Data Visualization

Visualizing 1D categorical and continuous variables

June 8th, 2023

New dataset - 2021 MVP Shohei Ohtani's batted balls

Created dataset of batted balls by the American League MVP Shohei Ohtani in 2021 season using baseballr:

```
library(tidyverse)
ohtani batted balls <-
  read csv("https://shorturl.at/mnwL1")
head(ohtani batted balls)
## # A tibble: 6 × 7
##
    pitch type batted ball type hit x hit y exit velocity launch angle outcome
                              <dbl> <dbl>
                                                 <dbl>
##
   <chr>
              <chr>
                                                            <dbl> <chr>
## 1 FC
           line drive
                              89.7 144.
                                                113.
                                                               20 home run
## 2 CH
           fly ball
                            3.35 83.9
                                                               55 field out
                                                83.9
## 3 CH
              fly ball
                       -65.6 126.
                                                102.
                                                               38 field out
## 4 CU
              ground ball 39.2 50.4
                                                82.5
                                                                8 field out
              fly_ball
## 5 FC
                             -37.6 138.
                                                               23 field out
                                                101.
                                                               65 field out
## 6 KC
              popup
                             -51.9 41.6
                                                 84
```

- each row / observation is a batted ball from Ohtani's 2021 season
- Categorical / qualitative variables: pitch_type, batted_ball_type, outcome
- Continuous / quantitative variables: hit_x, hit_y, exit_velocity, launch_angle

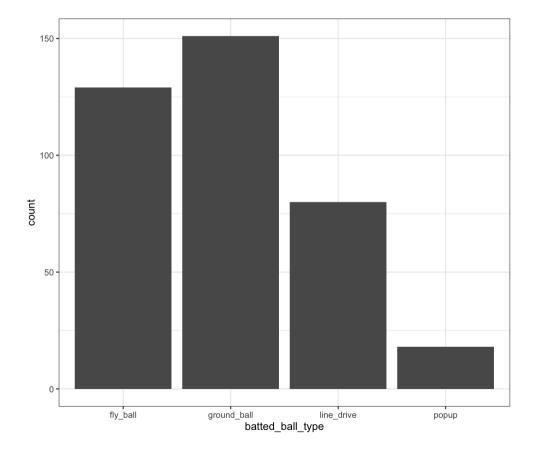
Visualizing 1D categorical data

How can we summarize batted_ball_type and other categorical variables?

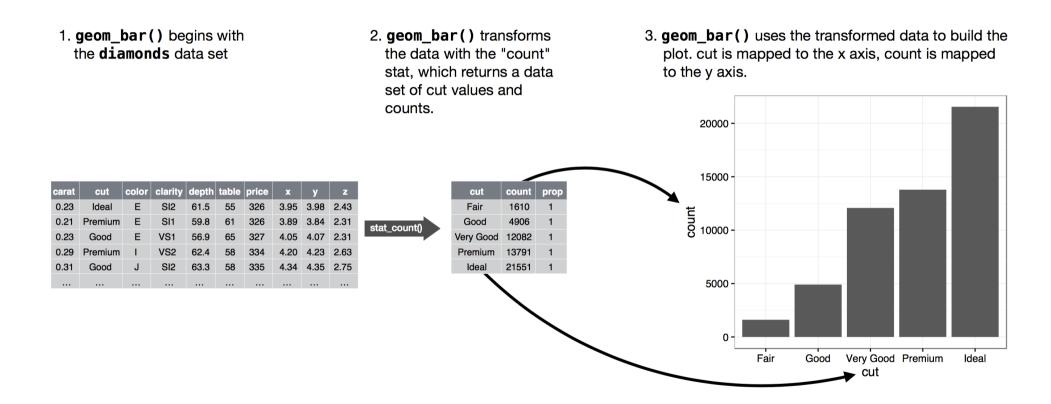
• We make a **bar chart** with geom_bar()

```
ohtani_batted_balls %>%
  ggplot(aes(x = batted_ball_type)) +
  geom_bar() +
  theme_bw()
```

- Only map batted_ball_type to the x-axis
- Counts of each type are displayed on y-axis...



Remember statistical summaries!

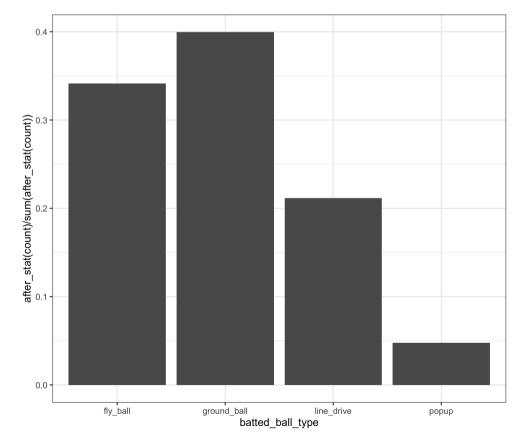


What does a bar chart show?

Marginal distribution: probability that categorical variable X (e.g., batted_ball_type) takes each particular value x (e.g. fly_ball). So how do we display the individual probabilities?

```
ohtani_batted_balls %>%
  ggplot(aes(x = batted_ball_type)) +
  geom_bar(aes(y = after_stat(count) / sum(af
  theme_bw()
```

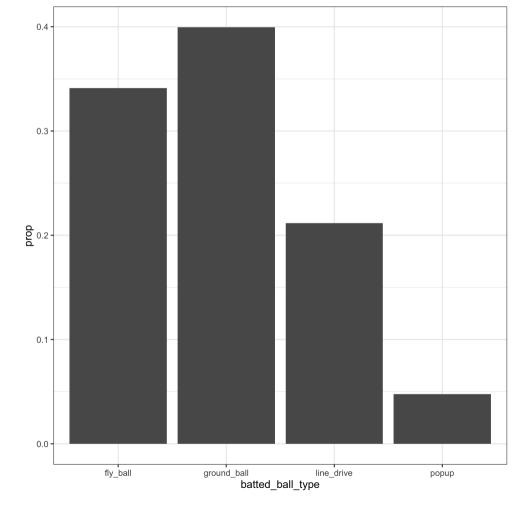
- after_stat() indicates the aesthetic mapping is performed after the statistical transformation
- Use after_stat(count) to access the stat_count() called by geom_bar()
- We can code this in a more clear way



Compute and display the proportions directly

- Category counts give info about sample size, but this could be labeled in the chart
- Proportions = the probability mass function (PMF) for discrete variables

```
\circ e.g. P (batted_ball_type = fly_ball)
```



Population versus sample...

We have the **population** of Ohtani's batted balls in the 2021 season \Rightarrow **we know the true probabilities**:

- P (batted_ball_type = fly_ball)
- P (batted_ball_type = ground_ball)
- P (batted_ball_type = line_drive)
- P (batted_ball_type = popup)

What if we pretend this is a sample from all hypothetical Ohtani 2021 seasons?

Empirical distribution: We estimate the true marginal distribution with observed (sample) data

 \Rightarrow Estimate P (batted_ball_type = C_j) with \hat{p}_j for each category C_j (e.g. $\hat{p}_{ t fly_ball}$)

Compute **standard error** for each \hat{p}_i :

$$SE({\hat p}_j) = \sqrt{rac{{\hat p}_j(1-{\hat p}_j)}{n}}$$

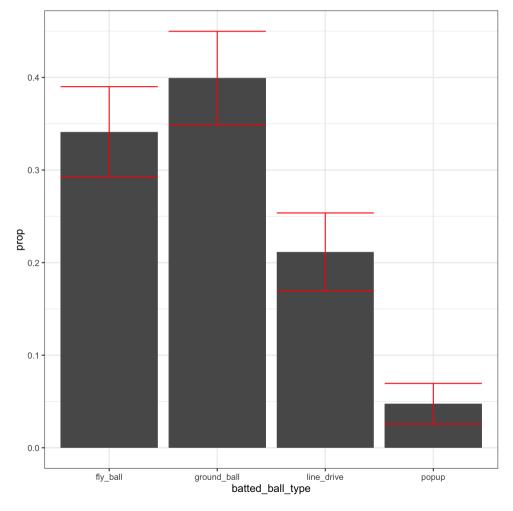
For large $n \Rightarrow pprox$ 95% **confidence interval (CI)**: $\hat{p}_{\,i} + / - 2 \cdot SE(\hat{p}_{\,i})$

Add confidence intervals to bar chart

```
ohtani_batted_balls %>%
 group_by(batted_ball_type) %>%
 summarize(count = n()) %>%
 ungroup() %>%
 mutate(total = sum(count),
         prop = count / total,
         se = sqrt(prop * (1 - prop) / total)
         lower = prop -2 * se,
         upper = prop + 2 * se) %>%
 ggplot(aes(x = batted_ball_type)) +
 geom_bar(aes(y = prop),
          stat = "identity") +
 geom_errorbar(aes(ymin = lower,
                   ymax = upper),
                color = "red") +
 theme bw()
```

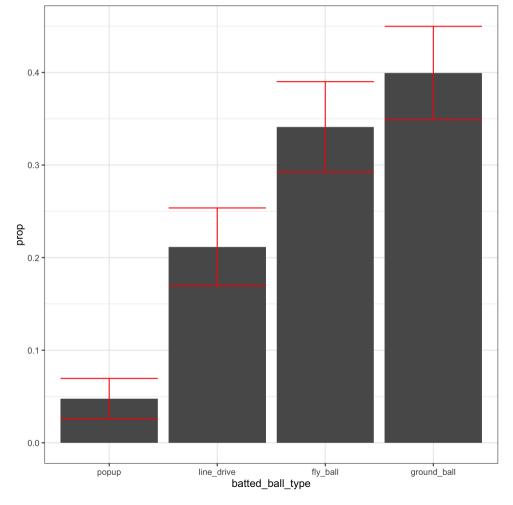
Be careful about your interpration of CIs...

You should remember to label your charts!



Fun with factors using forcats

```
ohtani_batted_balls %>%
 group_by(batted_ball_type) %>%
 summarize(count = n()) %>%
 ungroup() %>%
 mutate(total = sum(count),
         prop = count / total,
         se = sqrt(prop * (1 - prop) / total)
         lower = prop -2 * se,
         upper = prop + 2 * se,
         batted ball type =
           fct_reorder(batted_ball_type,
                       prop)) %>%
 ggplot(aes(x = batted_ball_type)) +
 geom_bar(aes(y = prop),
           stat = "identity") +
 geom_errorbar(aes(ymin = lower,
                   ymax = upper),
               color = "red") +
 theme bw()
```



Did you say pie chart?



This is the only pie chart I will show you all summer

(Note: These slides originally come from Professor Yurko, a known hater of pie charts)

Describing 1D continuous data

How can we summarize exit_velocity and other continuous variables?

- Center: mean, median, number and location of modes
- Spread: range (max min), quantiles, variance (standard deviation), etc.
- Shape: skew vs symmetry, outliers, heavy vs light tails, etc.
- Compute basic summary statistics

[1] NA

```
summary(ohtani_batted_balls$exit_velocity)

## Min. 1st Qu. Median Mean 3rd Qu. Max. NA's
## 27.50 83.75 96.00 93.26 105.55 119.00 27

sd(ohtani_batted_balls$exit_velocity)
```

Box plots visualize summary statistics

• We make a **box plot** with geom_boxplot()

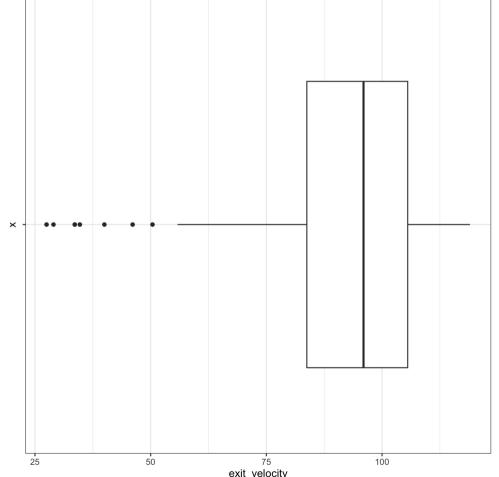
```
ohtani_batted_balls %>%
  ggplot(aes(y = exit_velocity)) +
  geom_boxplot(aes(x = "")) +
  theme_bw() +
  coord_flip()
```

• Pros:

- Displays outliers, percentiles, spread, skew
- Useful for side-by-side comparison (tomorrow)

• Cons:

- Does not display the full distribution shape!
- Does not display modes



Histograms display 1D continuous distributions

• We make **histograms** with geom_histogram()

```
ohtani_batted_balls %>%
  ggplot(aes(x = exit_velocity)) +
  geom_histogram() +
  theme_bw()
```

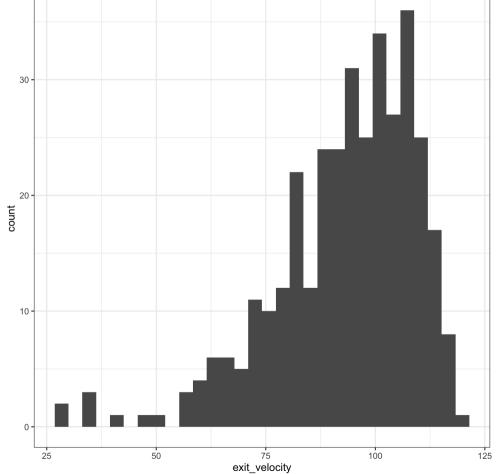
$$\# ext{ total obs.} = \sum_{j=1}^k \# ext{ obs. in bin } j$$

• Pros:

- Displays full shape of distribution
- Easy to interpret

• Cons:

 Have to choose number of bins and bin locations (will revisit later)



Display the data points directly with beeswarm plots

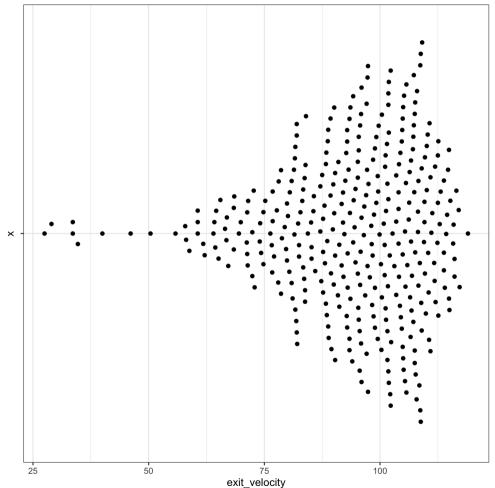
We make a beeswarm plot using the ggbeeswarm package

• Pros:

- Displays each data point
- Easy to view full shape of distribution

• Cons:

- Can be overbearing with large datasets
- Which algorithm for arranging points?



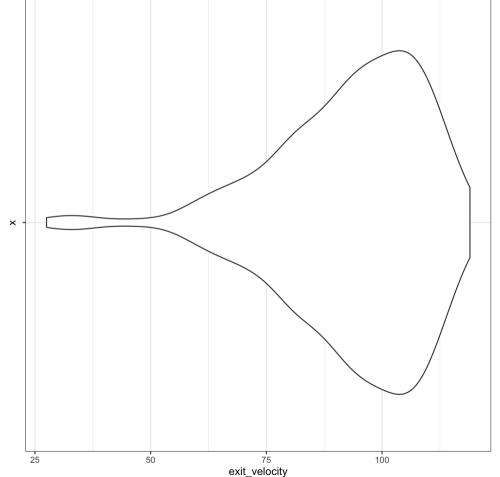
Smooth summary with violin plots

• We make **violin plots** with geom_violin()

```
ohtani_batted_balls %>%
  ggplot(aes(y = exit_velocity)) +
  geom_violin(aes(x = "")) +
  theme_bw() +
  coord_flip()
```

• Pros:

- Displays full shape of distribution
- Can easily layer...



Smooth summary with violin plots + box plots

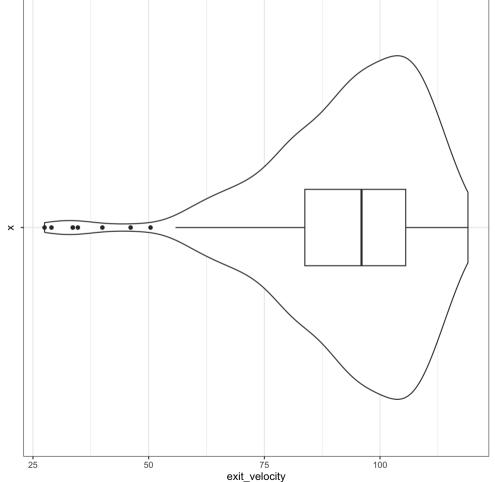
• We make **violin plots** with geom_violin()

• Pros:

- Displays full shape of distribution
- Can easily layer... with box plots on top

Cons:

- Summary of data via density estimate
- Mirror image is duplicate information



What do visualizations of continuous distributions display?

Probability that continuous variable X takes a particular value is 0

e.g.
$$P$$
 (exit_velocity = 100) = 0 , why ?

Instead we use the **probability density function (PDF)** to provide a **relative likelihood**

• Density estimation is the focus of lecture next Monday

For continuous variables we can use the **cumulative distribution function (CDF)**,

$$F(x) = P(X \le x)$$

For n observations we can easily compute the **Empirical CDF (ECDF)**:

$${\hat F}_n(x) = rac{ ext{$\#$ obs. with variable} \leq x}{n} = rac{1}{n} \sum_{i=1}^n \mathbb{1}(x_i \leq x)$$

• where 1() is the indicator function, i.e. ifelse(x_i <= x, 1, 0)

Display full distribution with ECDF plot

• We make **ECDF plots** with stat_ecdf()

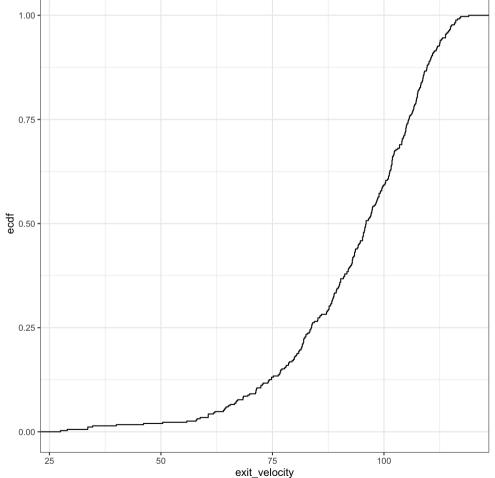
```
ohtani_batted_balls %>%
  ggplot(aes(x = exit_velocity)) +
  stat_ecdf() +
  theme_bw()
```

• Pros:

- ECDF displays all information in data (except for order)
- $\circ \:$ As $n o \infty$, our ECDF $\hat{F}_n(x)$ converges to the true CDF F(x)
- Easy to interpret...

• Cons:

• ... and yet it's not as popular!



Rug plots display raw data

• We make a **rug plot** with **geom_rug()**

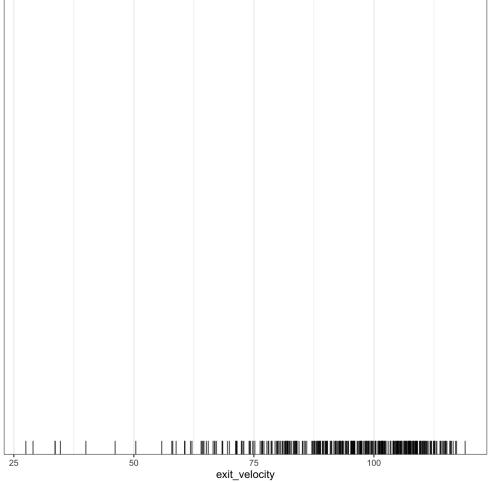
```
ohtani_batted_balls %>%
  ggplot(aes(x = exit_velocity)) +
  geom_rug(alpha = 0.7) +
  theme_bw()
```

• Pros:

- Displays raw data points
- Useful supplement for summaries and 2D plots...

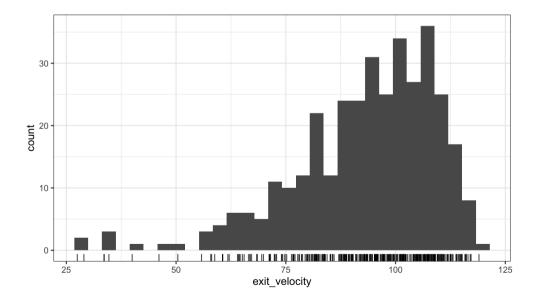
• Cons:

• Can be overbearing for larger datasets

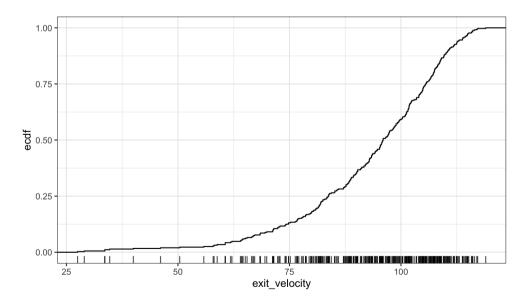


Rug plots supplement other displays

```
ohtani_batted_balls %>%
  ggplot(aes(x = exit_velocity)) +
  geom_rug(alpha = 0.7) +
  geom_histogram() +
  theme_bw()
```



```
ohtani_batted_balls %>%
  ggplot(aes(x = exit_velocity)) +
  geom_rug(alpha = 0.7) +
  stat_ecdf() +
  theme_bw()
```



Scatterplots for 2D continuous data

• We make a **scatterplot** with geom_point()

Easy to supplement with rug plots

Look at the plot: what question would you want to ask, assuming you know something about baseball?

To be continued...

