

Computer Vision on the D-Wave 2000Q

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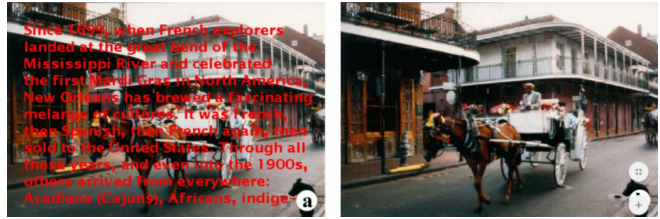
If you get robbed and the only way to get your wallet or purse back is for police to determine the identity of the thief based on a blurry surveillance video of a moving suspect, you might wish that a computer can “calculate” a sharp and clear version of the required image which shows clearly who it is that has your money. This is more complicated than the simple face-recognition algorithms used by Facebook for automatic tagging, or by Google for image search, because it involves first predicting what the unblurry version of an image should look like, and may involve video footage rather than simply stationary photographs.

The state-of-the-art method for solving this problem in industry is by solving a QUBO problem, and some examples from the classical-computer QUBO literature are below:

QUBO based in-painting by from Ref. [1].



QUBO based in-painting by from Ref. [1].



QUBO based de-blurring from Ref. [2].



QUBO based de-noising from Ref. [3].



Therefore this is a real-world problem that is “perfect” for the D-Wave machines, because the industry standard for solving the problem is to run a QUBO optimization on a classical computer. Image de-noising is performed by detectives for recovering partial finger-prints, by museums for reconstructing antique paintings, and by doctors for medical imaging, but in these cases the number of pixels (and hence the number of binary variables in the QUBO problem) is small. For terabyte-sized telescope images of galaxies, inter-stellar media, and possible life-containing exo-planets, runtimes are colossal and we welcome any speed-up even if only by a constant factor of 10 or even 2.

The algorithm works by minimizing two functions of binary variables simultaneously:

$$f_C(X_C) = \sum_{i=1}^K \alpha_i \log(1 + \frac{1}{2}(J_i \cdot X_C)^2) \quad (1)$$

$$f_v(X_v) = \frac{(N_v - X_v)^2}{2\sigma^2} \quad (2)$$

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$$29144x_6x_{11} - 3770x_6x_{13} - 1762x_6x_{18} - 32400x_6x_{19} - 20472x_6x_{20} - 4268x_6x_{26} - 4060x_6x_{28} - 9072x_6x_{29} + 45574x_7 + 1250x_7x_8 - 17192x_7x_{12} - 9702x_7x_{22} - 41416x_7x_{23} - 2760x_7x_{25} + 143330x_8 + 7026x_8x_9 - 17192x_8x_{12} - 3770x_8x_{13} - 9702x_8x_{22} - 41416x_8x_{23} - 7756x_8x_{24} - 4268x_8x_{26} - 816x_8x_{27} - 9072x_8x_{29} + 5396x_9 - 3770x_9x_{13} - 4268x_9x_{26} - 816x_9x_{27} - 4060x_9x_{28} + 35460x_{10} + 87432x_{11} + 25788x_{12} + 11310x_{13} + 2504x_{14} + 7288x_{15} + 13068x_{16} + 12018x_{17} + 1762x_{18} + 32400x_{19} + 20472x_{20} + 12064x_{21} + 9702x_{22} + 41416x_{23} + 15512x_{24} + 5520x_{25} + 4268x_{26} + 1632x_{27} + 4060x_{28} + 9072x_{29}$$

The embeddings obtained for the Chimera architecture are:

logical qubit 0 :	[339, 467, 595, 723, 851, 864, 973, 979, 981, 989, 992, 997, 1005, 1013]	chain length : 14
logical qubit 1 :	[590, 594, 598, 606, 614, 617, 622, 630, 638, 745]	chain length : 10
logical qubit 2 :	[251, 252, 379, 382, 507, 635, 636, 763, 891, 1019, 1021, 1147, 1148]	chain length : 13
logical qubit 3 :	[331, 332, 340, 344, 348, 354, 356, 364, 372, 380, 482, 610, 738, 866]	chain length : 14
logical qubit 4 :	[242, 370, 498, 626, 628, 754, 882, 1010, 1138]	chain length : 9
logical qubit 5 :	[346, 351, 359, 367, 375, 383, 474, 602, 605, 730, 858, 986]	chain length : 12
logical qubit 6 :	[243, 371, 499, 627, 755, 759, 767, 883, 1011, 1139]	chain length : 10
logical qubit 7 :	[578, 633, 706, 711, 761, 834, 838, 846, 854, 862, 870, 878, 886, 889, 894]	chain length : 15
logical qubit 8 :	[234, 237, 245, 253, 362, 490, 618, 620, 743, 746, 751, 874, 1002, 1130]	chain length : 14
logical qubit 9 :	[241, 369, 497, 621, 625, 629, 637, 753, 881, 1009, 1137]	chain length : 11
logical qubit 10 :	[459, 587, 715, 843, 844, 852, 860, 971, 1099, 1100, 1108, 1116, 1124, 1132, 1140]	chain length : 15
logical qubit 11 :	[232, 360, 488, 616, 744, 872, 876, 884, 892, 1000, 1128]	chain length : 11
logical qubit 12 :	[200, 204, 212, 217, 220, 228, 236, 244, 328, 456, 584, 589, 597, 712, 840]	chain length : 15
logical qubit 13 :	[448, 450, 452, 460, 466, 468, 476, 484, 492, 500, 508, 576, 704, 710]	chain length : 14
logical qubit 14 :	[219, 347, 350, 358, 366, 374, 475, 588, 596, 603, 604, 612, 731, 859]	chain length : 14
logical qubit 15 :	[336, 464, 592, 720, 848, 976, 982, 990, 998, 1006, 1014, 1022]	chain length : 12
logical qubit 16 :	[718, 726, 734, 742, 750, 752, 758, 766]	chain length : 8
logical qubit 17 :	[504, 632, 717, 725, 733, 741, 749, 757, 760, 765]	chain length : 10
logical qubit 18 :	[361, 462, 470, 478, 486, 489, 491, 494, 502, 510, 619, 747, 875, 1003]	chain length : 14
logical qubit 19 :	[352, 461, 469, 477, 480, 485, 493, 501, 505, 509, 608, 736]	chain length : 12
logical qubit 20 :	[378, 506, 634, 762, 845, 853, 861, 869, 873, 877, 885, 890, 893, 1001]	chain length : 14
logical qubit 21 :	[708, 716, 724, 732, 740, 748, 756, 764]	chain length : 8
logical qubit 22 :	[345, 473, 601, 729, 735, 857, 985, 988, 996, 1004, 1012, 1020]	chain length : 12
logical qubit 23 :	[472, 600, 728, 842, 847, 855, 856, 863, 871, 879, 887, 895]	chain length : 12
logical qubit 24 :	[337, 465, 593, 721, 849, 977, 983, 991, 999, 1007, 1015, 1023]	chain length : 12
logical qubit 25 :	[355, 463, 471, 479, 483, 487, 495, 503, 511, 611, 739, 867]	chain length : 12
logical qubit 26 :	[330, 333, 341, 349, 357, 365, 368, 373, 381, 458, 496, 586, 624, 714, 719]	chain length : 15
logical qubit 27 :	[457, 585, 591, 599, 607, 615, 623, 631, 639, 713, 841]	chain length : 11
logical qubit 28 :	[225, 353, 481, 609, 613, 737, 865, 868, 993, 1121, 1125, 1133, 1141, 1149]	chain length : 14

The embedded problem is:

((866, 870): 16326.0, (344, 350): -1822.0, (362, 367): 4238.0, (354, 358): -1822.0, (587, 590): -29144.0, (628, 636): 3694.0, (627, 628): 5439.0, (620, 628): 2243.0, (857, 862): -41416.0, (1009, 1013): -11820.0, (361, 367): -16200.0, (1011, 1012): -41416.0, (992, 998): -4356.0, (723, 726): -12018.0, (738, 742): -12018.0, (891, 893): -4021.333333333333, (602, 606): 27952.0, (882, 884): -17192.0, (626, 631): -4060.0, (634, 636): -4021.333333333333, (883, 884): -17192.0, (865, 870): -9072.0, (355, 359): -2134.0, (1010, 1014): -13068.0, (371, 372): -620.0, (490, 495): -2134.0, (370, 373): -408.0, (597, 605): -3770.0, (858, 862): 11230.0, (474, 479): -2134.0, (634, 638): -6032.0, (498, 500): -2504.0, (595, 598): 14854.0, (489, 617): -16200.0, (625, 630): -5910.0, (379, 383): 24318.0, (242, 245): 2243.0, (761, 764): -4851.0, (866, 871): -3878.0, (872, 878): -8596.0, (711, 719): -816.0, (234, 236): -3770.0, (754, 759): 5439.0, (761, 767): 625.0, (602, 607): -4060.0, (882, 885): -12064.0, (369, 372): -11820.0, (339, 340): 3284.0, (242, 244): -3770.0, (754, 756): -9702.0, (474, 478): -16200.0, (867, 870): -4268.0, (466, 594): -2504.0, (1011, 1015): -2760.0, (856, 862): -2585.333333333333, (632, 636): -881.0, (858, 860): -29144.0, (378, 382): -4021.333333333333, (979, 982): -4356.0, (1138, 1141): -9072.0, (840, 846): -3770.0, (592, 598): -13068.0, (595, 596): -7288.0, (608, 614): -20472.0, (635, 638): 10500.0, (624, 628): -408.0, (482, 484): -2504.0, (370, 375): 1478.0, (626, 630): 60370.0, (362, 365): -816.0, (755, 756): -9702.0, (739, 743): -2134.0, (626, 629): -5910.0, (345, 348): -41416.0, (507, 509): -20472.0, (617, 621): -5910.0, (360, 364): -17192.0, (352, 359): -10236.0, (370, 374): -7288.0, (745, 873): -6032.0, (610, 612): -1822.0, (763, 765): -881.0, (874, 878): 7026.0, (619, 622): -16200.0, (618, 623): -4060.0, (337, 340): -2760.0, (1138, 1140): -29144.0, (882, 886): 11602.0, (976, 981): -4356.0, (883, 886): 625.0, (498, 502): -32400.0, (889, 892): -8596.0, (610, 614): 1170.0, (474, 477): -10236.0, (842, 846): -2585.333333333333, (882, 887): -7756.0, (353, 359): -4536.0, (347, 348): -1822.0, (745, 750): -12018.0, (889, 895): -2585.333333333333, (754, 757): -1762.0, (625, 628): -5910.0, (344, 472): -3878.0, (605, 613): -4536.0, (370, 372): 12740.0, (1010, 1015): -2760.0, (706, 708): -4851.0, (1140, 1148): -29144.0, (1010, 1013): 14344.0, (730, 733): -1762.0]

II. CHIMERIZATION OF A QUBO PROBLEM FOR DENOISING A 4×4 IMAGE

$$I = \begin{pmatrix} 224 & 255 & 253 & 255 \\ 124 & 220 & 243 & 250 \\ 255 & 255 & 255 & 255 \\ 106 & 95 & 115 & 127 \end{pmatrix} P = \begin{pmatrix} 189 & 255 & 254 & 255 \\ 97 & 224 & 233 & 255 \\ 255 & 241 & 251 & 250 \\ 118 & 109 & 127 & 171 \end{pmatrix}$$

Initial number of binary variables (logical qubits): $Q_L = 16$.

Number of qubits after quadratization: $Q_Q = 44$

Graph connectivity for 44-spin ising problem:

The function to optimize, corresponding to the above matrix is:

$$\begin{aligned}
& 7560x_1 + 66x_1x_2 - 3595x_1x_5 + 15x_1x_6 - 24x_1x_{22} - x_1x_{23} - 79x_1x_{24} - 271x_2 + 52x_2x_3 + 41x_2x_5 + 374x_2x_6 - 748x_2x_7 - \\
& 152x_2x_{17} - 4x_2x_{21} - x_2x_{23} - 79x_2x_{24} - 273x_2x_{26} - 498x_2x_{27} - 95x_2x_{28} + 3469x_3 + 328x_3x_4 + 189x_3x_6 + 1288x_3x_7 + \\
& 154x_3x_8 - 152x_3x_{17} - 400x_3x_{18} - 283x_3x_{25} - 498x_3x_{27} - 95x_3x_{28} - 356x_3x_{30} - 214x_3x_{31} - 190x_3x_{32} + 867x_4 - 551x_4x_7 + \\
& 161x_4x_8 - 400x_4x_{18} - 43x_4x_{29} - 214x_4x_{31} - 190x_4x_{32} + 12795x_5 + 379x_5x_6 - 4522x_5x_9 - 955x_5x_{10} - 206x_5x_{19} - 4x_5x_{21} - \\
& 24x_5x_{22} - 79x_5x_{24} - 98x_5x_{34} - 191x_5x_{35} - 184x_5x_{36} + 765x_6 - 1430x_6x_7 + 244x_6x_9 + 38x_6x_{10} - 152x_6x_{17} - 206x_6x_{19} - \\
& 4x_6x_{21} - 24x_6x_{22} - x_6x_{23} - 283x_6x_{25} - 273x_6x_{26} - 95x_6x_{28} - 155x_6x_{33} - 191x_6x_{35} - 184x_6x_{36} - 587x_6x_{37} + 57165x_7 + \\
& 151x_7x_8 - 1597x_7x_{10} + 4668x_7x_{12} - 152x_7x_{17} - 400x_7x_{18} - 283x_7x_{25} - 273x_7x_{26} - 498x_7x_{27} - 43x_7x_{29} - 356x_7x_{30} - \\
& 190x_7x_{32} - 587x_7x_{37} - 903x_7x_{38} + 4168x_8 + 1069x_8x_{12} - 400x_8x_{18} - 43x_8x_{29} - 256x_8x_{30} - 214x_8x_{31} - 903x_8x_{38} + \\
& 21202x_9 - 113x_9x_{10} + 3614x_9x_{13} - 195x_9x_{14} - 206x_9x_{19} - 2534x_9x_{20} - 155x_9x_{33} - 98x_9x_{34} - 184x_9x_{36} - 4108x_9x_{40} - \\
& 2446x_9x_{41} - 2034x_9x_{42} + 32094x_{10} + 2817x_{10}x_{13} - 2819x_{10}x_{14} + 2504x_{10}x_{15} - 206x_{10}x_{19} - 2534x_{10}x_{20} - 155x_{10}x_{33} - \\
& 98x_{10}x_{34} - 191x_{10}x_{35} - 587x_{10}x_{37} - 2781x_{10}x_{39} - 2446x_{10}x_{41} - 2034x_{10}x_{42} - 4096x_{10}x_{43} + 7223x_{12} + 558x_{12}x_{15} - \\
& 1024x_{12}x_{16} - 903x_{12}x_{38} - 274x_{12}x_{44} + 456x_{13} + 3898x_{13}x_{14} - 2534x_{13}x_{20} - 2781x_{13}x_{39} - 4108x_{13}x_{40} - 2034x_{13}x_{42} + \\
& 15395x_{14} + 1762x_{14}x_{15} - 2534x_{14}x_{20} - 2781x_{14}x_{39} - 4108x_{14}x_{40} - 2446x_{14}x_{41} - 4096x_{14}x_{43} - 618x_{15} + 1185x_{15}x_{16} - \\
& 4096x_{15}x_{43} - 274x_{15}x_{44} + 1875x_{16} - 274x_{16}x_{44} + 456x_{17} + 600x_{18} + 618x_{19} + 7602x_{20} + 4x_{21} + 48x_{22} + x_{23} + 158x_{24} + \\
& 283x_{25} + 546x_{26} + 498x_{27} + 95x_{28} + 43x_{29} + 356x_{30} + 428x_{31} + 380x_{32} + 155x_{33} + 196x_{34} + 191x_{35} + 184x_{36} + 587x_{37} + \\
& 1806x_{38} + 2781x_{39} + 4108x_{40} + 2446x_{41} + 2034x_{42} + 8192x_{43} + 274x_{44}
\end{aligned}$$

The embeddings are:

logical qubit 0 :	[720, 848, 953, 956, 964, 968, 972, 976, 980, 984, 988, 996, 1004, 1012, 1020, 1081, 1112, 1209, 1337, 1465, 1593, 1721, 1849]	chain length : 23
logical qubit 1 :	[728, 818, 820, 828, 836, 844, 852, 856, 860, 868, 876, 884, 892, 946, 1074, 1202, 1330, 1458, 1586, 1714, 1842]	chain length : 21
logical qubit 2 :	[1496, 1583, 1591, 1599, 1607, 1615, 1623, 1624, 1631, 1639, 1647, 1655, 1663, 1752]	chain length : 14
logical qubit 3 :	[738, 866, 994, 1122, 1219, 1222, 1227, 1230, 1238, 1246, 1250, 1254, 1262, 1270, 1278, 1355, 1478, 1483, 1486, 1611, 1739]	chain length : 14
logical qubit 4 :	[1362, 1455, 1463, 1471, 1479, 1487, 1490, 1495, 1503, 1511, 1519, 1527, 1535, 1618, 1746]	chain length : 15
logical qubit 5 :	[1345, 1473, 1601, 1710, 1718, 1726, 1729, 1734, 1742, 1750, 1758, 1766, 1774, 1782, 1790]	chain length : 15
logical qubit 6 :	[747, 875, 1003, 1127, 1131, 1135, 1143, 1146, 1151, 1259, 1387, 1515, 1643, 1771]	chain length : 14
logical qubit 7 :	[731, 859, 987, 1111, 1115, 1118, 1119, 1126, 1134, 1142, 1150, 1243, 1371, 1499, 1627, 1755, 1883]	chain length : 17
logical qubit 8 :	[752, 880, 1008, 1136, 1264, 1392, 1520, 1648, 1776, 1904, 1908, 1916]	chain length : 12
logical qubit 9 :	[705, 819, 821, 829, 833, 837, 845, 853, 861, 869, 877, 885, 893, 947, 1075, 1203, 1331, 1459, 1587, 1715, 1843]	chain length : 21
logical qubit 10 :	[744, 749, 872, 1000, 1128, 1256, 1384, 1512, 1640, 1644, 1768, 1896, 2024, 2030, 2032, 2038, 2046]	chain length : 12
logical qubit 11 :	[1700, 1708, 1716, 1724, 1732, 1740, 1748, 1756, 1764, 1772, 1780, 1788]	chain length : 12
logical qubit 12 :	[682, 684, 692, 700, 708, 712, 716, 724, 732, 740, 748, 756, 764, 810, 938, 1066, 1194, 1322, 1450, 1578, 1706, 1834]	chain length : 22
logical qubit 13 :	[753, 757, 765, 881, 1009, 1137, 1265, 1393, 1521, 1649, 1777, 1905]	chain length : 12
logical qubit 14 :	[737, 865, 993, 1121, 1249, 1312, 1316, 1324, 1332, 1340, 1348, 1356, 1364, 1368, 1369, 1372, 1377, 1379, 1380, 1388, 1396, 1404, 1440, 1568, 1696]	chain length : 22
logical qubit 15 :	[723, 817, 822, 830, 838, 846, 850, 851, 854, 862, 870, 878, 886, 894, 945, 1073, 1201, 1329, 1457, 1585, 1713, 1841]	chain length : 22
logical qubit 16 :	[730, 735, 743, 751, 759, 767, 858, 986, 1114, 1242, 1370, 1498, 1502, 1626, 1754, 1882]	chain length : 16
logical qubit 17 :	[714, 842, 970, 1098, 1226, 1325, 1333, 1341, 1349, 1354, 1357, 1365, 1373, 1381, 1389, 1397, 1405, 1482, 1610, 1738]	chain length : 20
logical qubit 18 :	[715, 843, 955, 959, 967, 971, 975, 983, 991, 999, 1007, 1015, 1023, 1083, 1099, 1211, 1339, 1467, 1595, 1723, 1851]	chain length : 21
logical qubit 19 :	[683, 686, 694, 702, 710, 718, 726, 734, 742, 750, 758, 766, 811, 939, 1067, 1195, 1323, 1451, 1579, 1707, 1835]	chain length : 21
logical qubit 20 :	[1452, 1460, 1468, 1476, 1484, 1489, 1492, 1500, 1505, 1508, 1516, 1524, 1532, 1633, 1761]	chain length : 15
logical qubit 21 :	[1497, 1582, 1590, 1598, 1606, 1614, 1622, 1625, 1630, 1638, 1646, 1654, 1662, 1753]	chain length : 14
logical qubit 22 :	[755, 883, 1011, 1139, 1267, 1395, 1523, 1651, 1779, 1907, 2035, 2036, 2044]	chain length : 14
logical qubit 23 :	[721, 849, 954, 958, 966, 974, 977, 982, 990, 998, 1006, 1014, 1022, 1082, 1210, 1338, 1466, 1594, 1722, 1850]	chain length : 20
logical qubit 24 :	[754, 882, 1010, 1138, 1266, 1394, 1522, 1650, 1778, 1906, 2034, 2037, 2045]	chain length : 13
logical qubit 25 :	[707, 808, 815, 823, 831, 835, 839, 847, 855, 863, 871, 879, 887, 895, 936, 1064, 1192, 1320, 1448, 1576, 1704, 1832]	chain length : 22
logical qubit 26 :	[745, 873, 1001, 1129, 1257, 1385, 1510, 1513, 1518, 1526, 1534, 1641, 1769]	chain length : 13
logical qubit 27 :	[760, 888, 1016, 1144, 1272, 1400, 1528, 1656, 1784, 1912, 2040]	chain length : 11
logical qubit 28 :	[763, 891, 1019, 1147, 1275, 1403, 1531, 1652, 1659, 1660, 1787, 1915]	chain length : 12
logical qubit 29 :	[1612, 1617, 1620, 1628, 1745, 1824, 1831, 1833, 1839, 1847, 1855, 1863, 1871, 1873, 1879, 1887, 1895, 1897, 1899, 1903, 1911, 1919]	chain length : 22
logical qubit 30 :	[713, 841, 969, 1097, 1225, 1327, 1335, 1343, 1351, 1353, 1359, 1367, 1375, 1383, 1391, 1399, 1407, 1481, 1609, 1737]	chain length : 20
logical qubit 31 :	[746, 874, 1002, 1125, 1130, 1133, 1141, 1149, 1258, 1386, 1514, 1642, 1770, 1898]	chain length : 14
logical qubit 32 :	[729, 857, 985, 1080, 1084, 1092, 1100, 1106, 1108, 1113, 1116, 1124, 1132, 1140, 1148, 1208, 1241, 1336, 1464, 1592, 1720, 1848]	chain length : 22
logical qubit 33 :	[736, 864, 992, 1120, 1248, 1252, 1260, 1268, 1276, 1376, 1504, 1632, 1636, 1760]	chain length : 14
logical qubit 34 :	[1363, 1449, 1453, 1461, 1469, 1477, 1485, 1491, 1493, 1501, 1509, 1517, 1525, 1533, 1577, 1705]	chain length : 16
logical qubit 35 :	[1703, 1711, 1719, 1727, 1735, 1736, 1743, 1751, 1759, 1767, 1775, 1783, 1791]	chain length : 13
logical qubit 36 :	[739, 867, 944, 949, 957, 965, 973, 978, 981, 989, 995, 997, 1005, 1013, 1021, 1072, 1123, 1200, 1251, 1328, 1456, 1584, 1712, 1840]	chain length : 20
logical qubit 37 :	[1507, 1635, 1709, 1717, 1725, 1733, 1741, 1749, 1757, 1763, 1765, 1773, 1781, 1789]	chain length : 14
logical qubit 38 :	[704, 832, 960, 1088, 1199, 1207, 1215, 1216, 1223, 1231, 1239, 1247, 1255, 1263, 1271, 1279, 1344, 1472, 1600, 1728, 1856]	chain length : 21
logical qubit 39 :	[1360, 1488, 1581, 1589, 1597, 1605, 1613, 1616, 1619, 1621, 1629, 1637, 1645, 1653, 1744, 1747, 1875, 1878, 1886, 1894, 1902, 1910, 1918]	chain length : 23
logical qubit 40 :	[1326, 1334, 1342, 1350, 1352, 1358, 1366, 1374, 1378, 1382, 1390, 1398, 1406, 1480, 1506, 1608, 1634, 1762]	chain length : 18
logical qubit 41 :	[1197, 1205, 1213, 1218, 1221, 1229, 1237, 1240, 1245, 1253, 1261, 1269, 1277, 1346, 1474, 1602, 1730, 1858]	chain length : 18
logical qubit 42 :	[1274, 1347, 1402, 1475, 1530, 1603, 1658, 1731, 1786, 1837, 1845, 1853, 1857, 1859, 1861, 1869, 1877, 1885, 1893, 1901, 1909, 1914, 1917]	chain length : 23
logical qubit 43 :	[761, 889, 1017, 1145, 1273, 1401, 1529, 1657, 1661, 1785, 1913, 2041]	chain length : 12

(4)

The embedded problem is:

[(1752, 1758): 94.5, (1122, 1126): 80.5, (1392, 1398): -2446.0, (1008, 1015): -206.0, (1130, 1135): -63.3333, (1618, 1622): -12.0, (1387, 1389): -400.0, (1123, 1127): -293.5, (1393, 1396): 1762.0, (1843, 1845): -4096.0, (1755, 1757): -903.0, (832, 837): -1390.5, (1753, 1758): -12.0, (1129, 1135): -249.0, (875, 876): -748.0, (976, 982): -13.16667, (1771, 1773): -903.0, (1723, 1726): -206.0, (752, 756): 3614.0, (682, 686): -844.6667, (1355, 1357): -133.3333, (1586, 1591): 52.0, (1131, 1133): -63.3333, (1496, 1502): -76.0, (704, 708): -1390.5, (1402, 1404): -2048.0, (1473, 1476): -2.0, (883, 884): -1.0, (865, 870): 592.5, (1776, 1783): -184.0, (1225, 1230): -71.3333, (1627, 1631): 154.0, (1771, 1772): 4668.0, (1138, 1143): -263.0, (818, 823): -91.0, (1642, 1647): -190.0, (889, 894): -274.0, (1763, 1764): -903.0, (1355, 1359): -71.3333, (1626, 1631): -76.0, (1904, 1910): -2054.0, (1721, 1726): 15.0, (1905, 1909): -4096.0, (1473, 1479): 189.5, (705, 710): -2534.0, (1203, 1205): -2034.0, (835, 836): -91.0, (968, 974): -13.16667, (857, 861): -155.0, (1736, 1742): -92.0, (1785, 1788): -274.0, (1610, 1615): -400.0, (864, 869): -98.0, (1147, 1151): -43.0, (728, 735): -76.0, (1746, 1751): -184.0, (752, 758): -2534.0, (683, 684): -844.6667, (1449, 1455): -63.6667, (1465, 1471): -3595.0, (1489, 1495): -1.333333, (1259, 1262): -275.5, (1520, 1527): -4522.0, (1371, 1373): -400.0, (1755, 1756): 1069.0, (1459, 1461): -191.0, (1011, 1012): -1.0, (1720, 1726): -155.0, (1714, 1718): 374.0, (1705, 1710): -95.5, (1704, 1710): -273.0, (1194, 1197): -2034.0, (1601, 1607): 94.5, (1080, 885): -113.0, (1329, 1332): 592.5, (954, 956): -13.16667, (1761, 1766): -2.0, (1264, 1269): -2034.0, (753, 756): 3898.0, (1611, 1615): 328.0, (1905, 1908): -97.5, (1656, 1663): -95.0, (1003, 1005): -293.5, (1347, 1348): -2048.0, (1146, 1149): -63.3333, (1641, 1647): -498.0, (1754, 1758): -152.0, (865, 869): 1252.0, (1482, 1486): -133.3333, (1265, 1271): -2781.0, (747, 751): -152.0, (1771, 1772): -356.0, (888, 892): -95.0, (858, 860): -76.0, (1146, 1150): 50.3333, (1601, 1606): -12.0, (1779, 1782): -1.0, (1490, 1493): -63.6667, (867, 869): -293.5, (712, 718): -844.6667, (977, 980): -13.16667, (1371, 1375): -214.0, (1649, 1653): -2054.0, (1466, 1471): -79.0, (881, 885): -2819.0, (1275, 1278): -43.0, (1136, 1140): -155.0, (1490, 1492): -1.333333, (1784, 1790): -95.0, (1778, 1782): -283.0, (752, 757): -97.5, (1147, 1150): -43.0, (1264, 1268): -98.0, (1505, 1511): -1.333333, (1331, 1332): 1252.0, (1458, 1463): 41.0, (1593, 1598): -24.0, (1481, 1486): -71.3333, (1746, 1750): 189.5, (1776, 1782): 244.0, (1258, 1262): -95.0, (1491, 1495): -63.6667, (1393, 1398): -2446.0, (843, 845): -206.0, (1131, 1134): 50.3333, (1497, 1503): -12.0, (849, 852): -79.0, (1194, 1199): -1390.5, (753, 758): -2534.0, (1515, 1518): -249.0, (1467, 1471): -206.0, (1401, 1404): -274.0, (1119, 1127): 50.3333, (1459, 1463): -955.0, (1712, 1718): -587.0, (1473, 1477): -95.5, (1504, 1511): -98.0, (1226, 1230): -133.3333, (875, 879): -273.0, (856, 863): -91.0, (1617, 1623): -178.0, (1627, 1628): -178.0, (875, 877): -1597.0, (1122, 1127): -275.5, (1905, 1910): -2054.0, (1624, 1628): -178.0, (1578, 1581): -4108.0, (1696, 1700): 558.0, (947, 949): -293.5, (1713, 1716): -1024.0, (856, 884): 33.0, (1648, 1653): -2054.0, (705, 708): 2817.0, (1771, 1774): -1430.0, (1643, 1647): 1288.0, (1122, 1125): -95.0, (1729, 1735): -92.0, (1650, 1655): -283.0, (1883, 1887): -178.0, (1609, 1615): -214.0, (953, 958): -13.16667, (984, 990): -13.16667, (1243, 1246): 80.5, (848, 852): 33.0, (1203, 1207): -1390.5, (1458, 1460): -4.0, (873, 876): -498.0, (1331, 1334): -2446.0]

Figure 1.

