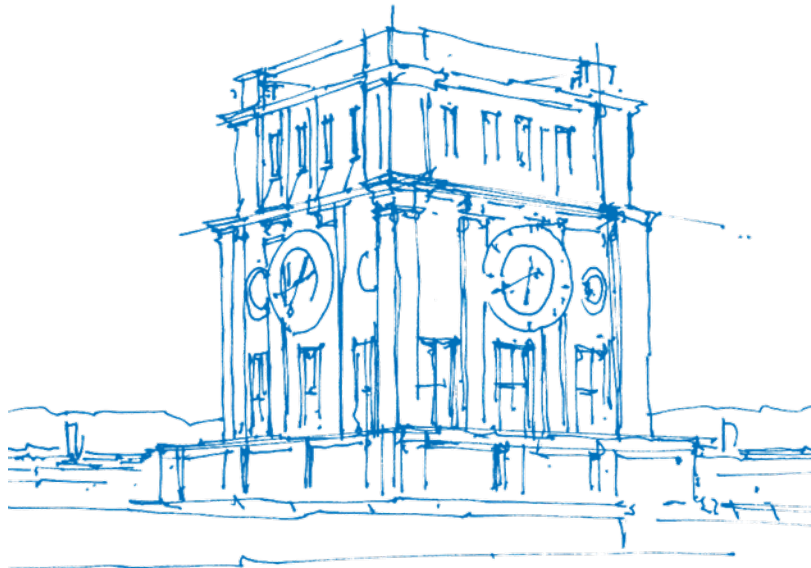


# MLCMS, Lecture 5: Extracting dynamical systems from data

Felix Dietrich

2023-06-12—organizational issues



*TUM Uhrenturm*

# Organizational issues

## Groups, Moodle, Reports

- Report due for exercise 4: 2023-06-12
- Report due for exercise 5: 2023-06-26
- Please send a one page summary of your planned final project until 2023-06-26
  - by email to me, [felix.dietrich@tum.de](mailto:felix.dietrich@tum.de),
  - and even better: a few days before, so I can give feedback and you can start right away.

# Recap / Outlook

## Lecture 1: Modeling crowd dynamics

- Modeling approaches, verification and validation

## Lecture 2: Simulation software

- Introduction to the Vadere software, SIR models

## Lecture 3: Representation of data

- Principal Component Analysis, Diffusion Maps, neural networks

## Lecture 4: Dynamical systems and bifurcation theory

- Introduction to the theory and examples

## Lecture 5: Extracting dynamical systems from data

- Function approximation, vector fields, time-delay embedding, (final projects)

## Lecture 6: Future directions of machine learning

- Challenges in data science, master's thesis topics, final projects

# Today: Machine Learning, take 2!

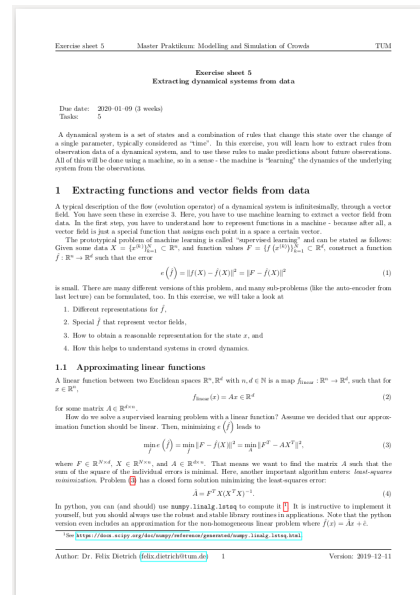
## Extracting dynamical systems from data

1. Video 2: Approximating functions from data
2. Video 2: Vector fields from observations
3. Video 2: Time-delay embedding
4. Exercise 5
5. Final projects

# Representation of data

## Exercise 5

You can find the exercise sheet on Moodle



# Next lecture

## Summary, outlook, final project

1. Lecture (but no exercise): summary and future topics of machine learning
2. Discussions of final projects (25% of your grade!)
  - 2.1 You have to decide on a final project for your group.
  - 2.2 Send me a one-page summary with five task descriptions for your project.
  - 2.3 On the day of the lecture (2023-06-26) we will briefly discuss the projects you chose.
  - 2.4 I will assign a presentation date for your group: 2023-07-10, or 2023-07-17.
  - 2.5 You have to hand in the report until 2023-07-17 (three weeks time!).
  - 2.6 Grading for the final project is 1/3 code, 1/3 report, and 1/3 presentation.
  - 2.7 This year the presentations will be online, on Zoom. You can present on-site if you like, but you must let me know (by email) at least a week before.
  - 2.8 The following final project suggestions can be taken by multiple groups each, so no first-come-first-served. You still need to send me your project description page, though!

# Final projects

(Example 1-page suggestion)

(from a previous semester)

# Final projects

## (Example 1) - Good visualization

Develop an efficient, robust and functional visualization for crowd trajectories.

**Task1** Setting up the software environment: Unity? Unreal? Own code?

**Task2** Two-dimensional visualization of individuals and obstacles

**Task3** Additional visualization elements: trajectories, target zones

**Task4** Basic user interaction: fast forward, jumping in time, zooming

**Task5** Three-dimensional visualization



# Final projects

## (Example 2) - Learning dynamical systems from data: Neural networks

Implement Euler and Runge-Kutta templates in neural networks. This is a review and implementation of the papers [Rico-Martinez et al., 1994, Rico-Martínez and Kevrekidis, 1995].

**Task1** Summary of the paper contents

**Task2** Setting up the neural network for Euler's method

**Task3** Setting up the neural network for the Runge-Kutta method

**Task4** Testing the networks in a two-dimensional dynamical system example

**Task5** Constructing bifurcation diagrams using the extracted dynamics

# Final projects

## (Example 3) - Adding a module to Vadere

Work with the Vadere software and add an interesting module (velocity processor, simple bifurcation analysis, 3D visualization).

**Task1** Description of the module structure: requirements, software, etc.

**Task2** Stand-alone implementation for testing

**Task3** Integration into Vadere

**Task4** Testing the module on a crowd dynamics example

**Task5** Unit tests

# Final projects

## (Example 4) - Learning dynamical systems from data: Koopman

Study the Koopman operator framework [Budišić et al., 2012, Williams et al., 2015b, Williams et al., 2015a, Li et al., 2017, Mauroy and Goncalves, 2017, Dietrich et al., 2020] and implement/understand the Extended Dynamic Mode Decomposition in [Williams et al., 2015b] (the `datafold` software already implements EDMD).

- Task1** Description of the Koopman operator
- Task2** First, own implementation of the EDMD algorithm
- Task3** Tests on an example in the paper by Williams et al.
- Task4** Tests on a simple example in crowd dynamics (I will give you one)
- Task5** Discussion of the results

# Final projects

## (Example 5) - Learn and visualize representations for large data sets

This is a review and implementation of the paper [McQueen et al., 2016]. Choose if you want to use “datafold”, or test neural network (auto-encoder) performance against theirs.

**Task1** Description of the data sets

**Task2** Using existing implementation of 2-3 fast representation algorithms

**Task3** Tests on a large dataset you make up yourself

**Task4** Tests on one of the large datasets in the paper

**Task5** Comparison to their results

# Final projects

## (Example 6) - Redo a bifurcation scenario from Prof. Starkes papers

You may have already read one of the bifurcation analysis papers by the group of Prof. Starke [Starke et al., 2014, Marschler et al., 2014, Marschler, 2014]. Decide on one and try to reproduce their results.

**Task1** Description of the example, discussion of challenges and your choice of method

**Task2** Implementation of the bifurcation analysis

**Task3** Tests on a simple example

**Task4** Tests on one of the examples in the paper

**Task5** Comparison to their results

# Final projects

## (Example 7) - Discuss a neural network paper for crowd dynamics

Do a literature review of [Tordeux et al., 2019]. Decide on one example and try to reproduce their results. Careful: they chose a very special neural architecture (very few neurons), so the discussion must be about that, too!

**Task1** Description of the example, discussion of challenges and your choice of method

**Task2** Implementation of the neural network

**Task3** Tests on a simple example

**Task4** Comparison to their results

**Task5** Discussion of the approach and architecture.

# Final projects

(Example 8) - Pedestrian trajectory prediction methods: deep learning and knowledge-based approaches

Discuss the two directions from the review of [Korbmacher and Tordeux, 2022].

**Task1** Introduction of the two approaches separately.

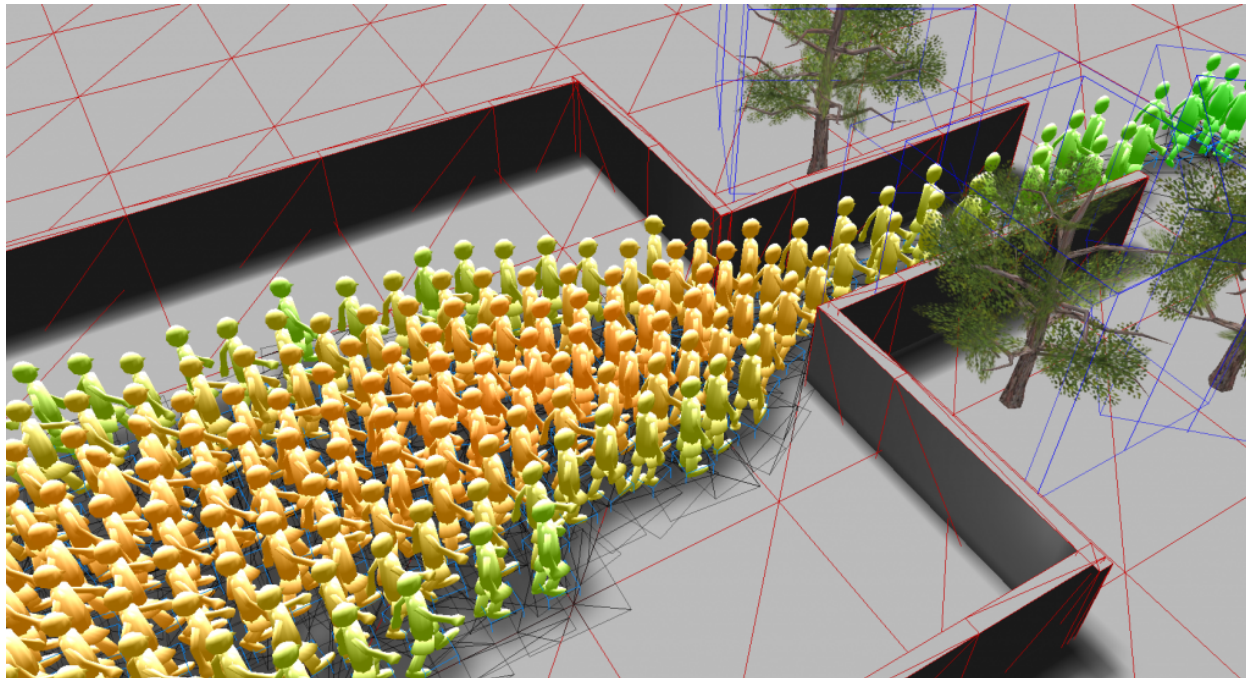
**Task2** Discussion of the benefits.

**Task3** Discussion of the drawbacks and challenges.

**Task4** Comparison of the approaches.

**Task5** Discussion of future work and other approaches, separate from the review paper [Korbmacher and Tordeux, 2022].

# Questions?



Homework 1: finish fourth exercise & upload report until 2023-06-12.










Homework 2: finish fifth exercise & upload report until 2023-06-26.

Final project: Send me a list of five tasks with a short description until 2023-06-26.



For questions / appointments: please ask via email, [felix.dietrich@tum.de](mailto:felix.dietrich@tum.de).



# Literature I

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# Literature II

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-  Williams, M. O., Rowley, C. W., Mezić, I., and Kevrekidis, I. G. (2015b).  
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