The University of Texas
at Austin

CS383C Numerical Analysis

Homework 03

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Department of Computer Science

STUDENT
Jimmy Lin
xl5224

COURSE COORDINATOR
Robert A. van de Geijn

UNIQUE NUMBER
53180

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Exercise 1. Classical Gram-Schmidt (CGS)

```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%% Project 01: CGS
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

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%                http://www.cs.utexas.edu/users/flame/license.html
%
% Programmed by: Jimmy Lin
%                jimmylin@utexas.edu

function [ A_out, R_out ] = CGS_unb( A, R )

  [ AL, AR ] = FLA_Part_1x2( A, ...
                             0, 'FLA_LEFT' );

  [ RTL, RTR, ...
    RBL, RBR ] = FLA_Part_2x2( R, ...
                               0, 0, 'FLA_TL' );

  while ( size( AL, 2 ) < size( A, 2 ) )

    [ A0, a1, A2 ]= FLA_Repart_1x2_to_1x3( AL, AR, ...
                                           1, 'FLA_RIGHT' );

    [ R00,  r01,   R02,  ...
      r10t, rho11, r12t, ...
      R20,  r21,   R22 ] = FLA_Repart_2x2_to_3x3( RTL, RTR, ...
                                                  RBL, RBR, ...
                                                  1, 1, 'FLA_BR' );

    %------------------------------------------------------------%

    r01 = A0' * a1;
    a1 = a1 - A0 * r01;
    rho11 = norm(a1, 2);
    a1 = a1 / rho11;

    %------------------------------------------------------------%

    [ AL, AR ] = FLA_Cont_with_1x3_to_1x2( A0, a1, A2, ...
                                           'FLA_LEFT' );

    [ RTL, RTR, ...
      RBL, RBR ] = FLA_Cont_with_3x3_to_2x2( R00,  r01,   R02,  ...
                                             r10t, rho11, r12t, ...
                                             R20,  r21,   R22, ...
                                             'FLA_TL' );

  end

  A_out = [ AL, AR ];

  R_out = [ RTL, RTR
            RBL, RBR ];

return
```

Exercise 2. Modified Gram-Schmidt (MGS)

```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%% Project 01: MGS (Alternative)
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

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function [ A_out, R_out ] = MGS_unb( A, R )

  [ AL, AR ] = FLA_Part_1x2( A, ...
                             0, 'FLA_LEFT' );

  [ RTL, RTR, ...
    RBL, RBR ] = FLA_Part_2x2( R, ...
                             0, 0, 'FLA_TL' );

  while ( size( AL, 2 ) < size( A, 2 ) )

    [ A0, a1, A2 ]= FLA_Repart_1x2_to_1x3( AL, AR, ...
                                       1, 'FLA_RIGHT' );

    [ R00,  r01,   R02,  ...
      r10t, rho11, r12t, ...
      R20,  r21,   R22 ] = FLA_Repart_2x2_to_3x3( RTL, RTR, ...
                                                  RBL, RBR, ...
                                                  1, 1, 'FLA_BR' );

    %------------------------------------------------------------%

    rho11 = norm(a1);
    a1 = a1 / rho11;
    r12t = a1' * A2;
    A2 = A2 - a1 * r12t;

    %------------------------------------------------------------%

    [ AL, AR ] = FLA_Cont_with_1x3_to_1x2( A0, a1, A2, ...
                                       'FLA_LEFT' );

    [ RTL, RTR, ...
      RBL, RBR ] = FLA_Cont_with_3x3_to_2x2( R00,  r01,   R02,  ...
                                             r10t, rho11, r12t, ...
                                             R20,  r21,   R22, ...
                                             'FLA_TL' );

  end

  A_out = [ AL, AR ];

  R_out = [ RTL, RTR
            RBL, RBR ];

return
```

Exercise 3. Householder QR Transformation

```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%% Project 01: Householder QR Transformation
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

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% Programmed by: Jimmy Lin
%                jimmylin@utexas.edu

function [ A_out, T_out ] = HQR_unb ( A, T )

  [ ATL, ATR, ...
    ABL, ABR ] = FLA_Part_2x2( A, ...
                               0, 0, 'FLA_TL' );

  [ TT, ...
    TB ] = FLA_Part_2x1( T, ...
                         0, 'FLA_TOP' );

  while ( size( ATL, 1 ) < size( A, 1 ) )

    [ A00,  a01,     A02,  ...
      a10t, alpha11, a12t, ...
      A20,  a21,     A22 ] = FLA_Repart_2x2_to_3x3( ATL, ATR, ...
                                                    ABL, ABR, ...
                                                    1, 1, 'FLA_BR' );
    [ T0, ...
      t1t, ...
      T2 ] = FLA_Repart_2x1_to_3x1( TT, ...
                                    TB, ...
                                    1, 'FLA_BOTTOM' );
    %------------------------------------------------------------%

    [ alpha11, a21, t1t ] = Housev( alpha11, a21 );
    w12t = (a12t + a21' * A22) / t1t;
    a12t = a12t - w12t;
    A22 = A22 - a21 * w12t;

    %------------------------------------------------------------%

    [ ATL, ATR, ...
      ABL, ABR ] = FLA_Cont_with_3x3_to_2x2( A00,  a01,     A02,  ...
                                             a10t, alpha11, a12t, ...
                                             A20,  a21,     A22, ...
                                             'FLA_TL' );
    [ TT, ...
      TB ] = FLA_Cont_with_3x1_to_2x1( T0, ...
                                       t1t, ...
                                       T2, ...
                                       'FLA_TOP' );
  end

  A_out = [ ATL, ATR
            ABL, ABR ];
  T_out = [ TT
            TB ];
return
```

Exercise 4. FormQ algorithm

```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%% Project 01: FormQ_unb algorithm
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

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% Programmed by: Jimmy Lin
%                jimmylin@utexas.edu

function [ A_out, T_out ] = FORMQ_unb ( A, T )

  [ ATL, ATR, ...
    ABL, ABR ] = FLA_Part_2x2( A, ...
                               0, 0, 'FLA_BR' );

  [ TT, ...
    TB ] = FLA_Part_2x1( T, ...
                         0, 'FLA_BOTTOM' );

  while ( size( ABR, 1 ) < size( A, 1 ) )
    [ A00,  a01,     A02,  ...
      a10t, alpha11, a12t, ...
      A20,  a21,     A22 ] = FLA_Repart_2x2_to_3x3( ATL, ATR, ...
                                                    ABL, ABR, ...
                                                    1, 1, 'FLA_TL' );
    [ T0, ...
      t1t, ...
      T2 ] = FLA_Repart_2x1_to_3x1( TT, ...
                                    TB, ...
                                    1, 'FLA_TOP' );
    %------------------------------------------------------------%

    alpha11 = 1 - 1 / t1t;
    a12t = - (a21' * A22) / t1t;
    A22 = A22 + a21 * a12t;
    a21 = - a21 / t1t;

    %------------------------------------------------------------%

    [ ATL, ATR, ...
      ABL, ABR ] = FLA_Cont_with_3x3_to_2x2( A00,  a01,     A02,  ...
                                             a10t, alpha11, a12t, ...
                                             A20,  a21,     A22, ...
                                             'FLA_BR' );

    [ TT, ...
      TB ] = FLA_Cont_with_3x1_to_2x1( T0, ...
                                       t1t, ...
                                       T2, ...
                                       'FLA_BOTTOM' );
  end

  A_out = [ ATL, ATR
            ABL, ABR ];
  T_out = [ TT
            TB ];

return
```