

CHEM 123: Summary of Important Concepts

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Thermodynamics

Equation/Concept	Info About Equation/Concept
System	The system is defined as a group of material and/or radiative contents. It's properties can be fully described by thermodynamic state variables.
Boundary	The boundary is the edge of a system. It may be a conceptual boundary or a real boundary.
Surroundings	The entire universe outside of the system and its boundary.
Isolated System	A system where neither energy nor mass can cross between the system and surroundings. The only truly isolated system is the entire universe, though we can produce approximately isolated systems (i.e. a well-insulated thermos).
Closed System	A system where energy can exchange with the environment, but mass cannot. A good example of a closed system would be a car's cooling system: when the car is on, heat moves from the radiator into the environment, but no coolant leaves the system.
Open System	A system where both energy and mass may freely exchange with the environment. Examples include open flask or cup of coffee.
State Variable	State variables are variables that describe the thermodynamic state (i.e. the conditions) of a system. They are only well-defined for systems in equilibrium. State variables do not depend on the path taken to get to a given thermodynamic state. Examples: temperature, pressure, internal energy, enthalpy, Gibbs free energy, entropy, volume, density, mass, particle number, and concentration.
Path Variable	Path variables, unlike state variables, are non-zero only during a change in a system's thermodynamic state (i.e. when not at equilibrium). Path variables depend on the particular way in which a system evolves through time from one state to another. Heat and work are the only path variables used in this course.
Intensive Variable	These are variables that are independent of the system size. Examples include: temperature, energy density, pressure, density, concentration, and specific heat capacity. The ratio of two intensive variables is still intensive.
Extensive Variable	Extensive variables are variables that are proportional to the size of the system. If the system grows, then so do all extensive variables that describe the system. Examples include: internal energy, entropy, volume, mass, particle number, heat capacity. Dividing one extensive state variable by another will always produce an intensive variable because the system size dependence will cancel out.
Equation of State	At equilibrium, state variables are not independent from one another. An equation of state defines the particular relationship between state variables. Equations of state for real systems are often extremely complicated and may not have a closed form, but certain model systems can have fairly simple and useful relationships. For example, the ideal gas law is an equation of state that describes the relationship between state variables for a model gas system in which the particles of gas occupy zero volume (are point particles) and do not interact with each other. Although the ideal gas equation does not perfectly describe any gases in our universe, it becomes a very good approximation for dilute monatomic gases at high temperature.
Internal Energy (E or U)	Internal energy is the sum total of all forms of energy within a system. It includes all forms of potential energy, translational energy, rotational energy, and vibrational energy. Generally, the total internal energy of a system is very difficult to measure, but changes in internal energy can be readily measured.
Heat (q)	Heat is the quantity of energy that transfers between the system and surroundings due to a difference in temperature. When heat is absorbed by the system, q is positive. When heat is removed from the system into the surroundings, q is negative. Heat only exists during a change in the system, it is a path variable.
Work (w)	Work is the energy transfer between system and surroundings due to a force applied over a distance. Work is associated with either an expansion (work done <i>by the system</i> , negative w) or a contraction (work done <i>on the system</i> , positive w) of the system. Work only exists during a change in the system, it is a path variable.

Equation/Concept	Info About Equation/Concept
Zeroth Law of Thermodynamics	<i>Two systems that are separately in thermal equilibrium with a third system are also in thermal equilibrium with one another.</i> This law was only formulated after the first three laws of thermodynamics were already written down, but is more fundamental in nature than the other three.
$\Delta E = q + w$	This is the equation for the first law of thermodynamics. It states that the change in energy <i>of the system</i> is equal to the heat flow q into the system (positive q is heat flow <i>into</i> the system) plus the work done on the system w . Work done <i>on the system</i> corresponds to positive w . This is simply a statement of the conservation of energy and only applies <i>for a particular path</i> .
$\Delta E = q_V$	Change in internal energy when the volume of the system remains constant. The subscript simply indicates that the heat is exchanged at constant volume.
$\delta w = -P_{\text{ext}}dV$	The most general definition of the increment of work. This equation is for the <i>improper</i> increment of work done <i>on</i> the system. It is improper because work is a path variable, so the increment of work done is not an exact differential.
$w = -\int_{V_i}^{V_f} P_{\text{ext}}dV$	The definition of total work done on the system for a process. It is the integral from the initial volume to the final volume of the incremental amounts of work done along that path. This can be conceptualized as adding up the tiny increments of work δw from the initial state to the final state. This is the most general expression for work done.
$w = -nRT \ln\left(\frac{V_f}{V_i}\right)$	This is the work done on an <i>ideal gas</i> expanding/contracting <i>reversibly and isothermally</i> . In this situation, $P_{\text{ext}} = P_{\text{sys}} = \frac{nRT}{V}$ at every point along the path, so the above integral can be solved analytically to obtain the result shown.
$w = -P_{\text{ext}}\Delta V$	This is the work done on a system with constant external pressure. This follows directly from the definition of total work done for the case in which P_{ext} is a constant.
Ideal Gas	An ideal gas is defined as a collection of point particles that do not interact with each other, but interact with the walls of their container elastically (i.e. energy and momentum is conserved for each collision). Ideal gas particles have masses, but the equation of state for ideal gases (ideal gas law) does not depend on particle mass. The internal energy of an ideal gas is $U = c_V nRT$, where c_V is the specific heat capacity at constant volume (approximately $\frac{3}{2}$ for a monatomic gas), n is the number of moles of gas, and T is the temperature. Hence the internal energy of an ideal gas only depends on T as long as the number of moles is held constant.
$PV = nRT$	This is the ideal gas law. It is the <i>equation of state</i> for a gas of point particles that do not interact with each other. P is the pressure of the system, V is the volume of the system, n is the number of moles of gas, R is the gas constant, and T is the absolute temperature. This equation works well to approximate the equation of state for real gases at low P and high T .
$P = \sum_i P_i = \sum_i \frac{n_i RT}{V}$	The equation of state for a mixture of ideal gases. P_i is called the partial pressure of gas i . The sum of the partial pressures for all gases in a mixture equals the total pressure. This is strictly true only for ideal gases, but is a good approximation otherwise.
$x_i = \frac{P_i}{P} = \frac{n_i}{n}$	For ideal gases only, the partial pressure for a component i in a mixture of ideal gases is proportional to the number of moles n . The partial pressure P_i divided by the total pressure is just $\frac{n_i}{n}$, known as the mole fraction x_i .
Isothermal Process	An isothermal process is a process that remains at a constant temperature along the entire path from its initial state to its final state.
Constant T Process	A process whose initial and final states have the same temperature, but may change temperature along the path between states.
Adiabatic Process	A process that occurs without exchange of heat at any point along the path. Adiabatic walls are system boundaries that do not allow exchange of heat. They are the walls of an isolated system. Inversely, Diathermal walls are boundaries that do allow heat exchange.

Equation/Concept	Info About Equation/Concept
Reversible Process	An idealistic process that moves from one state to another while remaining in equilibrium with the surroundings along the entire path. Reversible processes would necessarily occur over an infinite amount of time, and so are not actually possible. A reversible process represents the upper limit on the possible work that can be extracted by an expanding gas, as well as the lower limit on the amount of work required to compress a gas. Reversible processes are called “reversible” because they require the same but opposite amount of work and heat to run backwards as forwards.
Isobaric Process	An isobaric process is a process that occurs with no change in pressure along the entire path from initial to final state.
Isochoric Process	An isochoric process is a process that occurs with no change in volume along the entire path from initial to final state.
Heat Capacity C	Heat capacity is defined as the amount of energy required to raise the temperature of a system by 1 K. It is an extensive state variable, but may be made intensive by dividing by either the mass of the system or the number of moles.
$c_{sp} = \frac{C}{m}$	c_{sp} is called the specific heat capacity. It is an intensive state variable because it is the ratio of two extensive state variables. Here m is the mass of the system.
$c_m = \frac{C}{n}$	c_m is called the molar heat capacity. It is an intensive state variable because it is the ratio of two extensive state variables. Here n is the number of moles in the system.
$q = C\Delta T = mc_{sp}\Delta T = nc_m\Delta T$	The heat flow into the system is the product of the heat capacity C and the change in temperature $\Delta T = T_f - T_i$. Note that C is an extensive variable. This is only truly applicable for small changes in temperature, as C a temperature dependent state variable.
$H = E + PV$	Definition of enthalpy. Enthalpy is an extensive state variable which is most useful in constant pressure conditions and at equilibrium when $P = P_{ext}$. In this case, $\Delta H = q_p$ where q_p is the heat flow at constant pressure. Since pressure is often held constant in chemistry, enthalpy is a very useful state variable. The heat flow of a reaction is simply the change in enthalpy at constant pressure, so the enthalpy of formation for a reaction is quite easy to measure.
$\Delta H = \Delta E + P\Delta V$	The change in enthalpy for a constant pressure process. When a process results in $\Delta H < 0$ it is called exothermic and when a process results in $\Delta H > 0$ it is called endothermic . Reaction enthalpy alone is not enough to determine whether or not the process will proceed spontaneously.
Standard State	An arbitrary but agreed-up standard set of conditions for which many experimental state variables are measured: $P = 1 \text{ bar} \approx 1 \text{ atm}$ and either a pure substance or a 1 M solution. The standard state does not specify a temperature, but a separate term, standard temperature, is defined as $T = 273.15 \text{ K}$ while standard <i>ambient</i> temperature is defined as $T = 298.15 \text{ K}$.
ΔH_f°	ΔH_f° is the standard enthalpy of formation , sometimes called the standard heat of formation . It is defined as the change in enthalpy required to create one mole of a given substance at standard pressure (1 bar) starting from the compound’s constituent elements in their standard states. The standard enthalpy of formation of any pure element in its standard state is then, by definition, 0 kJ mol^{-1} . Because ΔH_f° depends on temperature, the temperature must be defined, although it is often assumed to be 298.15 K .
$\Delta H_{\text{rxn}}^\circ = \sum_P \Delta H_{\text{f,P}}^\circ - \sum_R \Delta H_{\text{f,R}}^\circ$	Hess’s Law. This law applies equally well to any state variable, such as total energy, entropy, etc. It is a reflection of the fact that the change in a state variable does not depend on the path taken. Here, P refers to products and R refers to reactants. Hess’s law tells us that we can sum up as many processes as we wish in order to “build up” the value of an unknown state variable (such as enthalpy) from a set of known ones.

Equation/Concept	Info About Equation/Concept
Entropy S	Entropy is an extensive state variable that can be thought of as a measure of the dispersal of energy within a system. Many people think of entropy as a measure of system disorder, but this is an imprecise and often wrong definition. Entropy is actually a measure of the number of possible microstates that would give rise to a given macrostate. For macrostates with a large number of potential microstates, entropy is high. From this we can see that very highly ordered macrostates will tend to (but not always) have relatively few microstates compatible with the macrostate, whereas disordered macrostates will have a high number of associated microstates.
General Cases of $\Delta S > 0$	Entropy generally increases when: temperature increases; pure liquids or solutions are formed from solids; the number of molecules of gas increases from a reaction; there is a decrease in pressure; and gases are formed from liquids.
$\Delta S_{\text{Universe}} \geq 0$	The second law of thermodynamics. The equality is only satisfied for reversible processes or systems in equilibrium, for all non-reversible processes the inequality is true. Here $\Delta S_{\text{Universe}}$ is the change in entropy of the <i>entire universe</i> as a result of a process. Any process that proceeds must satisfy this inequality, but not every process that satisfies the inequality will proceed quickly (or at all). For example, the formation of graphite from diamond is favoured by entropy, but the reaction rate is essentially zero at ambient temperature.
$dS = \frac{dq_{\text{rev}}}{T_{\text{Surr}}}$	This is one definition of entropy. It is calculable only along a reversible path, but since once calculated the resulting ΔS applies to any path between the initial and final state.
$dS \geq \frac{dq}{T_{\text{Surr}}}$	The Clausius inequality. This is another expression of the second law of thermodynamics, and is only equal for a reversible process. This inequality states that for irreversible processes, it is not possible to pass heat between system and surroundings without increasing the entropy of the universe. Whichever body (system or surroundings) receives heat during a process must increase its entropy more than is lost by the body that is cooled.
$\Delta S = \frac{q_{\text{rev}}}{T}$	True for constant T , reversible heat exchange only. This equation is often used to measure changes in entropy by following a pseudo-reversible path.
$G = H - TS$	Definition of Gibbs free energy. Gibbs free energy is the criterion for determining if a reaction mixture will evolve towards reactants or products when the system is at constant P and T . Reactions in which $\Delta G < 0$ are said to be exergonic . Exergonic reactions are always spontaneous at constant T and P (but may not proceed quickly due to kinetic effects). Reactions with $\Delta G > 0$ are called endergonic , and are not spontaneous at constant T and P .
$\Delta G_{\text{System}} = -T\Delta S_{\text{Universe}}$	At constant temperature and pressure , the change in Gibbs free energy of the system tells us whether or not a process increases the entropy of the universe. Since T is always positive, and $\Delta S_{\text{Universe}}$ must be positive for a process to proceed, a negative ΔG corresponds to a process that <i>may</i> proceed spontaneously, as long as the activation barrier is much greater than $k_B T$.
$\Delta G^\circ = -RT \ln(K)$ $= \Delta H^\circ - T\Delta S^\circ$ $K = \exp\left(\frac{-\Delta G^\circ}{RT}\right)$	The standard Gibbs free energy. ΔG° is the Gibbs free energy change per mole of reaction of pure reactants to pure products at standard conditions (298 K, 1 atm, solutions at 1 mol L ⁻¹ concentration, pure liquids and solids). K is the equilibrium constant for that reaction. $\Delta G^\circ < 0$ indicates products are favoured; $\Delta G^\circ > 0$ indicates reactants are favoured.
$S = k_B \ln(\Omega)$	The definition of entropy for an isolated system. Ω is the number of possible microstates and k_B is the Boltzmann constant, which is included to convert the units.
$\Delta G = \Delta H - T\Delta S$	The change in Gibbs free energy for a process done at constant temperature (although ΔH is most useful at constant P and T).
$\Delta G = \Delta G^\circ + RT \ln Q$	This equation can be used to predict the direction of a reaction. Q is called the “reaction quotient”, and is the same as the equilibrium constant K , but calculated when a reaction has not yet reached equilibrium. $\Delta G < 0$ indicates that there are too many reactants and the reaction will favour products. $\Delta G > 0$ indicates that the reaction will proceed to the reactants side.

Equation/Concept	Info About Equation/Concept
$K = \frac{[\text{Products}]}{[\text{Reactants}]}$	The definition of the equilibrium constant. Square brackets indicate concentrations, and the concentrations should be raised to the power of their stoichiometric coefficients.
$\Delta G = -T\Delta S_{\text{Universe}}$	This equation applies at constant temperature and pressure for a system. It is the reason that the change in Gibbs free energy is a measure of spontaneity under those conditions. $\Delta G < 0$ corresponds to an increase in the entropy of the universe when T and P are held fixed.
$\ln K = \frac{-\Delta H^\circ}{R} \frac{1}{T} + \frac{\Delta S^\circ}{R}$	The equation that describes a Van't Hoff plot: plot $\ln K$ vs $\frac{1}{T}$. The slope $m = \frac{-\Delta H^\circ}{R}$ and the y -intercept $b = \frac{\Delta S^\circ}{R}$. Using these plots assumes that the standard change in enthalpy and standard change in entropy are independent of T . This is only true for small changes in T . If the slope $m > 0$ then $\Delta H^\circ < 0$ and the reaction is exothermic. If $m < 0$ then $\Delta H^\circ > 0$ and the reaction is endothermic.
S°	The standard molar entropy. This is the absolute entropy of 1 mole of a substance in its standard state, usually measured at 298 K. By the third law, this is non-zero.
$S_{0\text{ K, perfect crystal}} = 0$	The third law of thermodynamics. Here $S_{0\text{ K, perfect crystal}}$ refers to the entropy of a pure, perfectly crystalline solid at 0 K. The third law of thermodynamics gives us a reference point to define the zero of entropy. Basically, it states that there's only one possible microstate for a perfect crystal with no internal energy. The entropy for a system with only one microstate is $S = k_B \ln(1) = 0$.

For constant T and P processes, $\Delta G = \Delta H - T\Delta S$:

Sign of ΔH	Sign of ΔS	Sign of ΔG	Spontaneous?
+	+	+ (Low T) OR - (High T)	At High T
+	-	+	Never
-	+	-	Always
-	-	+ (High T) OR - (Low T)	At Low T

Thermodynamics of Acids and Bases

Equation/Concept	Info About Equation/Concept
Le Chatelier's Principle	A useful principle used to predict the response of equilibrium reactions to the application of some change to the system's equilibrium. If a change in pressure, temperature, volume, or concentration of a reactant is applied to a system in equilibrium, the equilibrium will respond by shifting so as to partly counteract the effect of the change.
$K_a = \frac{[H_3O^+][A^-]}{[AH]}$	Definition of the acid dissociation constant. This is simply the equilibrium constant for acid reactions. AH is an arbitrary acid and A^- is its conjugate base. Concentrations should all be raised to the power of their stoichiometric coefficients. Strong acids have very large K_b values ($K_a \gg 1$) while weak acids tend to have $K_a < 1$.
$K_b = \frac{[OH^-][BH^+]}{[B]}$	Definition of the base dissociation constant. This is simply the equilibrium constant for base reactions. B is an arbitrary base and BH^+ is its conjugate acid. Concentrations should all be raised to the power of their stoichiometric coefficients. Strong bases have very large K_b values ($K_b \gg 1$) while weak bases tend to have $K_b < 1$.
Strong Acids and Bases	Strong acids to know: HCl , HBr , HI , H_2SO_4 , HNO_3 , $HClO_4$. Strong bases to know: $NaOH$, KOH , $Ca(OH)_2$. Strong acids and bases almost completely dissociate in solution, and thus have extremely high K_a and K_b values, respectively.
Buffer Solution	A solution containing an acid and its conjugate base in comparable concentrations ($10 \geq \frac{[Acid]}{[Base]} \geq 0.1$). Buffers resist large changes in pH brought on by addition of strong acids or bases by providing sources that neutralize both H^+ or OH^- in solution. Buffers always have $pH = pK_a \pm 1$ and $pOH = pK_b \pm 1$.

Equation/Concept	Info About Equation/Concept
$K_W = K_a K_b = [H_3O^+][OH^-]$	Water self-dissociation constant. This is equal to 10^{-14} at 25°C . It is the equilibrium constant for pure water undergoing dissociation. K_a and K_b refer to the acid and base dissociation constants of a conjugate pair in aqueous solution. The value of K_W increases with temperature.
$pH = -\log_{10}[H_3O^+]$	Definition of pH , pOH is defined similarly, where $[H_3O^+]$ is replaced by $[OH^-]$.
$pK_W = pK_a + pK_b = pH + pOH$	Equal to 14 at 25°C . The water self-dissociation constants in terms of negative logs.
$[AH]_{\text{Buffer}} \approx 0.1[A^-] \text{ to } 10[A^-]$	For effective buffers, the acid and conjugate base should be within 10 times concentration of each other.
$pH_{\text{Buffer}} \approx pK_a \pm 1$	A more succinct way of stating that buffers must be within 10 times concentration of each other.
$pH = pK_a + \log_{10} \left(\frac{[A^-]}{[HA]} \right)$	The Henderson-Hasselbalch equation. Here AH and A^- are an acid base conjugate pair. This equation is useful in determining how the pH changes as a result of addition of an acid or base to a <i>buffer solution</i> . The equation implicitly assumes that the change in concentrations of the acid and conjugate base is negligible. This is only appropriate for solutions that begin as buffers and stay as buffers upon addition of some small amount of another acid or base.
$\beta = \frac{\Delta n}{\Delta pH}$	β is the buffer Capacity: a measure of the efficiency of a buffer in resisting changes in pH. Buffer capacity is defined as the amount of a strong acid or a strong base that has to be added to 1 liter of a buffer to cause pH change of 1.0 pH unit. Here, Δn is the number of equivalents of strong acid/base added per liter of solution, and ΔpH is the resulting change in pH. The buffer capacity is maximized when the ratio of conjugate acid to conjugate base is 1:1.

Using ICE Tables: An Example

Calculate the new pH if 10.0 mL of 0.10 M HCl is added to the buffer made by mixing 25 mL of 1.0 M CH_3COOH and 25 mL of 0.50 M CH_3COONa . $K_a(\text{CH}_3\text{COOH}) = 1.8 \times 10^{-5}$

First step is to determine the initial number of moles of all reagents.

- HCl: $0.10 \text{ mol L}^{-1} \times 0.010 \text{ L} = 0.001 \text{ mol}$
- CH_3COOH : $1.0 \text{ mol L}^{-1} \times 0.025 \text{ L} = 0.025 \text{ mol}$
- CH_3COONa : $0.50 \text{ mol L}^{-1} \times 0.025 \text{ L} = 0.0125 \text{ mol}$

Since HCl is a strong acid, we know it will react entirely in solution. It will react with any available weak bases and convert them into their conjugate acids. The base in this solution will be generated by the dissociation of CH_3COONa into CH_3COO^- (a weak base) and Na^+ (an nonreactive spectator ion). We can build an ICE (Initial-Change-End) table based on this. ICE tables may be used with number of moles or concentrations of reagents *using the total volume of the solution*. Here we will use the number of moles.

	HCl	+	CH_3COO^-	\rightarrow	Cl^-	+	CH_3COOH
Initial amount	0.001 mol		0.0125 mol		0 mol		0.025 mol
Change	-0.001 mol		-0.001 mol		+0.001 mol		+0.001 mol
Ending amount	0 mol		0.0115 mol		0.001 mol		0.026 mol

Now we should test whether or not the new solution forms a buffer or not. If $10 \geq \frac{[\text{CH}_3\text{COOH}]}{[\text{CH}_3\text{COO}^-]} \geq 0.1$, then the solution is a buffer. Since volumes cancel out, we can use the number of moles or the concentration.

- $\frac{[\text{CH}_3\text{COOH}]}{[\text{CH}_3\text{COO}^-]} = \frac{0.026 \text{ mol}}{0.0115 \text{ mol}} = 2.26$.

This is within acceptable bounds, and so the mixture is still considered a buffer solution after addition of the strong acid.

If it were not a buffer solution, then we would need to construct a second ICE table where the changes in concentration would be unknown, and solve for the unknown variable using the definition of K_a and its known value.

To calculate the pH of a buffer solution, we may use the Henderson-Hasselbalch equation. This equation only works for buffer solutions because it assumes that the concentrations of the acid and base conjugate pair do not change much from their initial concentrations (in this case, the concentrations after addition of the strong acid).

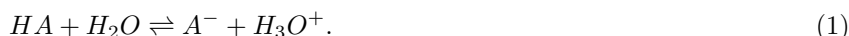
Notice that the volume dependence of the concentrations of acid and base in this equation cancel out. Therefore one may use either concentrations *or* number of moles in the second term of the equation.

$$\begin{aligned} pH &= pK_a + \log_{10} \left(\frac{[\text{CH}_3\text{COO}^-]}{[\text{CH}_3\text{COOH}]} \right) \\ &= -\log_{10} (1.8 \times 10^{-5}) + \log_{10} \left(\frac{0.0115 \text{ mol}}{0.026 \text{ mol}} \right) \\ &= 4.39 \end{aligned}$$

For buffer solutions, the pH should always be within ± 1 of the pK_a value, which in this case is $-\log(1.8 \times 10^{-5}) = 4.74$. This confirms that the solution is indeed a buffer, and can be used as a check to ensure your answer makes sense.

Derivation of the Henderson-Hasselbalch Equation for Buffers

We begin the derivation with an acid equilibrium reaction. This is just the acid dissociation reaction of a unspecified weak acid HA with water,



The ratio of products to reactants in this reaction defined by the equilibrium constant K_a (as long as T does not change). The definition of K_a is

$$K_a = \frac{[A^-][H_3O^+]}{[HA]}. \quad (2)$$

Strictly speaking, the chemical activities of each species should be used, not their concentrations. In practice, concentrations are a good working approximation as long as the solutions are not highly concentrated, and therefore highly non-ideal. The next step is to take the base ten logarithm of each side to obtain

$$\log_{10}(K_a) = \log \left(\frac{[A^-][H_3O^+]}{[HA]} \right). \quad (3)$$

Using the multiplicative log law, $\log(a \times b) = \log(a) + \log(b)$ we can rearrange to yield

$$\log_{10}(K_a) = \log \left(\frac{[A^-]}{[HA]} \right) + \log([H_3O^+]) \quad (4)$$

$$-\log([H_3O^+]) = -\log_{10}(K_a) + \log \left(\frac{[A^-]}{[HA]} \right) \quad (5)$$

$$pH = pK_a + \log \left(\frac{[A^-]}{[HA]} \right) \quad (6)$$

The Henderson-Hasselbalch equation is just a rearranged version of the equation for K_a . Why is it so useful for buffer solutions in particular? Buffer solutions contain both acids and their conjugate bases in similar concentrations (within an order of magnitude of each other). An assumption that is often made using the Henderson-Hasselbalch equation is that the initial concentrations of the acid and conjugate base do not change appreciably when mixed in solution. This assumption is only accurate for buffer solutions that are not too dilute, as it implies that the dissociation of either side of the buffer is negligible compared with their initial concentrations.

Another approximation of the Henderson-Hasselbalch equation is that it does not take into account the effect of self-ionization of water on the pH of a solution. Most of the time this effect is negligible, but it becomes significant for very dilute (less than $1 \times 10^{-5} \text{ mol L}^{-1}$) solutions.

So the Henderson-Hasselbalch equation has only a fairly narrow range of applicability in the form commonly used. Too dilute, and the effects of ionization of the weak acid/base become apparent as well as the self-ionization of water. Too concentrated, and the concentrations of the species deviate too far from their activities to yield high accuracy.

Free Energy vs Reaction Progress

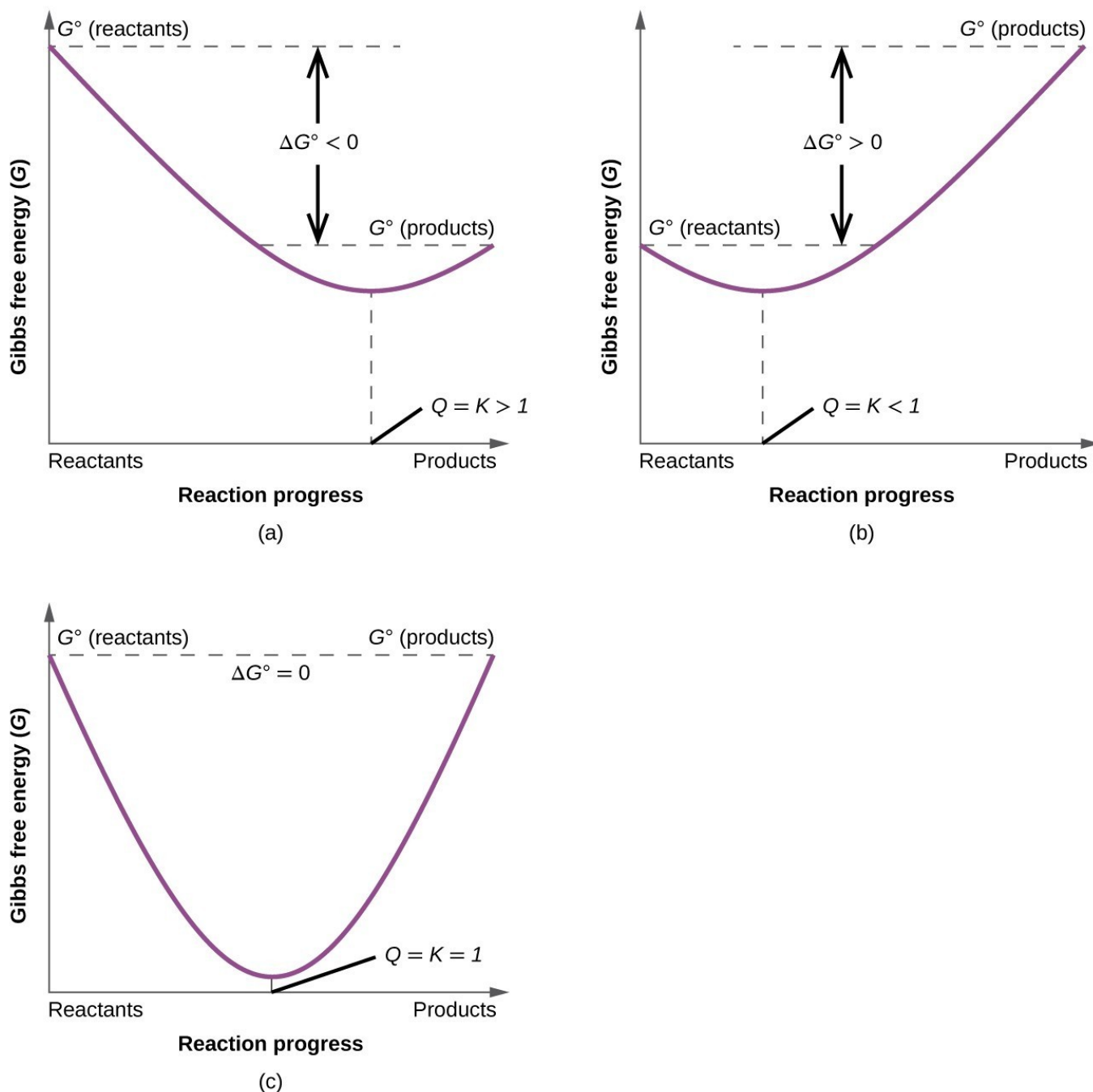


Figure 1: These useful figures¹ show the Gibbs free energy of a hypothetical reaction that goes from 100% pure reactants in their standard state on the left to 100% pure products in their standard state on the right. As the reaction mixture changes from 0% products to 100% products, the Gibbs free energy of the reaction mixture changes accordingly. The corresponding reaction progress at minimized standard Gibbs free energy represents the ratio of reactants to products at equilibrium, at standard pressure and the given temperature (usually 298 K). There are three possible cases: **(a)** $G^\circ(\text{reactants})$ is higher than $G^\circ(\text{products})$. In this case, we see that the ΔG° is negative, and at equilibrium there will be a greater proportion of products than reactants. **(b)** $G^\circ(\text{products})$ is higher than $G^\circ(\text{reactants})$. In this case, ΔG° is positive and the reaction mixture favours reactants at equilibrium. **(c)** $G^\circ(\text{products}) = G^\circ(\text{reactants})$, so that $\Delta G^\circ = 0$. This is an extremely unusual situation, but would result in an exactly equal ratio of products to reactants at equilibrium.

It should be emphasized that the plots on this page are **not** the same as plots for Gibbs free energy vs reaction coordinate. On the above plots, reaction progress represents the relative amount of reactants and products in a reaction mixture. It is inherently a bulk property of the mixture. Plots of Gibbs free energy vs **reaction coordinate** are different. Reaction coordinate is a more abstract idea that refers to the progress of a particular reagent or collection of reagents along what is considered to be the lowest energy reaction trajectory. In other words, the reaction coordinate represents the easiest pathway between a single molecule (or minimal group of molecules) of reactant to a single molecule (or minimal group of molecules) of product.

Kinetics

¹Taken From: <https://courses.lumenlearning.com/suny-mcc-chemistryformajors-2/chapter/free-energy/>

Equation/Concept	Info About Equation/Concept
Factors That Increase Reaction Rates	1. Increase the temperature to increase the average kinetic energy per particle to overcome the transition state energy barrier. 2. Add a catalyst which lowers the transition state energy barrier of the reaction. 3. Increase the concentration of reactants (except for zero order reactions) allowing more collisions to occur per unit time.
ΔG^\ddagger	The Gibbs free energy of activation. This is the free energy change required to reach the transition state, measured as the difference in Gibbs free energy between the transition state and the reactants.
Rate Determining Step	For a multi-step reaction, the rate determining step is the step with the highest Gibbs free energy barrier, ΔG^\ddagger .
Elementary Reaction	A reaction that proceeds through only one step, has only one energy barrier, and one transition state. For a general elementary reaction $aA + bB \rightarrow cC$ the rate law is always $\text{Rate} = k[A]^a[B]^b$ where k is the rate constant.
Thermodynamically Controlled	When ΔG^\ddagger for both reactants and products is small compared with RT , then the energy barrier between reactants and products is easily overcome with the available thermal energy. Such a situation is said to be under thermodynamic control. Equilibrium is quickly established, and the final ratio of reactants or products can be predicted by the equilibrium constant K . Under thermodynamic control, the lowest Gibbs free energy species will be favoured.
Kinetically Controlled	When $\Delta G^\ddagger \gg RT$ with respect to the reactants, products, or both, then the average molecule does not have enough kinetic energy to overcome the activation barrier and equilibrium cannot be quickly established. Such reactions are said to be under kinetic control, and may proceed very slowly or not at all in one or both directions. Kinetic control can be used to force a reaction to produce a side different product than would otherwise be favoured under thermodynamic control.
Reaction Mechanism	A detailed description of the steps leading from reactants to products. A reaction mechanism may be one elementary step or a series of elementary steps.
Transition state	The point(s) along a particular reaction pathway that are peaks in the Gibbs free energy.
Overall Reaction	The entire reaction from initial reactants to final products, as opposed to the elementary reactions that make up the reaction.
Catalyst	Any reagent that is used in a reaction but later regenerated <i>and</i> lowers the activation energy of a reaction. Living creatures contain countless protein-based catalysts called enzymes that allow fine control of the chemistry of their internal systems.
Zero Order Reactions	These types of elementary reactions do not depend on the concentration of the reactants. Such reactions usually depend on some catalyst, which is limiting the rate of the reaction. Zero order kinetics are an artifact of the reaction conditions, and will collapse to higher order kinetics when the concentration of reactants becomes low enough to limit the rate of reaction (instead of the catalyst).
$\text{Rate} = -\frac{b}{a} \frac{d[A]}{dt} = k$	The zero order differential rate law for a general reaction $a[A] \rightarrow b[B]$. This is used to calculate the rate constant k . $[A]$ is the concentration of reactants and a is its stoichiometric coefficient. b is the stoichiometric coefficient of the products. The "Rate" here is always the rate of product formation. Often times this equation will be written without the factor of $\frac{b}{a}$, with $k' = \frac{a}{b}k$.
$[A](t) = -kt + [A]_0$	This is the integrated rate law for a zero order reaction, note that the rate constant here is really $\frac{a}{b}k$. This equation will provide the concentration of the reactants as a function of time. Plots of $[A]$ vs t will be linear for zero order reactions, with a slope of $-k$ and a y -intercept of $[A]_0$.
$t_{\frac{1}{2}} = \frac{[A]_0}{2k}$	The half-life of a zero order reaction. This depends on the initial concentration of reactants.
First Order Reactions	These types of reactions depend on the concentration of only one reactant, which a stoichiometric coefficient of 1. For example, the elementary reaction $A \rightarrow bB$.
$\text{Rate} = -b \frac{d[A]}{dt} = k[A]$	The differential rate law for a first order reaction $A \rightarrow bB$. Often the rate constant k will include the factor of $\frac{1}{b}$.

Equation/Concept	Info About Equation/Concept
$[A](t) = [A]_0 e^{-kt}$	The integrated rate law for first order reactions. This can also be written as $\ln[A] = -kt + \ln[A]_0$. This equation can be used to determine the concentration of reactants as a function of time. Plots of $\ln[A]$ vs t will be linear for first order reactions, with a slope of $-k$ and a y -intercept of $\ln[A]_0$.
$t_{\frac{1}{2}} = \frac{\ln 2}{k}$	The half-life for a first order reaction. This does not depend on the initial concentration of the reactants.
Second Order Reactions	These types of reactions depend on the concentration of one reactant with a stoichiometric coefficient of 2, or on the concentration of two reactants. For example, the elementary reaction $2A \rightarrow bB$.
Rate $= -\frac{b}{2} \frac{[A]}{dt} = k[A]^2$	The differential rate law for a first order reaction $A \rightarrow bB$. Often the rate constant k will include the factor of $\frac{2}{b}$.
$\frac{1}{[A](t)} = kt + \frac{1}{[A]_0}$	The integrated rate law for second order reactions. This equation can be used to determine the concentration of reactants as a function of time. Plots of $\frac{1}{[A]}$ vs t will be linear for second order reactions, with a slope of k and a y -intercept of $\frac{1}{[A]_0}$.
$t_{\frac{1}{2}} = \frac{1}{[A]_0 k}$	The half-life for a second order reaction. This depends on the initial concentration of the reactants.
$k = \frac{k_B T}{h} e^{-\frac{\Delta G^\ddagger}{RT}}$	The Eyring equation. This applies only to elementary reactions, and can be used to determine the Gibbs free energy of activation. k_B is the Boltzmann constant, which is just $\frac{R}{N_A}$ where N_A is Avagadro's number. This reaction comes about by assuming that formation of the transition state is kinetically controlled (i.e. is in equilibrium) but the formation of products is thermodynamically controlled (i.e. is irreversible).
$k = Ae^{-\frac{E_a}{RT}}$	The Arrhenius equation. This applies to any reaction and describes the effect of temperature on the rate of reaction. A is the pre-exponential factor, and is usually assumed to be temperature independent over small changes in temperature; it describes the frequency of collisions that occur with the correct orientation (different for each reaction). E_a is the activation energy per mole, and is the minimum energy required to overcome the energy barrier for reaction. RT is the average thermal energy per mole. This equation is sometimes written $\ln k = -\frac{E_a}{R} \frac{1}{T} + \ln A$ so that plots of $\ln k$ vs $\frac{1}{T}$ are linear with a slope of $-\frac{E_a}{R}$ and a y -intercept of $\ln A$.
$\ln\left(\frac{k}{T}\right) = -\frac{\Delta H^\ddagger}{R} \frac{1}{T} + \frac{\Delta S^\ddagger}{R} + \ln\left(\frac{k_B}{h}\right)$	The linear form of the Eyring equation. Plots of $\ln\left(\frac{k}{T}\right)$ vs $\frac{1}{T}$ will be linear. The slope will be $-\frac{\Delta H^\ddagger}{R}$ and the y -intercept will be $\frac{\Delta S^\ddagger}{R} + \ln\left(\frac{k_B}{h}\right)$.
Reaction Intermediates	These are species that are generated in one step of a reaction and consumed in a subsequent step.
$\frac{d[\text{intermediates}]}{dt} = 0$	This is the steady-state approximation. Useful for reactions where the rate determining step is the production of an intermediate. This often greatly simplifies the rate laws for multi-step reactions.
$V_0 = \frac{V_{\max}[S]}{K_m + [S]}$	The Michaelis-Menton equation. Describes the kinetics of the enzyme equilibrium reaction $E + S \xrightleftharpoons[k_{-1}]{k_1} ES \xrightarrow{k_{\text{cat}}} E + P$. Here, $K_M = \frac{[E][S]}{[ES]} = \frac{k_{-1} + k_{\text{cat}}}{k_1}$ is the equilibrium constant for the enzyme-substrate binding; V_0 is the rate of product formation; $V_{\max} = k_{\text{cat}}[E]_{\text{total}}$ is the reaction rate when all available enzymes are saturated. Derivation of this equation involves the steady state approximation $\frac{d[ES]}{dt} = 0$. Notice that in the limit where the concentration of substrate is large compared to that of the enzyme, $K_M \ll [S]$ such that $K_M + [S] \approx [S]$ and $V_0 \approx V_{\max}$. In the limit of very low substrate concentration, $K_M \gg [S]$ such that $K_M + [S] \approx K_M$ and the kinetics become first order with respect to $[S]$.

Reaction Coordinate Diagrams

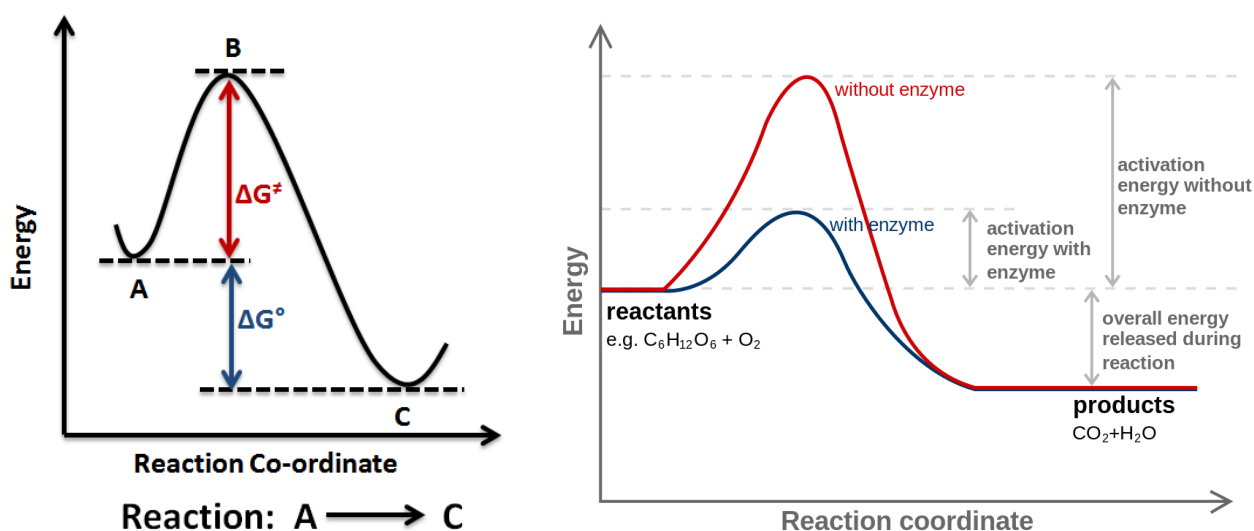


Figure 2: **(Left)** A diagram of Gibbs free energy vs reaction coordinate for an elementary reaction. In this context, the reaction coordinate refers to the point along the reaction pathway from reactant to product that requires the lowest raise in free energy. It is easy to imagine a multitude of potential pathways between a set of reactants and a set of products, but most of would be highly unlikely in reality. The reaction pathway that is most likely to occur is chosen, and its progress is delineated by the reaction coordinate. **(Right)** The effect of a biological catalyst (called an enzyme) on the reaction between glucose and oxygen. The catalyst does not change the free energy of the reactants or products, but lowers the energy of activation by stabilizing the transition state.²

As one moves along the reaction coordinate between reactant and product, there is always a potential energy barrier called the **energy of activation**. If there were no such barrier, the reactants could not exist for more than the length of a molecular vibration (approximately 1×10^{-10} s) without decaying into the products. The highest point along the energy barrier is called the **transition state** and is usually marked with the double dagger symbol (\ddagger). Transition states are not isolable species, they only exist for around the length of time of a molecular vibration before either decaying to products or back to reactants. Transition states generally look intermediate between reactants and products, but tend to be more similar in structure to the side with a smaller gap in free energy (reactants in this case). This principle is known as Hammond's postulate.

Free Energy vs Reaction Progress

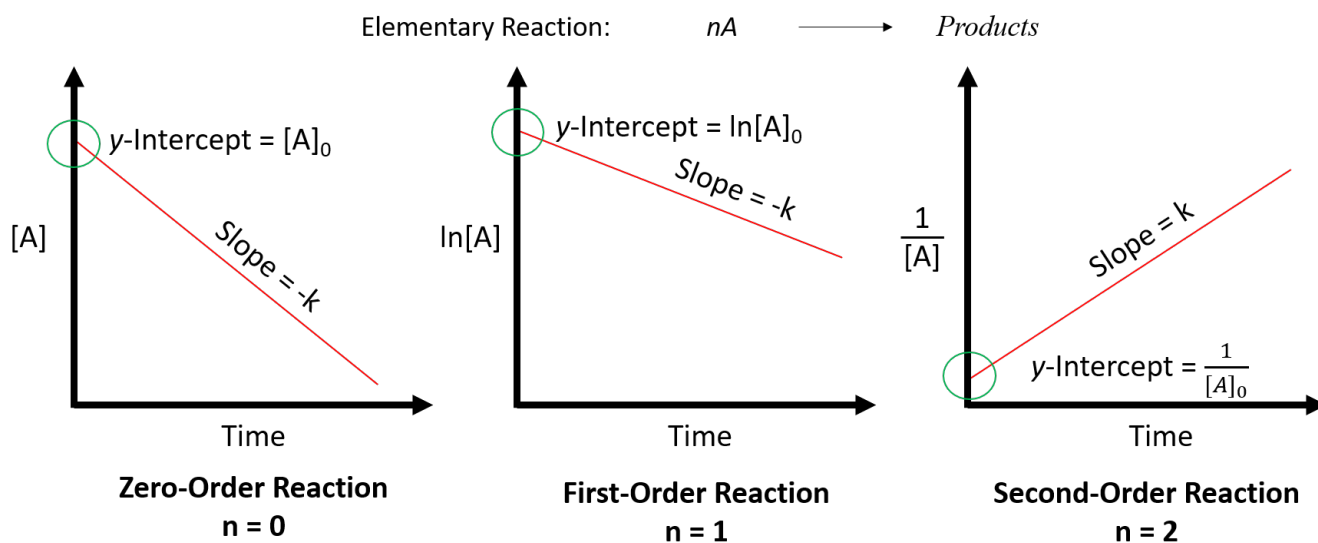


Figure 3: How we can use plots of concentration vs time to determine the order of a reaction with respect to a particular reactant. Only one of the above plots should be linear with respect to a particular reactant involved in a reaction. Find the linear plot to determine the reaction order. The reaction order is *also* the stoichiometric coefficient if the reaction is elementary.

²Left: [http://www.wikiwand.com/en/Energy_profile_\(chemistry\)](http://www.wikiwand.com/en/Energy_profile_(chemistry)) Right: https://en.wikipedia.org/wiki/Reaction_coordinate

Derivation of the Michaelis-Menton Equation

The Michaelis-Menton equation describes the kinetics of a biological catalyst E (called an enzyme) undergoing the following set of linked reactions:



- E is the enzyme
- S is the substrate
- ES is the enzyme-substrate bonded complex
- P is the product
- k_1 , k_{-1} , and k_{cat} are the rate constants for the three involved reactions.

We make the assumption that the reaction $E + P \rightarrow ES$ does not appreciably occur, and can therefore be ignored. This is a common situation for many biological enzymes under normal physiological conditions. Each of the reactions in equation 7 is an elementary reaction. Therefore, the rate of formation of ES is simply

$$\text{Rate}_{ES} = k_1[E][S]. \quad (8)$$

The rate of breakdown of ES is more complicated because it depends on two separate elementary reactions,

$$\text{Rate}_{-ES} = k_{-1}[ES] + k_{cat}[ES] = (k_{-1} + k_{cat})[ES]. \quad (9)$$

Now we make the steady-state approximation with regards to the concentration of ES . That is,

$$\frac{d[ES]}{dt} = 0. \quad (10)$$

The only way for the concentration of ES to remain constant is if the rate of formation for ES equals the rate of breakdown, i.e. $\text{Rate}_{ES} = \text{Rate}_{-ES}$. Therefore, under the steady-state approximation we can set equations 8 and 9 equal to obtain

$$\begin{aligned} k_1[E][S] &= (k_{-1} + k_{cat})[ES] \\ \frac{[E][S]}{[ES]} &= \frac{k_{-1} + k_{cat}}{k_1} \equiv k_M. \end{aligned} \quad (11)$$

Here we have defined a new quantity called the Michaelis constant, k_M . The rate of product formation V_0 for the reaction described by 7 can be written as

$$V_0 = k_{cat}[ES]. \quad (12)$$

We now define a new quantity, $[E]_T = [E] + [ES]$ which is just the total concentration of free and bound enzyme. Rearranging gives us $[E] = [E]_T - [ES]$. Plugging this into equation 11 yields

$$\begin{aligned} k_M &= \frac{([E]_T - [ES])[S]}{[ES]} \\ k_M[ES] &= [E]_T[S] - [ES][S] \\ [ES](k_M + [S]) &= [E]_T[S] \\ [ES] &= \frac{[E]_T[S]}{k_M + [S]}. \end{aligned} \quad (13)$$

Equation 13 is the expression for the enzyme-substrate complex under the steady-state approximation in terms of the easier-to-measure quantities $[E]_T$ and $[S]$. We now plug equation 13 back into equation 12 to get an expression for the rate of product formation in terms of these quantities,

$$V_0 = \frac{k_{cat}[E]_T[S]}{k_M + [S]}. \quad (14)$$

It is common to define $V_{max} \equiv k_{cat}[E]_T$ as the maximum possible rate of reaction for a given total concentration of enzyme, so equation 14 becomes

$$V_0 = \frac{V_{max}[S]}{k_M + [S]}. \quad (15)$$

This is the Michaelis-Menton equation in its common form.

The Michaelis-Menton equation has two interesting limiting behaviours. The first limit is when there is very little substrate, such that $[S] \ll [E]_T$. In this limit, $[E]$ will be very large and $[ES]$ will be very small such that

$$k_M + [S] = \frac{[E][S]}{[ES]} + [S] \approx \frac{[E][S]}{[ES]} = k_M. \quad (16)$$

This gives us the limiting behaviour

$$V_0 \approx \frac{V_{max}}{k_M}[S] \quad \text{if} \quad [S] \ll [E]_T. \quad (17)$$

which looks like first order kinetics for $[S]$ with a rate constant of $\frac{V_{max}}{k_M}$. The second limit occurs when there is a great excess of substrate such that $[S] \gg [E]_T$. In this case, $[E]_T \approx [ES]$ such that $k_M + [S] \approx [S]$ leading to

$$V_0 \approx V_{max} = k_{cat}[E]_T \quad \text{if} \quad [S] \gg [E]_T. \quad (18)$$

This looks like first order kinetics with respect to the total concentration of enzyme, as one might expect.

Converting Between Equilibrium Constants and Percentages:

Let's say you know the equilibrium constant K for some reaction at equilibrium,



but would like to express the amount of each reagent in terms of its mole fraction (equal to percent divided by 100) of the total reaction mixture. This is NOT the same as K , but they are closely related. K is defined as

$$K = \frac{[B]}{[A]},$$

while the mole fraction of products and reactants is (respectively)

$$\chi_B = \frac{[B]}{[A] + [B]} \quad \text{and} \quad \chi_A = \frac{[A]}{[A] + [B]}.$$

We can easily write these numbers in terms of K using some simple algebra. Divide both the numerator and denominator of each fraction by $[A]$ or $[B]$ respectively to obtain

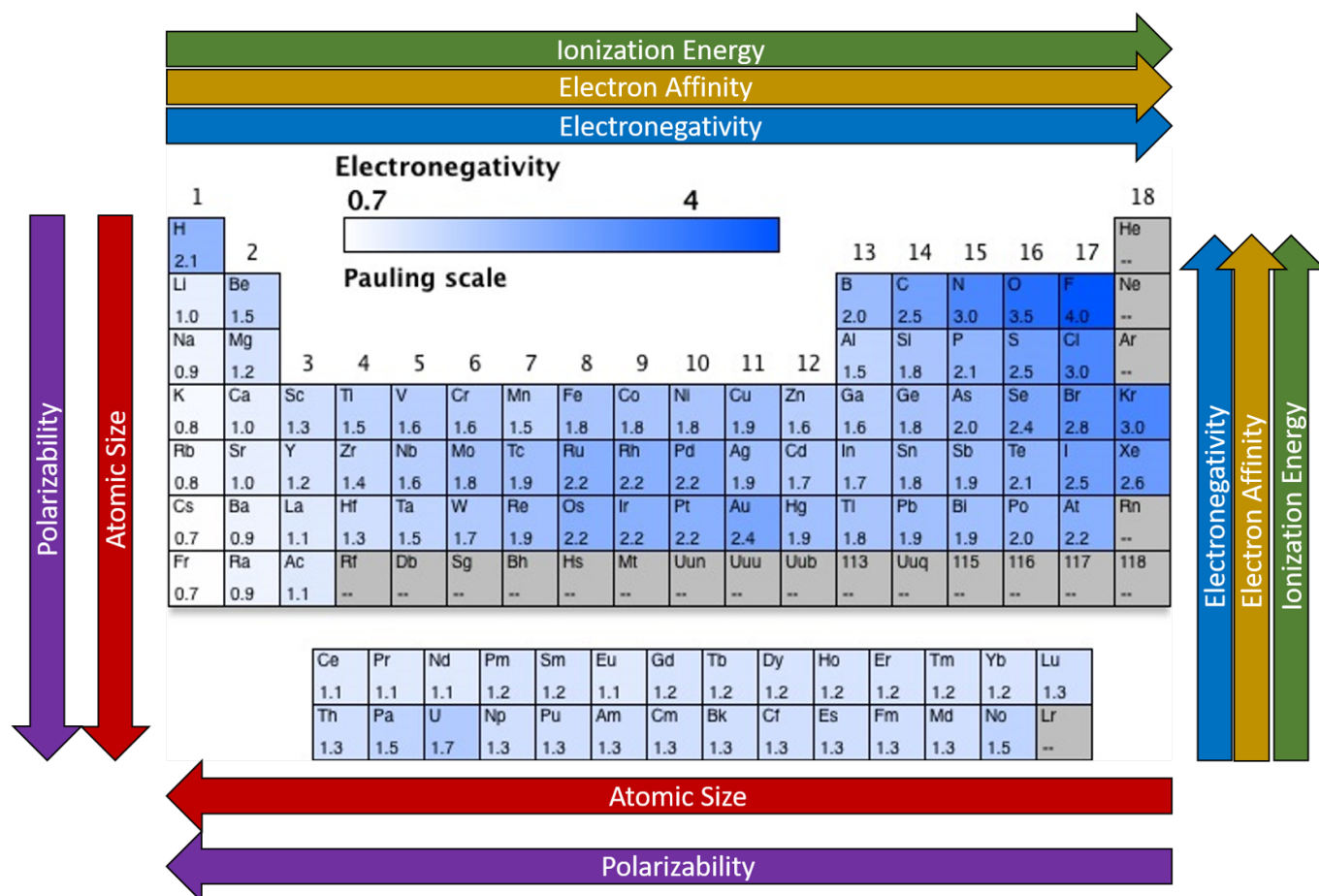
$$\chi_B = \frac{\frac{[B]}{[A]}}{\frac{[A]}{[A]} + \frac{[B]}{[A]}} = \frac{K}{1 + K}$$

and

$$\chi_A = \frac{\frac{[A]}{[B]}}{\frac{[A]}{[B]} + \frac{[B]}{[B]}} = \frac{K^{-1}}{K^{-1} + 1} = \frac{1}{1 + K}.$$

Physical Constants and Periodic Trends (for Reference)

Constant	Value and Units
Atomic mass unit (u)	$1\text{ u} = 1.660\,538\,9 \times 10^{-24}\text{ g}$ $1\text{ g} = 6.022\,142 \times 10^{23}\text{ u}$
Avogadro's number (N_A)	$N_A = 6.022\,142 \times 10^{23}\text{ mol}^{-1}$
Boltzmann's constant (k_B)	$k_B = 1.380\,648\,52 \times 10^{-23}\text{ J K}^{-1}$ $k_B = R/N_A$
Gas constant (R)	$R = 8.314\,459\,8\text{ J K}^{-1}\text{ mol}^{-1}$ $= 8.314\,459\,8 \times 10^{-3}\text{ kJ K}^{-1}\text{ mol}^{-1}$ $= 8.314\,459\,8\text{ kg m}^2\text{ s}^{-2}\text{ K}^{-1}\text{ mol}^{-1}$ $= 8.314\,459\,8\text{ m}^3\text{ Pa K}^{-1}\text{ mol}^{-1}$ $= 0.082\,057\,338\text{ L atm K}^{-1}\text{ mol}^{-1}$ $= 1.987\,203\,6 \times 10^{-3}\text{ kcal K}^{-1}\text{ mol}^{-1}$ $= 8.205\,733\,8 \times 10^{-5}\text{ m}^3\text{ atm K}^{-1}\text{ mol}^{-1}$ $= k_B N_A$
Mass of electron (m_e)	$m_e = 5.485\,799 \times 10^{-4}\text{ u}$ $= 9.109\,383 \times 10^{-28}\text{ g}$
Mass of proton (m_p)	$m_p = 1.007\,276\,5\text{ u}$ $= 1.672\,621\,7 \times 10^{-24}\text{ g}$
Mass of neutron (m_n)	$m_n = 1.008\,664\,9\text{ u}$ $= 1.674\,927\,3 \times 10^{-24}\text{ g}$
Planck constant (h)	$h = 6.626\,069 \times 10^{-34}\text{ J s}$
Reduced Planck constant (\hbar)	$\hbar = h/2\pi = 1.054\,572\,66 \times 10^{-34}\text{ J s}$
Speed of light (c)	$c = 2.997\,924\,58 \times 10^8\text{ m s}^{-1}$



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Equations and Constants

(note: conditions for applying equations are not specified)

$$R = 8.314 \text{ J K}^{-1} \text{ mol}^{-1} = 0.08206 \text{ L atm K}^{-1} \text{ mol}^{-1}$$

$$k = 1.3807 \times 10^{-23} \text{ J K}^{-1}$$

$$N_A = 6.0221 \times 10^{23} \text{ mol}^{-1}$$

$$F = 96485 \text{ C mol}^{-1}$$

$$0^\circ \text{C} = 273.15 \text{ K}$$

$$1 \text{ atm} = 101325 \text{ Pa}$$

$$1 \text{ L} = 0.001 \text{ m}^3$$

$$1 \text{ L atm} = 101.325 \text{ J}$$

$$PV = nRT$$

$$\left(P + a \frac{n^2}{V^2} \right) (V - nb) = nRT$$

$$\Delta U = U_2 - U_1 = q + w$$

$$dw = -P_{\text{ex}} dV$$

$$w = -P_{\text{ex}} (V_2 - V_1)$$

$$w = -nRT \ln \left(\frac{V_2}{V_1} \right)$$

$$dq = C \cdot dT$$

$$C_V = nC_{V,m} = \frac{dq_V}{dT}$$

$$\Delta U = q_V = \int_{T_1}^{T_2} nC_{V,m} dT = \int_{T_1}^{T_2} C_V dT$$

$$H = U + PV$$

$$C_P = nC_{P,m} = \frac{dq_P}{dT}$$

$$\Delta H = q_P = \int_{T_1}^{T_2} nC_{P,m} dT = \int_{T_1}^{T_2} C_P dT$$

$$\Delta H_{\text{rxn}}^0 = \sum_i \nu_i \Delta H_{m,i}^0 (\text{products}) - \sum_j \nu_j \Delta H_{m,j}^0 (\text{reactants})$$

$$C_{V,m} = \frac{3}{2} R, \quad C_{P,m} = \frac{5}{2} R$$

$$dS = dq_{\text{rev}} / T$$

$$\Delta S = S_2 - S_1 = \int_{\text{state 1}}^{\text{state 2}} \frac{dq_{\text{rev}}}{T}$$

$$(\Delta S)_{T,P} = \Delta H / T$$

$$(\Delta S)_T = nR \ln \left(\frac{V_2}{V_1} \right) = nR \ln \left(\frac{P_1}{P_2} \right)$$

$$(\Delta S)_V = nC_{V,m} \ln \left(\frac{T_2}{T_1} \right)$$

$$(\Delta S)_P = nC_{P,m} \ln \left(\frac{T_2}{T_1} \right)$$

$$\Delta S = nC_{V,m} \ln \left(\frac{T_2}{T_1} \right) + nR \ln \left(\frac{V_2}{V_1} \right)$$

$$\Delta S = nC_{P,m} \ln \left(\frac{T_2}{T_1} \right) + nR \ln \left(\frac{P_1}{P_2} \right)$$

$$\Delta S_{\text{univ}} = \Delta S_{\text{sys}} + \Delta S_{\text{surr}}$$

$$\ln \left(\frac{P_2}{P_1} \right) = \frac{-\Delta H_{\text{vap},m}^0}{R} \left(\frac{1}{T_2} - \frac{1}{T_1} \right)$$

$$\ln \left(\frac{K_2}{K_1} \right) = \frac{-\Delta H_{\text{rxn}}^0}{(1 \text{ mol}) \cdot R} \left(\frac{1}{T_2} - \frac{1}{T_1} \right)$$

$$F = C - P + 2$$

$$G = H - TS$$

$$\Delta G_{T,P} = -T \cdot \Delta S_{\text{univ}}$$

$$\Delta G_{\text{rxn}} = \Delta G_{\text{rxn}}^0 + (1 \text{ mol}) \cdot RT \ln Q$$

$$\Delta G_{\text{rxn}}^0 = -(1 \text{ mol}) \cdot RT \ln K$$

$$\Delta G_{\text{rxn}} = -nF\varepsilon, \quad \Delta G_{\text{rxn}}^0 = -nF\varepsilon^0$$

$$\varepsilon = \varepsilon^0 - \frac{(1 \text{ mol}) \cdot RT}{nF} \ln Q$$

$$\Delta T_b = T_{\text{b,mix}} - T_{\text{b,pure}} \approx K_b b_B$$

$$\Delta T_f = T_{\text{f,mix}} - T_{\text{f,pure}} \approx -K_f b_B$$

$$\Pi = c_B RT$$

$$\Delta \Pi = \Delta c \cdot RT$$

$$\varepsilon \approx \frac{-RT}{z_l F} \ln \left(\frac{[i]_{\text{R}}}{[i]_{\text{L}}} \right)$$

$$T = \frac{I}{I_0}$$

$$A = -\log_{10} T = lc\varepsilon$$

$$\nu = k[A]^a [B]^b [C]^c \dots$$

$$aA \rightarrow B: \quad \nu = -\frac{1}{a} \frac{d[A]}{dt} = k[A]^n$$

$$aA \rightarrow B: \quad [A] = [A]_0 - akt, \quad t_{1/2} = \frac{[A]_0}{2ak}$$

$$aA \rightarrow B: \quad \ln \left(\frac{[A]}{[A]_0} \right) = -akt, \quad t_{1/2} = \frac{\ln 2}{ak}$$

$$aA \rightarrow B: \quad \frac{1}{[A]} - \frac{1}{[A]_0} = akt, \quad t_{1/2} = \frac{1}{ak[A]_0}$$

$$t = \frac{t_{1/2}}{\ln 0.5} \ln \left(\frac{[A]}{[A]_0} \right), \quad \frac{[A]}{[A]_0} = 0.5^{\frac{\text{time}}{\text{half-life}}}$$

$$K = \frac{k_1}{k'_1} \times \frac{k_2}{k'_2} \times \frac{k_3}{k'_3} \times \dots$$

$$k = A e^{\frac{-E_a}{RT}} = A \exp \left(\frac{-E_a}{RT} \right)$$

$$\ln \left(\frac{k_2}{k_1} \right) = \frac{-E_a}{R} \left(\frac{1}{T_2} - \frac{1}{T_1} \right)$$

$$\nu = \frac{[S] \cdot \nu_{\text{max}}}{[S] + K_M}, \quad \nu_{\text{max}} = k_b [E]_{\text{tot}}$$

Useful Spectroscopic Data

IR Modes of Vibrational Frequency	
Vibration	ν (cm ⁻¹)
C–C stretch, bend	700–1250
C–H stretch	2850–3100 (strong)
C–H bend	1340–1465
C=C stretch	1620–1680
C=O stretch	1600–1850 (strong)
C≡C stretch	2100–2260
C≡N stretch	2100–2300
O–H stretch	3590–3650 (strong)
C=N stretch	2215–2275
N–H stretch	3200–3500 (strong)
Hydrogen-bonds	3200–3570 (broad)

Selected Isotopes & Their Masses		
Isotope	Natural Abundance	Mass
¹ H	99.98%	1.00783
¹² C	98.9%	12.0000
¹³ C	1.1%	13.0034
¹⁴ N	99.6%	14.0031
¹⁶ O	99.8%	15.9949
¹⁹ F	100.0%	18.9984
³⁵ Cl	75.8%	34.9689
³⁷ Cl	24.2%	36.9659
⁷⁹ Br	50.7%	78.9183
⁸¹ Br	49.3%	80.9163
¹²⁷ I	100.0%	126.904

Common Fragments & Their Masses	
Fragment	Mass
CH ₃	15
CH ₂ CH ₃	29
HC(=O)	29
HOCH ₂	31
CH ₃ C(=O)	43
HOC(=O)	45

UV-Visible Absorption Bands	
Chromophore	λ_{max} (nm)
C=O (carbonyl ketones, aldehydes, esters)	250–350 (weak)
CH=CH–CH=O (conjugated carbonyl)	200–300 (strong) and 300–400 (weak)
C=C (alkenes and conjugated alkenes)	160–340 (strong)
Benzene and derivatives	200–300 (moderate–strong)

¹ H NMR Downfield Shifts from TMS	
Type of Proton ¹ H	Chemical Shift δ
RCH ₃	0.8 – 1.0
RCH ₂ R	1.2 – 1.4
R ₃ CH	1.4 – 1.7
R ₂ C=C(R)–CH ₃	1.6 – 1.9
ArCH ₃ (Ar is benzene ring)	2.2 – 2.5
RCH ₂ Cl	3.6 – 3.8
RCH ₂ Br	3.4 – 3.6
RCH ₂ I	3.1 – 3.3
ROCH ₂ R	3.3 – 3.9
RCH ₂ OH	3.3 – 4.0
RC(=O)CH ₃	2.1 – 2.6
RC(=O)H	9.5 – 9.6
R ₂ C=CH ₂	4.6 – 5.0
R ₂ C=C(R)H	5.2 – 5.7
ArH	6.0 – 9.5
RC≡CH	2.5 – 3.1
ROH	0.5 – 6.0
RC(=O)OH	10 – 13
ArOH	4.5 – 7.7
R–NH ₂	1.0 – 5.0

¹³ C NMR Chemical Shift Ranges	
Group	¹³ C Shift δ
TMS	0.0
–CH ₃ (with only H or R at C _α or C _β)	0 – 30
–CH ₂ (with only H or R at C _α or C _β)	20 – 45
–CH (with only H or R at C _α or C _β)	30 – 60
C quaternary (with only H or R at C _α or C _β)	30 – 50
O–CH _n (n = 0–3)	50 – 80
N–CH _n (n = 0–3)	15 – 70
C≡C	75 – 95
C=C	105 – 145
C(aromatic)	110 – 155
C(heteroaromatic)	105 – 165
–C≡N	115 – 125
C=O (acids, esters, amides)	155 – 185
C=O (aldehydes, ketones)	185 – 225

Mathematical Relations

$\pi = 3.141\ 592\ 653\ 59 \dots$ $e = 2.718\ 281\ 828\ 46 \dots$

Logarithms & Exponentials

$\ln(x) + \ln(y) = \ln(xy)$
 $a \ln(x) = \ln(x^a)$
 $e^x e^y = e^{x+y}$
 $(e^x)^a = e^{ax}$

$\ln(x) - \ln(y) = \ln(x/y)$
 $\ln(x) = \ln(10) \cdot \log(x)$
 $e^x / e^y = e^{x-y}$
 $e^{-a} = 1/e^a$

Taylor Expansions

$$f(x) = \sum_{n=0}^{\infty} \frac{(x-a)^n}{n!} \left(\frac{d^n f}{dx^n} \right)_{x=a}$$
$$e^x = 1 + x + \frac{1}{2}x^2 + \dots$$
$$\ln(1+x) = x - \frac{1}{2}x^2 + \frac{1}{3}x^3 - \dots$$

$$\ln(x) = (x-1) - \frac{1}{2}(x-1)^2 + \frac{1}{3}(x-1)^3 - \frac{1}{4}(x-1)^4 + \dots$$
$$\frac{1}{1+x} = 1 - x + x^2 + \dots$$

Derivatives

$$d(f+g) = df + dg$$
$$d\left(\frac{f}{g}\right) = \frac{g \cdot df - f \cdot dg}{g^2}$$
$$\frac{dx^n}{dx} = nx^{n-1}$$

$$d(f \cdot g) = f \cdot dg + g \cdot df$$
$$\frac{df}{dx} = \frac{df}{dg} \cdot \frac{dg}{dx}$$
$$\frac{d}{dx} e^{ax} = ae^{ax}$$

$$\frac{d}{dx} \ln(x) = \frac{1}{x}$$

Integrals

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$
$$\int dx = x + C$$

$$\int \frac{1}{x} dx = \ln(x) + C$$
$$d \int dx = dx$$

$$\int_0^{\infty} x^n e^{-ax} dx = \frac{n!}{a^{n+1}}$$
$$\int_a^b dx = x|_a^b = b - a$$

Prefixes

z	zepto	10 ⁻²¹
a	atto	10 ⁻¹⁸
f	femto	10 ⁻¹⁵
p	pico	10 ⁻¹²
n	nano	10 ⁻⁹
μ	micro	10 ⁻⁶
m	milli	10 ⁻³
c	centi	10 ⁻²
d	deci	10 ⁻¹
da	deca	10 ¹
k	kilo	10 ³
M	mega	10 ⁶
G	giga	10 ⁹
T	tera	10 ¹²
P	peta	10 ¹⁵

Greek Alphabet

A, α	alpha	Π, π	pi
B, β	beta	Ρ, ρ	rho
Γ, γ	gamma	Σ, σ	sigma
Δ, δ	delta	Τ, τ	tau
Ε, ε	epsilon	Υ, υ	upsilon
Ζ, ζ	zeta	Φ, φ	phi
Η, η	eta	Χ, χ	chi
Θ, θ	theta	Ψ, ψ	psi
Ι, ι	iota	Ω, ω	omega
Κ, κ	kappa		
Λ, λ	lambda		
Μ, μ	mu		
Ν, ν	nu		
Ξ, ξ	xi		
Ο, ο	omicron		

USEFUL RELATIONSHIPS

Derivatives :-

$$d x^n = n x^{n-1}$$

$$d \ln x = \frac{1}{x}$$

$$d(xy) = x dy + y dx$$

Integrals :-

$$\int x^n dx = \frac{x^{n+1}}{n+1}$$

$$\int \frac{dx}{x} = \ln x$$

Note

$$\int dx = x$$

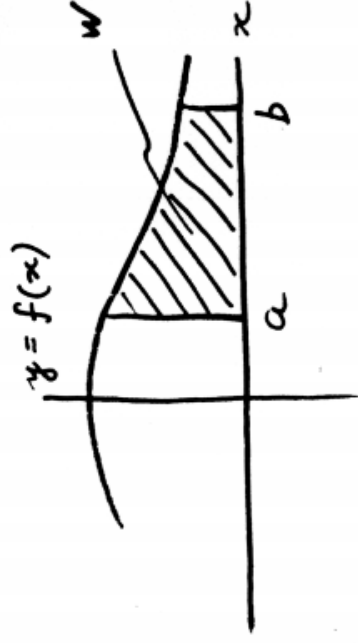
$$d \int dx = dx$$

Also note

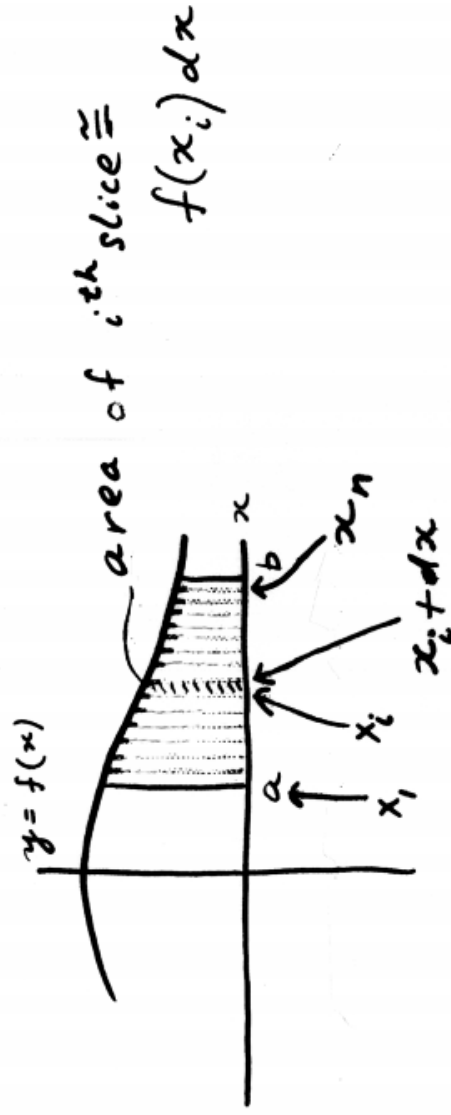
$$\int_a^b dx = x \Big|_a^b = b - a$$

INTEGRATION

what is the shaded area, A ?



Consider n small slices of width dx



Then

$$A \approx \sum_{x_i = a}^{x_i = b} f(x_i) dx$$

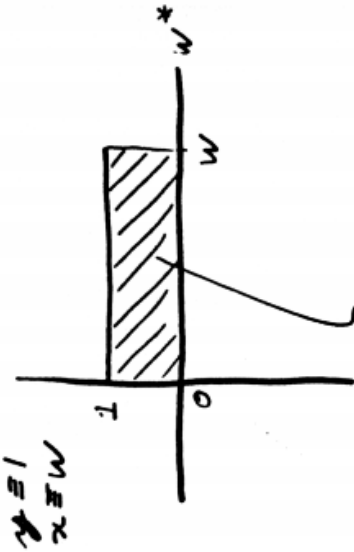
This is exact if dx is infinitesimally small. Then replace Σ by \int

$$\text{Total Area} \equiv A = \int_{x=a}^{x=b} f(x) dx$$

Example:- $-dw = PdV$ for ideal gas at const. T .

reversible

$$P = f(V) = nRT \frac{1}{V}$$



$$y \equiv P$$

$$x \equiv V$$

$$\text{Area} = \int_{V_i}^{V_f} PdV = \int_{V_i}^{V_f} nRT \frac{dV}{V}$$

$$= nRT \int_{V_i}^{V_f} \frac{dV}{V}$$

$$= nRT \ln V \Big|_{V=V_i}^{V=V_f}$$

$$= nRT \ln V_f - nRT \ln V_i$$

$$= nRT \ln \left(\frac{V_f}{V_i} \right)$$

$$\therefore -w = \int_{V_i}^{V_f} PdV$$

and for ideal gas at const. T + rev.

$$-w = nRT \ln \frac{V_f}{V_i}$$

$$\text{Area} = \int dw^*$$

$$w^* = 0$$

$$= w^* \Big|_{w^*=0}^{w^*=w}$$

$$= w - 0$$

$$= w$$