# MP6 - Scheme

# Logistics

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# **Objectives**

The objective for this MP is to build an interpreter for a minimalist dialect of Lisp called Scheme. You will learn to build a fully monadic evaluator, and a read-evaluate-print-loop (REPL) to accept input from user.

This language will have the normal things you would expect in a Lisp-like language, such as functions, numbers, symbols, and lists. You will also write a macro system and explore how to use it. Macros give you the ability to program your programming language, redefining it to be anything you want.

#### Goals

- Understand the basic syntax of Scheme and how to evaluate programs in it
- Understand how to simulate stateful computation by composing monads, and write seemingly imperative but under-the-hood functional code in Haskell
- Create an REPL for your interpreter which handles manipulating the environment based on inputs from the user
- Understand homoiconicity and metacircular evaluation via Scheme

# **Getting Started**

## Relevant Files

In the directory app/, you will find the program code, some of which is only partially implemented, and which you will have to modify to complete this assignment. The file test/Tests.hs contains the code used for testing.

# Running Code

As usual, you have to run stack init (you only need to do this once).

To run your code, start GHCi with stack ghci (make sure to load the Main module if stack ghci doesn't automatically do it). From here, you can test individual functions, or you can run the REPL by calling main. Note that the initial \$ and > are prompts.

```
$ stack ghci
... More Output ...
Prelude> :1 Main
Ok, modules loaded: Main.
*Main> main
```

To run the REPL directly, build the executable with stack build and run it with stack exec main.

# **Testing Your Code**

You are able to run the test-suite with stack test:

#### \$ stack test

It will tell you which test-suites you pass, fail, and have exceptions on. To see an individual test-suite (so you can run the tests yourself by hand to see where the failure happens), look in the file test/Spec.hs.

You can run individual test-sets by running stack ghci and loading the Spec module with :1 Spec. Then you can run the tests (specified in test/Tests.hs) just by using the name of the test:

Look in the file test/Tests.hs to see which tests were run.

# Given Code

In directory app/:

• Main.hs: a fully implemented REPL frontend

In directory app/Scheme/:

- Core.hs: partially implemented core language data structures
- Parse.hs: a fully implemented parser
- Eval.hs: partially implemented evaluator
- Runtime.hs: partially implemented runtime routines

#### Environment

Like previous assignments, the environment is a HashMap. You can access functions like lookup, union and insert through prefix H, such as: H.lookup

```
type Env = H.HashMap String Val
```

#### AST

Now we offer you the Scheme AST. From your previous experience, do you notice anything unusual?

That's right, the AST data type is Val, not Exp! Scheme, as well as other Lisps, is a homoiconic language, meaning that the text of the language and the values have the same structure as its AST.

Code is data. Data is code.

Expressions from the programmer are now encoded as values: numbers, booleans, symbols and lists. When you feed such a value to the evaluator, the evaluator treats it as an expression and evaluates it!

#### Kinds of values

# 1. Symbol

Symbol is just a symbol. In previous MPs, a symbol expression, a.k.a. SymExp, was meant to be evaluated as a variable name bound to a value. In Scheme, this is no longer the case. Not only can you have values bound to a symbol, you can also use symbols themselves as a value.

#### 2. Boolean

Can be true #t or false #f.

#### 3. Number

An integer. We do not support floating point in this MP.

#### 4. List

A List is a list of values.

#### 5. DottedList

A DottedList is a list of values ended by a non-null tail value (e.g. (1 2 . 3)). This distinction is an implementation detail for efficiency; dotted lists may occur as an intermediate state as a list is processed.

In Scheme, a list or a dotted list resembles a linked list, each cell of which is called a "cons cell". While we could totally define list as a chain of Cons Val Val and a Null, here we utilize Haskell's list data structure to reduce performance overhead and simplify the implementation of some primitive routines. Linked lists are bad!

Just because DottedList resembles a linked list, lists and dotted lists that are constructed differently can be equivalent by value. We offer you a useful helper function - flattenList, which flattens a DottedList to the simplest form, which can be a List or a DottedList. You will find it extremely useful when implementing primitive functions in the runtime.

Here are some examples illustrating the value equivalence of lists.

Nested	Flattened
( . ()) (1 . ())	()
(1 . (2 . 3))	(1 2 . 3)
(1 . (2 . 3 . ())) (1 . (2 3))	(1 2 3) (1 2 3)

#### 6. PrimFunc

A primitive function is a function defined in Haskell, lifted to Scheme. The type constructor PrimFunc takes a function that takes an argument list and returns an evaluation state, encapsulating either both the result of evaluation and the environment, or a Diagnostic thrown along the computation.

#### 7. Func

A closure has an argument list, a body, and a captured environment.

As a side note, we are not implementing the reference memory model for Scheme. Thus functions are passed by value, i.e. all variables of the closure environment will be copied upon the copy of a closure.

#### 8. Macro

A macro has an argument list and a body. The body will be first transformed to an expanded body by the evaluator, and the expanded body gets fed back into the evaluator again. We'll talk about it in detail in the evaluation section.

#### 9. Void

The evaluator returns a value for every expression. Void is a special return type of the (define ...) and (define-macro ...) special forms. It does not represent any data.

### Diagnostic

You are given a fully defined Diagnostic type, cases of which are runtime errors thrown along evaluation. You are responsible for choosing the right Diagnostic to throw, in your evaluator.

#### **Evaluation State**

At the end of Scheme/Core.hs, we defined for you the type of the evaluation state monad, EvalState a, where a is the type of the evaluation result.

```
type EvalState a = StateT Env (Except Diagnostic) a
```

StateT is the monad transformer version of State. But you do not need to fully understand monad transformers! Simply read the declaration above as: EvalState is a state encapsulating the evaluation result of type a and the environment of type Env, except when a Diagnostic is thrown along the evaluation.

Unlike evaluators you have previously written in this course, the Scheme evaluator will *look like imperative code*. Under the hood, the do notation is doing function composition. The following example is part of the evaluator of the define special form for functions:

```
do -- Save the current environment
  env <- get
    -- Create closure value
  val <- (\argVal -> Func argVal body env) <$> mapM getSym args
```

```
-- Modify environment
modify $ H.insert fname val
-- Return void
return Void
```

In order to work with the EvalState monad, you will use the following library functions. To explain briefly, because of how we defined our EvalState with StateT, EvalState is also an instance of the library typeclasses MonadState and MonadError, which provides us with these functions:

```
-- Return the state from the internals of the monad.

get :: MonadState Env EvalState => EvalState Env

-- Specify a new state to replace the state inside the monad.

put :: MonadState Env EvalState => Env -> EvalState ()

-- Monadic state transformer. Taking a function as its argument, it converts

-- the old state to a new state inside the state monad. The old state is lost.

modify :: MonadState Env EvalState => (Env -> Env) -> EvalState ()

-- Used within a monadic computation to begin exception processing. We'll use

-- it to throw `Diagnostic` errors and still return an `EvalState`.

throwError :: MonadError Diagnostic EvalState => Diagnostic -> EvalState a
```

#### Terminology

# 1. Value

A value is just a Val. It's sometimes referred to as "datum".

#### 2. Self-evaluating

We call a datum self-evaluating if it always evaluates to itself. Number and Boolean are self-evaluating.

#### 3. Form

A form is a Scheme datum (Val) that is also a program, that is, it can be fed into the evaluator. It can be a self-evaluating value, a symbol, or a list.

# 4. Special form

A special form is a form with special syntax and special evaluation rules, possibly manipulating the evaluation environment, control flow, or both.

#### 5. Macro

A macro is a form that stands for another form. An application of macro may look like a function application, but it goes through macro expansion first to get translated to the form it stands for, and then the expanded form will be evaluated.

#### 6. Diagnostic

A diagnostic is a run time error thrown along evaluation.

# **Problems**

# Caution

We recommend reading through the *entire* instructions PDF before beginning. Also, the notation may not appear correctly in the .md file, so please do read the PDF.

If you encounter an "unimplemented" error when evaluating a scheme expression in the examples, do not worry. It's up to you to go ahead and implement it, or keep following the order of the handout. You'll eventually implement these features, but you may have to go back and forth.

#### Execution

#### Problem 1. REPL

You'll have to fill in parts of the REPL function from Main.hs, implementing cases for each of the possible results of evaluation. repl :: Env -> IO ().

```
repl :: Env -> IO ()
repl env = do
 putStr "scheme> "
 1 <- getLine</pre>
                                                       -- Read
  case parse exprP "Expression" 1 of
                                                       -- Parse
    Left err -> print err
                                                       -- Diagnostics
   Right expr ->
      case runExcept $ runStateT (eval expr) env of
        -- Insert line here: If error, print error
        -- Insert line here: If return value is void,
                              loop with new env without printing
        -- Insert line here: Otherwise, print and loop with new env
        -- The following line may be removed when you're done implementing
        -- the cases above:
        _ -> print "Error in Main.hs: Finish implementing repl"
 repl env
                                                       -- Loop with old env
```

#### Main function

We've provided a main function for you, which just calls your repl with runtime as the initial environment. The runtime environment is explained further below.

```
main :: IO ()
main = repl runtime
To start the REPL, run stack ghci, then call main.

$ stack ghci
[1 of 4] Compiling Scheme.Core (...)
[2 of 4] Compiling Scheme.Eval (...)
[3 of 4] Compiling Scheme.Parse (...)
[4 of 4] Compiling Scheme.Runtime (...)
[5 of 5] Compiling Main (...)

*Main Scheme.Core Scheme.Eval Scheme.Parse Scheme.Runtime> main
scheme> (cons 'monad '(is just a monoid in the category of endofunctors))
(monad is just a monoid in the category of endofunctors)
scheme>
```

#### **Evaluation**

#### **Evaluator**

Here we will write and test our evaluator.

#### Problem 2. Integer & Boolean, the self-evaluating primitives

Integer and Boolean evaluate to themselves. They are examples of expressions in "normal form". When an expression evaluates, the goal is to continually evaluate it further, until it reaches a normal form.

Here, the notation means that when n is evaluated in environment  $\sigma$ , the result is n.

$$[n \mid \sigma] \downarrow n$$

$$[\#t \mid \sigma] \downarrow \#t$$

$$[\#f \mid \sigma] \downarrow \#f$$

# Problem 3. Symbol

Symbol evaluates to the value that it is bound to in the current environment.

Here, the large vertical bar notation shows a side condition, "where."

$$\llbracket s \mid \sigma \rrbracket \Downarrow v \mid (s \mapsto v) \in \sigma$$

$$[\![s\mid\sigma]\!]\Downarrow \mathtt{UndefSymbolError}\mid(s\mapsto v)\notin\sigma$$

#### Problem 4. Special form define for variables

Now we want to allow the user to define variables. The variable definition form is (define var exp) (an s-expression). var must be a Symbol. The evaluator will evaluate exp and insert to the environment the value as a binding for the symbol. Use modify to mutate the state.

$$\frac{ \llbracket e \mid \sigma \rrbracket \Downarrow v}{ \llbracket (define \; x \; e) \mid \sigma \rrbracket \Downarrow {\tt Void}}$$
 scheme> (define x (+ 10 20))

scheme> x 30

scheme> y

Error: Symbol y is undefined

#### Problem 5. Special form define for functions

We've already given you the ability to define functions. This has the form (define (f params) body). The parameters, body, and environment when the function is declared get wrapped into a Func value. It uses get to retrieve the environment from the state monad, and modify to mutate the state. A Func value is also a normal form.

The semantics for this can be given as follows. (Note: These functions do not allow for recursion.)

$$ps = (p_1 \cdots p_n)$$

$$\llbracket (define\ (f\ ps)\ e)\ |\ \sigma \rrbracket \Downarrow$$
 Func  $ps\ e\ \sigma'\ |\ valid(ps)$ 

$$\llbracket (define\ (f\ ps)\ e)\ |\ \sigma \rrbracket \Downarrow$$
 InvalidSpecialForm  $|\ \neg valid(ps)$ 

What you want to implement is a lambda-function form, (lambda (params) body), which also evaluates to a Func. The lambda creates an anonymous function to be used as a value, although it does not necessarily define it as part of the environment.

```
[(lambda (ps) e) | \sigma] \downarrow Func ps e \sigma | valid(ps)
```

```
[(lambda\ (ps)\ e)\ |\ \sigma]] \downarrow InvalidSpecialForm |\ \neg valid(ps)
scheme > (define x 1)
scheme > (define (inc y) (+ y x))
scheme> (inc 10)
11
scheme > (define x 2)
scheme> (inc 10)
11
scheme > (define (add x y) (+ x y))
scheme> (add 3 4)
scheme > (lambda (x) (+ x 10))
#<function:(lambda (x) ...)>
scheme> ((lambda (x) (+ x 10)) 20)
scheme> (define (mkInc x) (lambda (y) (+ x y)))
scheme > (define i2 (mkInc 2))
scheme> (i2 10)
scheme> (define (fact n) (cond ((< n 1) 1) (else (* n (fact (- n 1))))))
scheme> (fact 5)
120
```

## Problem 6. Special form cond

We should have some sort of if expression, because that's useful. Define the (cond ((c1 e1) ... (cn en))) form. If c1 is true, then e1 is evaluated. If it's false the next condition should be tried.

The last condition, cn, can optionally be symbol else. The expression following else will be evaluated when all previous conditions evaluate to false. If else appears in one of the conditions that is not the last condition, it's an invalid special form (throw an error). If conditions are not exhaustive, i.e. when all conditions evaluate to false, return Void.

$$\llbracket (cond \ ()) \mid \sigma \rrbracket \Downarrow \ Void$$

$$\frac{\llbracket e \mid \sigma \rrbracket \Downarrow}{\llbracket (cond \ ((else \ e)) \mid \sigma \rrbracket \Downarrow v}$$

$$\frac{\llbracket c_1 \mid \sigma \rrbracket \Downarrow \mathsf{Truthy} \quad \llbracket e_1 \mid \sigma \rrbracket \Downarrow v_1}{\llbracket (cond \ ((c_1 \ e_1) \cdots (c_n \ e_n)) \mid \sigma \rrbracket \Downarrow v_1} \text{where Truthy is any non-False value}$$

### Problem 7. Special form let

Define the (let ((x1 e1) ... (xn en)) body) form. The definitions made in ((x1 e1) ... (xn en)) should be added using *simultaneous assignment* to the environment that body is evaluated in. You'll need to check that the expressions being bound (the (x1 e1) ... (xn en)) are well-formed (they are a form with two entries, the first being a variable name).

# Problem 8. Special form let\*

```
Define the (let* ((x1 e1) ... (xn en)) body) form.
```

Special form let\* is like let, but evaluates e1, ..., en one by one, creating a location for each id as soon as the value is available. The ids are bound in the

remaining binding expressions as well as the bodies, and the ids need not be distinct; later bindings shadow earlier bindings.

# Problem 9. Special forms quote, quasiquote and unquote

The special form quote returns its single argument, as written, without evaluating it. This provides a way to include constant symbols and lists, which are not self-evaluating objects, in a program.

The special form quasiquote allows you to quote a value, but selectively evaluate elements of that list. In the simplest case, it is identical to the special form quote. However, when there is a form of pattern (unquote ...) within a quasiquote context, the single argument of the unquote form gets evaluated.

As a homoiconic language, most of Scheme's syntax is exactly the same as the AST representation. There are, however, three special tokens in the *read syntax* (human-readable, to be desugared by the parser to Scheme AST as the internal representation) as a syntactic sugar for quoting, quasi-quoting and unquoting. You do not need to implement the desugaring since it's handled by our parser.

- 'form is equivalent to (quote form)
- `form is equivalent to (quasiquote form)
- ,form is equivalent to (unquote form)

```
scheme> 'a
a
scheme> '5
5
scheme> (quote a)
a
scheme> '*first-val*
*first-val*
scheme> ''a
(quote a)
```

```
scheme> (car (quote (a b c)))
scheme > (car '(a b c))
scheme > (car ''(a b c))
quote
scheme> '(2 3 4)
(234)
scheme> (list (+ 2 3))
(5)
scheme> '( (+ 2 3))
((+23))
scheme> '(+ 2 3)
(+23)
scheme > (eval '(+ 1 2))
scheme> (eval ''(+ 1 2))
(+12)
scheme> (eval (eval ''(+ 1 2)))
scheme> (define a '(+ x 1))
scheme > (define x 5)
scheme> (eval a)
scheme> (define a 5)
scheme> ``(+ ,,a 1)
(quasiquote (+ (unquote 5) 1))
scheme> ``(+ ,,a ,a)
(quasiquote (+ (unquote 5) (unquote a)))
scheme> `(+ a ,,a)
Error: `unquote` not in a `quasiquote context: (unquote (unquote a))`
scheme> ``(+ a ,,a)
(quasiquote (+ a (unquote 5)))
scheme> (eval ``(+ ,,a 1))
(+51)
scheme> (eval (eval ``(+ ,,a 1)))
```

#### Problem 10. Special form define-macro

Define the (define-macro (f params) exp) form which defines a Macro. A Macro almost exactly like a function, except we do evaluation twice. First, we evaluate the body of the macro, processing the arguments as frozen syntactic pieces without evaluating them, and get the resulting syntax blob. Then, we feed the result back into the evaluator to get the final result. In essence, macros use

lazy evaluation.

In your evaluator skeleton, we implemented a special form if for you, but it's commented out. We do not need if as a special form because it can be defined as a macro using cond!

```
scheme> (define-macro (if con then else) `(cond (,con ,then) (else ,else)))
scheme> if
#<macro (con then else) ...>
scheme> (define a 5)
scheme> (if (> a 2) 10 20)
10
scheme> (if (< a 2) 10 20)
20
scheme> (define (fact n) (if (< n 1) 1 (* n (fact (- n 1)))))
scheme> (fact 10)
3628800
scheme> (define-macro (mkplus e) (if (eq? (car e) '-) (cons '+ (cdr e)) e))
scheme> (mkplus (- 5 4))
```

# Problem 11. Application Form

If none of those forms were matched, then assume that the left-most part of the form is to be applied to the rest of the arguments. The format is:

```
(f arg1 ... argn)
```

Recall that the main distinction between macros and non-macros is that a macro manipulates its arguments at the syntax level before actually evaluating them.

- 1. Application when f is a macro
  - 1. Save the environment (Hint: use get to get the environment from the state)
  - 2. Bind arguments (without evaluating them) to the parameters of the macro and insert them to the environment (Hint: use modify to mutate the state)
  - 3. Evaluate the macro body (i.e. expand the macro body)

- 4. Restore the environment we saved in step 1
- 5. Evaluate the expanded form (the result of step 3) and return it

#### 2. Application in other cases

Instead of handling other application form directly in eval, you are going to implement it as a separate function apply :: Val -> [Val] -> EvalState Val. It takes an applicable value (Func, PrimFunc) and applies it to a list of arguments. The list of arguments passed to apply are assumed to have been already evaluated.

In eval, we evaluate the arguments and pass them to apply.

In apply, we are going to handle three cases of first argument:

- If it's a Func:
  - 1. Save the environment
  - 2. Insert bindings of the closure environment to the current environment
  - 3. Bind arguments to the parameters of the function and insert them to the environment
  - 4. Evaluate the function body
  - 5. Restore the environment we saved in step 1
  - 6. Return the result of step 4
- If it's a PrimFunc, we directly apply the primitive function to the argument list
- Otherwise, throw a diagnostic CannotApply.

# Runtime Library

The constant runtime is the initial runtime environment for the repl; it is a map from String (identifiers) to Val (values). This will be used to hold the values of defined constants, operators, and functions. The main call to repl should provide this runtime as the starting environment. (It is also possible to call repl with a different starting environment for experimental purposes.)

You need to initialize runtime with predefined primitive operators as well. This will make these operators available to users of your language. Some of them have already been filled in, however you will need to implement the rest.

You will not be able to do this right away! Even the cases that have been filled in use functions that are unimplemented. You'll need to implement a variety of lifting functions and primitive functions first.

We have provided the following translators to go between Scheme values and Haskell values. These can help when defining the various operator lifters.

```
-- Primitive function `symbol?` predicate
isSymbol :: [Val] -> EvalState Val
isSymbol [Symbol _] = return $ Boolean True
isSymbol [_] = return $ Boolean False
isSymbol vv = throwError $ UnexpectedArgs vv

-- Primitive function `list?` predicate
isList :: [Val] -> EvalState Val
isList [v] =
   return . Boolean $ case flattenList v of
   List _ -> True
   _ -> False
isList vv = throwError $ UnexpectedArgs vv
```

You can test your runtime using the REPL. Implement the REPL first!

#### **Operators**

Problem 12. Variadic arithmetic operators (+, -, \*, /): implement liftIntVargOp

Note: In this release of the assignment, this function has already been provided for you.

You need to implement liftIntVargOp that takes an operator and a base-case. If the supplied list of values is empty, then the base-case (lifted into the Scheme world) is used. If it's non-empty, then the operator is applied between all the elements of the list.

You should use liftIntVargOp to construct a PrimFunc for +, -, \*, and /, and put it in runtime.

```
scheme> (+ 3 4 5)
12
```

```
scheme> (- 3 4 5)

-6

scheme> (-)

0

scheme> (+)

0

scheme> (* 3 5 9)

135
```

# Problem 13. Variadic boolean operators (and, or): implement liftBoolVargOp

Unlike arithmetic operators which we have to apply pairwise to the list, variadic boolean operators, and and or, are provided by Haskell Prelude. You simply have to implement liftBoolVargOp to lift a function of type [Bool] -> Bool to a PrimFunc.

Boolean rule of thumb: In Scheme, everything except #f is considered true.

Note that you'll need eval working on at least the quote form for these examples and tests to work.

```
scheme> (and #t #t #t 'nil)
#t
scheme> (and #t #t #t #f)
#f
scheme> (and)
#t
scheme> (or)
#f
scheme> (or 't #t)
#t
scheme> (or 'to-be 'not-to-be)
#t
scheme> (or #f #f #f #f)
#f
scheme> (and 3 2 5)
#t
scheme> (and 3 2 5 #f)
#f
scheme> (or 3 2 5)
#t
```

Add boolean operators and and or to your runtime environment.

#### Problem 14. Binary comparison operators:

- > Integer greater than
- $\bullet$  < Integer less than
- >= Integer greater than or equal
- <= Integer less than or equal

You should use liftCompOp for these. liftCompOp takes an integer comparison function in Haskell and lifts it to a variadic Scheme comparison operator. If the list is empty it should return Scheme's True, i.e. Boolean True. If the list is larger, it should compare the elements of the list pair-wise using the given operator and then logically and all of those together.

```
scheme> (< 3 4 5)
#t
scheme> (>= 3 4 2)
#f
scheme> (>=)
#t
scheme> (>= 7)
#t
```

#### Problem 15. List operators

These are the functions for composing and decomposing lists. For historical background on the naming of these functions, you might want to read this article:

https://en.wikipedia.org/wiki/CAR and CDR

- car :: [Val] -> EvalState Val

  Get the first element of the list or dotted list (single argument)
- cdr :: [Val] -> EvalState Val

  Get the rest of the list or dotted list (single argument)
- cons :: [Val] -> EvalState Val: Construct a DottedList from 2 arguments
- list :: [Val]  $\rightarrow$  EvalState Val: Construct a List from as many arguments as given (hence it's variadic)

You must check the number of arguments, verify argument types, and throw appropriate Diagnostics on mismatch.

```
scheme> (car)
Error: Unexpected arguments ()
scheme> (cdr)
Error: Unexpected arguments ()
scheme> (car '(3 5))
3
scheme> (cdr '(3 5 6 7))
```

```
(567)
scheme > (cdr '(3 5 . 6))
(5.6)
scheme > (cdr '(3 5 . (6 . 7)))
(56.7)
scheme> (list (> 3 4) #t 15 #f (< 5 2 3 5) (cons 3 (cons 4 3)))
(#f #t 15 #f #f (3 . (4 . 3)))
scheme > (car (cons 'a 'b))
scheme > (cdr (cons 'a 'b))
scheme> (car (list 'a 'b 'c))
scheme > (cdr (list 'a 'b 'c))
(b c)
scheme > (cdr (list 'a))
()
scheme> (cdr 'a)
Error: Unexpected arguments (a)
scheme> (cons 2 (cons 3 4))
(2 3 . 4)
scheme > (cons 2 (cons 3 (cons 4 #f)))
(2 3 4 . #f)
scheme> (cons 4 (cons 2 (cons 1 '('cs421 'is 'easy . ()))))
(4 2 1 (quote cs421) (quote is) (quote easy))
```

We want to put these unary operators in our runtime, which means we'll need to wrap them in a PrimFunc.

#### Problem 16. Unary boolean operator (not)

not is implemented for you. It's lifted from Haskell by liftBoolUnaryOp.

```
scheme> (not #t)
#f
scheme> (not #f)
#t
scheme> (not 'mattox)
#f
scheme> (not 'false)
#f
scheme> (not)
Error: Unexpected arguments ()
scheme> (not #f #t)
Error: Unexpected arguments (#f #t)
scheme> (not 'nil #t 3)
```

```
Error: Unexpected arguments (nil #t 3)
scheme> (not 3)
#f
```

# Problem 17. Equality (=, eq?)

You will implement two variants of Scheme's equality:

• =

Equality for numbers and booleans, throwing TypeError on type mismatch or unsupported types such as function

eq?

Equality for atom values, including numbers, booleans, and symbols, returning #f on type mismatch or unsupported types (not throwing diagnostics!)

Both = and eq are variadic with default value #t.

```
scheme> (=)
#t
scheme> (= #f)
#t
scheme> (= #t #f #t)
#f
scheme> (= 1 1)
#t
scheme> (= 3 3 2)
#f
scheme> (= 'a)
Error: Value a has unexpected type Symbol
scheme> (eq? 3 3 2)
#f
scheme> (eq? 'a 'a)
#t
```

#### Problem 18. Modulo (modulo)

Implement the modulo function (a binary operator taking two integers, and finding the remainder of one divided by the other, in accordance with Haskell's mod operator). Use liftIntBinOp.

```
scheme> (modulo)
Error: Unexpected arguments ()
scheme> (modulo 1)
Error: Unexpected arguments (1)
scheme> (modulo 1 5)
1
```

```
scheme> (modulo 5 1)
0
scheme> (modulo 5 2)
1
scheme> (modulo 6 (- 3))
0
scheme> (modulo (- 3) 1)
0
scheme> (modulo 7 (- 3))
-2
scheme> (modulo (- 7) 2)
1
scheme> (modulo 9 4)
```

# Problem 19. Abs (abs)

Implement the abs function, which calculates the absolute value of the given integer. Use liftIntUnaryOp.

```
scheme> (abs)
Error: Unexpected arguments ()
scheme> (abs 1)
1
scheme> (abs 1 2)
Error: Unexpected arguments (1 2)
scheme> (abs (- 5))
```

# Problem 20. Dynamic Type Tests (symbol?, list?, pair?, number?, boolean?, null?)

A check that takes exactly one argument of any type, and returns whether the argument is of the corresponding type. The less obvious tests here are the list? test, which checks whether a "flattened" version of the list is really a list, the pair? test, which accepts either lists or dotted lists, and the null? test, which checks for an empty list.

```
scheme> (symbol? 'a)
#t
scheme> (symbol? 'b)
#t
scheme> (symbol?)
Error: Unexpected arguments ()
scheme> (symbol? 3)
#f
```

```
scheme> (list? '(3 5))
scheme> (list? '())
scheme > (list? '(3 . (6 . 7)))
scheme> (list? '(3 5 . 6))
#f
scheme> (list? '(3 5 (6 . 7)))
scheme> (list? 3)
scheme> (list? 3 5)
Error: Unexpected arguments (3 5)
scheme> (list?)
Error: Unexpected arguments ()
scheme> (pair?)
Error: Unexpected arguments ()
scheme> (pair? 3)
scheme > (pair? '(3 . 6))
scheme > (pair? '(3 5))
scheme> (number? '(3))
scheme> (pair? '())
scheme> (number? 3)
scheme> (boolean? 3)
scheme> (boolean? #f)
scheme> (number? #t)
#f
scheme> (number?)
Error: Unexpected arguments ()
scheme> (boolean? 3 #f)
Error: Unexpected arguments (3 #f)
scheme> (null? '())
scheme> (null? '('()))
scheme> (null? '(3 5))
#f
```

```
scheme> (null?)
Error: Unexpected arguments ()
```

# Further steps

# Problem 21. Extend the Runtime Library

Now that our evaluator is fully functional, we can implement the following functions that make use of the evaluator.

```
-- Primitive function `apply`
-- It applies a function to a list of parameters
-- Examples:
-- (apply + '(1 2 3)) => 6
-- (apply car '((1 2 3))) => 1
applyPrim :: [Val] -> EvalState Val
applyPrim = undefined
-- Primitive function `eval`
-- It evaluates the single argument as an expression
-- All you have to do is to check the number of arguments and
-- feed the single argument to the evaluator!
-- Examples:
-- (eval '(+ 1 2 3)) => 6
evalPrim :: [Val] -> EvalState Val
evalPrim = undefined
```

Now, add these functions to the runtime and test them.

# Testing

Aside from the provided testcases, you may want to manually enter the examples shown above, to observe that everything is working correctly (and for your benefit).

# Finally, more cool stuff

This section is not graded, but you'll absolutely love it.

Now you have finished the MP! We believe that you've had a lot of fun implementing Scheme. But the fun doesn't end here—what you have implemented is merely a subset of Scheme. Try to implement a few tasks below:

1. More parsing capabilities

- The parser for the current REPL supports one expression per line. But you can extend it to accept multiple expressions in a single line.
- Accepting file inputs will also be an important feature for a real programming language.
- Comments begin with; and continue until the end of the line.

#### 2. Memory model and side effects

The subset of Scheme you've implemented so far is purely functional, but Scheme is not a purely functional language. Special form set! is used to modify a variable. Scheme also has a memory model, which has reference semantics. In particular, a closure that captures the environment is treated as a "heap object", which gets passed by reference.

For example, Scheme lets us define a counter without using any global variables:

Hint: You'll need to give Env an overhaul, simulate pointers (for which you might need the IORef monad), and properly handle global scoping and lexical scoping.

#### 3. Higher-order functions

Why not implement map and reduce in Scheme? Create your own functional library in Scheme, store the functions in a file, and load it every time you start the REPL.

#### 4. Metacircular evaluator

Data is code. Code is data.

With all the primitive functions that you implemented, did you know you can implement a Scheme evaluator in Scheme? Try to implement eval directly in Scheme!

```
scheme> (eval '(+ 1 2 3))
6
scheme> (eval '(apply + '(1 2 3)))
6
```

Here's an introduction to the metacircular evaluator in one page:

https://xuanji.appspot.com/isicp/4-1-metacircular.html

5. Learn everything else from SICP

Structure and Interpretation of Computer Programs is an excellent textbook for teaching the principles of programming.

Special thanks to Richard Wei for major contributions to this MP.