

Supporting Information – Computer Modeling

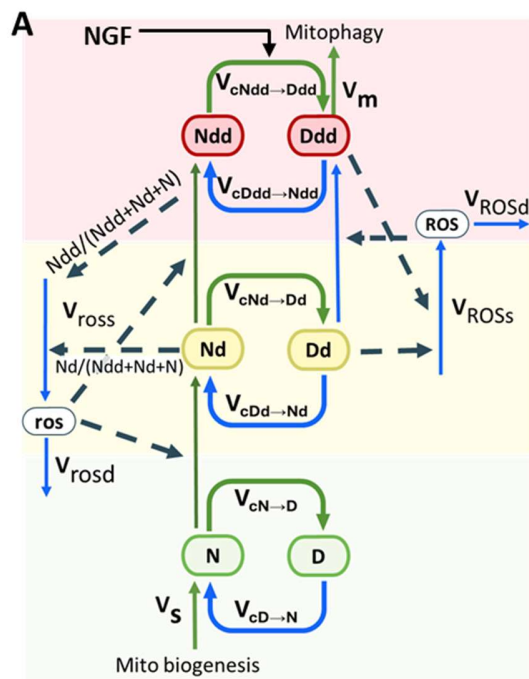
Fusion-fission-mitophagy cycling and metabolic reprogramming coordinate Nerve Growth Factor (NGF)-dependent neuronal differentiation

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Computational Modeling: Raw data, instructions and recipes/Global quantities for the Copasi simulations

Diagram of the fusion-fission-mitophagy model

The Figure shows the diagram for the model (Figure 5, main text): Networked mitochondria are indicated by capital N and dispersed mitochondria by capital D. For each of these mitochondria there are three versions, i.e. undamaged (N, or D), somewhat damaged (Nd and Dd) and severely damaged (Ndd and Ddd). *ros* refers to ROS in the vicinity of the networked mitochondria. Nd and Ndd activate 'ros' synthesis beyond a constitutive process, whereas 'ROS' synthesis is fully dependent on Dd and Ddd. The rate constants for the three fission processes from networked to dispersed are identical and called the 'fission rate constant'. Analogously, the rate constants for the fusion of dispersed to networked mitochondria are all equal to the 'fusion rate constant'. Solid arrows refer to mass flow (mitochondria or ROS). Dashed arrows refer to influence/regulation. 'v' refers to reaction rates. It will be assumed that NGF addition increases the rate constant for fission.



In our preliminary modeling studies, the concentration of mitochondria changed strongly by a factor of 2.5 within a few hours after NGF addition (Westerhoff, unpublished). Although this simulated the doubling of the respiratory rate observed in (Martorana et al., 2018), it was considered unrealistic as no such a strong change was observed microscopically in the mitochondrial mass. We therefore turned to a model where the total number of mitochondria did not change so fast by so much. In order to explain the 2-fold increase in respiration observed experimentally 24h after NGF addition, we instead considered the possibility that the strongly damaged mitochondria would be so damaged in their Complex I of the respiratory chain that they had strongly reduced respiration.

The preliminary model exhibited a strong decrease in mitophagy flux within a few hours (after a rapid transient 4-folds increase) (Westerhoff, unpublished). The experimental data were consistent with a substantial increase in mitophagy however (and autophagy in Martorana et al. 2018). We gathered that the strong dependence of the mitophagy flux on the Ddd concentration kept the concentration change of Ddd small.

This made us consider a variant of the model in which the rate of mitophagy was a Michaelis-Menten function ($v = \frac{Ddd \cdot \frac{V}{K_M}}{1 + \frac{Ddd}{K_M}}$) of the concentration of Ddd, where the K_M was chosen around the average Ddd concentration in the model (Westerhoff, unpublished). This was inspired by the experimental observation that the number of mitochondria around a potential mitophagy site was often much higher than the number of lysosomes, potentially making the lysosomal concentration limiting (Westerhoff and Colangelo, unpublished).

This Copasi file was optimized further. This optimization involved minor further parameter changes and a facility exhibiting the time dependence before NGF addition. This facility was added to ensure that (e.g. upon parameter changes) the model should always start from the steady state. This Copasi was used for the simulations showed in Figure 5 in the main manuscript. The corresponding files are in the directory called 'fusion fission models' including:

- The text file 'instructions'
- The model file 'fig5.cps'
- Fig5D data
- Fig 5 Global quantities of the model with values

In modeling the effect of NGF addition, the crucial parameter is the fission rate constant, which is the sole parameter changed (i.e., increased by a factor of 20) to simulate the effect of NGF addition. $k_cnd0_final = 3.6$ is increased from $0.18 (=k_cnd0_initial)$, which was the value at the initial steady state. This increase is gradual at a $t_{1/2}$ of $t_half_cnd=3.33$ h through the formula:

$k_cycling\ network\ to\ disperse = \{Values[k_cnd0_initial].InitialValue\} + \{Values[NGF\ added]\} * (\{Values[k_cnd0_final].InitialValue\} - \{Values[k_cnd0_initial].InitialValue\}) * (1 - EXP(-(\{Time\} - \{Values[NGF\ addition\ time]\}) / \{Values[t_half_cnd].InitialValue\}))$.

The model starts from the parameter setting $k_cnd0_final_0 = 0.01$, which is then equal to $k_cnd0_initial_0$ and which, if maintained at the value, corresponds to the *initial* steady condition (see

below). This may be checked by time integration for 100 h after addition of NGF (or by asking for steady state and ignoring a Copasi warning), which should show that all variables are constant in time. The *final* steady state may be obtained by setting $k_{\text{cnd0_initial_0}} = 0.2$ (equal to $k_{\text{cnd0_final_0}}$) and then asking for steady state. These settings of $k_{\text{cnd0_initial_0}}$ and $k_{\text{cnd0_final_0}}$ lead to the settings mentioned above for the actual rate constant for fission, i.e. $k_{\text{cnd0_final}} = 3.6$ and $k_{\text{cnd0_initial}} = 3.6$.

The Copasi file of the model that produces Figure 5 carries the name: Fig5.cps

The model has the following concentrations of the variables in the two steady states (initial and final steady-states):

| Initial steady state | (small fission rate constant) Obtained by setting both $k_{\text{cnd0_initial_0}}$ and $k_{\text{cnd0_final_0}}$ to 0.01 | |
|-----------------------------|---|-------------------------------|
| Species | Concentration [$\mu\text{mol/l}$] | Concentration/Nmitomax |
| D | 0.000176513 | 0.0882565 |
| Dd | 8.20E-06 | 0.004097735 |
| Ddd | 0.000214598 | 0.107299 |
| N | 0.000151928 | 0.075964 |
| Nd | 9.50E-05 | 0.047512 |
| Ndd | 0.000306239 | 0.1531195 |
| ros | 0.127895 | |
| ROS | 1.0734 | |
| final steady state | (high fission rate constant) Obtained by setting both $k_{\text{cnd0_initial_0}}$ and $k_{\text{cnd0_final_0}}$ to 0.2 | |
| Species | Concentration [$\mu\text{mol/l}$] | Concentration/Nmitomax |
| D | 0.000844049 | 0.4220245 |
| Dd | 2.30E-05 | 0.01151525 |
| Ddd | 0.000103507 | 0.0517535 |
| N | 0.000353532 | 0.176766 |
| Nd | 1.56E-05 | 0.00780955 |
| Ndd | 4.35E-05 | 0.02177415 |
| ros | 0.0248888 | |
| ROS | 0.518685 | |

The global parameters are in the model file fig5.cps and in 'Fig 5 Global quantities of the model with values.xlsx' in the folder 'fusion fission model'

The model Fig5.cps produces the simulations of Figure 5B, 5C and 5E and can be used to reproduce the simulations used for the figure 5F, 5G and 5H.

Recipe for the simulation of the figures 5B, 5C, 5E and 5E_2

Open model Fig5.cps with Copasi, press task, time course and run simulation.

Recipe for the simulation used for the figures 5F

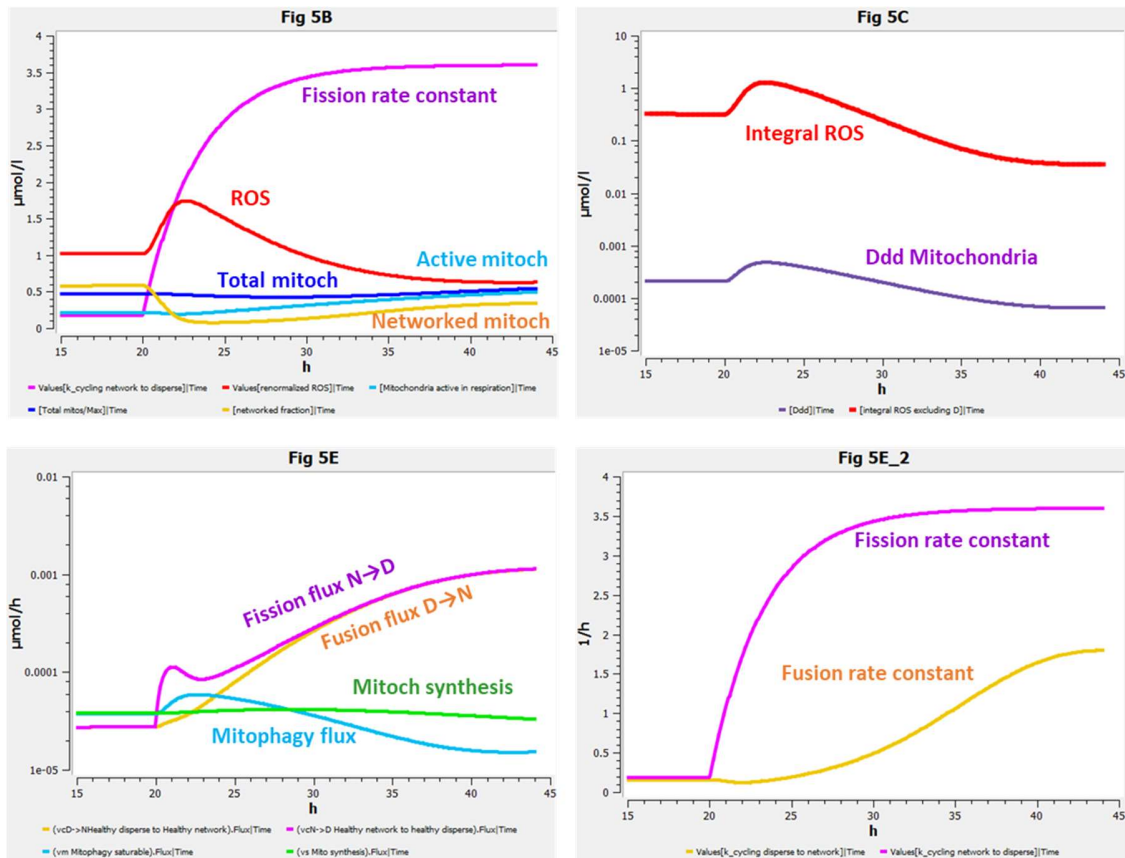
Open model fig5.cps and set the global quantity “k_cnd0_final_0” to 0.1, 0.05 or 0.02. Then run time course.

Recipe for the simulation used for the figures 5G and 5H

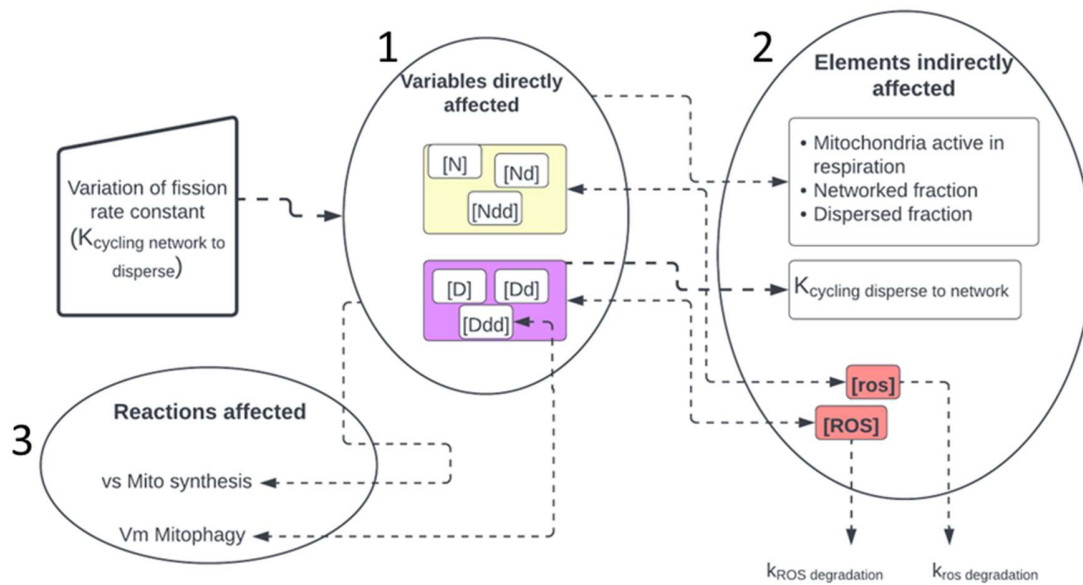
Open model fig5.cps and set the global quantity “ $K_{\text{MMitophagy}}$ ” to 1×10^{-4} , 1×10^{-5} 1×10^{-2} . Then run time course and see the change in ROS curve. Furthermore, setting the value of $K_{\text{MMitophagy}}$ equal to 1×10^{-2} it is possible to reproduce the curve of active and total mitochondria shown in figure 5H.

Results of the Copasi simulations discussed in the main text and Figure 5

The Copasi in 5E_2 shows the trends of fission and fusion constants in the NGF differentiation model. After increasing the fission rate constant from 0.18 to 3.6, also fusion starts to increase to 1.8.



Modeling scheme representing the computational modeling procedure and its direct/indirect effect on the other variable of the network. What happens if we alter the fission rate constant? Variation in the fission rate constant directly affects the concentration of all mitochondrial populations because it acts on the fission reaction that transforms network mitochondria into dispersed mitochondria (circle 1). Indirectly, this variation alters the concentration of ROS and ros through modifications in the concentration of dispersed and networked mitochondria (circle 2). These events affect changes in the actively respiring mitochondria (including the healthy fraction plus those slightly damaged) and the ratios of dispersed and networked mitochondria over the total. Furthermore, the reactions of mitophagy (V_m mitophagy) and of the synthesis of new mitochondria (V_s Mito synthesis) are affected (circle 3).



Although the mathematical model developed in this paper fits the experimental data at hand, it cannot yet be considered complete and it may not even be quite correct as it stands. For it is very difficult to measure the values of the model's kinetic parameters directly inside the living cells. In vitro experiments come with the difficulty of precisely mimicking the in vivo conditions inclusive of the spatial aspects, binding of molecules to the mitochondrial membranes, and variations due to cell type differences. Consequently, the parameter values used in the model had to be based on 'reasonable assumptions', e.g. such that the parameters do not exceed the diffusion limit and are not too disparate from parameter values used in other models for cell biology. We have also attempted to limit the number of parameters, for with an unlimited number of parameters one may fit almost every dynamic behavior. An example is our choice to keep the fission rate constant the same, independent of the state of damage of the networked mitochondria to be split. This still allows the fission rates to depend on the damage state, but

only through mass action, which is the simplest option. The assumption boils down to assuming that the damage per se does not interfere with the fission process.

An advantage of having the model at hand is that if one doubts the validity of these simplicity assumptions, one can readily modify the model so add any better information one may have available. We have simulated this for the example of the fission constant. As shown below, quite an appreciable differentiation between the three fission rate constants did affect the simulated curves, but not to the extent that the fit of the experimental data became significantly better.

Model behavior with different fission rate constants k for distinct mitochondrial states (i.e. D, Dd and Ddd)

Distinct mitochondrial populations (healthy, mildly damaged, and highly damaged mitochondria) might be differently prone to undergo fission, this implying different fission rate constants k . To examine whether this could affect our conclusions, we tested how the model would behave when applying different fission rate constants for the distinct types of mitochondria.

The following table shows the new global quantities based on three fission rate constants and three relative constants for the initial and final value, whose total sum (sum of rate constants) would be 3.6 (the value of the fission rate constant in the original model).

We arbitrarily distributed the old value of 3.6, considering a damage-dependent increase (Fig. 4B Suppl1, named after the corresponding Figure 4B in the main text).

For the reaction $N \rightarrow D$ the final constant is: **$k_{\text{cnd0_final_D}} = 0.6$**

For the reaction $Nd \rightarrow Dd$ the final constant is **$k_{\text{cnd0_final_Dd}} = 1$**

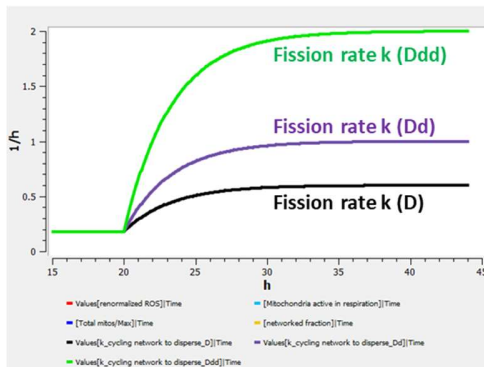
For the reaction $Ndd \rightarrow Ddd$ the final constant is **$k_{\text{cnd0_final_Ddd}} = 2$**

| Name | Initial Value [Unit] | Initial Expression [Unit] | Expression [Unit] or [Unit/h] |
|-----------------------------------|----------------------|---------------------------|--|
| k_cycling network to disperse_Ddd | 0.18 | | Values[k_cnd0_initial_Ddd].InitialValue+Values[NGF added]*(Values[k_cnd0_final_Ddd].InitialValue-Values[k_cnd0_initial_Ddd].InitialValue)*(1-EXP(-(Time-Values[NGF addition time])/Values[t_half_cnd].InitialValue)) |
| k_cycling network to disperse_D | 0.18 | | Values[k_cnd0_initial_D].InitialValue+Values[NGF added]*(Values[k_cnd0_final_D].InitialValue-Values[k_cnd0_initial_D].InitialValue)*(1-EXP(-(Time-Values[NGF addition time])/Values[t_half_cnd].InitialValue)) |
| k_cycling network to disperse_Dd | 0.18 | | Values[k_cnd0_initial_Dd]+Values[NGF added]*(Values[k_cnd0_final_Dd].InitialValue-Values[k_cnd0_initial_Dd].InitialValue)*(1-EXP(-(Time-Values[NGF addition time])/Values[t_half_cnd].InitialValue)) |
| k_cnd0_final_D | 0.6 | 0.6 | Values[time_factor].InitialValue*Values[k_cnd0_final_0_D].InitialValue |
| k_cnd0_final_Dd | 1 | 1 | Values[time_factor].InitialValue*Values[k_cnd0_final_0_Dd].InitialValue |
| k_cnd0_final_0_D | 0.033333 | 0.033333 | |

| | | | |
|-------------------------|----------|----------|--|
| k_cnd0_final_0_Dd | 0.055556 | 0.055556 | |
| k_cnd0_initial_D | 0.18 | | Values[time_factor].InitialValue*Values[k_cnd0_initial_0_D].InitialValue |
| k_cnd0_initial_Dd | 0.18 | | Values[time_factor].InitialValue*Values[k_cnd0_initial_0_Dd].InitialValue |
| k_cnd0_initial_0_D | 0.01 | | |
| k_cnd0_initial_0_Dd | 0.01 | | |
| k_cnd0_final_Ddd | 2 | 2 | Values[k_cnd0_final_0_Ddd].InitialValue*Values[time_factor].InitialValue |
| k_cnd0_initial_Ddd | 0.18 | 0.18 | Values[k_cnd0_initial_0_Ddd].InitialValue*Values[time_factor].InitialValue |
| k_cnd0_final_0_Ddd | 0.111111 | 0.111111 | 0 |
| k_cnd0_initial_0_Ddd | 0.01 | 0.01 | 0 |

Results of Copasi simulations with 3 fission rates

The following Copasi plot shows the time dependent first-order fission rate constants k used for the extended model 'Fusion fission model bis' with distinct rate constants for the three types of dispersed mitochondria.



Using the above damage-dependent fission rate constant k , we observed that the trends of ROS, and of the distinct mitochondrial populations (total, active and network) (shown below) do not change substantially (Figure 5Bbis, 5Cbis, 5Dbis, 5Ebis), compared to the original model (Figure 5, main text). Fission, fusion and mitophagy fluxes, as well as mitochondrial synthesis behave similarly.

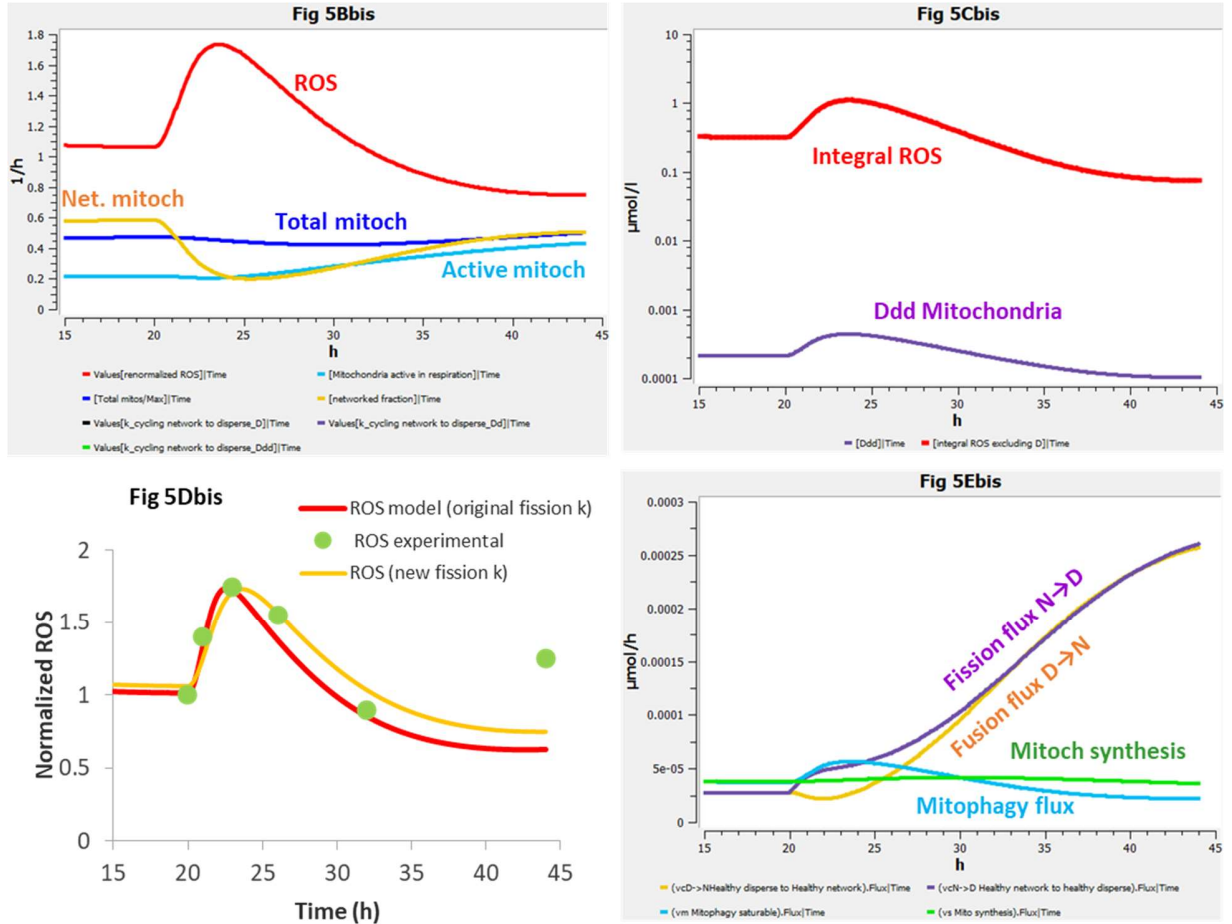


Figure 5bis. 5B-Cbis) Modeling NGF-induced differentiation by applying different fission rate constants to distinct mitochondrial populations (for the reactions: $N \rightarrow D$, $k = 0.6$; $Nd \rightarrow Dd$, $k = 1$; $Ndd \rightarrow Ddd$, $k = 2$) and model response in terms of: ROS content, total mitochondria, active mitochondria and networked mitochondria (Bbis), Integral ROS and Ddd mitochondria (Cbis). **Dbis)** Fit of the model based on the three new fission rate k (orange line) to experimental (dots) data of ROS induced by NGF, compared to the model based on one single fission rate K (red line) (Copasi Fig5.cps). **Ebis)** Modeling the effect of increasing the fission rate constant on fission, fusion, mitophagy flux, and mitochondrial synthesis.

The Copasi figures (5Bbis, 5Cbis and 5Eb1s) show that the model behavior (Ddd mitochondria, ROS, mitophagy flux, mitochondrial quality and fusion flux) does not change when applying distinct fission rate k for the distinct mitochondria populations ($N \rightarrow D$, $Nd \rightarrow Dd$, and $Ndd \rightarrow Ddd$). Also the ROS behavior with the new fission rate constant k does not change significantly (Figure 5Dbis), compared to the fitting of model and experimental data observed with one single fission rate constant k (compared to Figure 5D, main text). However, the ROS curve with the three distinct rate constants k improves the fitting of the experimental point 4 ($t = 26$ h), while slightly decreasing the fitting of the experimental point 5 ($t = 31.98$ h).

Table 1. Description of the equations used to model and quantify the concentrations of mitochondria, ROS, mitochondrial fractions and cycling constants.

| Differential equation | Variables and constants | Reactions involved | Explanation |
|--|---|--|---|
| $\frac{d([D] \cdot V_{compartment})}{dt}$ $= +V_{compartment} \cdot (k_{cycling\ network\ to\ disperse} \cdot [N]) - V_{compartment} \cdot (k_{cycling\ disperse\ to\ network} \cdot [D])$ | <p>$[D]$= Concentration of healthy dispersed mitochondria $V_{compartment}$= total volume</p> <p>$k_{cycling\ network\ to\ disperse}$ = first order rate constant of fission reactions</p> <p>$[N]$= Concentration of healthy networked mitochondria</p> <p>$k_{cycling\ disperse\ to\ network}$ = first order rate constant of fusion reactions</p> | <p>1) $vcD \rightarrow N$: Healthy (undamaged) disperse to Healthy network (fusion)</p> <p>2) $vcN \rightarrow D$: Healthy network to healthy disperse (fission)</p> <p>3) vc stands for cycle rate</p> | D is equal to the mitochondria that undergo fission starting from N minus the mitochondria D subjected to fusion |
| $\frac{d([N] \cdot V_{compartment})}{dt}$ $= -V_{compartment} \cdot (k_{cycling\ network\ to\ disperse} \cdot [N]) - V_{compartment} \cdot (k_{constitutive\ damage\ generation\ networked\ mitochondria} \cdot [N]) + V_{compartment} \cdot (k_{cycling\ disperse\ to\ network} \cdot [D]) - V_{compartment} \cdot (k_{damaging} \cdot [N] \cdot [ros]) + V_{compartment} \cdot \left(k_{mitosynthesis} \cdot \frac{N_{mitomax} - [N] - [Nd] - [Ndd] - [D] - [Dd] - [Ddd]}{N_{mitomax}} \right)$ | <p>$k_{constitutive\ damage\ generation\ networked\ mitochondria}$ = first order rate constant of the reaction "$N \rightarrow Nd$"</p> <p>$k_{damaging}$= second order rate constant of reaction "$N \rightarrow Nd$; ros" and "$Nd \rightarrow Ndd$; ros" This determines the rate of the damaging of networked mitochondria by ROS</p> <p>$[ros]$= Concentration of ROS produced by and affecting networked mitochondria</p> <p>$k_{mitosynthesis}$ = first order rate constant of the reaction "$\rightarrow N$; $Nd \rightarrow Ndd$; $D \rightarrow Dd$; Ddd"</p> <p>$N_{mitomax}$= maximum number of mitochondria</p> | <p>1) $vcD \rightarrow N$: Healthy disperse to Healthy network (fusion)</p> <p>2) $vcN \rightarrow D$: Healthy network to healthy disperse (fission)</p> <p>3) $\rightarrow N$ (synthesis of N)</p> <p>4) $N \rightarrow Nd$ (damaging of N)</p> | N is equal to mitochondria that undergo fusion from "D" plus mitochondria synthesized de novo minus mitochondria that undergo fission starting from N, minus the amount of N which becoming Nd damaged mitochondria (caused by constitutive damage non-ROS and ROS dependent) |

| Differential equation | Variables and constants | Reactions involved | Explanation |
|---|--|---|--|
| $\frac{d([Dd] \cdot V \text{ compartment})}{dt}$ $= +V \text{ compartment} \cdot (k_{\text{cycling network to disperse}} \cdot [Nd])$ $- V \text{ compartment} \cdot (k_{\text{cycling disperse to network}} \cdot [Dd])$ $+ V \text{ compartment} \cdot (k_{\text{damaging}_{\text{dispersed}}} \cdot [Dd] \cdot [ROS])$ | <p>[ROS] = Concentration of ROS produced by and affecting dispersed mitochondria</p> | <p>1) $vcDd \rightarrow Nd$ Damaged disperse to damaged network (fusion)</p> <p>2) $vNd \rightarrow Dd$ Damaged network to damaged disperse (fission)</p> <p>3) $Dd \rightarrow Ddd$; Activator: ROS</p> | <p>Dd concentration is determined by the amount of Nd that undergoes fission, minus Dd that fuse into Nd minus the amount of Dd damaged by ROS</p> |
| $\frac{d([Nd] \cdot V \text{ compartment})}{dt}$ $= -V \text{ compartment} \cdot (k_{\text{cycling network to disperse}} \cdot [Nd])$ $- V \text{ compartment} \cdot (k_{\text{damaging}} \cdot [Nd] \cdot [ros])$ $+ V \text{ compartment} \cdot (k_{\text{constitutive damage generation networked mitochondria}} \cdot [N])$ $+ V \text{ compartment} \cdot (k_{\text{cycling disperse to network}} \cdot [Dd])$ $+ V \text{ compartment} \cdot (k_{\text{damaging}} \cdot [N] \cdot [ros])$ | | <p>1) $vcDd \rightarrow Nd$ Damaged disperse to damaged network (fusion)</p> <p>2) $vNd \rightarrow Dd$ Damaged network to damaged disperse (fission)</p> <p>3) $N \rightarrow Nd$; ros</p> | |
| $\frac{d([ROS] \cdot V \text{ compartment})}{dt}$ $= +V \text{ compartment} \cdot (k_{\text{ROS synthesis by damage}} \cdot [S])$ $+ V \text{ compartment} \cdot ([Dd] + \text{relative}_{\text{impact}} \cdot [Ddd])$ $- V \text{ compartment} \cdot (k_{\text{ROS degradation}} \cdot [ROS])$ | <p>$k_{\text{ROS synthesis by damage}}$ = constant of ROS synthesis by damaged dispersed mitochondria (Dd and Ddd)</p> <p>[S] = fixed concentration equal to 1. This models the substrate for the synthesis of ROS</p> <p>$\text{relative}_{\text{impact}}$ = parameter that makes Ddd more determinant in setting ROS than Dd. This should have the effect that once there is strong damage, much more ROS is produced leading to much higher ratio of Ddd to Dd and hence to more mitophagy.</p> <p>$k_{\text{ROS degradation}}$ = first order rate constant of ROS degradation</p> | <p>1) $S \rightarrow ROS$; Dd Ddd (ROS synthesis by damaged dispersed mitochondria)</p> <p>2) $ROS \rightarrow$ (ROS degradation)</p> | <p>[ROS] increase is equal to ROS synthesized by Dd and Ddd minus ROS degraded</p> |

| Differential equation | Variables and constants | Reaction involved | Explanation |
|---|--|--|--|
| $\frac{d([Ddd] \cdot V \text{ compartment})}{dt}$ $= +V \text{ compartment}$ $\cdot (k_{\text{cycl}ing \text{ network to disperse}} \cdot [Ndd]) - V \text{ compartment}$ $\cdot (k_{\text{cycl}ing \text{ disperse to network}} \cdot [Ddd]) - V \text{ compartment}$ $\cdot \left(\frac{V_{by} K_{M \text{ mitophagy}} \cdot [Ddd]}{1 + \frac{[Ddd]}{K_{M \text{ mitophagy}}}} \right)$ $+ V \text{ compartment}$ $\cdot (k_{\text{damaging_dispersed}} \cdot [Dd] \cdot [ROS]) - V \text{ compartment}$ $\cdot (k_{\text{mitophagy}} \cdot [Ddd])$ | <p>$K_{M \text{ Mitophagy}}$ = K_M of the Michaelis Menten reaction used to model the mitophagy reaction "Ddd →"</p> <p>$k_{\text{damaging_dispersed}}$ = first order rate constant of the reaction "Dd → Ddd; ROS" It determined the damage related to ROS</p> <p>$k_{\text{mitophagy}}$ = first order rate constant of mitophagy from an older version of the model. When the global quantity "Mitophagy saturation switch" is equal to 1 the $k_{\text{mitophagy}}$ is equal to 0 and only v_m (i.e. the saturable mitophagy reaction) acts.</p> | <p>1) $vcDdd \rightarrow Ndd$ Highly damaged disperse to highly damaged network (fusion)</p> <p>2) $vcNdd \rightarrow Ddd$ Highly Damaged network to highly damaged disperse (fission)</p> <p>3) "Ddd →" v_m saturable mitophagy reaction</p> | Ddd concentration is calculated with the sum of Ndd undergo fission, plus Dd damaged by ROS, minus Ddd eliminated by mitophagy. |
| $\frac{d([Ndd] \cdot V \text{ compartment})}{dt}$ $= -V \text{ compartment}$ $\cdot (k_{\text{cycl}ing \text{ network to disperse}} \cdot [Ndd]) + V \text{ compartment}$ $\cdot (k_{\text{cycl}ing \text{ disperse to network}} \cdot [Ddd]) + V \text{ compartment}$ $\cdot (k_{\text{damaging}} \cdot [Nd] \cdot [ros])$ | | <p>1) "$vcDdd \rightarrow Ndd$" Highly damaged disperse to highly damaged network (fusion)</p> <p>2) "$vcNdd \rightarrow Ddd$" Highly Damaged network to highly damaged disperse (fission)</p> <p>3) "$Nd \rightarrow Ndd$; ros" Networked mitochondria damaged by the ROS around them (called ros)</p> | Ndd concentration is determined by the amount of Ddd that fused to Ndd, minus the quantity of Ndd that undergoes fission plus the amount of Nd damaged by ros. |

| Differential equation | Variables and constants | Reaction involved | Explanation |
|---|---|--|---|
| $\frac{d([ros] \cdot V_{compartment})}{dt} = -V_{compartment} \cdot (k_{ros \text{ degradation}} \cdot [ros]) + V_{compartment} \cdot \left(\frac{k_{ros \text{ synthesis by low damage}} \cdot [S] \cdot [Nd]}{[Nd] + [Ndd] + [N]} \right) + V_{compartment} \cdot \left(\frac{k_{ros \text{ synthesis by high damage}} \cdot [S] \cdot [Ndd]}{[Ndd] + [Nd] + [N]} \right) + V_{compartment} \cdot (v \cdot (\text{"constitutive ros generation"}))$ | <p><i>k_{ros synthesis by low damage}</i> = constant of reaction "S→ ros" (activated by Nd)</p> <p><i>k_{ros synthesis by high damage}</i> = constant of reaction "S→ ros" (activated by Ndd)</p> <p><i>k_{ros degradation}</i> = constant of ros degradation</p> | <p>1) "ros →" (ros degradation) 2) "→ ros" (constitutive ros generation) 3) "vN → Nd" 4) "vNd → Ndd" 5) S → ros (ros synthesis low damage activated) 6) S → ros (ros synthesis high damage activated)</p> | <p>"ros" concentration determined by ros generated constitutively, minus ros degraded, plus ros synthesized by Nd, plus ros synthesized by Ndd.</p> |
| <p>[Networked fraction]</p> $= \frac{[N] + [Nd] + [Ndd]}{[N] + [Nd] + [Ndd] + [D] + [Dd] + [Ddd]}$ | | | <p>Fraction of Networked mitochondria: the sum of networked mitochondria divided by the sum of all the mitochondrial species</p> |
| <p>[Dispersed fraction]</p> $= \frac{[D] + [Dd] + [Ddd]}{[N] + [Nd] + [Ndd] + [D] + [Dd] + [Ddd]}$ | | | <p>Fraction of dispersed mitochondria: the sum of dispersed mitochondria divided by the sum of all the mitochondrial species</p> |
| <p>"k_cycling network to disperse"</p> $= Values[k_cnd0_initial].InitialValue + \text{"NGF added"} \cdot (Values[k_cnd0_final].InitialValue - Values[k_cnd0_initial].InitialValue) \cdot (1 - e^{\frac{-(Time - \text{"NGF addition time"})}{Values[t_half_cnd].InitialValue}})$ | <p><i>k_cnd0_initial</i> = initial value of a rate constant that determines the starting value of k_(cycling network to disperse).</p> <p><i>k_cnd0_final</i> = final value of a constant that determines the final value of k_(cycling network to disperse).</p> <p>NGF added = determines the beginning of the variation of the k_(cycling network to disperse). It is 0 before NGF addition (time < 20 min) and 1 after NGF addition (time>20).</p> <p>t_half_cnd: the time of change from network to dispersed as initiated by NGF addition</p> | | <p>First order rate constant of reaction "Networked→Dispersed".</p> |

| Differential equation | Variables and constants | Reaction involved | Explanation |
|--|---|-------------------|---|
| $\text{"}k_{\text{cycling disperse to network}}\text{"} = 0.01 \cdot \text{Values}[\text{time_factor}].\text{InitialValue} \cdot \left(\frac{[D] + [Dd]}{[Ddd]} \right)$ | <p>0.01</p> <p>time_factor = global property used to adjust time dimension</p> | | <p>Constant of reaction "Dispersed→networked".</p> <p>It is made directly proportional to the concentration of the mitochondria D and Dd and indirectly proportional to the Ddd. The rationale is that fusion is pushed further as mitochondrial quality increases.</p> |
| $\text{"renormalized ROS"} = [ROS] \cdot \text{Values}[\text{ROSfactor}].\text{InitialValue} + \text{Values}[\text{ROSbackground}].\text{InitialValue}$ | | | <p>ROS signal multiplied by ROSfactor after which ROS background has been added. The idea behind this is that only some of the ROS is measured because much reacts before detection and that we are here modeling only part of the ROS generating processes.</p> |

