

EE2030 Linear Algebra

1st Computer Exercise: Determining the rank of a matrix

Due Tuesday Nov. 25, 2014

Brought to you by Yi-Wen Liu, Ph.D.

- (a) Write a function `r = myRank(A)` that takes a random unknown matrix `A` and returns its rank `r`. You may need to write sub-functions for elementary matrix operations (such as to swap two rows or two columns). Below is an example of swapping two rows of the matrix `A`:

```
A([j k], :) = A([k j], :);
```

- (b) Download `LinAlg2013Ex1.mat` from LMS. Type

```
load LinAlg2013Ex1.mat
```

at the command line, and then `whos` to see what's inside. You will find a few random matrices. Determine the rank of these matrices. Verify your answers against the answers given by MATLAB's function `rank()`.

Remarks:

- 評分方式：我會另外湊出幾個《秩》已知的矩陣，並且請助教跑你們的 `function`，若是全對，則本次作業滿分。
- 若有瑕疵但準時交上，則也會斟酌給予分數。請勿遲交。
- Please do not use advanced MATLAB functions, such as `eig()`, `svd()`.
 - 其實你們可以在 `command line` 鍵入 `type rank`，則 MATLAB 就會顯示 `rank()` 這個函式的寫法：

```
%  
% RANK(A) provides an estimate of the number of  
% linearly independent rows or columns of matrix A.  
  
s = svd(A);  
if nargin==1  
    tol = max(size(A)) * eps(max(s));  
end  
r = sum(s > tol);
```

其中會發現使用到 Singular Value Decomposition (SVD), 這是課本第六章的內容，目前對於我們還太超過。所以還是請你們使用 elementary matrix operations 來解題。

- 鼓勵互相討論，鼓勵隨時發問，可以互相參考，但請勿抄襲。
 - 不得已要抄襲的話，請確定抄到正解。
 - [醜話在先] 如果經助教發現程式有錯誤卻讓別人抄襲，我們將找你喝下午茶，並給予被抄者與抄襲者同等處罰。
- 本次作業無須繳交紙本。請於 LMS 上傳你的 `.m` 檔，並請命名為 `myRank_[學號].m`。例如：學號為 102060789 者，請將檔案命名為 `myRank_102060789.m`，以方便助教半自動批改。