variables are conditionally independent in each stratum and that there is no 3-way interaction. This analysis included 4 time points and all patients, using a contingency table where CPAP adherence and ESS score were treated as categorical variables. The p-value of the χ² test was 0.16, suggesting no significant difference between groups.

Secondly, classification methods were used to cluster patients and summarize key information. Various clustering approaches employed different distance metrics including Euclidean4, Manhattan4, Cosine4, Correlation-based4 or dynamic time warping5–7 distances.

1. LCA method8–14

*Objective* - Identify unobserved (latent) clusters sharing common characteristics.

*Advantages* - Powerful tool for analyzing relationships between categorical variables, exploring and interpreting complex contingency tables and testing hypotheses on the structures of categorical latent variables; low classification error rate and a robust model; supports mixed data types, allowing for variables with different measurements scales; if continuous variables are involved, Latent Profile Analysis can be applied.

*Limits* – Computationally intensive, limiting the number of variables based on available computing power; sensitive to outliers; the percentage of individuals in each cluster is unknown; requires making several a priori decisions, such as the number of clusters.

*Example* – LCA was performed using CPAP adherence as a categorical variable across 5 time points. The optimal number of clusters was determined to be 2, based on the smallest AIC and BIC (see Supplementary Material (SM)). At the first time point, patients classified as almost adherent were more likely to belong to the Cluster 1, while adherent patients had a higher probability of belonging to the Cluster 2 (Figure 5). At the 2nd time point, Cluster 1 was mainly composed of adherent patients, while Cluster 2 included both almost adherent and adherent patients in similar proportions. At the 3rd, 4th and 5th time points, Cluster 1 had a greater probability of including adherent patients while the Cluster 2 was more likely to include almost adherent and, to a lesser extent, adherent patients (see table in SM).

1. K-means method9,15–17

*Objective* - To group patients’ trajectories into clusters based on their similarities.

*Advantages* - No need for a priori assumptions and avoids the problems associated with model selection; ability to analyze a large data set; can group trajectories that do not follow a polynomial trajectory.

*Limits* - Complete data are required; if missing data are observed and these patients are to remain included, imputations must be performed before statistical analysis, or the chosen method must take data imputations into account; correlation between individuals is not taken into account; tests to find the initial parameters and the optimal number of clusters must be performed; no way of knowing whether it's a global maximum or one of the local maxima when the algorithm converges to the maximum; assessed the longitudinal trajectory of only one variable; the algorithm agglomerates trajectories with a similar overall shape, but if 2 trajectories are transferred in time, they could be in 2 distinct clusters; no tests to check the algorithm's goodness of fit.

*Example* - For this analysis, numerical CPAP adherence was used including all patients and 5 time points. Parameters of the model were detailed in SM. According to the Calinski-Harabatz score, the model with 2 clusters was the best model. Moreover, there was a pretty equal number of individuals in each cluster: 66% in the 1st cluster and 34% in the second cluster (Figure 6). The first cluster was fairly stable around 4h while the 2nd cluster increased after the 3rd time point from around 4h to around 5h30.

1. LTA model9,13,18

*Objective* - Study the probability of transition from one cluster at one time to another at the next.

*Advantages* - Model changes over time and identifies predictors of that change; compare different clusters to determine their characteristics and assess the contribution of different measures for each latent cluster.

*Limits* - Need for a large data set as the model has to estimate many parameters and generally uses the burn-in process; a large number of time points (>6) increase the complexity of the model; problems in defining the optimal number of latent clusters and assigning them a label; problems in including covariates.

*Example* - LTA model ~~implemented discrete or categorical outcome, so~~ categorical CPAP adherence was used. All patients were included with 500 time points. Parameters and validation of the model were described in SM. According to the Loglikelihood and the BIC or AIC criteria, the best model created 2 clusters. The conditional response probabilities to belong to the 2nd cluster, were 0.22 for the CPAP adherence [0h; 2h[, 0.59 for the [2h; 4h[ group and 0.19 for the ≥4h group (Figure 9). To the 1st cluster, the conditional response probabilities were, respectively 0.03, 0.33, 0.63 (table in SM). The transition probability was 0.29 from the 1st cluster to the 2nd cluster, 0.67 from the 2nd cluster to the 1st cluster and 0.33 to stay in the 2nd cluster, 0.71 to stay in the 1st cluster.

Thirdly, modeling and forecasting methods were used to compare and study data trajectories, and to simulate the next trajectory.

1. GBTM model13,19,20

*Objective* - Analyze cluster trajectories to study and forecast variations over time.

*Advantages* - Simpler than the GMM method, as there are fewer parameters to estimate; faster, with fewer errors; ability to handle missing data and correlated residuals; easier to interpret, especially visually, as less complex.

*Limits* - Missing data must be Missing Completely At Random; clusters must be qualitatively different from the dependent variable; dependent and independent variables must have no direct relationship; strong assumptions on trajectory distributions must be respected; possibility of overestimating the number of clusters and the number of trajectories when individual trajectories have the same profile and are distributed on a continuum around the mean trajectory; no intra-class variation.

*Example* - Continuous CPAP adherence was used including 5 time points and all patients. First, we performed GBTM method with different curve and number of clusters to find the best model (detailed in SM). According to some criteria (BIC, loglikelihood, Average Posterior Probability and Proportion of assignment parameters), the model with 2 clusters was the best model. The first cluster had a decreased CPAP adherence unlike the second cluster (Figure 8).

1. Mixed model19,21–23

*Objective* - Estimate the relationship between the dependent variables and the fixed and random effects of the independent variables.

*Advantages* - Ability to simultaneously analyze 2, 3 or more dependent variables; ability to deal with missing values; estimation of the odd ratios and the rate ratios.

*Limits* - Interpretation of coefficients possible if random effects are controlled by the analyst; even if differences are statistically significant between estimated trajectories of the dependent variable, these may be non-different in terms of clinical relevance; unobserved variables are assumed to be Missing At Random (MAR).

*Example* - ~~Any type of variable was accepted~~ but for this example, continuous outcome was used while time and baseline ESS score were categorical variables. All patients and all time points were included. A random intercept on patient was added.

Validation of the model and results were detailed in SM. According to the results, CPAP adherence were negatively associated with some time points and ESS baseline was not significantly associated with CPAP adherence.

1. GMM model9,13,17,24–27

*Objective* - Identify trajectory patterns and describe longitudinal changes for each unobserved group identified.

*Advantages* - Deal with missing data and correlated residuals; identify differences between and within individuals over time; trajectory may change qualitatively over time according to different groups.

*Limits* - Many parameters are estimated; complexity of interpreting results; some parameters need to be defined a priori; possibility of identifying false clusters.

*Example* – All patients were included with 5 time points. There is a random intercept and slope and a mixture parameter on the time variable.

According to the BIC criteria, the model with 2 clusters was the best model (detailed in SM). Moreover, the distribution of patients in the clusters was fairly equally distributed (detailed in SM). The first cluster overall tended to decrease over time while the second cluster overall tended to increase over the 5 time points (Figure 7).

1. ARIMA model & Cross-correlation method28–35

*Objective* - Analyze time series and evaluate the correlation between two time series varying over time, coinciding or not over time intervals.

*Advantages* - Assumption of local stationarity only; robust results even if non-linear trends are mixed in the data or if the time scale is different between time series; ability to define correlations when multiple signals are linked, when the system is complex.

*Limits* - Multiple signals must have linear relationships; better with at least 100 observations.

*Example* - First, the ARIMA model used numerical outcome for time series. We compared the CPAP adherence and the ESS score, transformed into time series. All time points were used but only one patient was included. We can repeat the model for each patient. The frequency used was 7, for week scale. To validate the time series, autocorrelation, partial autocorrelation, QQpLot and Box-Ljung test were studied (in SM). For CPAP adherence, the final model was ARIMA(0, 0, 0) while for ESS score, it was ARIMA(1, 1, 0)(1, 0, 0).

Then, a cross-correlation function was performed to compare the correlation between these two time series (the variables detrend by the ARIMA model).

There was no correlation between ESS score and CPAP adherence with or without lag according to scatterplots (Figure 10); except for the 11th time points (seen on the ACF plot). Interestingly, this meant that an above value of CPAP is likely to lead to an above value of ESS score, about 11 time points later.

These lags could be implemented to a regression to study the association of the ESS score and the CPAP adherence at different lags (in SM).

1. Joint model21,36

*Objective* - Account for the joint behavior of the evolution of a quantitative longitudinal marker and the time of occurrence of an event considering their joint density.

*Advantages* - The estimated regression coefficients are unbiased; the association between two outcomes can be estimated; additional random effects can be added; the functional form of the time effect can be generalized using fractional polynomials or splines; patients lost to follow-up can be added to the survival model.

*Limits* - For some Monte-Carlo methods (e.g. Quasi Monte-Carlo), MC error estimation is not possible.

*Example* - One covariate was added to the linear mixed-effect model, the sex of the patient. This variable was a categorical random sample between Male and Female values. The joint model was separated into three steps: 1) the linear mixed-effect model, 2) the Cox model and 3) the joint model. All patients and 7 time points were included in these analyses.

First, the mixed model was performed using continuous CPAP adherence and a random intercept and slope on patient. Parameters of the model were detailed in SM.

No variable was significant.

Next, the Cox model was run using the categorical ESS score (ESS score < 10 corresponded to the value of death and ESS score ≥ 10 corresponded to the value of life). The sex variable was added as a covariate and the model was clustered by patient.

Validation of the model and results were detailed in SM. However, according to the results, the sex did not significantly influence the survival curve (p-value = 0.64 > 0.05).

Finally, the joint model did not highlight significant result. The verification of the model showed not good observations for the CPAP adherence but good observations for the other parameters (in SM).

For example, the prediction of the cumulative risk for the patient 49 increased (risk to have ESS score < 10) from the 4th time points (cumulative risk around 0.00) to the 5th time points (cumulative risk around 0.58) (Figure 9).

1. Hidden Markov model37–43

*Objective* - Assess changes in individual characteristics when these are not directly observable.

*Advantages* - For Bayesian estimates, the model has a very flexible and robust approach; the model is more appropriate for small samples; Bayesian multiple imputation can handle missing data (MAR) without loss of information or introduction of bias; possibility of obtaining the latent clusters of the final model (LMM); efficient algorithms; possible predictions.

*Limits* - The number of classes must be well chosen, as the model could be overestimated or fail to find occasional clusters ; no criteria or model selection to choose the optimal number of latent clusters ; the estimation process cannot be generalized for non-homogeneous transitions ; the number of hidden states must be sufficiently small and/or the covariates must have small dimension for the model to function properly; Bayesian estimation assumes that the distribution of model parameters must be known a priori; label change imposes an order restriction on the parameters for the different states; the status lost of follow-up cannot be exchanged with other states.

*Example* - This method needed one known categorical variable, e.g. in our analysis, CPAP adherence with 3 states and one hidden categorical variable with a known number of hidden states, e.g. 2 states: Adherent vs. Non-adherent. All time points but only one patient was included. We can repeat the model for each patient. Parameters and results were detailed in SM. The initial state probabilities model was 1.0 for the 2nd state. The transition probability matrix was around 0.5 for the initial state of non-adherence to the two arrived states, around 0.6 for the state of adherence to the non-adherent group and 0.4 for remaining in the adherent state (Table 1). The states prediction included 59.1% of time points in the 1st state and 40.9% in the 2nd state (detail in SM).

# Summary and perspectives

Selecting the best statistical method for analyzing longitudinal data requires careful consideration of data type, data source and study objectives. Statistical methods vary in complexity, depending on the data characteristics and the study design. Before conducting an analysis, it is essential to evaluate the strengths and limitations of each method to ensure its suitability. Some methods are more suitable for comparisons (e.g., ANOVA, χ² tests), classification (e.g., LCA, K-means clustering, LTA), or modeling and forecasting (e.g., GBTM, mixed models, GMM, ARIMA, cross-correlation, joint models, and Hidden Markov Models).

This study did not consider all possible data limitations, yet proper data description and verification remain crucial first steps in longitudinal data analysis. Outliers and missing values are common in such datasets, and specific techniques exist for their imputation or removal44. Another limitation of the study is its focus on the most commonly used statistical methods. Many other techniques can be used for classification (e.g., Configural Frequency Analysis9, Latent growth Curve Model19, hierarchical methods45–47, such as Principal Component Analysis, Multiple Correspondence Analysis, Hierarchical Ascending Classification, as well as partitioning methods45–47 like X-means, DBSCAN, and K-medoids) or for modeling and forecasting (e.g.,BKMR48). There are more complex methods that can be applied to predict data trajectories, but were outside the scope of this study.

This work is not an exhaustive review of statistical methods, but provides a detailed overview of methods commonly used in the literature (illustrated with implementation examples in R and Python). A comprehensive, step-by-step approach for analyzing longitudinal data is proposed.

Longitudinal data are particularly relevant in healthcare studies, where they are often collected through follow-up visits, hospitalizations and, more recently, through connected devices (e.g., CPAP treatment for sleep apnea). However, the methodological framework outlined in this study is broadly applicable to other domains, including climat31,35, finance49 or insurance50,51.

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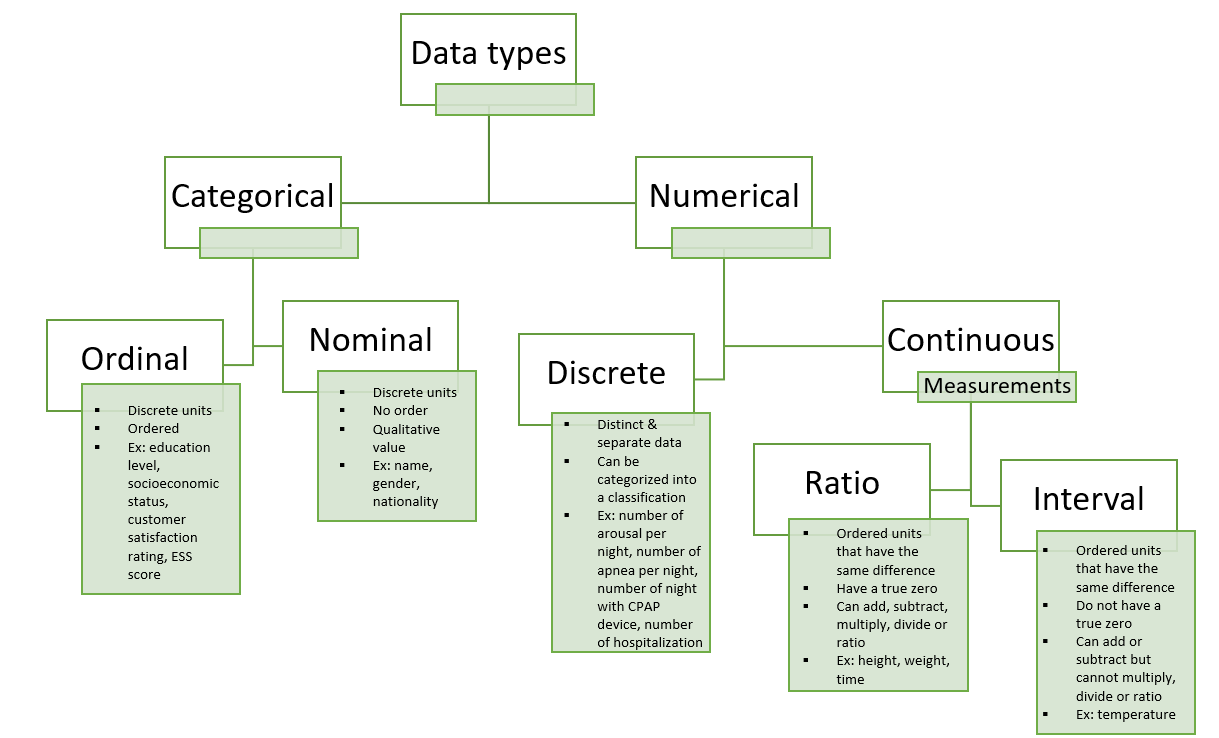
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# Tables

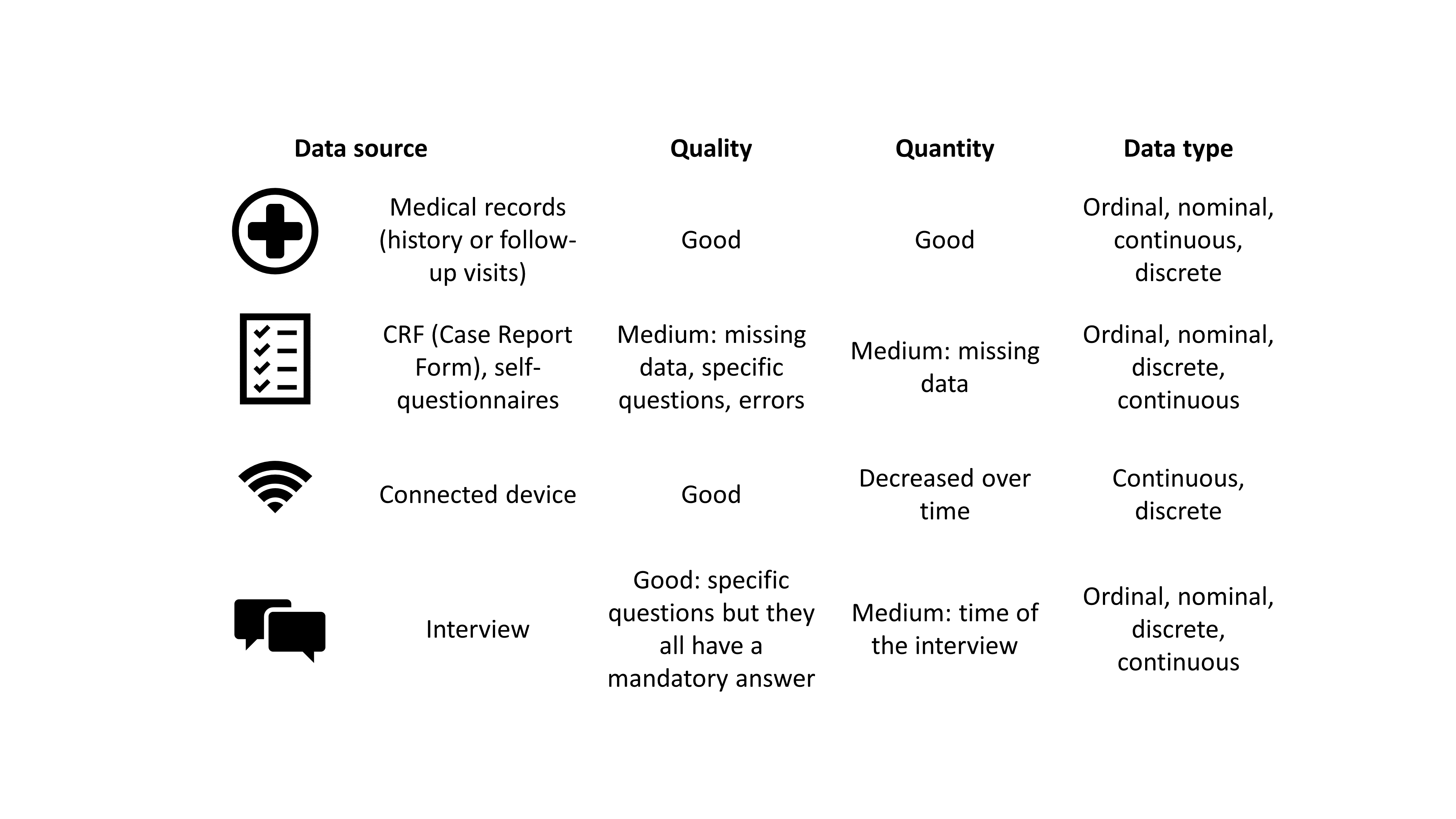
**Table 1: Matrix of transition probability from number of hours to CPAP use to hidden state of CPAP adherence using Hidden Markov model.**

|  |  |  |
| --- | --- | --- |
|  | **Non-adherent** | **Adherent** |
| **Non-adherent** | 0.53 | 0.47 |
| **Adherent** | 0.56 | 0.44 |

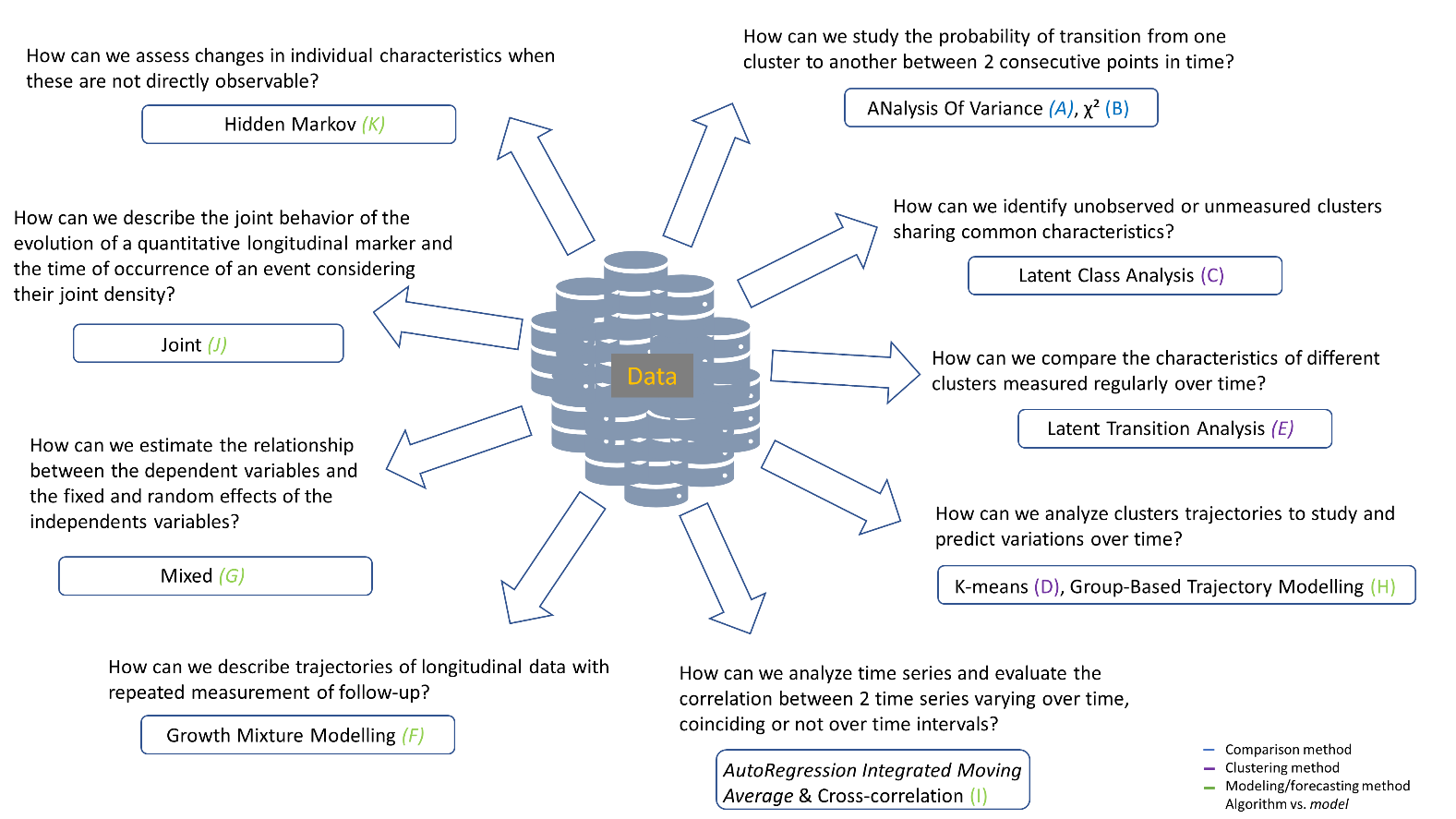
# Figures legend

**Figure 1: Data types**. *CPAP, continuous positive airway pressure; ESS, Epworth sleepiness scale*

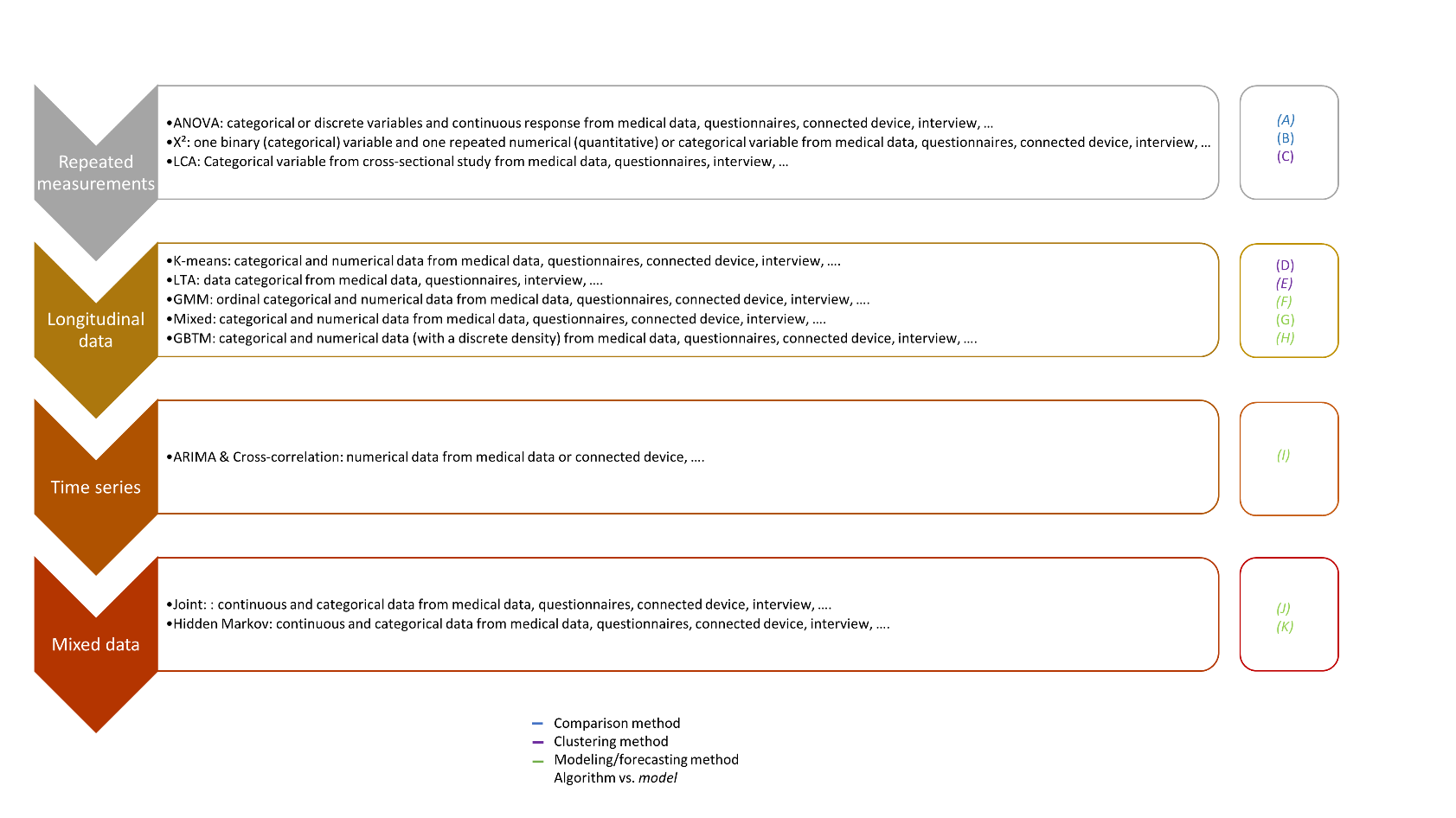
**Figure 2: Data sources**.



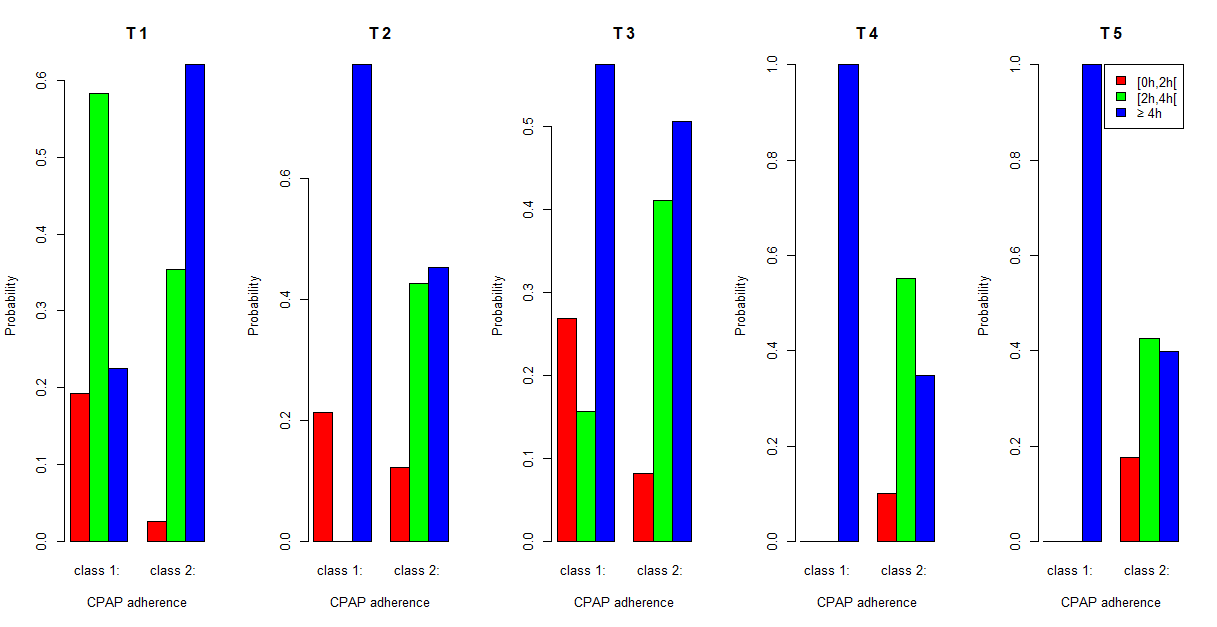
**Figure 3: Statistical methods according to objectives and question of the study**.



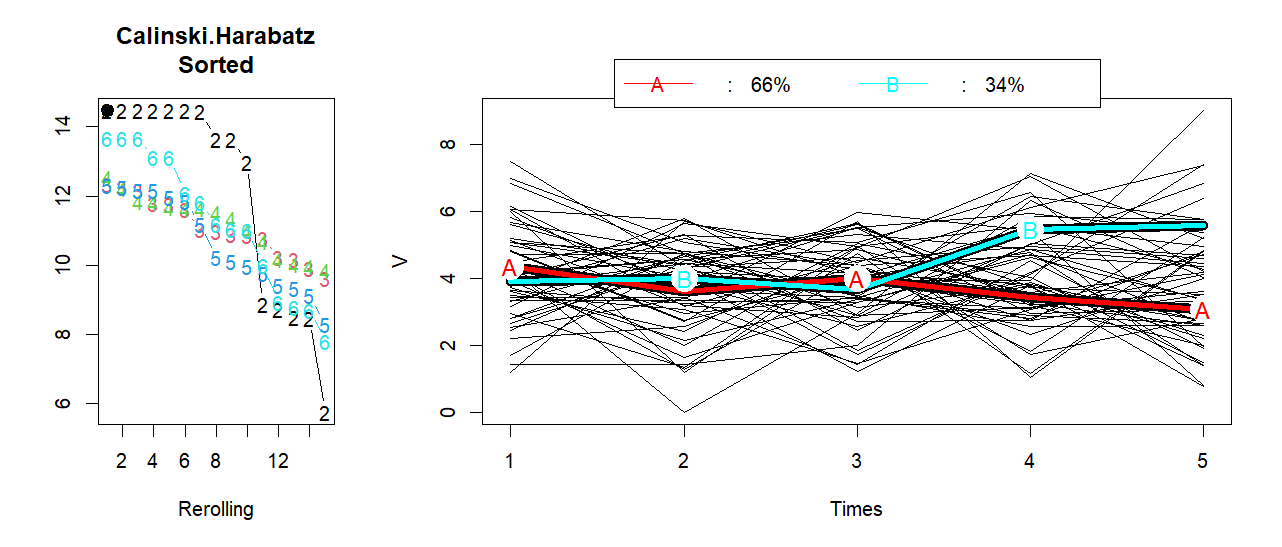
**Figure 4: Statistical methods classified according to complexity, data format and objectives**. *ANOVA, analysis of variance; ARIMA, autoregression integrated moving average; DTW, dynamic time warping; GBTM, group-based trajectory modelling; GMM, growth mixture modelling; LCA, latent class analysis; LTA, latent transition analysis.*



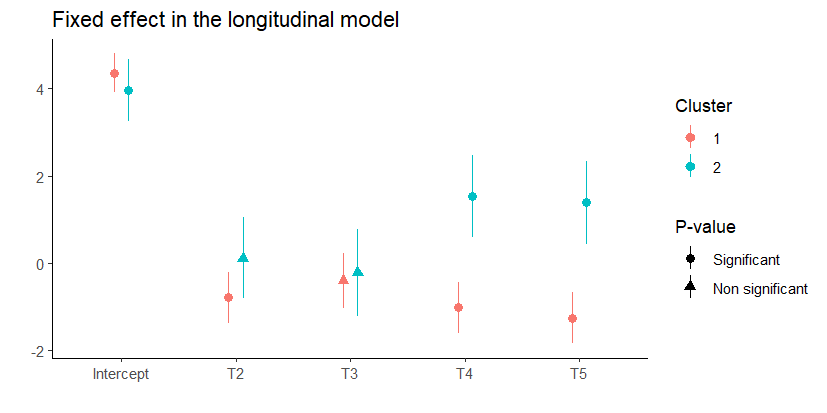
**Figure 5: Probability to belong to clusters using LCA method**. *CPAP, continuous positive airway* *pressure*



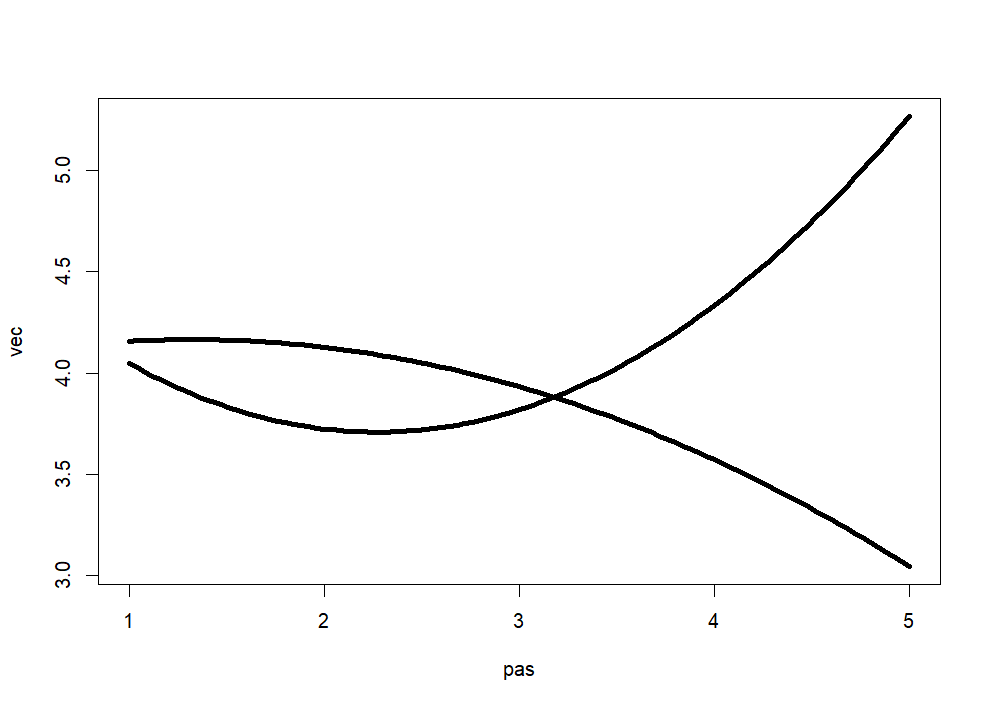
**Figure 6: Trajectories of clusters using K-means.**



**Figure 7: Trajectories of the clusters over 5 time points using GMM model.**



**Figure 8: Trajectories of the two clusters using GBTM model.**



**Figure 9: Prediction of the cumulative risk of sleepiness according to CPAP adherence for one patient, using joint model.**

