### What point groups can a molecule of a certain size or formula have?

Nike Dattani,<sup>1,2,\*</sup> Sichao Xiong,<sup>1,†</sup> and Hemanth H.<sup>1,‡</sup>

<sup>1</sup>HPQC Labs, Waterloo, Canada

<sup>2</sup>HPQC College, Waterloo, Canada

(Dated: 5th September 2023)

We list all possible point groups for 1, 2, 3, 4 and n atoms as well as for n-atom molecules with specified formulas. For each point group, we give examples of molecules of each size and formula if they are known, and hence we determine the yet-to-be discovered molecules with under 5 atoms for each point group. We establish a small set of principles that can be used for proofs about the possibility or impossibility for a molecule of a certain size and/or formula to have a point group symmetry.

#### INTRODUCTION

One might wonder why, despite group theory being applied to molecules for about 100 years [19], the questions that are being addressed in this paper do not appear to have been answered yet. Indeed we have asked all living authors of [1–18, 36] if they have ever come across a list of all possible point groups for a 4-atom (tetraatomic) system, and in all cases we were explicitly told that they were unaware of such a list, or we received no response at all.

Our need for answers to the question in the present paper's title, arose during other work. GW100 is a dataset of 100 systems (95 molecules and 5 atoms) which was introduced in a 2015 paper [37] and by the end of 2020, already more than 100 electronic structure methods/codes were used to calculate energies for all systems in the dataset. It has therefore become a monumental dataset for benchmarking, and efforts were made in [20] and [21] to improve the most accurate calculations that had been done on the system until then (and used to benchmark the other 100+ calculations from various research groups) [22]. But the geometries were wrong and we need to be able to generate them from places like the Landolt-Bornstein volumes [23–35]. Such volumes provide only the point group, a 3D diagram, and a minimal set of bond lengths, angles and dihedrals. For example H<sub>2</sub>Si<sub>2</sub> (not in GW100 but good for illustrating this point) gives only two bond lengths and a dihedral, but to do electronic structure calculations we need either the XYZ coordinates of all atoms, or a z-matrix for the molecule, and there is no softawre for obtaining either of these from just the limited information given. A software for generating a zmatrix from this data would be significantly simpler to write than a software for generating XYZ coordinates of all atoms, but the z-matrix for this system would need at least one bond angle, and you might find it surprising that the simplest formulas for the H-Si-H angle in H<sub>2</sub>Si<sub>2</sub> are (in terms of the provided dihedral angle  $\varphi$ , the provided Si-Si bond length  $r_1$  and the provided Si-H bond length  $r_2$ ):

$$\theta = \arccos\left(\frac{\cos\varphi\left(4r_1^2 - r_2^2\right) + r_2^2}{4r_1^2}\right) \tag{1}$$

$$= \arcsin\left(\frac{\sin\left(\frac{\varphi}{2}\right)\sqrt{4r_2^2 - r_1^2}}{r_2}\right). \tag{2}$$

Determining this bond angle can be accomplished with some high school level trigonometry (applications of the ordinary cosine law), and applications of the *dihedral cosine law* which is unlikely to be taught in high school or university-level curricula, but can be learned and applied to such small molecules within a day by most researchers; however with the pace of research today, the derivation of such a formulas as in Eqs. 1-2 would ideally be done by softawre rather than by hand. Unfortunately, not even the most advanced symbolic computation or comptuer algebra software can provide a user with Eqs. 1-2 based on the information given.

Furthermore, the interest today in machine learning and big data analysis has lead to the introduction of much larger datasets such as GW5000 and OE62 (both from Stuke et al. [38]) which involve more than 5000 and 61000 molecules respectively, but they have the same geometry problem (crystal structures vs spectroscopic geometries). This reinforces our motivation for constructing a software that could, for example, convert the ~5000 geometries from Landolt-Bornstein into z-matrices or XYZ coordinates. We believe that as machine learning and big data analysis become more popular over the next century, there will be a rise in interest in being able to categorieze molecules (e.g. for training neural networks) and the question of which point groups are possibel for molecules of a certain size of formula, will be asked more and more (and those seeking the answers will be able to find them in this paper).

A software to generate z-matrices (or even XYZ coordinates) for molecules with the data presented in experimental papers, such as  $(r_1=2.2079,r_2=1.6839,\varphi=103.18^\circ)$  for  $H_2Si_2$  would require specific code blocks for each molecular shape. It is possible for two molecules with the same point group to have very different shapes (e.g.  $C_{2v}$  for  $H_2Si_2$  and  $C_{2v}$  planar and

maybe another 4-atom  $C_{2v}$ , all have 4 atoms but one is pyramidal, one is planar, etc.), so a "z-matrix generator" or "xyz coordinates generator" would need specific code blocks for n-atom molecules not just based on their point group, but also based on other characteristics (perhaps their graph, formula, etc.), but a natural first step towards constructing such a software would be to categorize n-atom molecules based on their point groups (as done in the Landolt Bornstein series and a lot of other places, check CRC), and to construct code for each case. For n atoms, how many cases do we need to consider in order to cover each point group at **least once in the software?** That is the essence of the question in the present paper's title, and everyone tell us that it hasn't been done yet. We take this even one step further, by looking at the possible formulas, for example for a 7-atom molecule to have the point group Ci you need its formula to be A<sub>2</sub>B<sub>2</sub>C<sub>2</sub>D (with any of B,C,D being allowed to be a duplicate of one of the previous letters) but a molecule with any other formula cannot have the point group Ci (for example A<sub>2</sub>B<sub>2</sub>C<sub>2</sub> would no work unless B and C are A, which would bring us back to the previously mentioned formula in the case in which A=B=C=D).

In the initial stages of the development of our z-matrix constructor, we found that the Landolt-Bornstein series had all these molecules, but we realized that we missed the tadpole structure because we know that there's 6 connected 4-vertex graphs. Likewise we tried to see if we had representation from all possible point groups, and this required us to first determine the possible point groups for 4-atom molecules (which surprisingly we couldn't find, and we found that experts who wrote books on the topics were also unaware). In doing this, we discovered that  $D_2$  and  $D_{2d}$  are possible but not yet found, so this may be an avenue for further experimental research.

Another motivation was geometry optimization. Roland Lindh and others have discovered that you can get fewer cycles, but if point group symemtry is included, then we can have a smaller Wilson-B matrix.

In this paper we provide general principles, 3-atom and 4-atom possible groups, formulas and examples, n-atom groups and formulas for minimal structures, all of which seems to be novel. We skip the polyhedral groups  $T, T_d, T_h, O, O_h, I, I_h$  since we discovered something with fewer vertices than the snub cube that has O symmetry.

#### GENERAL PRINCIPLES FOR POSSIBLE MOLECULES

The following general principles will be used. They might seem obvious, but we don't see them in textbooks (maybe the first one is in textbooks).

Ability to orient a molecule according to the valid point group operations on the molecule:

Any molecule with a rotation axis, or  $C_n$ -axis, can be oriented in an xyz (Caterian) coordinate system such that for the largest possible n value in  $C_n$ , the z-axis is aligned with a  $C_n$  axis, and the  $\sigma_h$  plane is the xy-plane in the coordinate system.

#### Existence of a $C_n$ axis:

This is only possible if the molecule contains a subset of atoms that are vertices of an n-sided polygon with equal side-lengths (a regular n-gon). The  $C_n$  axis would be in the center of this polygon, and if it is the z-axis, then all atoms that form vertices of the polygon, would have to have the same z-coordinates. Therefore, a minimum of n atoms is needed in order to have a  $C_n$  axis. If a candidate  $C_n$  axis is the z-axis, then after a  $C_n$  rotation, an atom that originally had coordinates (x, y, z), will have coordinates (x', y', z) in which the z-coordinate does not change, because of the definition of a  $C_n$  rotation, and the new coordinates (x', y') can be different from the old ones (x, y) but will coincide with the original xy-coordinates of another identaical atom in the molecule if the molecule indeed has a  $C_n$ 

# Necessary and sufficient conditions for the $D_{nh}$ point group:

A regular n-gon with uniform vertices (in a molecule, this would mean the presence of identical atoms at the vertices) has a point group of  $D_{nh}$ , and any object with the  $D_{nh}$  point group must contain a subset of identical vertices that form a regular n-gon.

#### Action of the $S_n$ operation:

An  $S_n$  operation is by definition a  $C_n$  operation followed by a  $\sigma_h$  reflection operation. If we define the associated  $C_n$ -axis to be the z-axis, and the  $\sigma_h$  plane to be the xy-plane, then if an atom originally had coordinates (x,y,z), it will have coordinates (x',y',z) after the  $C_n$  rotation, and coordinates (x',y',-z) after the  $\sigma_h$  reflection. So  $S_n$  operation moves atoms from (x,y,z) to (x',y',-z). As described in the section about the existence of a  $C_n$  axis, the the new coordinates (x',y') can be different from the old ones (x,y) but will coincide with the original xy-coordinates of another identaical atom in the molecule if the molecule indeed has a  $C_n$  axis.

#### Action of the inversion operation, i:

We can always choose center of inversion to be at the origin (0,0,0), so if an atom is located at (x,y,z), the inversion operator will move it to (-x,-y,-z).

## MINIMUM NUMBER OF ATOMS AND POSSIBLE MOLECULAR FORMULAS FOR EACH POINT GROUP

As usual, we only consider the maximum point group. All in order of number of atoms, except for D2h which is paired with Dnh. What about D2, C2, C2v, C2h, D2d?

 $C_s$ 

Any two atoms form a line, and if all atoms of a molecule are on the same line, then the point group will be promoted to either  $C_{\infty v}$  or  $D_{\infty h}$ . Likewise, a single atom has the point group  $K_h$ , so it is not possible for a molecule with fewer than three atoms to have the point group  $C_s$ . three atoms is enough for the point group of a molecule to be  $C_s$  though, as in the example ABC. The minimum number of atoms required is three, and any formula is allowed.

 $C_1$ 

Any three atoms form a plane or a line, and if all atoms of a molecule are on the same plane, then that plane is a reflection/mirror plane. Therefore if a molecule has three or fewer atoms, it will at least have one reflection plane, and would be promoted from  $C_1$  to at least  $C_s$ . Four atoms is enough for the point group of a molecule to be  $C_1$  though, as in the example ABCD. The minimum number of atoms required is four, and any formula is allowed.

 $C_i$ 

Any five atoms with an inversion center will lie on the same plane (or same line) and will therefore have a reflection/mirror plane. Since the  $C_i$  point group does not have any reflection elements, for any five atom molecule with an investion center the maximal point group must be larger than  $C_i$ .

If we have three or fewer atoms, then there does not even need to be an inversion center for the atoms to be confined to a plane (or line).

If we have four atoms, and we make the inversion center the origin, the atoms must come in pairs according to the inversion operation i that was described earlier:  $A=(x_1,y_1,z_1)$  will be paired with  $-A=(-x_1,-y_1,-z_1)$  and  $B=(x_2,y_2,z_2)$  will be paired with  $-B=(-x_2,-y_2,-z_2)$ . Assuming that no two atoms will have the same xyz-coordinates, none of these four atoms can be on the origin.A and A form a line, and B and B form another line, and that these two lines both intersect at the origin, and two lines that cross are always co-planar.

If we have five atoms, the fifth one must be at the origin, because atoms need to either be paired or at the origin in order for the inversion operation to be valid on the system of atoms. However, the other four atoms form a plane that contains the origin (because the plane is formed by two lines that intersect at the origin). Therefore the fifth atom will also be on the same plane as the other four atoms, and the point group will be promoted beyond  $C_i$ .

Six atoms is enough for a molecule's maximal point group to be  $C_i$ , for example  $C_2H_2Br_2Cl_2$  with the two carbons removed. The minimum number of atoms required is six, and the formula must be of the form  $A_2B_2C_2D_2\cdots$  or  $AB_2C_2D_2\cdots$  depending on if the number of atoms is even or odd.

$$D_{nh}, n=2$$

1 or two atoms would be linear, and a 3-atom molecule can't have an inversion center unless it's linear, so you need at least 4 atoms, as in the case of Br2Na2.

$$D_{nh}, n \geq 3$$

Regular n-gon

$$C_{nv}, n \geq 3$$

Pyramid formed from regualr n-gon is Dnh, so add one more atom that's not on the same plane but still on the Cn axis that goes through the center of the n-gon to break the horizontal mirror plane and the Sn axis, while maintaining the n vertical mirror planes. The only point group with a Cn axis and n vertical mirror planes, without having any horizontal mirror planes or Sn axes, is Cnv. The minimum number of atoms required is n+1.

$$C_n, n \geq 3$$

Pyramid formed from regualr n-gon is Dnh, we need to add at least one atom to break all mirror planes. To preserve the Cn axis we need to either add any number of atoms on the Cn axis, or at least n atoms that are not on the Cn axis (forming a regular n-gon with the Cn axis in the centre of it). However, adding any atoms on the axis will not break the vertical mirror planes, so we must add at least n more atoms and form a second concentric regular n-gon around the Cn axis, but it cannot be on the same plane as the original n-gon because then it would still have the horizontal mirror plane and the point group would be promoted at least to  $C_{nh}$ , and the new n-gon would have to be rotated from the original one in order to avoid Dnh in the case where the side-lengths are the same (horizontal mirror plane is just halfway between the planes of the two n-gons), and Cnv where the two regular n-gons have their own distinct side-lengths. The minimum number of atoms required is 2n.

As in the case of Cn, any structure with fewer than 2n atoms will not have enough atoms to break the vertical planes of a 2n Dnh 2n n-gon, and without maintaining the 2n axis. Having two concentric 2n n-gons on the same plane, with one of them rotated from the other in order to avoid having 2n n-gonh, would be one way to construct a 2n n-gonh molecule with the minimum number of atoms. Another way would be to add the extra 2n n atoms to the plane containing the original regular 2n n-gonh and no rotation would be necessary if we are careful about how we place the bonds. The minimum number of atoms required is 2n.

$$D_n, n \geq 3$$

The minimum number of atoms required is 2n.

$$D_{nd}, n \geq 3$$

The minimum number of atoms required is 2n.

$$S_{2n}, n \geq 2$$

Since S2n is a generator of the S2n point group (or is it Sn) then Cn is in the point group because Cn = Sn^2. This means we need a regular polygon, but that wouldn't satisfy the S2n operaton unless all atoms were to be at the origin. You need 2n to have an S2n axis, but then you'd get Dnh, so you need another 2n to break the Dnh.

The minimum number of atoms required is 4n.

Point groups		Number of atoms								
		Minimum	1	2	3	4	5	6	7	8
$K_h$		1	V	X	X	X	X	X	X	X
$D_{\infty h}$		2	X	1	1	1	1	1	1	1
$C_{\infty v}$		2	X	1	1	1	1	1	1	/
D	$n \ge 3$	n	X	X	1	1	1	1	1	/
$D_{nh}$	n = 2	4	X	X	X	•	-	1	•	1
$D_{nd}$	$n \ge 2$	2n	X	X	X	•	-	-	•	1
$D_n$	$n \ge 2$	2n	X	X	X	1	•	•	1	/
$S_{2n}$	$n \ge 2$	4n	X	X	X	X	X	X	X	/
$C_{nv}$	$n \ge 2$	n+1	X	X	1	1	1	1	1	/
$C_{nh}$	$n \ge 2$	2n	X	X	X	1	•	•	1	/
$C_n$	$n \ge 2$	2n	X	X	X	1	1	1	1	/
$C_s$		3	X	X	1	1	1	1	1	/
$C_i$		6	X	X	X	X	X	•	1	/
$C_1$		4	X	X	X	/	/	/	/	/

#### Possible point groups for 3-atom (triatomic) molecules

Point group	Chemical formula type					
	$A_3$	$A_2B$	ABC			
$D_{\infty h}$ $C_{\infty v}$ $D_{3h}$ $C_{2v}$ $C_s$	Unlikely H <sub>3</sub> <sup>+</sup>	<b>X</b> H <sub>2</sub> O	HOS X X HNO			

#### N Possible groups (not including subgroups)

1									$K_h$
2									$D_{\infty h} C_{\infty v}$
3	$C_s$			$C_{2v}$			$D_{3h}$		$D_{\infty h} C_{\infty v}$
4	$C_s$	$C_1$ $C_2$	$C_{2h}$	$C_{2v}C_{3v}$	$D_2$	$D_{2d}$	$D_{2h} D_{3h} D_{4h}$	$T_d$	$D_{\infty h} C_{\infty v}$
5	$C_s$	$C_1$ $C_2$	$C_{2h}$	$C_{2v}C_{3v}$ $C_{4v}$	$D_2$	$D_{2d}$	$D_{2h} D_{3h} D_{4h} D_{5h}$	$T_d$	$D_{\infty h} C_{\infty v}$
6	$C_s$ $C_i$	$C_1$ $C_2$ $C_3$	$C_{2h}$ $C_{3h}$	$C_{2v}C_{3v} C_{4v} C_{5v}$	$D_2$ $D_3$	$D_{2d} D_{3d}$	$D_{2h} D_{3h} D_{4h} D_{5h} D_{5h}$	$0_{6h}$	$O_h D_{\infty h} C_{\infty v}$
7	$C_s$ $C_i$	$C_1$ $C_2$ $C_3$	$C_{2h}$ $C_{3h}$	$C_{2v}C_{3v} C_{4v} C_{5v} C_{6v}$	$D_2$ $D_3$	$D_{2d} D_{3d}$	$D_{2h} D_{3h} D_{4h} D_{5h} D_{5h}$	$D_{6h} D_{7h}$	$O_h D_{\infty h} C_{\infty v}$
8	$C_s$ $C_i$	$C_1$ $C_2$ $C_3$ $C_4$	$C_{2h} C_{3h} C_4$	$_{h}C_{2v}C_{3v} C_{4v} C_{5v} C_{6v} C_{7v}$	$v_v D_2 D_3$	$D_{2d} D_{3d}$	$D_{2h} D_{3h} D_{4h} D_{5h} D_{5h}$	$O_{6h} D_{7h} T_d$	$O_h D_{\infty h} C_{\infty v}$

#### Possible point groups for 4-atom (tetraatomic) molecules

Point group	Chemical formula type						
	$A_4$	$A_3B$	$A_2B_2$	$A_2BC$	ABCD		
$T_d$	$P_4$	×	×	X	×		
$D_{\infty h}$	$C_4$	×	$C_2H_2$	X	×		
$C_{\infty v}$	Unlikely	$C_3H$	ABAB?	$H_2BN$			
$D_{4h}$	$S_4^{2+}$	X	X	X	X		
$D_{3h}$	$\overset{\mathtt{d}}{C_4}$	$H_3B$	X	X	X		
$D_{2h}$	-	Unlikely	$Br_2Na_2$	X	X		
$D_{2d}$	$S_4$	X	X	X	X		
$D_2$	Unknown	X	X	X	X		
$C_{3v}$		$H_3N$	X	×	X		
$C_{2v}$		$IF_3$	$H_2Si_2$	$CH_2O$	X		
$C_{2h}$		Unlikely	$H_2N_2$	X	X		
$C_2$		Unlikely	$H_2O_2$	X	X		
$C_s$		$HO_3^+$		$Cl_2OS$	CHFO		
$C_1$		Ü		$H_2OS$	CHBrCl		

- \* nike@hpqc.org
- † sichao@hpqc.org
- <sup>‡</sup> hemanth@hpqc.org
- [1] P. W. Atkins, *Tables for Group Theory* (London, Oxford University Press, 1970).
- [2] D. M. Bishop, *Group Theory and Chemistry* (Clarendon Press, Oxford, 1973).
- [3] R. L. Carter, Molecular Symmetry and Group Theory (J. Wiley, New York, 1998).
- [4] F. A. Cotton, Chemical Applications of Group Theory (Interscience, New York, 1963).
- [5] G. Davidson, *Group Theory for Chemists*, Macmillan physical science (Macmillan, Basingstoke, 1991).
- [6] M. Diem, Introduction to Modern Vibrational Spectroscopy (Wiley, New York, 1993).
- [7] R. S. Drago, *Physical Methods in Chemistry*, Saunders golden sunburst series (Saunders, Philadelphia, 1977).
- [8] J. Ferraro and J. Ziomek, Introduction to Group Theory and Its Application to Molecular Structure (Plenum Press, 1969).

- [9] L. Hall, *Group Theory and Symmetry in Chemistry* (McGraw-Hill, 1969).
- [10] D. Harris and M. Bertolucci, Symmetry and Spectroscopy: An Introduction to Vibrational and Electronic Spectroscopy (Oxford University Press, 1978).
- [11] R. M. Hochstrasser, *Molecular Aspects of Symmetry* (W. A. Benjamin, New York, 1966).
- [12] J. M. J. M. Hollas, Symmetry in Molecules, Chapman and Hall chemistry textbook series (Chapman and Hall, London, 1972).
- [13] P. W. M. P. W. M. Jacobs, Group Theory with Applications in Chemical Physics (Cambridge University Press, Cambridge, 2005).
- [14] Y. Ohrn, Elements of Molecular Symmetry (Wiley Interscience, New York, 2000).
- [15] D. S. D. S. Urch, *Orbitals and Symmetry*, Penguin library of physical sciences. Chemistry. (Penguin Books, Harmondsworth, 1970).
- [16] J. P. Lowe, Quantum Chemistry (Academic Press, New York, 1978).
- [17] J. P. Lowe, *Quantum Chemistry*, 2nd ed. (Academic Press, Boston, 1993).
- [18] A. Vincent, Molecular Symmetry and Group Theory: a Programmed Introduction to Chemical Applications (Wiley, Chichester, 1977).
- [19] H. Bethe, Annalen der Physik 395, 133 (1929).
- [20] F. Bruneval, N. Dattani, and M. Setten, Frontiers in Chemistry 9 (2021), 10.3389/fchem.2021.749779.
- [21] L. Monzel, C. Holzer, and W. Klopper, The Journal of Chemical Physics 158, 144102 (2023).
- [22] K. Krause, M. E. Harding, and W. Klopper, Molecular Physics 113, 1952 (2015).
- [23] L. E. Sutton and H. J. M. Bowen, *Tables of Interatomic Distances and Configuration in Molecules and Ions* (Chemical Society London, London, 1958).
- [24] L. E. Sutton, *Tables of Interatomic Distances and Configuration in Molecules and Ions* (Chemical Society London, London, 1965).
- [25] N. N. Vogt, Structure Data of Free Polyatomic Molecules (Springer, Cham, Switzerland, 2019).
- [26] K. Kuchitsu, Structure Data of Free Polyatomic Molecules Inorganic Molecules (Springer, 1998).
- [27] K. Kuchitsu, Structure Data of Free Polyatomic Molecules -Molecules containing One or Two Carbon Atoms (Springer, 1999).
- [28] K. Kuchitsu, *Structure Data of Free Polyatomic Molecules* · *Molecules containing Three or Four Carbon Atoms* (Springer, 2001).
- [29] K. Kuchitsu, Structure Data of Free Polyatomic Molecules · Molecules Containing Five or More Carbon Atoms (Springer, 2003).

- [30] N. V. K. Kuchitsu, M. Tanimoto, Structure Data of Free Polyatomic Molecules · Inorganic Molecules Supplement to Volume II/25 (Springer, 2006).
- [31] N. V. K. Kuchitsu, M. Tanimoto, Structure Data of Free Polyatomic Molecules · Molecules containing One or Two Carbon Atoms Supplement to Volume II/25 (Springer, 2006).
- [32] N. V. K. Kuchitsu, M. Tanimoto, Structure Data of Free Polyatomic Molecules · Molecules containing Three or Four Carbon Atoms Supplement to Volume II/25 (Springer, 2007).
- [33] N. V. K. Kuchitsu, M. Tanimoto, Structure Data of Free Polyatomic Molecules · Molecules containing Five or More Carbon Atoms Supplement to Volume II/25 (Springer, 2007).
- [34] M. T. K. Kuchitsu, N. Vogt, Structure Data of Free Polyatomic Molecules · Molecules Containing No Carbon

- Atoms and Molecules Containing One or Two Carbon Atoms (Springer, 2014).
- [35] M. T. K. Kuchitsu, N. Vogt, Structure Data of Free Polyatomic Molecules · Molecules Containing Three or Four Carbon Atoms and Molecules Containing Five or More Carbon Atoms (Springer, 2014).
- [36] E. B. E. B. Wilson, Molecular vibrations: the theory of infrared and Raman vibrational spectra (McGraw-Hill, New York;, 1955).
- [37] M. J. van Setten, F. Caruso, S. Sharifzadeh, X. Ren, M. Scheffler, F. Liu, J. Lischner, L. Lin, J. R. Deslippe, S. G. Louie, C. Yang, F. Weigend, J. B. Neaton, F. Evers, and P. Rinke, Journal of Chemical Theory and Computation 11, 5665 (2015), pMID: 26642984.
- [38] A. Stuke, C. Kunkel, D. Golze, M. Todorovi'c, J. T. Margraf, K. Reuter, P. Rinke, and H. Oberhofer, Scientific Data 7, 58 (2020).