

Pegasus: The second connectivity graph for large-scale quantum annealing hardware

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Pegasus is a graph which offers substantially increased connectivity between the qubits of quantum annealing hardware compared to the graph Chimera. It is the first fundamental change in the connectivity graph of quantum annealers built by D-Wave since Chimera was introduced in 2011 for D-Wave's first commercial quantum annealer. In this article we describe an algorithm which defines the connectivity of Pegasus and we provide what we believe to be the best way to graphically visualize Pegasus in 2D and 3D in order to see which qubits couple to each other. As Supplemental Material, we provide open source codes for generating Pegasus graphs.

The 128 qubits of the first commercial quantum annealer (D-Wave One, released in 2011) were connected by a graph called Chimera, which is rather easy to describe: A 2D array of $K_{4,4}$ graphs, with one partition of each $K_{4,4}$ being also connected to the same corresponding partition on the $K_{4,4}$ unit cell above it, and the other partition being connected to the same corresponding partition on the $K_{4,4}$ to the right of it (see Figure 1). The degree of the graph is six, since each qubit couples to four qubits within its $K_{4,4}$ unit cell, and to one qubit in a $K_{4,4}$ above it and one qubit in a $K_{4,4}$ to the right of it. All commercial quantum annealers built to date follow this graph connectivity, with just larger and larger numbers of $K_{4,4}$ unit cells (See Table 1).

Figure 1. The Chimera graph, with open edges to show that the pattern repeats.

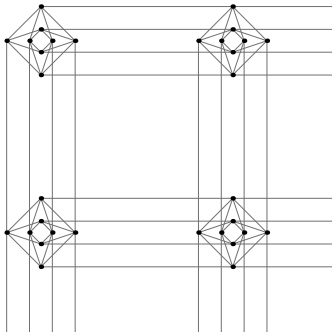


Table I. Chimera graphs in all commercial quantum computers to date.

	Array of $K_{4,4}$ unit cells	Total # of qubits
D-Wave One	4×4	128
D-Wave Two	8×8	512
D-Wave 2X	12×12	1152
D-Wave 2000Q	16×16	2048

In 2018, D-Wave announced the construction of a (not yet commercial) quantum annealer with a greater connectivity than Chimera offers, and a publicly available program (NetworkX) which allows users to generate Pegasus graphs of arbitrary size. However, no explicit description of the graph connectivity in Pegasus has been published yet, so we have had to apply the process of reverse engineering to determine it, and the following section describes our algorithm for generating Pegasus.

I. ALGORITHM FOR GENERATING PEGASUS

Start with K layers of Chimera graphs, each being an $I \times J$ array of $K_{4,4}$ unit cells (therefore we have an $I \times J \times K$ array of $K_{4,4}$ unit cells). The indices (i, j, k) will be used to describe the location of each unit cell along the indices corresponding to the dimension picked from (I, J, K) . Each $K_{4,4}$ cell has two partitions, labeled $l \in \{1, 2\}$, so that there's 4 qubits (vertices) for every (i, j, k, l) . We will arbitrarily label these 4 qubits using two more labels: $(m, n) \in \{1, 2\}^2$. Therefore every qubit is associated with 5 indices: (i, j, k, l, m, n) , with their ranges and descriptions given in Table 2.

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Figure 2. The Pegasus graph, with open edges to show that the pattern repeats.

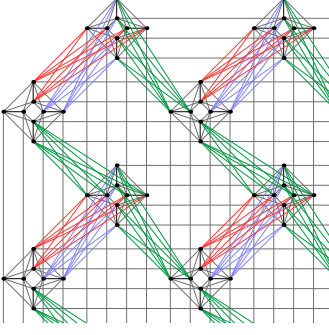


Table II. Indices used to describe each qubit (vertex) in Pegasus

i	1 to I	Row within a Chimera layer
j	1 to J	Column within a Chimera layer
k	1 to K	Chimera layer
l	1,2	Bi-partition within $K_{4,4}$
m	1,2	Top partition within each bi-partition of $K_{4,4}$
n	1,2	Bottom partition within each bi-partition of $K_{4,4}$

We then have the connections between $K_{4,4}$ cells of a particular layer, which would normally appear in Chimera, as in Figure 1: [insert mathematical description here].

Pegasus first adds connections within each $K_{4,4}$ cell (drawn in black color in Figure 2). The rest of the new connections in Pegasus come from connecting $K_{4,4}$ cells between different layers of $I \times J$ Chimera graphs. The qubits of $K_{4,4}$ will be connected to three different $K_{4,4}$ cells from a specific Chimera graph (i, j) on a different Chimera layer, and each pair of connected $K_{4,4}$ cells will have eight different connections in the form of $K_{2,2}$: [insert mathematical description here].

II. ALTERNATIVE GRAPHICAL REPRESENTATIONS OF PEGASUS

There are many ways that Pegasus can be drawn, so we show some of these in Figures 3 and 4.

III. COMPARISON TO CHIMERA AND DISCUSSION

A. Graph degree

As the yellow vertex in Fig. ? indicates, the vertices of Pegasus (except for vertices on an edge) have a degree 15, which is 2.5 times larger than the maximum degree achieved in Chimera.

B. Non-planarity

We note that certain binary optimization problems forming planar graphs can be solved in polynomial time on a classical computer using

Figure 3.

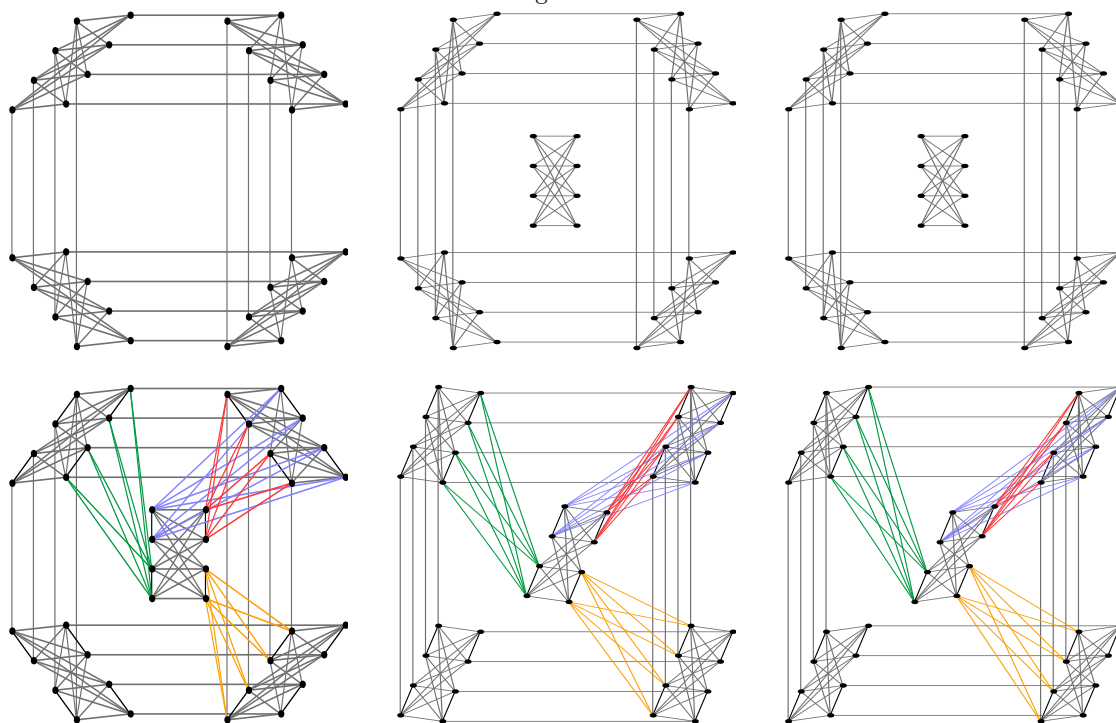


Figure 4.

