# Construction and Verification of Software

2019 - 2020

MIEI - Integrated Master in Computer Science and Informatics

Consolidation block

Lecture 8 - Concurrent Abstract Data Types
João Costa Seco (joao.seco@fct.unl.pt)
based on previous editions by Luís Caires (lcaires@fct.unl.pt)



#### Outline

- Concurrent ADTs
- Concurrency Control (Monitors)
- Verifying Monitors
- Applying and Verifying Monitor Conditions
- Concurrent ADTs construction
- An example of construction

# Construction and Verification of Software

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**Lecture 8 - Part I - Concurrent ADTs** 

João Costa Seco (joao.seco@fct.unl.pt) based on previous editions by Luís Caires (lcaires@fct.unl.pt)



# Concurrency

- To execute several units of computation out of the prescribed order (non strictly sequential).
- An undetermined number of interleaving executions between units
- Allows parallel computation (Hardware permitting) no state sharing
- Allows asynchronous programming (blocking IO)
  - improves efficiency
  - improves responsiveness (UI)
- Models with concurrency
  - Message passing
  - Shared Memory
  - Optimistic (Transactions)

# Concurrency

- To execute several units of computation out of the prescribed order (non strictly sequential).
- An undetermined number of interleaving executions between units
- Allows parallel computation (Hardware permitting) no state sharing
- Allows asynchronous programming (blocking IO)
  - improves efficiency
  - improves responsiveness (UI)
- Models with concurrency
  - Message passing
  - Shared Memory <<< most common in the imperative setting</li>
  - Optimistic (Transactions)

# Concurrency with shared memory

- Several threads of execution share the same state footprint
- Interference is expected:
  - the local view of a thread may change without notice (another thread may act "under the hood" and cause state changes).
- Interference is the essence of concurrency

#### Key issue:

- how to keep state consistency in the presence of state sharing and control interference
- how to reason about the effects of concurrent code
- Reasoning about concurrency is very challenging!
- Modularity brought by ADT based design is crucial!

#### Verification of ADTs

- The verification of sequential uses of ADTs caracterizes the observable states of objects implementing them.
- All ADT operations (public methods) preserve the consistency of the ADT.
- Consistency is expressed by the representation and abstract invariants (and the abstraction mapping).
- The following Hoare/Sep Logic triple is valid for all method bodies (mbody) of ADT operations
  - { RepInv && pre-cond } mbody { RepInv && post-cond}
- This line of reasoning works well under the assumption of sequentiality. What if method executions overlap in time?

#### Verification of ADTs

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#### Verification of Concurrent ADTs

 Challenge: how to program and reason about ADTs with interfering methods

### Interference between ADT operations

- Consider a Stack ADT
  - push(v), pop(), isEmpty()
  - push() interferes with pop()?
  - pop() interferes with isEmpty()?
  - pop() interferes with pop()?
- Consider a Dictionary ADT
  - assoc(key,data), find(key)
  - assoc() interferes with find()?
  - assoc() interferes with assoc() ?
  - find() interferes with find()?

#### Verification of Concurrent ADTs

- Challenge: how to program and reason about ADTs with interfering methods
- The verification of concurrent uses of ADTs should also observe stable states of objects implementing them.
- All ADT operations (public methods) must also preserve the consistency of the ADT.
- The following Hoare/Sep Logic triple should also be valid for all method bodies (mbody) of ADT operations
  - { RepInv && pre-cond } mbody { RepInv && post-cond}
- A sound approach is to consider the ADT operations as the unit of concurrency and structuring of reasoning (later to be refined).

# Operation Level Behaviour

- Reason at the level of ADT operations and not at the level of unstructured low level instructions and state changes
- Each ADT operation is performed in three steps
  - The operation is called (by the client thread)
  - The operation is executed (inside the ADT)
  - The operation returns
- Example:
  - push\_call(2)
    - ... execute (internally to the ADT)
  - push\_return
  - pop\_call()
    - .... execute (internally to the ADT)
  - pop\_return(2)

# Operation Level Behaviour

- We may consider several levels of concurrency
  - Several threads are invoking ADT operations but only one may actually be executing the operation
    - strict serialisation, easier to implement and reason about
    - less chances of "unsound" interference
- Several threads are invoking ADT operations but more than one may be executing an operation
  - more parallelism, more concurrency, harder to implement and reason about
  - more chances of "unsound" interference
- How does the concurrent object behaviour relate to the intended sequential object specification?

#### Two Basic Models

#### Serializability

 The global trace is always consistent with some sequential serialisation of previous operations (no overlaps of calls and returns), compatible with the sequential specification.

#### Linearizability

- The global trace is always consistent with a view in which previous operations appear to occur instantaneously between calls and returns, and the obtained serialisation is compatible with the sequential specification.
- Linearizability is more flexible than serializability, as it allows for more parallel behaviour.

# Desired properties ADT operations (ACID)

#### Atomicity

 No intermediate states are visible (not compatible with the representation invariant)

#### Consistency

 Operations lead from a sound state to a sound state (invariants and soundness are preserved)

#### Isolation

- This is another word for "no unsafe interference"
- Durability (this goes without saying)
  - Effects are undoable (N.B: this is more useful to highlight in the context of database transactions)

- With naive concurrency, it is hard (or impossible) for client code to be sure if a specific **post-condition** holds.
- E.g: two clients modify the concrete state at the same time, bringing the state inconsistent, breaking the representation invariant, or even crashing the code.

```
void push(int v)
//@ requires StackInv(this,?n,?m) &*& n < m;
//@ ensures StackInv(this,n+1,m);
{
   int i = nelems;
   store[i] = v;
   nelems++;
}</pre>
```

```
// Thread 1
int i = nelems;
int i = nelems;
store[i] = v;
nelems = i + 1;
nelems = i + 1;
```

- With naive concurrency, it is hard (or impossible) for client code to be sure if a specific post-condition holds.
- E.g: two clients modify the concrete state at the same time, bringing the state inconsistent, breaking the representation invariant, or even crashing the code.
- Solution using serialisation:
  - serialise usages of concrete states, so that just a single thread may be accessing the state at each given moment (mutual exclusion of concrete state)
  - We may then safely reason about such mutually exclusive code fragments as we have done for sequential code.

- With naive concurrency, it is hard (or impossible) for client code to be sure if a specific post-condition holds.
- E.g: two clients modify the concrete state at the same time, bringing the state inconsistent, breaking the representation invariant, or even crashing the code.

```
int pop()
                                                       // Thread 1
//@ requires StackInv(this,?n,?m) &*& n > 0;
                                                                                       // Thread 2
//@ ensures StackInv(this,n-1,m);
                                                   pop() {
                                                                                   pop() {
  int v = store[nelems-1];
                                                       int v = store[nelems-1];
  nelems--;
                                                       nelems--;
  return v;
                                                                                       int v = store[nelems-1];
                                                                                       nelems--;
                                                                                       return v;
                                                       return v;
```

- With naive concurrency, it is hard (or impossible) for client code to be sure if a specific post-condition holds.
- E.g: two clients modify the concrete state at the same time, bringing the state inconsistent, breaking the representation invariant, or even crashing the code.

```
int pop()
                                                       // Thread 1
//@ requires StackInv(this,?n,?m) &*& n > 0;
                                                                                       // Thread 2
                                                   pop() {
//@ ensures StackInv(this,n-1,m);
                                                                                   pop() {
  int v = store[nelems-1];
                                                       int v = store[nelems-1];
  nelems--;
                                                       nelems--;
  return v;
                                                                                       int v = store[nelems-1];
                                                                                       nelems--;
                                                                                       return v;
                                                       return v;
```

Is this safe in all situations?

- With naive concurrency, it is hard (or impossible) for client code to be sure if a specific pre-condition holds.
- E.g: client checks that a buffer is not empty, but other thread empties it under the hood.

#### • Solution:

- Concurrency control replaces pre-condition checking (on the client side) by explicit waiting for the precondition to hold (inside the ADT).
- The pre-condition for some ADT op can only be enabled by executing some other ADT op
- So waiting for a pre-condition must be managed by special programming language or system support, in a coordinated way with other ADT operations

# Concurrent Programming

- Reasoning about concurrency is hard
- Making sure the code is right is much more difficult than in sequential code
- Trying to simulate the program running in your head and debug it does not work anymore :-)
  - It does not work in the sequential case either, actually..., although you may still believe.
- We will now study how to design and construct correct concurrent code, based on monitors
- monitor = invariant preserving concurrent ADT
- Nicely supported by java.concurrent.util

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Consolidation block

**Lecture 8 - Part II - Concurrency Control (Monitors)** 

João Costa Seco (joao.seco@fct.unl.pt) based on previous editions by Luís Caires (lcaires@fct.unl.pt)



#### Monitors

Operating Systems

C. Weissman Editor

# Monitors: An Operating System Structuring Concept

C.A.R. Hoare The Queen's University of Belfast

This paper develops Brinch-Hansen's concept of a monitor as a method of structuring an operating system. It introduces a form of synchronization, describes a possible method of implementation in terms of semaphores and gives a suitable proof rule. Illustrative examples include a single resource scheduler, a bounded buffer, an alarm clock, a buffer pool, a disk head optimizer, and a version of the problem of readers and writers.

Key Words and Phrases: monitors, operating systems, scheduling, mutual exclusion, synchronization, system implementation languages, structured multiprogramming CR Categories: 4.31, 4.22









#### Monitors

- An ADT where operations may be called concurrently
- 2 key mechanisms provided for ensuring consistency: synchronization (a.k.a. mutual exclusion)
  - only a single thread may "own" the shared state at any time object, and has permission to change it
  - All that client code may expect from shared state is the invariant, and nothing more than the invariant
  - any context switches must preserve the invariant (observable states)

#### concurrency control

- pre-condition checking must be usually replaced by explicit waiting for the pre-condition to hold.
- conditions refine the invariant into finer partitions.

### Implementation of monitors

- To implement monitors in Java, we will use locks
  - You have already heard about locks (FSO, CP)
  - A lot harder to reason about programs if we just think of using locks in an unstructured way
- We may later refine the borders of serialisability to get more concurrency (approach linearisability)
  - Use locks as delimiters of abstract operations on the shared state
  - Use the java.util.concurrent API (Doug Lea)
  - Will learn how to design concurrent ADTs without thinking "operationally", but rather in terms of (partitioned) ownership, invariants, and conditions.

Consider a counter with a maximum value (Bounded)

```
class BCounter {
  int N;
  int MAX;
  BCounter(int max) { N = 0 ; MAX = max; }
  void inc() { N++; }
  void dec() { N--; }
  int get() { return N; }
}
```

```
/*@
    predicate BCounterInv(BCounter c; int v,int m) = c.N \mid -> v \& *\& c.MAX \mid -> m \& *\& v>=0 \& *\& v<=m;
@*/
class BCounter {
  int N; int MAX;
  BCounter(int max)
  // @ requires 0 <= max;</pre>
  // @ ensures BCounterInv(this,0,max);
  \{ N = \emptyset; MAX = max; \}
  void inc()
  // @ requires BCounterInv(this,?n,?m) &*& n < m;</pre>
  // @ ensures BCounterInv(this,n+1,m);
  { N++; }
  void dec()
  // @ requires BCounterInv(this,?n,?m) &*& n > 0;
  // @ ensures BCounterInv(this,n-1,m);
  { N--; }
  int get()
  // @ requires BCounterInv(this,?n,?m);
  // @ ensures BCounterInv(this,n,m) &*& 0<=result &*& result<=m;</pre>
  { return N;}
```

 The use of the bounded counter is safe in a sequential setting.

```
public static void main(String[] args)
//@ requires true;
//@ ensures true;
{
   int MAX = 100;
   BCounter c = new BCounter(MAX);
   //@ assert BCounterInv(c,0,MAX);
   if (c.get() < MAX) {
      c.inc(); // this is ok, precondition satisfied
   }
}</pre>
```

 But... in a concurrent setting where the reference to the counter is used elsewhere??

```
public static void main(String[] args)
//@ requires true;
//@ ensures true;
{
   int MAX = 100;
   BCounter c = new BCounter(MAX);
   //@ assert BCounterInv(c,0,MAX);
   giveaway(c); // potentially give other thread access to c
   if (c.get() < MAX) {
      //@ assert BCounterInv(c,?v,MAX) &*& v < MAX;
      c.inc();
      // not safe any more as other thread may have acted
   }
}</pre>
```

#### 1st: Serialise access to shared state

```
import java.util.concurrent.*;
import java.util.concurrent.locks.*;

class CCounter {
   int N;
   int MAX;
   ReentrantLock mon;

   CCounter(int max) {
      N = 0;
      MAX = max;
      mon = new ReentrantLock();
   }
   ...
```

```
import java.util.concurrent.*;
import java.util.concurrent.locks.*;
class CCounter {
 int N;
 int MAX;
 ReentrantLock mon;
 void inc()
      mon."enter"(); //request permission to the shared state
      N++;
      mon."leave"(); //release ownership of the shared state
  }
 void dec()
      mon."enter"(); //request permission to the shared state
      N--;
      mon."leave"(); //release ownership of the shared state
  }
```

```
import java.util.concurrent.*;
import java.util.concurrent.locks.*;
class CCounter {
 int N;
  int MAX;
 ReentrantLock mon;
 void inc()
      mon.lock(); //request permission to the shared state
      N++;
      mon.unlock(); //release ownership of the shared state
  }
 void dec()
      mon.lock(); //request permission to the shared state
      N--;
      mon.lock(); //release ownership of the shared state
  }
```

```
import java.util.concurrent.*;
import java.util.concurrent.locks.*;
class CCounter {
  int N;
  int MAX;
  ReentrantLock mon;
  int get()
      int r;
      mon."enter"();
      r = N; // put a copy on the stack, private to the thread
      mon."leave"();
      return r;
  }
```

# Summary

- Undisciplined concurrent access to shared memory causes unexpected (thus invalid) behaviour.
- (Conservatively) Implement all operations in a monitor, where only one thread is allowed at a time.

```
T op()
{
    T result;
    mon."enter"();
    // Thread has access to shared state
    result = Expression;
    // Thread releases access to shared state
    mon."leave"();
    return result;
}
```

 (Next) will define more flexible mechanisms that allow more interleaving of operations.

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**Lecture 8 - Part III - Verifying Monitors** 

João Costa Seco (joao.seco@fct.unl.pt) based on previous editions by Luís Caires (lcaires@fct.unl.pt)



# Reasoning about monitor operations

- Monitor "guards" the access to the ADT shared state.
   shared state = footprint of the monitor operations
- The "enter" operation gives access to the footprint
- The "leave" operation captures the footprint back

## Hoare Rule for enter/leave (lock/unlock)

```
{ emp } m.enter() { SharedStateInv() }
{ SharedStateInv() } m.leave() { emp }
```

SharedStateInv() is the representation invariant of the ADT that is used to verify operations in exclusive ownership of the monitor

#### In our example ...

```
//@ predicate CCounterInv(CCounter c) =
    c.N |-> ?v &*& c.MAX |-> ?m &*& v>=0 &*& v<=m;
so:
    { emp } m.lock() { CCounterInv(this) }</pre>
```

## Hoare Rule for enter/leave (lock/unlock)

Representation Invariant is available inside the monitor

```
class CCounter {
  int N;
  int MAX;
  ReentrantLock mon;
 void inc()
  //@ requires ...
  //@ ensures ...
      //@ request permission to the shared state
      mon.lock();
      //@ assert CCounterInv(this,?n,?m)
      N++;
      //@ assert CCounterInv(this,n+1,m)
      mon.unlock();
      //@ release ownership of the shared state
  }
```

## Warning: Red assertions not available!

Representation Invariant is available inside the monitor

```
class CCounter {
  int N;
  int MAX;
  ReentrantLock mon;
 void inc()
  //@ requires CCounterInv(this,?n,?m) &*& n < m;</pre>
  //@ ensures CCounterInv(this,n+1,m);
  {
      //@ request permission to the shared state
      mon.lock();
      //@ assert CCounterInv(this,?n,?m)
      N++;
      //@ assert CCounterInv(this,n+1,m)
      mon.unlock();
      //@ release ownership of the shared state
  }
```

### How can a client check n<m?

## How can an ADT capture the footprint in a lock?

#### "invisible" abstract state

- Many threads may be interfering, so the only thing one may assume is the invariant, only after entering the shared state a client may know extra details about the concrete state.
- In fact, nothing specific about the abstract state may be revealed to client code, and we need to be less informative about the abstract state (e.g., no current val)
- Inside the object, the only unprotected objects are the locks (or the single lock).
- Each lock can be used to ask permission to access a disjoint part of the shared state.
- We must precisely define which part of the shared state is separately owned by each lock.

## Example (Bounded Counter)

```
/*@
    predicate_ctor CCounter_shared_state (BCounter c) () =
         c.N \mid -> ?v \& *\& v >= 0 \& *\& c.MAX \mid -> ?m \& *\& 0 < m \& *\& v <= m;
*@/
/*@ predicate CCounterInv(CCounter c) =
           c.mon I \rightarrow ?1
      &*& l != null
      &*& lck(l, 1, CCounter_shared_state(c))
 @*/
class CCounter {
  int N;
  int MAX;
  ReentrantLock mon;
  CCounter(int max)
  //@ ensures CCounterInv(this);
    N = \emptyset;
    MAX = max;
    mon = new ReentrantLock();
```

## First-order predicates

 Define a family of predicates that can be stored by other predicates through a predicate constructor

```
predicate_ctor CCounter_shared_state (CCounter c) () =
    c.N I-> ?v &*& v >= 0 &*& c.MAX I-> ?m &*& 0 < m &*& v <= m;</pre>
```

and then instantiate them to produce a predicate instance

```
lck(l, 1, CCounter_shared_state(c))
```

and use it in other predicates

```
CCounter_shared_state(this)()
```

#### ReentrantLock constructor

 The ReentrantLock class signature ensures the establishment of the "native" predicate lck based on the invariant predicate inv

```
predicate enter_lck(real p, predicate() inv) = inv();
predicate lck(Lock s; real p, predicate() inv);

public class ReentrantLock {
    public ReentrantLock();
    //@ requires enter_lck(1,?inv);
    //@ ensures lck(this, 1, inv);
    ...
}
```

## Example (Bounded Counter)

```
class CCounter {
  int N;
  int MAX;
  ReentrantLock mon;
  CCounter(int max)
  //@ ensures CCounterInv(this);
    N = \emptyset ;
    MAX = max;
    //@ close CCounter_shared_state(this);
    //@ close enter_lck(1, CCounter_shared_state(this));
    mon = new ReentrantLock();
    //@ assert lck(mon, 1, CCounter_shared_state(this));
    //@ close CCounterInv(this);
```

## Example (Bounded Counter)

Representation invariant captures the resources that can be used in a concurrent context

```
class CCounter {
 int N;
 int MAX;
 ReentrantLock mon;
 void inc()
 //@ requires CCounterInv(this);
 //@ ensures CCounterInv(this);
   mon.lock(); // request permission to the shared state
   //@ open CCounter_shared_state(this)();
   N++;
   //@ close CCounter_shared_state(this)();
   mon.unlock(); // release ownership of the shared state
```

## ReentrantLock operations

 The ReentrantLock methods lock and unlock use the predicate lck to make the invariant available inside the monitor and captured again outside the exclusive access region.

## Example (Bounded Counter)

Representation invariant captures the resources that can be used in a concurrent context

```
class CCounter {
  int N;
  int MAX;
  ReentrantLock mon;
 void dec()
 //@ requires CCounterInv(this);
 //@ ensures CCounterInv(this);
    mon.lock();
    //@ open CCounter_shared_state(this)();
   N--;
    //@ close CCounter_shared_state(this)();
    mon.unlock();
```

## What if N==0?

### What if N==0?

 The "public" representation invariant cannot reveal information to make the pre-condition hold.

```
class CCounter {
  int N;
  int MAX;
  ReentrantLock mon;
 void dec()
 //@ requires CCounterInv(this); // no way to reveal a pre-cond!
  //@ ensures CCounterInv(this);
   mon.enter();
    //@ open CCounter_shared_state(this)();
   N--;
    //@ close CCounter_shared_state(this)(); // must ensure N>=0!
   mon.leave();
}
```

## Summary

- This structured monitor implementation makes the shared state representation invariant available inside the exclusive access area.
- The operations lock and unlock release and capture the representation invariant.
- Operations cannot enforce preconditions in the caller context due to possible interleaving of operations outside the monitor.

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**Lecture 8 - Part IV - Conditions** 

João Costa Seco (joao.seco@fct.unl.pt) based on previous editions by Luís Caires (lcaires@fct.unl.pt)



### How can a client check n<m?

## What if N==0?

#### How can a client check n<m?

- Concurrency control mechanisms replaces pre-condition checking (on the client side) by explicit waiting for the precondition to hold (inside the ADT).
- The pre-condition for some ADT operation can only be enabled by executing some other ADT operation.
- Waiting for a pre-condition is managed by special programming language or system support, in a coordinated way with other ADT operations.

**Monitor Conditions** 

## Partition shared state using conditions

Conditions implement queues of suspended threads...

```
class CCounter {
  int N;
  int MAX;
  ReentrantLock mon;
  Condition notzero;
  Condition notmax;
 void dec()
  //@ requires CCounterInv(this);
  //@ ensures CCounterInv(this);
    mon.enter();
    //@ open CCounter_shared_state(this)();
    if (N==0) notzero.await();
    N--;
    //@ close CCounter_shared_state(this)();
    mon.leave();
```

## Partition shared state using conditions

 Conditions represent operations' preconditions, that are checked in the callee context, where access is granted

```
class CCounter {
  int N;
  int MAX;
  ReentrantLock mon;
  Condition notzero;
  Condition notmax;
  void dec()
  //@ requires CCounterInv(this);
  //@ ensures CCounterInv(this);
    mon.enter();
    //@ open CCounter_shared_state(this)();
    if (N==0) notzero.await();
    N--;
    //@ close CCounter_shared_state(this)();
    mon.leave();
```

## Hoare Rule for wait (await)

```
\{ SharedStateInv() \} C.wait() \{ SharedStateInv() \land Cond(C) \}
```

Cond(C) is the refinement of the shared state property denoted by condition C.

In our example:

- Cond(notzero) = (N > 0)
- Cond(notmax) = (N < MAX)

## Partition shared state using conditions

```
/*@
predicate_ctor CCounter_shared_state (CCounter c) () =
   C.N \mid -> ?V \& *\& V >= 0 \& *\& C.MAX \mid -> ?m \& *\& m > 0 \& *\& V <= m;
predicate_ctor CCounter_nonzero (CCounter c) () =
   C.N \rightarrow ?V \& *\& C.MAX \rightarrow ?m \& *\& V > 0 \& *\& m > 0 \& *\& V <= m;
predicate_ctor CCounter_nonmax (CCounter c) () =
   C.N \rightarrow ?V \& *\& C.MAX \rightarrow ?m \& *\& V < m \& *\& m > 0 \& *\& V >= 0;
predicate CCounterInv(CCounter c) =
         c.mon \mid -> ?1
    &*& l != null
    &*& lck(l,1, CCounter_shared_state(c))
    &*& c.notzero |-> ?cc
    &*& cc != null
    &*& cond(cc, CCounter_shared_state(c), CCounter_nonzero(c))
    %*& c.notmax |-> ?cm
    &*& cm != null
    &*& cond(cm, CCounter_shared_state(c), CCounter_nonmax(c));
@*/
```

#### ReentrantLock Conditions await

 The Condition method await makes a transformation from the generic shared state (inv) to the refined state corresponding to that condition (acond).

```
public interface Condition {
    public void await();
        //@ requires cond(this,?inv,?acond) &*& inv();
        //@ ensures cond(this,inv, acond) &*& acond();
    ...
}
```

## Partition shared state using conditions

Conditions grant the access to the refined state condition

```
class CCounter {
  int N;
  int MAX;
  ReentrantLock mon;
  Condition notzero; Condition notmax;
  void dec()
  //@ requires CCounterInv(this);
  //@ ensures CCounterInv(this);
  {
    mon.lock();
    //@ open CCounter_shared_state(this)();
    if (N == 0) notzero.await();
    //@ open CCounter_notzero(this)(); // refined state with N > 0
   N--;
    //@ close CCounter_shared_state(this)();
    mon.unlock();
```

## Example (Bounded Counter)

 Conditions are defined with relation to both the representation invariant and the refined state.

```
class CCounter {
 int N;
 int MAX;
 ReentrantLock mon;
 Condition notzero;
 Condition notmax;
 BCounter(int max)
 //@ requires max > 0;
 //@ ensures CCounterInv(this);
  MAX = max;
  mon = new ReentrantLock();
  //@ close CCounter_shared_state(this)();
  //@ close set_cond(CCounter_shared_state(this),CCounter_nonzero(this));
   notzero = mon.newCondition(); // notzero set to mean N > 0 !!
  //@ close set_cond(CCounter_shared_state(this),CCounter_nonmax(this));
  notmax = mon.newCondition(); // notmax set to mean N < MAX !!</pre>
```

#### ReentrantLock Conditions await

 Conditions are defined with relation to the representation invariant (inv) and the refined state (pred).

```
public class ReentrantLock {
    ...
    public Condition newCondition();
    //@ requires lck(?t, 1, ?inv) &*& set_cond(inv, ?pred);
    //@ ensures lck(t, 1, inv) &*& result != null &*& cond(result,inv,pred);
}
```

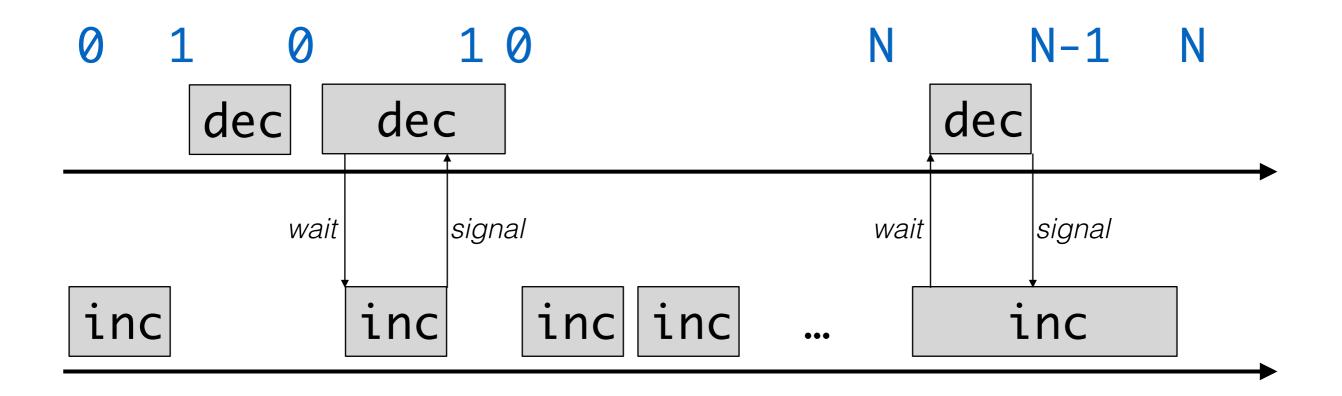
## Partition shared state using conditions

Different conditions give access to different refinements

```
class CCounter {
  int N;
  int MAX;
  ReentrantLock mon;
  Condition notzero; Condition notmax;
 void inc()
 //@ requires CCounterInv(this);
  //@ ensures CCounterInv(this);
    mon.enter();
    //@ open CCounter_shared_state(this)();
    if (N == MAX) notmax.await();
    //@ open CCounter_notmax(this)(); // refined state N < max</pre>
    N++;
    //@ close CCounter_shared_state(this)();
    mon.leave();
```

## Wait and Signal work together

- Wait and signal represents a voluntary yielding of control flow and exclusive access to the monitor.
- Wait suspends a thread until a precondition is "satisfied"
- Signal states that a precondition is explicitly "satisfied"



## Ensure progress using signalling

 Wait and signal represents a voluntary yielding of control flow and exclusive access to the monitor.

```
void inc()
//@ requires CCounterInv(this);
//@ ensures CCounterInv(this);
{
    mon.enter();
    //@ open CCounter_shared_state(this)();
    if (N == MAX) notmax.await();
    //@ assert CCounter_notmax(this)();
    N++;
    //@ close CCounter_notzero(this)();
    notzero.signal();
    //@ close CCounter_shared_state(this)();
    mon.leave();
}
```

## Ensure progress using signalling

 Wait and signal represents a voluntary yielding of control flow and exclusive access to the monitor.

```
void dec()
//@ requires CCounterInv(this);
//@ ensures CCounterInv(this);
{
    mon.enter();
    //@ open CCounter_shared_state(this)();
    if (N == 0) notzero.await();
    //@ assert CCounter_notzero(this)();
    N--;
    //@ close CCounter_notmax(this)();
    notmax.signal();
    //@ close CCounter_shared_state(this)();
    mon.leave();
}
```

## Hoare Rule for wait/signal (await/signal)

```
\{ SharedStateInv() \} C.wait() \{ SharedStateInv() \land Cond(C) \}  \{ SharedStateInv() \land Cond(C) \} C.signal() \{ SharedStateInv() \}
```

Cond(C) is the refinement of the shared state property denoted by condition C.

#### In our example:

- Cond(notzero) = (N > 0)
- Cond(notmax) = (N < MAX)

#### **Excerpt from Java API documentation:**

#### **Implementation Considerations**

When waiting upon a Condition, a "spurious wakeup" is permitted to occur, in general, as a concession to the underlying platform semantics.

This has little practical impact on most application programs as a Condition **should always be waited** upon in a loop, testing the state predicate that is being waited for.

An implementation is free to remove the possibility of spurious wakeups but it is recommended that applications programmers always assume that they can occur and so always wait in a loop.

```
void inc()
//@ requires CCounterInv(this);
//@ ensures CCounterInv(this);
{
    mon.lock();
    //@ open CCounter_shared_state(this)();
    while(N==MAX) notmax.await();
    //@ assert CCounter_notmax(this)();
    N++;
    //@ close CCounter_notzero(this)();
    notzero.signal();
    //@ assert CCounter_shared_state(this)();
    mon.unlock();
}
```

```
void dec()
//@ requires CCounterInv(this);
//@ ensures CCounterInv(this);
{
    mon.lock();
    //@ open CCounter_shared_state(this)();
    while (N==0) notzero.await();
    //@ assert CCounter_notzero(this)();
    N--;
    //@ close CCounter_notmax(this)();
    notmax.signal();
    //@ assert CCounter_shared_state(this)();
    mon.unlock();
}
```

```
void inc()
//@ requires CCounterInv(this);
//@ ensures CCounterInv(this);
  mon.lock();
  //@ open CCounter_shared_state(this)();
 while (N == MAX)
   /*@ invariant this.N |-> ?v &*& v >= 0
             &*& this.MAX |-> ?m
             &*& m > 0 &*& v <= m
             &*& this.notzero |-> ?cc &*& cc !=null
             &*& cond(cc,CCounter_shared_state(this), CCounter_nonzero(this))
             &*& this.notmax |-> ?cm
             &*& cm !=null &*& cond(cm, CCounter_shared_state(this),CCounter_nonmax(this));
   @*/
     //@ close CCounter_shared_state(this)();
     try { notmax.await(); } catch (InterruptedException e) {}
     //@ open CCounter_nonmax(this)();
  N++;
  //@ close CCounter_nonzero(this)();
   notzero.signal();
  mon.unlock();
   //@ close CCounterInv(this);
```

## Summary

- Implementing preconditions using monitor conditions
- The operations await and signal yield control in a structured way.
- unsound real implementations lead to active waiting code (that can also be verified) on the conditions.

# Construction and Verification of Software

2019 - 2020

MIEI - Integrated Master in Computer Science and Informatics

Consolidation block

**Lecture 8 - Part V - Construction of Concurrent ADTs** 

João Costa Seco (joao.seco@fct.unl.pt) based on previous editions by Luís Caires (lcaires@fct.unl.pt)



## Concurrent ADT Construction Steps

Challenge: Can we systematically transform and verify correct a "sequential" ADT implementation into an efficient "concurrent" ADT implementation?

## Concurrent ADT Construction Steps

- Associate a monitor to the ADT (ReentrantLock mon)
- 2. Define the "sequential" ADT Representation Invariant (**RepInv**) that talks about the shared state.

The Representation Invariant describes the memory footprint of the shared state, subject to other various conditions.

- 3. Defined the concurrent ADT Representation Invariant that talks about the monitor and associated conditions.
- 4. In the implementation of each operation of the CADT
  - 1. Get access to the shared state representation invariant, use mon.lock()
  - 2. When done and only if the shared state representation invariant holds use mon.unlock()
- 5. Replace the ADT operation pre-conditions by monitor conditions inside the monitor (this part must be carefully though).
- 6. Design voluntary yielding points to implement the correct interleaving of operations.

## Concurrent ADT Construction Steps

To replace ADT operation pre-conditions by monitor conditions inside the monitor, we must consider the following aspects:

- When a thread enters a CADT operation and gets ownership of the representation invariant, it should check the state to satisfy (or not) the pre-condition (e.g., wants to decrement but counter value is zero)
- The thread must then await for the condition to hold (e.g, for the value to be > 0).
- Conversely, whenever a thread running inside the CADT establishes any one of the monitor conditions (e.g., inc establishes value >0), it has the duty to signal the condition (so that the runtime system, may awake a waiting thread).
- Notice: signalling is there to help the system to progress, and simplify the implementation of monitors.

# Construction and Verification of Software

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Consolidation block

**Lecture 8 - Part VI - Example of a Concurrent ADT** 

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# Another Example...