CITS5501 Software Testing and Quality Assurance Alloy

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Overview

- More on motivation for formal methods
- Alloy specification language and Alloy analyser

Issues with specifications

System specifications can suffer from a few potential problems:

- contradictions
- ambiguities
- vagueness
- incompleteness

(NB: these terms all have precise meanings. Don't assume they're interchangeable.)

- Contradictions. In a very large set of specifications, it can be difficult to tell whether there are requirements that contradict each other.
 - Can arise where e.g. specifications are obtained from multiple users/stakeholders
 - Example: one requirement says "all temperatures" in a chemical reactor must be monitored, another (obtained from another member of staff) says only temperatures in a specific range.

- Ambiguities. i.e., statements which can be interpreted in multiple different ways.
 - "The operator identity consists of the operator name and password; the password consists of six digits. It should be displayed on the security screen and deposited in the login file when an operator logs into the system."

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- "Should" can be ambiguous does "The system should do X"
 mean the system must do X, or that it is optional but desirable
 that the system do X?
- Many terms have both technical and non-technical meanings (possibly multiple of each): for instance, "reliable", "robust", "composable", "category", "failure", "orthogonal", "back end", "kernel", "platform", "entropy" . . .

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- "is tall" is vague: some people are definitely tall, and some are definitely short, but it can be difficult to tell when exactly someone meets the criterion of being tall.
- Likewise "fast", "performant", "efficiently", "scalable", "flexible", "is user-friendly", "should be secure", "straightforward to understand" are all vague.

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- e.g. An obviously incomplete requirement: "A user may specify normal or emergency mode when requesting a system shutdown. In normal mode, pending operations shall be logged and the system shut down within 2 minutes."
- ... So what happens in emergency mode?
- But other cases of incompleteness may be harder to spot.

- In addition to these, there are many other ways requirements can be written poorly –
 - e.g. Overly long and complex sentences, mixed levels of abstraction (mixing high-level, abstract statements with very low-level ones \rightarrow difficult to distinguish high-level architecture from low-level details), undefined jargon terms, specifying implementation rather than requirements (how vs what), over-specifying, don't satisfy business needs, etc.

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- Formal specifications can potentially help avoid ambiguity, vagueness, contradiction and some gaps in completeness.
- Other problems, not so much. Just as it's possible to write programs badly in any language, it's also possible to write formal specifications badly.
 - There is still a need for *review* of specifications, as with any artifact.

Some example requirements¹:

- "The system shall be highly reliable."
- "Credit card details must be encrypted."
- "The system should be easy to use by medical staff and should be organized in such a way that user errors are minimized."
- "The system shall have a response time of under 0.1 seconds."
- "If the LAUNCH-MISSILE signal is set to TRUE and the ABORT-MISSILE signal is set to TRUE then do not launch the missile, unless the ABORT-MISSILE signal is set to FALSE and the ABORT-MISSILE-OVERRIDE is also set to FALSE, in which case the missile is not to be launched."

¹Sources: Pressman; LaPlante, Requirements Engineering; bitter experience.

Formal specifications

- Formal specifications can help with ameliorating these problems.
- Sometimes, just the process of attempting to formalize a requirement can reveal problems with it.
- Using a formal model can help reveal ambiguity and vagueness and allow them to be eliminated
- It may also be possible (depending on the mathematical model used) to detect inconsistencies
- Detecting whether a specification is complete is more difficult.
 - Some gaps may be able to be detected
 - But there are nearly always some details that are left undefined, or scenarios that may not have been considered.

Formal specifications

- Formal specifications have a meaning defined in terms of mathematics.
- Similar to programming languages, there are different sorts of formal specification languages and tools, with different sorts of scope.
- Some are small and specific in scope. For instance:
 - State charts, which we have seen, define states and transitions between them.
 - Backus-Naur Form, which we have also seen, defines languages

 sets of strings.
 - Regular expressions also define sets of strings (most programming languages have an implementation of them)
 - π -calculus is used to represent concurrent systems
- Highlights another reason to use formal specifications: sometimes they're the
 most concise way of saying something. Writing a grammar or set of state
 transitions in natural language (rather than BNF or as a state chart) would be a
 gruelling and horrible exercise.
- Some are more general, and are intended to be able to describe a wide range of systems. They may be based on numerous different mathematical formalisms – predicate logic + set theory, category theory, etc.

Formal specification languages

Some examples of general-purpose specification languages:

Z notation

- based on set theory and predicate logic
- developed in the 1970s.
- Now has an ISO standard, and variations (e.g. object-oriented versions)

TLA+:

- Stands for "Temporal Logic of Actions"
- A general-purpose specification language
- Especially well-suited for writing specifications of concurrent and distributed systems
- For finite state systems, can check (up to some number of steps) that particular properties hold (e.g. safety, no deadlock)

Formal specification languages

- We'll be using the **Alloy** specification language
- Alloy is both a language for describing structures, and a tool (written in Java) for exploring and checking those structures.
- Influenced by Z notation, and modelling languages such as UML (the Unified Modelling Language).
- Website: http://alloy.mit.edu/ (The Alloy Analyzer tool can be downloaded from here.)

Alloy language and analyser

Alloy idea

The idea behind Alloy is that:

- It lets you capture the essence of a design at a high level
- It lect you identify risky aspects of a design
- It lets you develop a model incrementally
- It lets you simulate and analyze the model as you go

Alloy idea

In other words, *before* you start implementing a system, you can start specifying the entities that make it up, what constraints (i.e. invariants) hold for them, and how they hang together.

What is Alloy?

- A flexible *language* for describing structures (and how they interrelate)
- It can describe both
 - static structures
 - dynamic behaviours²

²Alloy now also has an extension, Electrum, for modelling properties of systems over time using temporal logic, but we will restrict ourselves to plain Alloy.

What is Alloy?

- A flexible *language* for describing structures (and how they interrelate)
- It can describe both
 - static structures
 - dynamic behaviours²
- Comes with a tool, the Alloy Analyzer
 - Generates counterexamples to theorems/statements

²Alloy now also has an extension, Electrum, for modelling properties of systems over time using temporal logic, but we will restrict ourselves to plain Alloy.

Alloy advantages

- Small and easy to use
- Has a simple and uniform semantics based on mathematical relations
- Can be easily analysed using automated tools

Comparison with UML

Alloy has some similarities with UML -

- It has a graphical notation
- It is somewhat similar to the Objects Constraint Language use by UML³

And several differences:

- Unlike UML, Alloy has precise semantics
- It is a far smaller and simpler formalism than UML
 - UML allows for many constructs (e.g. use cases, state charts) that don't have an equivalent in Alloy

 $^{^3}$ https://en.wikipedia.org/wiki/Object_Constraint_Language

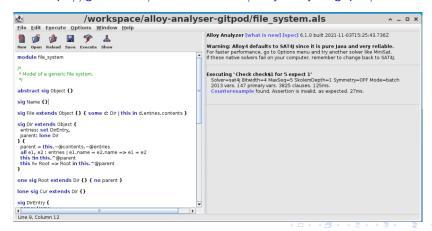
Using Alloy

- The Alloy analyser is distributed as a Java .jar file (or a .dmg file for Mac OS X) see the Alloy 6.0 release page
 - The . jar file can be run like this:

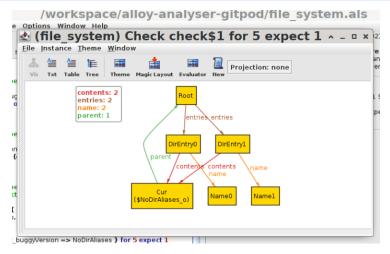
```
java -jar org.alloytools.alloy.dist.jar
```

Using Alloy

I have also set up a GitHub repository which lets you use the Alloy analyser from within an online IDE using Gitpod – visit https://github.com/arranstewart-dev/alloy-analyser-gitpod/



Using Alloy



Alloy analyser displaying a counterexample

Alloy

In Alloy, we declare rules about a mini-universe: things that exist, and properties that should be true of them.

• "There are things called animals"

```
sig Animal {}
```

• "A cat is a sort of animal"

```
sig Cat extends Animal {}
```

Alloy

When modelling entities in Alloy – we normally include only the bare minimum of properties needed in order to show how the system "hangs together".

Alloy language

- For example we'll look at a simple model of a file system (based on the Alloy tutorial at http://alloytools.org/tutorials/online/)
- The Alloy specification looks a little like Java:

```
// A file system object in the file system
sig FSObject { parent: lone Dir }

// A directory in the file system
sig Dir extends FSObject { contents: set FSObject }

// A file in the file system
sig File extends FSObject { }
```

Alloy primitives

- In Alloy, everything is built up from atoms and relations
- An atom in alloy is an indivisible, immutable value
 - We don't create these directly they get automatically generated by the analyser
 - Example atoms: A0, A1, B0, R0 . . .
- A relation is a structure that relates atoms together
 - It is a set of tuples

Alloy primitives

The easiest way to think of relations is probably to think of them as a sort of table – which show how columns of things are **related**.

e.g. "shares an office with":

Person A	Person	В
Alice	Bob	
Bob	Alice	
Dan	Eve	
Eve	Dan	

Each row is called a tuple.

In other languages, we might have scalar values (e.g. ints, doubles), various types of containers (e.g. array, List), and ways of combining types together into a class (or struct in C).

In Alloy, these are all subsumed under relations.

We will see that sets, scalars, properties and so on, are all defined in terms of relations.

Alloy's semantics are defined in terms of relations.

Example relations:

- "Is less than". e.g. "2 < 4", "10 < 9".
- "Is the blood relative of". e.g. "Alice is the blood relative of Bob".
- "Shares an office with". e.g. "Bob shares an office with Carol".

These are all *binary relations*. Statements about two entities, which can be true or false.

Relations can also be *unary* (about one entity):

- "Is even". e.g. "even(2).
- "Is an employee". e.g. "Dan is an employee".

They can be ternary:

• "_ is delivered to _, by _". e.g. "The *blue book* was delivered to *Alice*, by *Bob*".

Or, in general, they can be n-ary — a statement about n things.

We can think of predicates as being functions — an n-ary predicate isn't true or false in itself, until we supply it with n arguments.

• "Is less than" isn't true or false, but "2 < 4" is.

Relations can be finite, or infinite.

An infinite relation: "is less than"

Number A	Number B
1	2
1	3
2	3

• Sets are unary (1-column) relations. e.g.

```
Name = { N0,
N1,
N2 }
```

• Scalars are actually 1-element sets:

```
myName = N0
```

• Binary or ternary or higher relations are possible:

Alloy – sigs

sig Animal {} says "There are things called animals".

It defines a unary relation, "Animal". Something thing can be-an-animal, or not.

Alloy - sigs

sig Cat extends Animal {} says "Cats are a sort of animal".

If something has the property "is-an-animal", *then* it might also have the property "is-a-cat".

We can read "extends" as also meaning "is a kind of", or "is a subtype of".

Alloy – subtypes

- So, extends indicates subtypes (similar to Java).
- Here, Dir and File are both subtypes of FSObject:

```
sig FSObject {}
sig Dir extends FSObject {}
sig File extends FSObject {}
```

- When we declare Dir or a File to be sub-types of FSObject, they are considered to be mutually disjoint sets
- The above says "There are things called FSObjects. An FSObject might be a Dir or it might be a File, but not both".

```
We can specify properties of entities:
// A file system object in the file system
sig FSObject { parent: lone Dir }

// A directory in the file system
sig Dir extends FSObject { contents: set FSObject }

// A file in the file system
sig File extends FSObject { }
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```

These are usually written within the sig of an entity.

They actually represent *relations* between entities.

```
// A file system object in the file system
sig FSObject { parent: lone Dir }
```

There are multiple ways of reading this:

- "There are such things as FSObjects. An FSObject has the property 'parent'. An FSObject can have zero or one parents."
 Or –
- "A relation 'parent' exists between FSObjects and Dirs.
 Whenever an FSObject appears in the relation, it can be association with at most one Dir."

These are exactly equivalent.

```
// A file system object in the file system
sig FSObject { parent: lone Dir }
```

- The "lone" means "zero or one". It is a cardinality.
- Other possible cardinalities are:
 - "some" (one or more)
 - "one" (exactly one)
 - "set" (zero or more)
- When we specify a property using a colon in this way, the default multiplicity is one.
- We can use cardinalities whenever we are specifying a set or relation: since sigs also represent sets (e.g. the set of Dirs), we can give them cardinalities, too.

```
one sig RootDir extends Dir { }
```

There exists a "RootDir", but only one of them.

Games:

- There are things called games.
- Games can be board games, or field games.
- There may be other sorts of games.

Alloy language – comments

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// A file system object in the file system
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// A directory in the file system
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Comments can be written in multiple ways

Alloy language – comments

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- Comments can be written in multiple ways
 - single-line comments with "//" or " - "

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- Comments can be written in multiple ways
 - single-line comments with "//" or "--"
 - multile comments with "/* ... */"

Alloy – facts

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 (i.e., there are no other sorts of FSObject)

Alloy – facts

- How can we express that any FSObject is either a Dir or a File?
 (i.e., there are no other sorts of FSObject)
- Alloy also allows us to specify constraints. These are introduced with the keyword fact.

```
sig FSObject { parent: lone Dir }
sig Dir extends FSObject { contents: set FSObject }
sig File extends FSObject { }

// All file system objects are either files or directories
fact { File + Dir = FSObject }
```

Alloy – facts

The general syntax for a fact is

```
fact name { formulas }
```

 formulas are Boolean expressions, and by putting them in a fact, we're constraining them to be true.

Alloy – abstract signatures

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Alloy – abstract signatures

- (An alternative way to say that all FSObjects must be Dirs or Files would be to declare FSObject abstract)
- (This is similar to the use of the abstract keyword in Java; it means there are no objects that are directly of type FSObject; they must be members of some subtype, instead.)

Alloy – operators

Operators are available to construct Boolean expressions.

- subset: in
 - set1 in set2 set1 is a subset of set2
 - informally: "some set2 are set1", or "a set2 may be set1"; but the set-theoretic meaning is more precise.
- set equality: =
 - set1 = set2 set1 equals set2
- scalar equality: =
 - scalar = value scalar equals value

Alloy – subsets

- We saw that subtypes are disjoint.
- We can also declare subsets:

```
sig signame in supername { ... }
```

 Subsets are not necessarily disjoint, and may have multiple parents

Alloy – subsets

```
sig Animal {}
sig Cat extends Animal {}
sig Dog extends Animal {}
sig FurryPet in Cat + Dog {}
```

- "FurryPet" is a subset of the union of Cat and Dog.
- Some dogs and cats may not be furry (hairless breeds).
- We could make them all furry as follows:

```
fact { Cat + Dog = FurryPet }
```

Are there animals other than cats and dogs?
 Can they be furry?

More operators

- We can use Boolean connectives and, or, implies, iff, not to join Boolean expressions.
- e.g.

fact
$$\{A + B = C \text{ and } X + Y = Z\}$$

- In our file-system example, we also saw things in the *body* of signatures (i.e., between the braces).
- // A file system object in the file system
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  sig File extends FSObject { }
```

- To a first approximation, we can think of relations as behaving like fields in an OO language.
- sig FSObject { parent: lone Dir } can be read as
 "Things of type FSObject have a parent, which is of type Dir".
- lone means "at most one" i.e., you can have zero or one parents. (We need this because the root directory has no parent.)

```
  // A file system object in the file system
  sig FSObject { parent: lone Dir }

  // A directory in the file system
  sig Dir extends FSObject { contents: set FSObject }

  // A file in the file system
  sig File extends FSObject { }
```

More precisely, parent is a relation between FSObject and Dir.

Relations – multiplicities

- **lone** is a type of multiplicity it says how many of something there are.
- Other multiplicities:
 - one one
 - some at least one; one or more
 - set zero or more
 - o no zero
- The default multiplicity is one.

Relations – multiplicities

- In set theory terms . . .
- one means the relation is a total function —
 sig Student { name : one String } —
 for every Student, we can map to a string which is their name.
- lone means the relation is a partial function —
 sig Student { driverLicenseNum : lone String } \
 for every Student, we may be able to map to a diver's license number.

(Here, it's assumed you can't have more than one license.)

• So, signature declarations will look like:

```
sig SomeName {
  field1 : FieldType,
  field2a, field2b : OtherFieldType
}
```

 The order of declarations doesn't matter – SomeName, FieldType and OtherFieldType could be declared in any order in a file.

- // A directory in the file system
 sig Dir extends FSObject { contents: set FSObject }
- Here, we say that a Dir has a field contents, which is a set of FSObjects.
- The could contain one item, many items, or no items.

Examples

"A car has one engine"

```
sig Car { engine: one Engine }, or
sig Car { engine: Engine }
```

"People have zero or more hobbies"

```
sig Person { hobbies: set Activity }
```

• Classes have at least one lecturer, and zero or more students.

- Classes have at least one lecturer, and zero or more students.
- Animals have zero or more legs

- Classes have at least one lecturer, and zero or more students.
- Animals have zero or more legs
- Some animals are carnivores

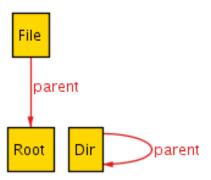
- Classes have at least one lecturer, and zero or more students.
- Animals have zero or more legs
- Some animals are carnivores
- Textbooks have one or more pages

```
sig FSObject { parent: lone Dir }
sig Dir extends FSObject { contents: set FSObject }
sig File extends FSObject { }
// There exists a root
one sig Root extends Dir { } { no parent }
```

- FSObjects have parents, and directories have contents, and we have constrained the multiplicities . . .
- but there's currently no connection between them.

File system

So we could have this situation:



File system

• We will need to constrain things more, so we'll use a fact.

```
// A directory is the parent of its contents
fact { all d: Dir, o: d.contents | o.parent = d }
```

- This says: "for any thing (let's call it d for the moment) of type Dir, and for any thing (let's call it o for the moment) which is in the set d.contents: o's parent is d.
- It uses a quantifier ("all") we'll look at these more later.