Computer Vision on the D-Wave 2000Q

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If you get robbed and the only way to get your wallet or purse back is for police to determine the identity of the thief based on a blurry surveillance video of a moving suspect, you might wish that a computer can "calculate" a sharp and clear version of the required image which shows clearly who it is that has your money. This is more complicated than the simple face-recognition algorithms used by Facebook for automatic tagging, or by Google for image search, because it involves first predicting what the unblurry version of an image should look like, and may involve video footage rather than simply stationary photographs.

The state-of-the-art method for solving this problem in industry is by solving a QUBO problem, and some examples from the classical-computer QUBO literature are below:

QUBO based in-painting by from Ref. [1].

QUBO based in-painting by from Ref. [1].



OUBO based de-blurring from Ref. [2].





QUBO based de-noising from Ref. [3].





Therefore this is a real-world problem that is "perfect" for the D-Wave machines, because the industry standard for solving the problem is to run a QUBO optimization on a classical computer. Image de-noising is performed by detectives for recovering partial finger-prints, by museums for reconstructing antique paintings, and by doctors for medical imaging, but in these cases the number of pixels (and hence the number of binary variables in the QUBO problem) is small. For terabyte-sized telescope images of galaxies, inter-stellar media, and possible life-containing exo-planets, runtimes are colossal and we welcome any speed-up even if only by a constant factor of 10 or even 2.

The algorithm works by minimizing two functions of binary variables simultaneously:

$$f_C(X_C) = \sum_{i=1}^K \alpha_i \log(1 + \frac{1}{2}(J_i \cdot X_C)^2)$$

$$f_v(X_v) = \frac{(N_v - X_v)^2}{2\sigma^2}$$
(2)

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 (2)

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The first function was calibrated by using billions of good and bad images such that the minimization of this function removes as much noise as possible. Minimizing the second function helps to maintain fidelity to the original image (its minimum occurs when the new pixel N_v at location v is the same as the original pixel X_v , but it is minimized simultaneously with Eq. 1 so our new pixels will not be exactly the same). C denotes a clique of size 2×2 , yielding 4-local interactions in the Hamiltonian. More accurate results can be obtained by using, for example, a 3×3 mask for the image processing, but this has never been applied in the literature since it would require quadratizing a 9-local Hamiltonian, which would greatly increase the number of auxiliary qubits required.

The number of binary variables (logical qubits) Q_L is equal to the number of pixels in the image. At each iteration, we would either accept the pixel from I or from P depending on whether the variable associated with that pixel is 0 or 1. The clique terms in Eq. 1 are quartic. We used auxiliary qubits to quadratize this quartic function, and what we are left with is a quadratic unconstrained boolean optimization (QUBO) problem involving Q_2 qubits coupled at most quadratically. Once we have quadratized the problem into QUBO form, we can chimerize it so that it can run on D-Wave annealers. Efficient chimerization is an active area of research, with new methods being proposed frequently, however we estimate the number of physical qubits Q_P needed by $\mathcal{O}(Q_2^2)$, which we know is an upper bound in the case for chimerizing a fully connected graph. Therefore, with $Q_A = 2048$ qubits available, we can have at least $Q_2 = 45$ qubits in the QUBO problem, so we will explore images of size 3×3 pixels ($Q_L = 9$ logical qubits) and 4×4 pixels ($Q_L = 16$ logical qubits). We do not investigate smaller images because the size of the image processing mask is 2×2 . Below we show that the computer vision algorithm still works even for small images:

I. CHIMERIZATION OF A QUBO PROBLEM FOR DENOISING A 3×3 IMAGE

$$I = \begin{pmatrix} 201 & 180 & 195 \\ 183 & 209 & 210 \\ 173 & 171 & 162 \end{pmatrix} P = \begin{pmatrix} 242 & 230 & 255 \\ 234 & 252 & 239 \\ 238 & 204 & 241 \end{pmatrix}$$

The original third order equation is:

 $13188x_1 + 16083x_2 - 1754x_4 - 20215x_5 + 7729x_6 - 9792x_7 - 45722x_8 + 5166x_9 - 58x_2x_4x_5 + 2088x_1x_4x_5 - 4602x_1x_2x_5 - 881x_1x_2x_4 + 898x_2x_5x_6 + 2598x_5x_7x_8 + 1612x_4x_7x_8 + 241x_4x_5x_8 + 575x_4x_5x_7 - 1213x_6x_8x_9 + 1731x_5x_8x_9 + 202x_5x_6x_9 - 603x_5x_6x_8 - 157x_4x_5 + 2909x_2x_5 + 561x_2x_4 + 1118x_1x_5 + 802x_1x_4 + 1228x_1x_2 + 99x_5x_6 - 4196x_2x_6 + 40144x_7x_8 - 5211x_5x_8 - 448x_5x_7 - 1108x_4x_8 - 16x_4x_7 + 524x_8x_9 - 312x_6x_9 + 3467x_6x_8 + 72x_5x_9 - 825x_1x_2x_4x_5 - 694x_4x_5x_7x_8 + 152x_5x_6x_8x_9$

Initial number of binary variables (logical qubits): $Q_L = 9$.

Number of qubits after quadratization: 29

Graph connectivity for 29 spin Ising problem:

```
-41416-7756-2760
                                                                                                           -12064-9702 0
                                                                                                                            -7756-2760
                                                                                         0
                                                                                            -1762-32400
                                                                                            \hbox{-}1762\hbox{-}32400\hbox{-}20472
                                                                                                                                   0 -4268-816
                                                                                                                  -9702-41416-7756
                0 4486 4238
-11820-11820 0
                                        7026 5396
                                                                                                                                      -4268-816-4060
11820-11820
                                                  35460
               .4 0 -29144-29144
-17192-17192 0 -
     -29144-29144
                                                        87432
                                 -17192-17192
                                                             25788
       0
                0 -3770 -3770

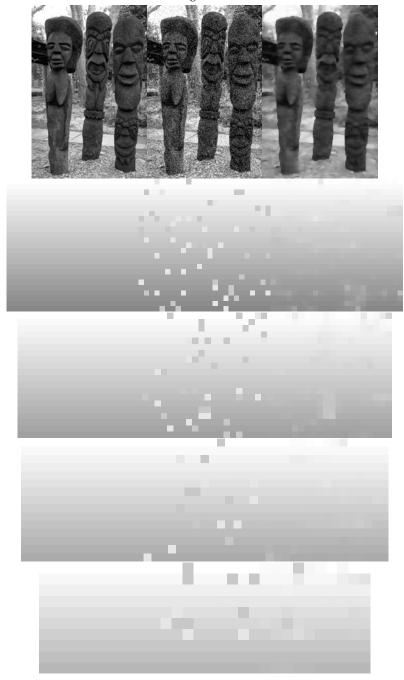
-2504 -2504 0

-7288 -7288 0
                                        -3770 -3770
                                                                  11310
-7288
                                                                             7288
                                                                         0
                0 -13068
-12018 0
13068-13068
            0
                                                                                 13068
                                                                                         0
                      0 0
-1762 -1762
                                                                                       12018
           -1762
                                                                                         0
     -32400
                                                                                                 32400
                      -32400-32400
                                                                                              0
     -20400-20472
                            -20472
                                                                                                   0
                                                                                                       20472
                      -12064
-9702
     -12064-12064
                                                                                                             12064
                                                                                                                              _{0}^{0}
                -41416
                                                                                                                       41416
                 -41416 0
-7756 -7756
                                 -41416-41416
                                               0
                                                                                                                   0
                                                                                                                            15512
                                                                                                                                 5520
                            -4268
                                        -4268 -4268
                                                                                                                                      4268
                                                                                                                                   0
                       -816
                                                                                                                                        0
0
0
                                                                                                                                          1632
                                        -816 -816
                                                                                                                                   0
                      -4060 -4060
-9072 -9072
                                             -4060
0
                                        -9072
```

The function to optimize, corresponding to the above matrix is:

```
11768x_1 + 14864x_1x_2 + 3284x_1x_4 + 14344x_1x_5 - 11820x_1x_{10} - 7288x_1x_{15} - 13068x_1x_{16} - 12018x_1x_{17} + 44700x_2 + 10500x_2x_3 + 1170x_2x_4 + 60370x_2x_5 + 27952x_2x_6 - 11820x_2x_{10} - 29144x_2x_{11} - 2504x_2x_{14} - 13068x_2x_{16} - 12018x_2x_{17} - 32400x_2x_{19} - 20472x_2x_{20} - 12064x_2x_{21} + 33716x_3 + 3694x_3x_5 + 24318x_3x_6 - 29144x_3x_{11} - 1762x_3x_{18} - 20472x_3x_{20} - 12064x_3x_{21} + 111320x_4 + 12740x_4x_5 - 620x_4x_7 + 16326x_4x_8 - 11820x_4x_{10} - 17192x_4x_{12} - 2504x_4x_{14} - 7288x_4x_{15} - 12018x_4x_{17} - 41416x_4x_{23} - 7756x_4x_{24} - 2760x_4x_{25} + 78878x_5 + 1478x_5x_6 + 10878x_5x_7 + 11602x_5x_8 + 4486x_5x_9 - 12018x_5x_8 + 12018x_5x_8
```





 $11820x_5x_{10} - 29144x_5x_{11} - 17192x_5x_{12} - 3770x_5x_{13} - 2504x_5x_{14} - 7288x_5x_{15} - 13068x_5x_{16} - 1762x_5x_{18} - 32400x_5x_{19} - 12064x_5x_{21} - 9704x_5x_{22} - 7756x_5x_{24} - 2760x_5x_{25} - 816x_5x_{27} - 4060x_5x_{28} - 9072x_5x_{29} + 29988x_6 + 11230x_6x_8 + 4238x_6x_9 - 29144x_6x_{11} - 3770x_6x_{13} - 1762x_6x_{18} - 32400x_6x_{19} - 20472x_6x_{20} - 4268x_6x_{26} - 4060x_6x_{28} - 9072x_6x_{29} + 45574x_7 + 1250x_7x_8 - 17192x_7x_{12} - 9702x_7x_{22} - 41416x_7x_{23} - 2760x_7x_{25} + 143330x_8 + 7026x_8x_9 - 17192x_8x_{12} - 3770x_8x_{13} - 9702x_8x_{22} - 41416x_8x_{23} - 7756x_8x_{24} - 4268x_8x_{26} - 816x_8x_{27} - 9072x_8x_{29} + 5396x_9 - 3770x_9x_{13} - 4268x_9x_{26} - 816x_9x_{27} - 4060x_9x_{28} + 35460x_{10} + 87432x_{11} + 25788x_{12} + 11310x_{13} + 2504x_{14} + 7288x_{15} + 13068x_{16} + 12018x_{17} + 1762x_{18} + 32400x_{19} + 20472x_{20} + 12064x_{21} + 9702x_{22} + 41416x_{23} + 15512x_{24} + 5520x_{25} + 4268x_{26} + 1632x_{27} + 4060x_{28} + 9072x_{29}$

The embeddings obtained for the Chimera architecture are:

```
logical qubit 0:
                        [339, 467, 595, 723, 851, 864, 973, 979, 981, 989, 992, 997, 1005, 1013]
                                                                                                       chain length: 14
logical qubit 1:
                                   [590, 594, 598, 606, 614, 617, 622, 630, 638, 745]
                                                                                                       chain length: 10
logical qubit 2:
                         [251, 252, 379, 382, 507, 635, 636, 763, 891, 1019, 1021, 1147, 1148]
                                                                                                       chain length: 13
logical qubit 3:
                         [331, 332, 340, 344, 348, 354, 356, 364, 372, 380, 482, 610, 738, 866]
                                                                                                       chain length: 14
logical qubit 4:
                                     [242, 370, 498, 626, 628, 754, 882, 1010, 1138]
                                                                                                       chain length: 9
logical qubit 5:
                              [346, 351, 359, 367, 375, 383, 474, 602, 605, 730, 858, 986]
                                                                                                       chain length: 12
                                                                                                       chain length: 10
logical qubit 6:
                                  [243, 371, 499, 627, 755, 759, 767, 883, 1011, 1139]
logical qubit 7:
                       [578, 633, 706, 711, 761, 834, 838, 846, 854, 862, 870, 878, 886, 889, 894]
                                                                                                       chain length: 15
logical qubit 8:
                        [234, 237, 245, 253, 362, 490, 618, 620, 743, 746, 751, 874, 1002, 1130]
                                                                                                       chain length: 14
logical qubit 9:
                                [241, 369, 497, 621, 625, 629, 637, 753, 881, 1009, 1137]
                                                                                                       chain length: 11
logical qubit 10: [459, 587, 715, 843, 844, 852, 860, 971, 1099, 1100, 1108, 1116, 1124, 1132, 1140]
                                                                                                       chain length: 15
                                                                                                        chain length: 11
logical qubit 11:
                                [232, 360, 488, 616, 744, 872, 876, 884, 892, 1000, 1128]
logical qubit 12:
                       [200, 204, 212, 217, 220, 228, 236, 244, 328, 456, 584, 589, 597, 712, 840]
                                                                                                        chain length: 15
logical qubit 13:
                         [448, 450, 452, 460, 466, 468, 476, 484, 492, 500, 508, 576, 704, 710]
                                                                                                        chain length: 14
                                                                                                        chain length: 14
logical qubit 14:
                         [219, 347, 350, 358, 366, 374, 475, 588, 596, 603, 604, 612, 731, 859]
                                                                                                                              (3)
logical qubit 15:
                             [336, 464, 592, 720, 848, 976, 982, 990, 998, 1006, 1014, 1022]
                                                                                                        chain length: 12
logical qubit 16:
                                                                                                        chain length: 8
                                        [718, 726, 734, 742, 750, 752, 758, 766]
logical qubit 17:
                                   [504, 632, 717, 725, 733, 741, 749, 757, 760, 765]
                                                                                                        chain length: 10
logical qubit 18:
                         [361, 462, 470, 478, 486, 489, 491, 494, 502, 510, 619, 747, 875, 1003]
                                                                                                        chain length: 14
logical qubit 19:
                               [352, 461, 469, 477, 480, 485, 493, 501, 505, 509, 608, 736]
                                                                                                        chain length: 12
logical qubit 20:
                         [378, 506, 634, 762, 845, 853, 861, 869, 873, 877, 885, 890, 893, 1001]
                                                                                                       chain length: 14
logical qubit 21:
                                         [708, 716, 724, 732, 740, 748, 756, 764]
                                                                                                        chain length: 8
logical qubit 22:
                             [345, 473, 601, 729, 735, 857, 985, 988, 996, 1004, 1012, 1020]
                                                                                                        chain length: 12
logical qubit 23:
                               [472, 600, 728, 842, 847, 855, 856, 863, 871, 879, 887, 895]
                                                                                                        chain length: 12
logical qubit 24:
                             [337, 465, 593, 721, 849, 977, 983, 991, 999, 1007, 1015, 1023]
                                                                                                        chain length: 12
logical qubit 25:
                              [355, 463, 471, 479, 483, 487, 495, 503, 511, 611, 739, 867]
                                                                                                        chain length: 12
logical qubit 26:
                       [330, 333, 341, 349, 357, 365, 368, 373, 381, 458, 496, 586, 624, 714, 719]
                                                                                                       chain length: 15
logical qubit 27:
                                 [457, 585, 591, 599, 607, 615, 623, 631, 639, 713, 841]
                                                                                                        chain length: 11
logical qubit 28:
                      [225, 353, 481, 609, 613, 737, 865, 868, 993, 1121, 1125, 1133, 1141, 1149]
                                                                                                        chain length: 14
```

The embedded problem is:

(866, 870): 16326.0, (344, 350): -1822.0, (362, 367): 4238.0, (354, 358): -1822.0, (587, 590): -29144.0, (628, 636): 3694.0, (627, 628): 5439.0, (620, 628): 2243.0, (857, 862): -41416.0, (1009, 1013): -11820.0, (361, 367): -16200.0, (1011, 1012): -41416.0, (992, 998): -4356.0, (723, 726): -12018.0, (738, 742): -12018.0, (891, 893): -4021.333333333335, (602, 606): 27952.0, (882, 884): -17192.0, (626, 631): -4060.0, (634, 636): -4021.333333333335, (883, 884): -17192.0, (865, 870): -9072.0, (355, 399): -2134.0, (1010, 1014): -13068.0, (371, 372): -620.0, (490, 495): -2134.0, (370, 373): -408.0, (597, 605): -3770.0, (885, 862): 11230.0, (474, 479): -2134.0, (634, 638): -6032.0, (498, 500): -2504.0, (595, 598): 14854.0, (489, 617): -16200.0, (482, 485): -3770.0, (754, 764): -8780.0, (767, 764): -4851.0, (866, 871): -3878.0, (877): -3878.0, (878): -8788.0, (204, 245): -2243.0, (242, 245): -2243.0, (767, 764): -4851.0, (866, 878): -3878.0, (878, 878): -8780.0, (711, 719): -816.0, (234, 236): -33770.0, (754, 756): 5490.0, (767, 764): -4851.0, (868, 860): -29144.0, (378, 382): -4021.333333333333, (979, 982): -4356.0, (1138, 1141): -9072.0, (490, 496): -3770.0, (592, 598): -13068.0, (595, 596): -7288.0, (608, 614): -20472.0, (635, 638): 10500.0, (624, 628): -5904.0, (307, 347): -7288.0, (482, 484): -2594.0, (307, 347): -7388.0, (482, 484): -2594.0, (307, 347): -7388.0, (482, 484): -2594.0, (307, 347): -7388.0, (482, 484): -2594.0, (307, 347): -7388.0, (482, 484): -2594.0, (307, 347): -7388.0, (482, 484): -2594.0, (307, 347): -7388.0, (482, 484): -2594.0, (307, 347): -7388.0, (482, 484): -2594.0, (482, 486): -2585.333333333333, (879, 982): -4356.0, (482, 486): -4288.0, (482, 486): -4288.0, (482, 486): -4288.0, (482, 486): -4288.0, (482, 486): -4288.0, (482, 486): -4288.0, (482, 486): -4288.0, (482, 486): -4288.0, (482, 486): -4288.0, (482, 486): -4288.0, (482, 486): -4288.0, (482, 486): -4288.0, (482, 486): -4288.0, (482, 486): -4288.0, (482, 486): -4288.0, (482, 486): -4288.0, (482, 486): -4288.0, (482, 486): -4288.0, (4

II. CHIMERIZATION OF A QUBO PROBLEM FOR DENOISING A 4×4 IMAGE

$$I = \begin{pmatrix} 224 & 255 & 253 & 255 \\ 124 & 220 & 243 & 250 \\ 255 & 255 & 255 & 255 \\ 106 & 95 & 115 & 127 \end{pmatrix} P = \begin{pmatrix} 189 & 255 & 254 & 255 \\ 97 & 224 & 233 & 255 \\ 255 & 241 & 251 & 250 \\ 118 & 109 & 127 & 171 \end{pmatrix}$$

The original third order equation is:

```
9557x_1 - 2916x_2 + 1153x_3 + 249x_4 - 27206x_5 + 22161x_6 + 39099x_7 + 6108x_8 - 27695x_9 - 2065x_{10} + 35248x_{11} + 22240x_{12} + 32419x_{13} + 224x_{14} + 2429x_{15} + 7329x_{16} - 5327x_5x_6 + 2235x_2x_6 - 252x_2x_5 + 103x_1x_6 - 7005x_1x_5 + 393x_1x_2 - 1562x_6x_7 - 893x_3x_7 + 114x_3x_6 + 5067x_2x_7 - 201x_2x_3 - 547x_7x_8 - 41x_4x_8 - 326x_4x_7 - 141x_3x_8 + 46x_3x_4 + 534x_9x_{10} + 132x_6x_{10} - 1313x_6x_9 + 258x_5x_{10} - 849x_5x_9 + 225x_{10}x_{11} - 19046x_7x_{11} + 755x_7x_{10} - 5145x_6x_{11} - 30553x_{11}x_{12} - 695x_8x_{12} - 867x_8x_{11} - 7430x_7x_{12} - 1428x_{13}x_{14} - 10x_{10}x_{14} - 921x_{10}x_{13} - 610x_9x_{14} + 16961x_9x_{13} - 78x_{14}x_{15} + 1477x_{11}x_{15} + 33x_{11}x_{14} - 11x_{10}x_{15} - 1069x_{15}x_{16} - 327x_{12}x_{16} - 207x_{12}x_{15} + 7032x_{11}x_{16} + 449x_2x_5x_6 - 1374x_1x_5x_6 + 312x_1x_2x_6 + 1249x_1x_2x_5 - 102x_3x_6x_7 - 11124x_2x_6x_7 + 1522x_2x_3x_7 + 63x_2x_3x_6 + 20x_4x_7x_8 + 117x_3x_7x_8 - 38x_3x_4x_8 - 49x_3x_4x_7 + 38x_6x_9x_{10} - 2570x_5x_9x_{10} + 35x_5x_6x_{10} + 6542x_5x_6x_9 - 1107x_7x_{10}x_{11} + 538x_6x_{10}x_{11} - 1679x_6x_7x_{11} - 686x_6x_7x_{10} + 401x_8x_{11}x_{12} + 401x_8x_{11}x_{12}
```

 $8664x_7x_{11}x_{12} + 185x_7x_8x_{12} - 1611x_7x_8x_{11} - 2x_{10}x_{13}x_{14} + 713x_9x_{13}x_{14} + 73x_9x_{10}x_{14} + 382x_9x_{10}x_{13} + 17x_{11}x_{14}x_{15} - 2x_{10}x_{14}x_{15} + 5x_{10}x_{11}x_{15} + 1x_{10}x_{11}x_{14} - 65x_{12}x_{15}x_{16} + 1503x_{11}x_{15}x_{16} - 4124x_{11}x_{12}x_{16} - 535x_{11}x_{12}x_{15} + 531x_{1}x_{2}x_{5}x_{6} - 859x_2x_3x_6x_7 + 34x_3x_4x_7x_8 - 856x_5x_6x_9x_{10} + 483x_6x_7x_{10}x_{11} + 1866x_7x_8x_{11}x_{12} - 70x_9x_{10}x_{13}x_{14} - 306x_{11}x_{12}x_{15}x_{16}$ Initial number of binary variables (logical qubits): $Q_L = 16$.

Number of qubits after quadratization: $Q_Q = 44$ Graph connectivity for 44-spin ising problem:

F 75	560	66	0	0 -	3595	15	0	0	0	0 (0 (0	0	0	0	0	0	0	0 ()-24-	1 -79	0	0	0 (0 (0	0	0	0 (0 0	0	0	0	0	0	0	0	0	0 7
ϵ	36 -	271	52	0	41	374	-748	0	0	0 (0 (0	0	0	0 -	152	0	0	0 -	4 0 -	1-79	0 -	273-	498-9	5 0	0	0	0	0 (0 0	0	0	0	0	0	0	0	0	0
	0	52 3	34693	328	0	189	1288	154	0	0 (0 (0	0	0	0 -	152-	400	0	0 (0 0	0 (-283	0 -	498-9	5 0	-356-	214-	190	0 (0 0	0	0	0	0	0	0	0	0	0
	0	0	328 8	367	0	0	-551	161	0	0 (0 (0	0	0	0	0 -4	400	0	0 (0 0	0 (0	0	0 0	-43	0 -	214-	190	0 (0 0	0	0	0	0	0	0	0	0	0
-37	595	41	0	0 1	2795	379	0	0	-4522	-955 (0 (0	0	0	0	0	0 -	206	0 -	4-24(-79	0	0	0 (0 (0	0	0	0 -9	8-19	1-184	4 0	0	0	0	0	0	0	0
			189				-1430	0	244	38 (0	0	0	0	0 -	152	0 -:	206	0 -	4-24-	1 0	-283-	273	0 -9	5 0	0	0	0 -	155 () -19	1-18	4-587	0	0	0	0	0	0	o l
							57165			-15970		Õ	ő	Ö		152-								498 (-903	o o	Ŏ.	o o	Ŏ.	Ő.	ő
			154				151				1069		ő	ō	Õ		400		0 (0			-356-			0 (-903	o o	Ô	0	Ŏ.	o o	ő
	ő	ő	0		4522		0			-113 (3614		ő	Ö				25340			ő	ő		0	0					-184		0		4108-2	2446-5	2034	0	ŏ
	o .	Õ	ñ		-955		-1597			320940			-2819		ő				25340			Ô	o o	0 0		0					91 0			-2781			2034-4		ň
	0	0	0	0	0	0	0	0	0	0 (0	0	0	o o	0		0		0 0		0	0	0 (0	0 -	0 () 1	0	0	0	0	0 -2	0			ő
	0	0	0	0	0		4668				7223	-		558 -			-	0		0 (0	0	0 0		0	0	0	0 (0		-	-903	0	0	0			274
	0	0	0	0	0	0	0	0		2817			3898	0	0	0	0		25340			0	0	0 (0	0	0	0 (0		-2781-	4100	0 -2	-	-	0
	0	0	0	0	0	0	0	0		-28190			15395		0		-		2534 (2534 (0	0	0 (, ,	0	0	0	0 (0			4108 - 4108 - 2			4096	~
	0	0	0		0	0	0						1762					0 -2				0	0	0 (, ,	0	0	0	0 (0	0	0 -	0	4100-2	0		4096 4096-2	
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	0	0	0 -152	0	0	0 -152	0	0	0)-1024) 0	0	0	1185			0	0		0 0		0	0	0 (, ,	0	0	0	0 (, ,	. 0	0	0	0	0	0			0
								0	0			0	0	0	0 4			0		0 (0	0	0 (, ,	0	0	0	0 (, ,	. 0	0	0	0	0	0	0		0
			-400-		0		-400				0 0	-			0	0 6				0 0		0	0	0 (, ,	0	0	0	0 (, ,	. 0	0	0			0	-		0
	0	0	0			-206	0	0	-206	-206 (0	0	0	0	0		318		0 0		0	0	0 (, ,	0	0	U	0 (, ,		U	0	0	0	0	0	0	0
	0	0	0	0	0	0	0			-25340			-2534	0	0	0	0		602 (0	0	0 () ()	0	0	0	0 () (0	0	0	0	0	0		0	0
	-	-4	0	0	-4	-4	0	0	0	0 (0	0	0	0	0	0	0		1 0 0		0	0	0 () ()	0	0	0	0 () ()	0	0	0	0	0	0	0	0	0
M = 1		0	0	0	-24	-24	0	0	0		0 0	0	0	0	0	0	0	0) 48 (0	0	0 () ()	0	0	0	0 () ()	0	0	0	0	0	0	0	0	0
		-1	0	0	0	-1	0	0	0		0	0	0	0	0	0	0	0		0 0 1		0	0	0 () ()	0	0	0	0 () ()	. 0	0	0	0	0	0	0	0	0
	79 -		0	0	-79	0	0	0	0		0	0	0	0	0	0	0	0		0 (0	0 (0	0	0	0 () ()	. 0	0	0	0	0	0	0	0	0
				0		-283		0	0		0	0	0	0	0	0	0	0				283		0 (0	0	0	0 () ()	0	0	0	0	0	0	0	0	0
		273		0			-273	0	0		0	0	0	0	0	0	0	0		0 (0		0 (0	0	0	0 () ()	0	0	0	0	0	0	0	0	0
			-498		0	0	-498	0	0		0	0	0	0	0	0	0	0		0 (0		498 (0	0	0	0 () ()	0	0	0	0	0	0	0	0	0
				0	0	-95	0	0	0		0	0	0	0	0	0	0	0		0 (0	0		5 0	0	0	0	0 (0	0	0	0	0	0	0	0	0	0
	0	0		-43	0	0		-43	0		0	0	0	0	0	0	0	0		0 (0	0) 43		0	0	0 (0	0	0	0	0	0	0	0	0	0
			-356		0	0	-356				0	0	0	0	0	0		0		0 0		0	0	0 (356		0	0 () 0	0	0	0	0	0	0	0	0	0
	0		-214-			0		-214			0	0	0	0	0	0	0	0		0 0		0	0	0 (0 -		0	0 (0	0	0	0	0	0	0	0	0	0
		0 .	-190-		0	0	-190	0	0		0	0	0	0	0	0	0	0		0 0		0	0	0 (0 (0	0 3	380	0 () 0	0	0	0	0	0	0	0	0	0
	0	0	0	0		-155	0	0		-155 (0	0	0	0	0	0	0	0 (0	0	0 (0			155 (0	0	0	0	0	0	0	0
	0	0	0	0	-98	0	0	0	-98	-98 (0	0	0	0	0	0	0		0 0		0	0	0 (0	0	0	0	0 19			0	0	0	0	0	0	0	0
	0	0	0			-191	0	0	0	-191 (0	0	0	0	0	0	0	0 (0	0	0 (0	0	0	0	0 () 19		0	0	0	0	0	0	0	0
	0	0	0			-184	0	0	-184	0 (0	0	0	0	0	0	0	0 (0	0	0 (0 (0	0	0	0 (0			0	0	0	0	0	0	0
	0	0	0	0	0	-587	-587	0	0	-587 (0	0	0	0	0	0	0	0	0 (0 0	0 (0	0	0 (0 (0	O	0	0 (0 0	0	587	0	0	0	0	0	0	0
	0	0	0	0	0	0	-903	-903	0	0 (903 -	0	0	0	0	0	0	0	0 (0 0	0 (0	0	0 (0 (0	0	0	0 (0 (0	0	1806	0	0	0	0	0	0
	0	0	0	0	0	0	0	0		-27810			-2781	0	0	0	0	0	0 (0 (0 (0	0	0 (0 (0	0	0	0 (0 (0	0	0	2781	0	0	0	0	0
	0	0	0	0	0	0	0	0	-4108	0 (0 (-4108	-4108	0	0	0	0	0	0 (0 (0 (0	0	0 (0 (0	0	0	0 (0 (0	0	0	0 4	4108	0	0	0	0
	0	0	0	0	0	0	0	0	-2446	-24460	0 (0	-2446	0	0	0	0	0	0 (0 (0 (0	0	0 (0 (0	0	0	0 (0 (0	0	0	0	0 2	446	0	0	0
			0	0	0	Ω	0	0	2024	-20340		-2034	. 0	0	0	0	0	0	0 (0.0	0 (0	0	0 0	0 (0	0	0	0 (0 0	0	0	0	0	0	0 2	2034	0	0
	0	0	U	U	0	U	U	U	-2034	-20340	, ,	2001																											
	0	0	0	0	0	0	0	o		-40960			-4096-	4096	0	0	0	ō	0 0	0 0	0	ō	ō	0 (0	0	0	0	0 (0	0	0	0	0	0	0	0 8	3192	0 274

The function to optimize, corresponding to the above matrix is:

```
7560x_1 + 66x_1x_2 - 3595x_1x_5 + 15x_1x_6 - 24x_1x_{22} - x_1x_{23} - 79x_1x_{24} - 271x_2 + 52x_2x_3 + 41x_2x_5 + 374x_2x_6 - 748x_2x_7 - 748x_2x_
152x_{2}x_{17} - 4x_{2}x_{21} - x_{2}x_{23} - 79x_{2}x_{24} - 273x_{2}x_{26} - 498x_{2}x_{27} - 95x_{2}x_{28} + 3469x_{3} + 328x_{3}x_{4} + 189x_{3}x_{6} + 1288x_{3}x_{7} + 1288x_{7}x_{7} + 1
154x_3x_8 - 152x_3x_{17} - 400x_3x_{18} - 283x_3x_{25} - 498x_3x_{27} - 95x_3x_{28} - 356x_3x_{30} - 214x_3x_{31} - 190x_3x_{32} + 867x_4 - 551x_4x_7 + 200x_3x_{31} - 200x_3x_{32} - 200x_3x_{31} - 20
161x_4x_8 - 400x_4x_{18} - 43x_4x_{29} - 214x_4x_{31} - 190x_4x_{32} + 12795x_5 + 379x_5x_6 - 4522x_5x_9 - 955x_5x_{10} - 206x_5x_{19} - 4x_5x_{21} - 206x_5x_{19} - 4x_5x_{21} - 206x_5x_{19} - 206x_5
24x_5x_{22} - 79x_5x_{24} - 98x_5x_{34} - 191x_5x_{35} - 184x_5x_{36} + 765x_6 - 1430x_6x_7 + 244x_6x_9 + 38x_6x_{10} - 152x_6x_{17} - 206x_6x_{19} - 120x_6x_{19} - 120x
4x_{6}x_{21} - 24x_{6}x_{22} - x_{6}x_{23} - 283x_{6}x_{25} - 273x_{6}x_{26} - 95x_{6}x_{28} - 155x_{6}x_{33} - 191x_{6}x_{35} - 184x_{6}x_{36} - 587x_{6}x_{37} + 57165x_{7} + 186x_{15}x_{15} + 186x_{15}x_{15
151x_7x_8 - 1597x_7x_{10} + 4668x_7x_{12} - 152x_7x_{17} - 400x_7x_{18} - 283x_7x_{25} - 273x_7x_{26} - 498x_7x_{27} - 43x_7x_{29} - 356x_7x_{30} - 400x_7x_{18} - 280x_7x_{29} - 400x_7x_{29} - 400x_7
190x_{7}x_{32} - 587x_{7}x_{37} - 903x_{7}x_{38} + 4168x_{8} + 1069x_{8}x_{12} - 400x_{8}x_{18} - 43x_{8}x_{29} - 256x_{8}x_{30} - 214x_{8}x_{31} - 903x_{8}x_{38} + 1069x_{8}x_{10} - 400x_{8}x_{18} - 43x_{8}x_{29} - 256x_{8}x_{30} - 214x_{8}x_{31} - 903x_{8}x_{38} + 1069x_{8}x_{10} - 400x_{8}x_{18} - 400x_{8}
21202x_9 - 113x_9x_{10} + 3614x_9x_{13} - 195x_9x_{14} - 206x_9x_{19} - 2534x_9x_{20} - 155x_9x_{33} - 98x_9x_{34} - 184x_9x_{36} - 4108x_9x_{40} - 1206x_9x_{10} - 1206x_9x
2446x_{9}x_{41} - 2034x_{9}x_{42} + 32094x_{10} + 2817x_{10}x_{13} - 2819x_{10}x_{14} + 2504x_{10}x_{15} - 206x_{10}x_{19} - 2534x_{10}x_{20} - 155x_{10}x_{33} - 206x_{10}x_{10} - 206x_{10}x
98x_{10}x_{34} - 191x_{10}x_{35} - 587x_{10}x_{37} - 2781x_{10}x_{39} - 2446x_{10}x_{41} - 2034x_{10}x_{42} - 4096x_{10}x_{43} + 7223x_{12} + 558x_{12}x_{15} - 2781x_{10}x_{10}x_{10} - 2781x_{10}x_{10} - 2781x_{10}x_{10} - 2781x_{10}x_{10}x_{10} - 2781x_{10}x_{10} 
1024x_{12}x_{16} - 903x_{12}x_{38} - 274x_{12}x_{44} + 456x_{13} + 3898x_{13}x_{14} - 2534x_{13}x_{20} - 2781x_{13}x_{39} - 4108x_{13}x_{40} - 2034x_{13}x_{42} + 466x_{13}x_{13}x_{14} - 266x_{13}x_{13}x_{14} - 266x_{13}x_{13}x_{14} - 266x_{13}x_{14}x_{15}x_{15} - 266x_{15}x_{15}x_{15}x_{15} - 266x_{15}x_{15}x_{15}x_{15}x_{15} - 266x_{15}x_{15}x_{15}x_{15}x_{15} - 266x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x_{15}x
15395x_{14} + 1762x_{14}x_{15} - 2534x_{14}x_{20} - 2781x_{14}x_{39} - 4108x_{14}x_{40} - 2446x_{14}x_{41} - 4096x_{14}x_{43} - 618x_{15} + 1185x_{15}x_{16} - 4006x_{14}x_{15} - 4006x_{15}x_{15} - 4006
4096x_{15}x_{43} - 274x_{15}x_{44} + 1875x_{16} - 274x_{16}x_{44} + 456x_{17} + 600x_{18} + 618x_{19} + 7602x_{20} + 4x_{21} + 48x_{22} + x_{23} + 158x_{24} + 48x_{24} + 48x_{25} + 28x_{25} + 28x_
283x_{25} + 546x_{26} + 498x_{27} + 95x_{28} + 43x_{29} + 356x_{30} + 428x_{31} + 380x_{32} + 155x_{33} + 196x_{34} + 191x_{35} + 184x_{36} + 587x_{37} + 184x_{36} + 184x_{
1806x_{38} + 2781x_{39} + 4108x_{40} + 2446x_{41} + 2034x_{42} + 8192x_{43} + 274x_{44}
```

The embeddings are:

```
[720, 848, 953, 956, 964, 968, 972, 976, 980, 984, 988, 996, 1004, 1012, 1020, 1081, 1112, 1209, 1337, 1465, 1593, 1721, 1849]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      chain length: 23
 logical qubit 0
                                                                                                [728, 818, 820, 828, 836, 844, 852, 856, 860, 868, 876, 884, 892, 946, 1041, 1122, 1209, 1537, 1405, 1595, 1721, 1649} [728, 818, 820, 828, 836, 844, 852, 856, 680, 868, 876, 884, 892, 946, 1041, 1202, 1330, 1458, 1586, 1714, 1842] [1496, 1583, 1591, 1599, 1607, 1615, 1623, 1624, 1631, 1639, 1647, 1655, 1663, 1752] [738, 866, 994, 1122, 1219, 1222, 1227, 1230, 1238, 1246, 1250, 1254, 1262, 1270, 1278, 1355, 1478, 1483, 1486, 1611, 1739] [1362, 1455, 1463, 1471, 1479, 1487, 1490, 1495, 1503, 1511, 1519, 1527, 1535, 1618, 1746] [1345, 1473, 1601, 1710, 1718, 1726, 1729, 1734, 1742, 1750, 1758, 1766, 1774, 1782, 1790]
 logical qubit 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      chain length: 21
 logical qubit 2
logical qubit 3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     chain length : 14
chain length : 21
 logical qubit 4
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      chain length: 15
 logical qubit 5
logical qubit 6
logical qubit 7
                                                 [1345, 1473, 1601, 1710, 1718, 1726, 1739, 1734, 1742, 1750, 1758, 1766, 1774, 1782, 1790] \\ [747, 875, 1003, 1127, 1131, 1135, 1143, 1146, 1151, 1259, 1387, 1515, 1643, 1771] \\ [731, 859, 987, 1111, 1115, 1118, 1119, 1126, 1134, 1142, 1150, 1243, 1371, 1499, 1627, 1755, 1883] \\ [752, 880, 1008, 1136, 1264, 1392, 1520, 1648, 1776, 1904, 1908, 1916] \\ [705, 819, 821, 829, 833, 837, 845, 853, 861, 869, 877, 885, 89, 947, 1075, 1203, 1331, 1459, 1587, 1715, 1843] \\ [744, 749, 872, 1000, 1128, 1256, 1384, 1512, 1640, 1644, 1768, 1896, 2024, 2030, 2032, 2038, 2046] \\ [1700, 1708, 1716, 1724, 1732, 1740, 1748, 1756, 1764, 1772, 1780, 1788] \\ [682, 684, 692, 700, 708, 712, 716, 724, 732, 740, 748, 756, 764, 810, 938, 1066, 1194, 1322, 1450, 1578, 1706, 1834] \\ [753, 757, 765, 881, 1009, 1137, 1265, 1393, 1521, 1649, 1777, 1905] \\ [737, 865, 993, 1121, 1249, 1312, 1316, 1324, 1332, 1340, 1348, 1356, 1364, 1372, 1377, 1379, 1380, 1388, 1396, 1404, 1440, 1568, 1696] \\ [738, 817, 822, 830, 838, 846, 850, 851, 854, 862, 870, 878, 886, 894, 945, 1073, 1201, 1329, 1457, 1585, 1713, 1841] \\ [730, 735, 743, 751, 759, 767, 858, 986, 1114, 124, 1370, 1498, 1502, 1626, 1754, 1882] \\ [744, 842, 970, 1098, 1226, 1325, 1333, 1341, 1349, 1354, 1357, 1365, 1373, 1381, 1389, 1397, 1405, 1482, 1610, 1738] \\ [745, 843, 955, 999, 697, 971, 975, 983, 991, 999, 1007, 1015, 1032, 1083, 1099, 1211, 139, 1467, 1595, 1793, 1851] \\ [683, 686, 694, 702, 710, 718, 726, 734, 742, 750, 758, 766, 811, 939, 1067, 1195, 1323, 1451, 1579, 1707, 1835] \\ [1452, 1460, 1468, 1476, 1484, 1489, 1492, 1500, 1505, 1508, 1516, 1524, 1532, 1633, 1761] \\ [1497, 1582, 1599, 1598, 1606, 1614, 1622, 1625, 1630, 1638, 1646, 1654, 1662, 1753]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      chain length: 15
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      chain length : 12
 logical qubit 8
 logical aubit 9
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      chain length: 21
logical qubit 10:
logical qubit 11
logical qubit 12
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      chain length: 22
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    chain length : 12
chain length : 25
chain length : 22
logical qubit 13
logical qubit 14
logical qubit 15
logical aubit 16
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      chain length: 16
logical qubit 17
logical qubit 18
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     chain length : 20
chain length : 21
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      chain length: 21
logical qubit 19
logical qubit 20
logical qubit 21
                                                                              chain length: 15
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      chain length : 14
logical qubit 23
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      chain length :
logical qubit 24
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      chain length: 13
logical qubit 25
logical qubit 26
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     chain length : 22
chain length : 13
logical qubit 27
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      chain length: 11
 logical qubit 28
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      chain length: 12
logical qubit 29
logical qubit 30
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     chain length : 22
chain length : 20
logical qubit 31
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      chain length: 14
logical qubit 32:
logical qubit 33
                                                                                      \begin{bmatrix} 729, 857, 985, 1080, 1084, 1092, 1100, 1106, 1108, 1113, 1116, 1124, 1132, 1140, 1148, 1208, 1241, 1336, 1464, 1592, 1720, 1848 \end{bmatrix} \\  \begin{bmatrix} 736, 864, 992, 1120, 1248, 1252, 1260, 1268, 1276, 1376, 1504, 1632, 1636, 1760 \end{bmatrix} \\  \begin{bmatrix} 1363, 1449, 1453, 1461, 1469, 1477, 1485, 1491, 1493, 1501, 1599, 1517, 1525, 1533, 1577, 1705 \end{bmatrix} \\  \begin{bmatrix} 1703, 1711, 1719, 1727, 1735, 1736, 1743, 1751, 1759, 1767, 1775, 1783, 1791 \end{bmatrix} 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     chain length : 22
chain length : 14
chain length : 16
 logical qubit 34
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      chain length: 13
 logical qubit 35
                                                                 [1703, 1711, 1719, 1727, 1735, 1736, 1743, 1751, 1759, 1767, 1775, 1783, 1791]
[739, 867, 944, 949, 957, 965, 973, 978, 981, 989, 995, 997, 1005, 1013, 1021, 1072, 1123, 1200, 1251, 1328, 1456, 1584, 1712, 1840]
[1507, 1635, 1709, 1717, 1725, 1733, 1741, 1749, 1757, 1763, 1765, 1773, 1781, 1789]
[704, 832, 960, 1088, 1999, 1207, 1215, 1216, 1223, 1231, 1239, 1247, 1255, 1263, 1271, 1279, 1344, 1472, 1600, 1728, 1856]
[1360, 1488, 1581, 1589, 1597, 1605, 1613, 1616, 1619, 1621, 1629, 1637, 1645, 163, 1744, 1747, 1875, 1878, 1886, 1894, 1902, 1910, 1918]
[1326, 1334, 1342, 1350, 1352, 1358, 1366, 1374, 1378, 1382, 1390, 1398, 1406, 1480, 1506, 1608, 1634, 1762]
[1197, 1205, 1213, 1218, 1221, 1229, 1237, 1240, 1245, 1253, 1261, 1269, 1277, 1346, 1474, 1602, 1730, 1858]
[1274, 1347, 1402, 1475, 1530, 1603, 1658, 1731, 1786, 1837, 1845, 1853, 1857, 1859, 1861, 1869, 1877, 1885, 1893, 1901, 1909, 1914, 1917]
[761, 889, 1017, 1145, 1273, 1401, 1529, 1657, 1661, 1785, 1913, 2041]
logical qubit 36
logical qubit 37
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     chain length : 24
chain length : 14
logical qubit 38
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      chain length: 21
logical qubit 39
logical qubit 40
logical qubit 41
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     chain length : 23
chain length : 18
chain length : 18
chain length : 23
logical qubit 43:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      chain length: 12
```

The embedded problem is:

(1752, 1758); 94.5, (1122, 1126); 80.5, (1392, 1398); -2446.0, (1008, 1015); -206.0, (1130, 1135); -63.3333, (1618, 1622); -12.0, (1137, 11389); -400.0, (1123, 1127); -293.5, (1393, 1396); 1762.0, (1484, 1845); -4096.0, (1755, 1757); -903.0, (832, 837); -1390.5, (1173, 1758); -12.0, (1129, 1135); -249.0, (875, 876); -748.0, (976, 982); -13.16667, (1771, 1773); -903.0, (1723, 1726); -206.0, (752, 756); 3614.0, (682, 686); -844.6667, (1355, 1357); -133.3333, (1618, 1591); 52.0, (1131, 1138); -63.3333, (1406, 1502); -760, (704, 708); -1390.5, (1402, 1404); -2048.0, (1473, 1476); -204.0, (883, 884); -274.0, (1616, 1404); -2048.0, (1404); -2048.0, (1473, 1476); -204.0, (876, 876); -748.0, (976, 982); -13.16667, (857, 861); -135.0, (1736, 1742); -92.0, (135, 1359); -71.3333, (1626, 1631); -76.0, (1904, 1910); -2054.0, (1271, 1726); -15.0, (1905, 1909); -4096.0, (1473, 1479); 1895, (705, 710); -2534.0, (1203, 1205); -2034.0, (838, 884); -91.0, (1427, 1457); -13.16667, (857, 861); -155.0, (1736, 1742); -92.0, (1786, 1787); -274.0, (1610, 1615); -400.0, (864, 869); -98.0, (1751, 5718); 38.0, (1471, 1151); -3595.0, (1489, 1485); -1333333, (1259, 1272); -274.0, (1610, 1615); -400.0, (864, 869); -98.0, (1751, 5718); 38.0, (1471, 1716); -375.0, (1494, 1497); -3955.0, (1489, 1485); -13.0, (1329, 1323); -272.0, (194, 1497); -3955.0, (1489, 1485); -13.0, (1329, 1323); -272.0, (194, 1497); -273.0, (1194, 1139); -2034.0, (1631, 1497); -2034.0, (1631, 1497); -2034.0, (1631, 1497); -2034.0, (1631, 1497); -2034.0, (1631, 1497); -2034.0, (1631, 1497); -2034.0, (1631, 1497); -2034.0, (1631, 1407); -273.0, (1194, 1139); -2034.0, (1631, 1407); -273.0, (1194, 1139); -2034.0, (1631, 1407); -273.0, (1194, 1139); -2034.0, (1631, 1407); -273.0, (1194, 1419); -2033333, (1611, 1606); -12.0, (1779, 1782); -13.0, (1329, 1323); -273.0, (1781, 1407); -273.0, (1194, 1419); -2033333, (1611, 1606); -12.0, (1779, 1782); -13.0, (1497, 1479); -13.0, (1497, 1477); -13.0, (1497, 1479); -13.0, (1497, 1477); -13.0, (1497, 1477); -13.0, (1497, 1477); -13.0,

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