

Summary of Results: Graph of Riem. Zeta(s) Fct. with $\text{Im}(s)=0$

As a summary and final result of the work done in the Jupyter Notebook

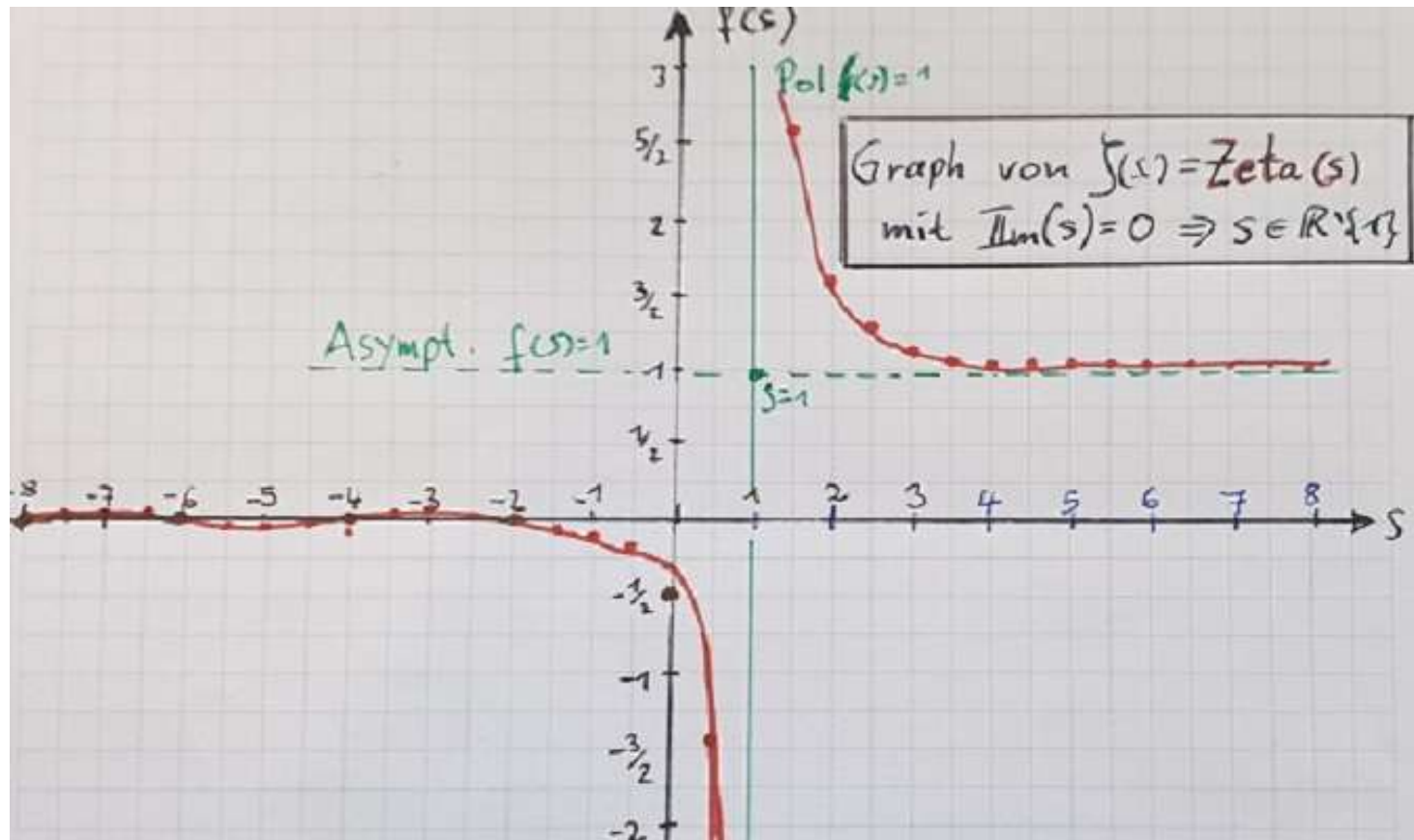
"RiemannZetaFct_and_RiemannHypothesis.ipynb"

(see <https://github.com/HVoellinger/Mathematics>) we show the graph of $\zeta(s)$ where $\text{Im}(s)=0$, s.t. $s=\text{real number}$ (without $s=1$).

We use the calculated values of $\zeta(s)$ for this special s and summaries them in a small table (see below). we see a pole of $\zeta(s)$ at $s=1$ and an asymptote at $f(s)=1$ for $s>1$. Compare also the remarks about the $\lim(\zeta(s))$ for s goes to positive infinity:
 $\lim(s \rightarrow +\infty)(\zeta(s))=1$.

s	Calculation of zetas(s) with (cRZ) Rounding errors may occur in proc. (cRZ)	zeta(s) with (RFE)
-8	$\text{zeta}(-8) = 1.3859169880942308\text{e-}05$	0
-7,5	$\text{zeta}(-15/2) = 0.003274799574186712$	
-7	$\text{zeta}(-7) = 0.004167422013553654$	$1/240 = 0.0041666... \rightarrow \text{Rounding E.}$
-6,5	$\text{zeta}(-13/2) = 0.0027469095530168607$	
-6	$\text{zeta}(-6) = 2.8347851868673592\text{e-}08$	0
-5,5	$\text{zeta}(-11/2) = -0.0026714542649568995$	
-5	$\text{zeta}(-5) = -0.003968252590985674$	$-1/252 = 0.003968253968 \rightarrow \text{Rounding E.}$
-4,5	$\text{zeta}(-9/2) = -0.003091668796611392$	
-4	$\text{zeta}(-4) = 6.429216196053237\text{e-}11$	0
-3,5	$\text{zeta}(-7/2) = 0.004441011354616652$	
-3	$\text{zeta}(-3) = 0.008333333335927267$	$1/120 = 0.008333... \rightarrow \text{Rounding}$
-2,5	$\text{zeta}(-5/2) = 0.008516928778669624$	
-2	$\text{zeta}(-2) = 1.5603186562147366\text{e-}13$	0
-1,5	$\text{zeta}(-3/2) = -0.025485201889790032$	
-1	$\text{zeta}(-1) = -0.0833333333332381$	$-1/12 = 0.08333... \rightarrow \text{Rounding Error}$
-0,5	$\text{zeta}(-1/2) = -0.2078862249773517$	
0	$\text{zeta}(0) = -0.49999999999999906$	$-1/2 = 0.5 \rightarrow \text{Rounding Error}$
0,5	$\text{zeta}(1/2) = -1.460354508809586$	
1	infinity	Pole
1,5	$\text{zeta}(3/2) = 2.612375348685488$	
2	$\text{zeta}(2) = 1.6449340668482266$	$\pi^2/6$
2,5	$\text{zeta}(5/2) = 1.341487257250917$	
3	$\text{zeta}(3) = 1.2020569031595942$	
3,5	$\text{zeta}(7/2) = 1.1267338673170566$	
4	$\text{zeta}(4) = 1.0823232337111381$	$(\pi^2)^2/90$
4,5	$\text{zeta}(9/2) = 1.0547075107614543$	
5	$\text{zeta}(5) = 1.03692775514337$	
5,5	$\text{zeta}(11/2) = 1.0252045799546856$	
6	$\text{zeta}(6) = 1.0173430619844488$	$(\pi^2)^3/945$
6,5	$\text{zeta}(13/2) = 1.0120058998885244$	
7	$\text{zeta}(7) = 1.0083492773819225$	
7,5	$\text{zeta}(15/2) = 1.0058267275365227$	
8	$\text{zeta}(8) = 1.0040773561979444$	$((\pi^2)^2)^2/9450$

Graph of the Riem. Zeta Fct. Zeta(s) with $\text{Im}(s)=0$



Values of Zeta(s) with Im(s)=0

s	Zetas(s)	Remark
-8	$\zeta(-8) = 1.3859169880942308e-05$	0
-7,5	$\zeta(-15/2) = 0.003274799574186712$	
-7	$\zeta(-7) = 0.004167422013553654$	1/240
-6,5	$\zeta(-13/2) = 0.0027469095530168607$	
-6	$\zeta(-6) = 2.8347851868673592e-08$	0
-5,5	$\zeta(-11/2) = -0.0026714542649568995$	
-5	$\zeta(-5) = -0.003968252590985674$	-1/252
-4,5	$\zeta(-9/2) = -0.003091668796611392$	
-4	$\zeta(-4) = 6.429216196053237e-11$	0
-3,5	$\zeta(-7/2) = 0.004441011354616652$	
-3	$\zeta(-3) = 0.008333333335927267$	1/120
-2,5	$\zeta(-5/2) = 0.008516928778669624$	
-2	$\zeta(-2) = 1.5603186562147366e-13$	0
-1,5	$\zeta(-3/2) = -0.025485201889790032$	
-1	$\zeta(-1) = -0.083333333332381$	-1/12
-0,5	$\zeta(-1/2) = -0.2078862249773517$	
0	$\zeta(0) = -0.4999999999999906$	-1/2
0,5	$\zeta(1/2) = -1.460354508809586$	
1	infinity	Pol
1,5	$\zeta(3/2) = 2.612375348685488$	
2	$\zeta(2) = 1.6449340668482266$	$\pi^2/6$
2,5	$\zeta(5/2) = 1.341487257250917$	
3	$\zeta(3) = 1.2020569031595942$	
3,5	$\zeta(7/2) = 1.1267338673170566$	
4	$\zeta(4) = 1.0823232337111381$	$(\pi^2)^2/90$
4,5	$\zeta(9/2) = 1.0547075107614543$	
5	$\zeta(5) = 1.03692775514337$	
5,5	$\zeta(11/2) = 1.0252045799546856$	
6	$\zeta(6) = 1.0173430619844488$	$(\pi^2)^3/945$
6,5	$\zeta(13/2) = 1.012005899885244$	
7	$\zeta(7) = 1.0083492773819225$	
7,5	$\zeta(15/2) = 1.0058267275365227$	
8	$\zeta(8) = 1.0040773561979444$	$((\pi^2)^2)^2/9450$

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