The density profile of the Milky Way's stellar halo to 80 kpc

Xiang-Xiang Xue¹, Hans-Walter Rix¹, Zhibo Ma², Jo Bovy³, Braimir Sesar¹

ABSTRACT

We present the density profile of SEGUE-2 spectroscopic halo K giants by considering the selection function information. A sample of ~ 2400 halo K giants up to 80 kpc from the Galactic center and its well-understood selection function enable us to get a robust measurement of the shape and radial profile of the Milky Way's stellar halo out to 80 kpc. The data show the stellar halo is oblate and its shape has strong dependence on metallicity (i.e. the more metal-poor stars show rounder density profile.). In addition, we find a strong evidence for variations in flattening with radius. After fitting the data to Einasto profile and a broken power-law with a constant halo flattening, we find the best-fitting Einasto profile with an effective radius at 21 kpc, a steepness index of 2.2, and a flattening (i.e. ratio of minor axis to major axis) of 0.78, and the best-fitting broken power-law with an inner slope of 2.7 and an outer slope of 4.2, together with a break radius at 30 kpc and a flattening of 0.78. These two best-fitting models are consistent within $1-\sigma$. Assuming the halo flattening varies with radii, the best-fitting Einasto profile has a smaller effective radius of 8 kpc, but a larger steepness index of 4.6, and the flattening changing from 0.5 at 10 kpc to 0.95 at 80 kpc. Furthermore, the Einasto profile with variable flattening is consistent with the density profiles with a constant flattening within $1-\sigma$.

Subject headings: galaxies: individual(Milky Way) - Galaxy: halo - Galaxy: stellar content - stars: K giants

1. Introduction

The Milky Way's extended stellar halo contains only a small fraction ($\lesssim 1\%$) of the Galactic stars, but is an important diagnostic of the Milky Way's formation and dark matter

¹Max-Planck-Institute for Astronomy Königstuhl 17, D-69117, Heidelberg, Germany

²Department of Astronomy, Case Western Reserve University, Cleveland, OH 44106, USA

³Institute for Advanced Study, Einstein Drive, Princeton, NJ 08540, USA

distribution. The position-kinematics-abundance substructure in the stellar halo reflects the Galactic formation history, whether halo stars were born in situ or are disrupted satellite debris. By now, individual stars are the by far the largest sample of kinematic tracers with 10 kpc $\gtrsim R_{GC} \lesssim 100$ kpc (as opposed to globular clusters or satellite galaxies), and are hence the best tracers to determine the mass profile of Milky Way's dark matter halo. It is obvious that kinematic tracer samples should have sizeable membership, cover a wide radial range at good individual distances. But the spatial distribution of the tracers, in particular their radial profile, must be well understood to use such tracers in dynamical inferences. This is perhaps most obvious when considering the Jeans (1915) Equation, even in its simplest version, spherical and isotropic: the tracer density profile, $\nu(r)$, in particular its logarithmic radial derivative, $\partial \ln \nu / \partial \ln r$, scales the inferred enclosed mass, M(< r), almost linearly. If we do not know the local power-law exponent to better than, say, 25\%, we cannot infer the mass to better than 25% irrespective of the size and quality of the kinematic sample. To a somewhat lesser extent, the inferred mass also depends on teh flattening of the tracer population. Yet, at present there is little consensus on the shape and the radial profile of the stellar halo. The most straightforward way to quantify the stellar halo distribution is star counts. However, this method requires large samples of well-understood completeness, so it is often applied to the photometric catalogs. Very early studies adopted star counts to analyze globular clusters(?), RR Lyrae variables(??), blue horizontal branch (BHB) stars(?), combination of BHBs and RR Lyraes(?), a star sample near the north galactic pole(?), or K dwarfs(?), and found the stellar halo is well fitted by a single power-law ($\nu \approx (distance)^{-\alpha}$) with index α of $3 \sim 3.5$ and flattening of $0.5 \sim 1$. However, ? found dozens of RR Lyraes are well described by a broken power-law with $\alpha \sim 3$ out to 25 kpc, and $\alpha \sim 5$ beyond 25 kpc. All of above studies were based on a few hundred objects at most. Recent years, with the development of sky surveys, the sizes of the photometric samples expand more than 10 times. ? used a wide set of deep star counts in pencil-beam survey at high and intermediate galactic latitudes to model the density profile and found the best-fit density profile with a flattening of 0.76, a power index of 2.44. ? found 70,000 stars in seven Kapteyn selected areas are consistent with a power-law density with index of 2.75 and flattening of 0.6. ? made use of BHB stars from the Two-degree Field Quasar Redshift Survey to find that the halo is almost spherical with a power-law index of $\alpha \sim 2.5$ out to ~ 100 kpc. ? used 27,544 near-turnoff main-sequence stars out to ~ 35 kpc selected from Canada-France-Hawaii Telescope Legacy Survey to find the flattening of stellar halo is 0.7 and the density distribution is consistent to a broken power low with an inner slope of 2.62 and an outer slope of 3.8 at the break radius of 28 kpc, or an equally good Einasto profile(?) with steepness index of 2.2 and effective radius of 22.2 kpc. ? analyzed $\sim 20,000$ A-type photometric stars selected from Sloan Digital Sky Survey data release 8(?) and obtained the best-fitting broken power-law density with an inner slope of 2.3, and an outer slope of 4.6, with a break radius at 27 kpc and a constant flattening of 0.6. Straight after that, ? found a very steep outer halo profile with slope of 6 beyond 50 kpc, and even steeper slopes of $6 \sim 10$ at larger radii. In addition, several pieces of work point to variations of the stellar halo flattening with radius. ? found the density distribution for RR Lyraes follow a power-law with $\alpha \sim 3.2$, together with a variable flattening changing linearly from 0.54 at center to 1 at 20kpc. But, other work (???) found no evidence for flattening, but no evidence for a change with radius. Position-velocity maps of the stellar halo beyond ~ 20 kpc, practically require luminous post main-sequence (MS) stars, is turn-off or other MS stars are too faint for large-sample spectroscopy. RR Lyraes and BHBs have repeatedly been used as tracers to study the halo density profile, because they have precise distances and are bright enough to be observed at radii out to ~ 100 kpc (e.g. X08, Deason, etc..). Yet, such stars, most prevalent in particularly old and metal-poor populations(??) are known to have a different structure and profile from e.g. RGB stars in the outer halo, that are representative of all halo populations. K-giants, as tracers common to all relevant halo sub-populations are traces that can both reflect the (mass-weighted) sub-structure, reflecting the formation history, and to probel the halo mass. To this end, it is crucial to construct the halo shape and radial profule in K-giants. ? presents a catalog of K giants with unbiased distance estimates, metallicities, velocities and photometric information, drawn from the Sloan Extension for Galactic Understanding and Exploration(?, SEGUE), which contains ~ 300 stars beyond 50 kpc. For K giants observed in SEGUE-2, one can understand and model their selection function well/ Therefore, it is possible to determine the halo profile and shape in these tracers, which is the main goal of the paper here. Specifically, we set out to describe stellar halo distribution, presuming the density is stratified on (oblate) spheroids, with a radial profile from 10-80 kpc that can be characterized by simple functional forms (Einasto profile and broken power-law). We also explore the metallicity dependence of the shape and radial profile of the stellar halo. In the next section, we lay out the properties and the selection function of the SEGUE K giants. In §3, we present the method of fitting a series of parameterized models to SEGUE-2 K giants, explicitly and rigorously considering the selection function. This step is key in obtaining accurate radial profiles. The results for the stellar halo's radial profile and flattening are presented in §4, along with an illustration of the metallicity dependence of the shape and radial profile. Finally, §5 discusses the comparison between our results and previous work, and implications for dynamical models.

2. SEGUE-2 K giants and their selection function

The Sloan Digital Sky Survey(SDSS; ?) is an imaging and spectroscopic survey covering roughly a quarter of the sky, which has both ugriz imaging (?????) and low resolution spec-

tra ($\lambda/\Delta\lambda \sim 2000$). SEGUE is one of the key projects and has two phases named SEGUE-1 and SEGUE-2, which aim to explore the nature of stellar populations from 0.5 kpc to 100 kpc(?, and Rockosi et al. in prep.). The original SEGUE-1 obtained spectra of 240,000 stars with g = 14 - 20 to investigate Milky Way structure, and SEGUE-2 spectroscopically observed around 120,000 stars, focusing on the in situ stellar halo of the Galaxy. To understand the underlying spatial distribution of the K giants on the basis of this sample, we need understand (and account for) the probability that a star of a given luminosity, color and metallicity ends up in the sample, given its direction and distance. Spectroscopic surveys of the Milky Way are inevitably affected by such selection effects (cf. ?), often referred to as "selection biases", which are due to a set of objective and repeatable decisions of what to observe, necessitated by the survey design. In particular, only a small fraction of the sky was covered by SEGUE plates, and for most plates only a fraction of stars that satisfy the photometric selection criteria could be targetted with fibers. Finally, not all stars targetted yield spectra good enough to result in a catalog entry, i.e. had S/N high enough to verify that they are giants and yield a metallicity. ? and ? spelled out how to incorporate this selection function in fitting a parameterized model for the stellar density and we follow their approach in this and the next Section. Both the SEGUE-1 and SEGUE-2 surveys targeted halo giant star candidates, using a variety of photometric and proper motions cuts. About 90% of the final K-giant sample came from objects observed as l-color K-giant targets. The l-color is a photometric metallicity indicator for stars in the color range $0.5 < (g - r)_0 < 0.8$, designed to select metal-poor K giants¹. Only SEGUE-2 adopted a consistent color-magnitude cut to select K giants throughout its entire survey: $15.5 < g_0 < 18.5, r_0 > 15, 0.7 < (u-g)_0 < 3$ $0.5 < (g-r)_0 < 0.8, 0.1 < (r-i)_0 < 0.6, \text{ and } l-color > 0.09, \text{ and we restict our analysis to}$ this category. We also insist that l-color K giant candidates have good proper motion measurements with $\leq 11 \text{ masyr}^{-1}$. But as broadband photometry is a poor main-sequence giant discriminator, not all stars targeted under the above criteria will be giants. The subsequent identification of K-giants is based solely on their spectral properties. As described in?, this requires spectra that have good Mg index and stellar atmospheric parameters determined by the SEGUE Stellar Parameter Pipeline(SSPP; ???), but have no strong G band. We can now compare the color-magnitude distribution these spectroscopically confirmed K giants to the the analogous distribution of the photometric l -color K giant candidates. Figure 2 shows these two distribution (as contours and gray-scale, respectively), summed over all SEGUE-2 plates. As in particular the marginalized histograms at the sides of the panels show, these two distributions are nearly indistinguishable: the chance of a photometric candidate being confirmed as a K-giant is independent of color and magnitude. This simplifies the subse-

 $^{{}^{1}}https://www.sdss3.org/dr9/algorithms/segue_target_selection.php\#S2_table.$

quent analysis and is testament to SEGUE-2's consistency of target selection, targetting and spectral analysis. While the selection function is constant with apparent magnitudes and de-reddened colors, it varies from plate to plate, in particular with the Galactic latitude of the plate. Given the pencil-beam nature of SEGUE survey, it makes sense to specify the selection fraction plate by plate. For each plate we define the number of spectroscopically confirmed K giant as N_{sp} , and the number of l-color K giant candidates in the plate (both those that were targetted, and those that were not) as N_{ph} . Thus, the plate-dependent selection function (shown as Figure 3) is given by

$$S(plate) = \frac{N_{sp}}{N_{ph}} \tag{1}$$

As we want to analyze the spatial distribution, we also restrict our sample to SEGUE-2 l -color K giants that have sensible distance estimates from ?. To eliminate the contamination from disk component, we cull K giants with [Fe/H] > -1.2 and |z| < 4 kpc, which leads to a final sample of 2413 l-color K giants. Figure 1 illustrate the basic sample properties: its sky coverage and spatial distribution without accounting for the selection function, and the metallicity distribution along with the distances from ?. The stars' distribution reflects the pencil-beam pattern of the SEGUE survey; their galactocentric distances range from 7 kpc to 85 kpc; their mean metallicity is -1.75 dex, with some being as metal-poor as -3.5.

3. Modelling the Stellar Halo Density Distribution

We presume that the stellar halo distribution can be sensibly approximated by a spheroidal distribution with a parameterized radial profile and flattening. For this case we spell out a straightforward and rigorous approach to determine the posterior probability distributions for these *halo parameters* in light of the above data, our knowledge of the SEGUE selection function (see Figures 2, 3 and 1), and astrophysical priors on the luminosity function of giants stars.

3.1. Functional Forms for the Radial Profile

In this approach, the choice of one, or more, functional forms for the possible stellar density distribution is inevitable. The foremost goal of our analysis is to find the best axisymmetric approximation to the actual spatial distribution, to have a gross description of the halo structure and as input for simple dynamical models. Our basic assumptions, or restrictions, are that we assume 1) the stellar density to be stratified on (oblate) spheroids,

2) the radial profile to be simple or even smooth, and 3) the flattening to be constant or smoothly and monotonically varying. In light of the well-established sub-structure of the stellar these are obviously only approximation.

The first assumption implies that the stellar profile $\nu_*(x, y, z)$ is only a function of r_q , where

$$r_q \equiv s\sqrt{R^2 + (z/q)^2},\tag{2}$$

where $R \equiv \sqrt{x^2 + y^2}$ and q is the flattening, in the simplest case constant.

For the functional form of $\nu_*(r_q)$ we resort to two profile families, previously employed. For one, the Einasto profile (?) that is the 3D analog to the Sérsic's law(?) for surface brightnesses, and has been used in this context (???):

$$\nu_{\star}(r_q) \equiv \nu_0 \, \exp\left\{-d_n \left[\left(r_q/r_{eff}\right)^{1/n} - 1 \right] \right\},\tag{3}$$

where $d_n \approx 3n - 1/3 + 0.0079/n$, for $n \ge 0.5$, and n is a concentration index. Flattening and the (here irrelevant) normalization aside, the Einasto profile has two parameters, r_{eff} and n.

Alternatively, we consider a broken (or multiply-broken) power law, a form that has been used extensively to described the radial profile of the Galactic stellar halo(????). In most cases the change in the power-law index, $d \ln \nu_*/d \ln r$ has been taken as a step function (e.g. ?). We adopt:

$$\nu_{\star}\left(\mathbf{r}_{\mathbf{q}}\right) = \begin{cases} \nu_{0} \ \mathbf{r}_{\mathbf{q}}^{-\alpha_{\mathrm{in}}}, & \mathbf{r}_{\mathbf{q}} \leq \mathbf{r}_{\mathrm{break}} \\ \nu_{0} \times \mathbf{r}_{\mathrm{break}}^{(\alpha_{\mathrm{out}} - \alpha_{\mathrm{in}})} \times \mathbf{r}_{\mathbf{q}}^{-\alpha_{\mathrm{out}}}, & \mathbf{r}_{\mathbf{q}} > \mathbf{r}_{\mathrm{break}} \end{cases}$$
(4)

In addition to the flattening and normalization, a (singly) broken power-law has three parameters, α_{in} , α_{out} , r_{break} . Of course, this can be generalized to a multiply-broken power-law, by introducing an additional pair of (α, r_{break}) (cf. ?).

3.2. Halo parameter estimates, explicitly including the Selection Function

For the parameter estimates, we essentially follow the approach of ? (cf. ?). Since we have already good estimates of \mathcal{DM} and M_r for all objects in the sample (?), we treat $(\mathcal{DM}, M_r, [\text{Fe/H}], l, b)$ as the observables (rather than $(m_r, c, [\text{Fe/H}], l, b)$, as it makes the fitting formalism more intuitive. However, the apparent magnitudes m_r and (dereddened) colors c, will appear explicitly in the selection function. We denote angular selection function as $S(l, b) \equiv S(plate(l, b))$ (Eq. 1), and the magnitude-color selection function by

 $S(m(\mathcal{DM}, M_r), c(M_r, [Fe/H]))$, expressed in terms of the "observables" above; we denote the priors on absolute magnitude and metallicity as $p(M_r)$ and ([Fe/H]), respectively. Then the expected rate function for finding a star with $(\mathcal{DM}, M_r, [Fe/H], l, b)$ in our context is

$$\lambda(M_{r}, \mathcal{DM}, [Fe/H], l, b|p_{H}) = |J(x, y, z; \mathcal{DM}, l, b)| \times \nu_{\star}(r_{q}(\mathcal{DM}, l, b)|p_{H}) \times p(M_{r}) \times p([Fe/H]) \times S(l, b) \times S(m(\mathcal{DM}, M_{r}), c(M_{r}, [Fe/H])).$$
(5)

The Jacobian term $|J(x, y, z; \mathcal{DM}, l, b)|$ accounts for the transformation from cartesian (x, y, z) to the Heliocentric polar coordinates (\mathcal{DM}, l, b) . Note that all the SEGUE plates have the same solid angle of $7 \ deg^2$. When analysing the data plate by plate, the Jacobian term should be $|J(x, y, z; \mathcal{DM})|$. $\nu_{\star}(r_q(\mathcal{DM}, l, b)|p_H)$ describes the underlying spatial number density of K giants (i.e. halo density profile), in principle from the base to the tip of the giant branch. The explicit form for each term in Eq.(2) in the present context is given by:

$$|J(x,y,z;\mathcal{DM})|_{plate} = \Omega_{plate} \cdot \ln 10/5 \cdot d^3$$
, where $\Omega_{plate} = 7 \ deg^2$ and $d = 10^{\frac{\mathcal{DM}}{5}-2}$ kpc.

$$p(M_r) \propto \left\{ \begin{array}{c} 10^{0.32 M_r}, & \mbox{if } M_{r \ min,obs} < M_r < M_{r \ max,obs} \\ 0, & \mbox{otherwise} \end{array} \right.$$

$$p([Fe/H]) \propto \begin{cases} p([Fe/H])_{obs}, & if [Fe/H]_{min,obs} < [Fe/H] < [Fe/H]_{max,obs} \\ 0, & otherwise \end{cases}$$

$$S(l_{plate}, b_{plate}) = \begin{cases} \frac{N_{spec.}}{N_{phot.}}, & \text{if in plate} \\ 0, & \text{otherwise} \end{cases}$$

$$S(m(\mathcal{DM}, M_r), c(M_r, [Fe/H])) \propto \left\{ \begin{array}{l} 1, & \text{if } m_{min,obs} < m < m_{max,obs} \text{ and } c_{min,obs} < c < c_{max,obs} \\ 0, & \text{otherwise} \end{array} \right.$$

The specific functional forms for the stellar halo profiles $\nu_{\star}(r_q(\mathcal{DM}, l, b)|p_H)$ for Einasto, or broken power-law profiles with different flattening profiles are given in the subsequent Sections.

Following? the likelihood of the data given p_H and the rate function, can be written as

$$\mathscr{L}(\mathrm{data}_{i}|p_{H}) = c_{\lambda}^{-N_{\mathrm{KG}}} \prod_{i=1}^{N_{\mathrm{KG}}} \lambda(M_{\mathrm{ri}}, \mathcal{DM}_{i}, [\mathrm{Fe}/\mathrm{H}]_{i}, l_{i}, b_{i}|p_{H}), \tag{6}$$

where the normalization c_{λ} is the integral over the volume in $(\mathcal{DM}, l, b, M_r, [Fe/H])$ space.

$$c_{\lambda} = \sum_{i=1}^{N_{\text{plate}}} \int \int \int \lambda(M_{r}, \mathcal{DM}, [Fe/H], l_{\text{plate}}, b_{\text{plate}}|p_{H}) dM_{r} d\mathcal{DM} d[Fe/H]$$
 (7)

This normalization integral is the most CPU time-consuming part of the parameter estimates; it can be computed efficiently using Gaussian quadrature rule. We adopt 48 transformation points (Question: are these 48 Gaussian points in each dimension?), and then the parameter-independent parts such as Jacobian term, priors of luminosity and metallicity and selection function can be pre-computed on a dense grid. We then vary the p_H to sample the parameter PDF, using emcee(?).

4. Results

In this section, we present the results of applying the approach from §3 to the sample of §2. We first focus on the radial profiles, fitting for a radially constant flattening, and taking halo giants of all metallicities. We then show how these results compare for subsamples of different metallicities, and explore radial variations of the flattening, and their impact on the radial profile estimate.

4.1. Radial profile at constant flattening

Figure 4 presents the fit results for the Einasto profile, showing the PDFs of the three parameters: $r_{eff} = 21 \pm 1 \; kpc$, $q = 0.78 \pm 0.02$, and $n = 2.2 \pm 0.3$. To get a sense whether this best fit provides a sensible representation of our data, we compare in Figure 5 the distribution of the \mathcal{DM} s in the sample to that predicted by the best-fit model. The distributions are summed over all survey directions in both cases, and the overall match is very good.

Figure 6 shows the analogous results for a broken power-law: we find an inner slope of $\alpha_{\rm in} = 2.7 \pm 0.1$, an outer slope of $\alpha_{\rm out} = 4.2 \pm 0.2$, and a break radius of $r_{\rm break} = 30 \pm 3$ kpc, together with a flattening of $q = 0.78 \pm 0.02$. The flattening is consistent with that of the best-fit Einasto profile. The broken power-law profile also predicts a consistent $p(\mathcal{DM})$ to the observation (shown as Figure 5).

As ? claimed much more rapid drop of the stellar density (in BHB stars) beyond 50 kpc, we also fit a doubly-broken power-law with parameters (α_{inner} , α_{middle} , α_{outer} , r_{break1} , r_{break2} , q), that denote the three slopes and two break-radii; q is the flattening. However, our data provided no constraints on a second break radius, i.e. no evidence of strong drop beyond 50 kpc. We find the best first break radius r_{break1} is at 30 kpc, the inner slope α_{inner} is 2.7, the middle slope is equal to the outer slope ($\alpha_{middle} = \alpha_{outer} = 4.2$), and the flattening q is still 0.78.

How these fits using different functional forms compare, in particular in their logarithmic slopes as a function of radius, we discuss in Section 4.4sec:ModelComparison.

4.2. Metallicity-dependence of radial profile and flattening

As some parts of the halo have presumably formed 'in situ', while other parts were accreted frmo satellites, i.e. through different formation paths that may be reflected in their metallicities, we may expect that the overall spatial structure of the halo depends on metallicity. To explore any metallicity-dependence of the flattening and radial profile, we split our sample by metallicity into three almost equally size sub-samples. We then fit Einasto profiles with fixed n=2.2 to these sub-samples to obtain the best-fit parameters q and $r_{\rm eff}$. The results of these fits are shown in Figure 7. The three sub-samples have very similar effective radii ($r_{\rm eff} \sim 20~{\rm kpc}$), but the less metal-poor stars (q ~ 0.7) appear significantly flatter than the more metal-poor stars (q ~ 0.85). So, while the shape of the halo varies somewhat with metallicity, there is no significant overall metallicity gradientin the halo ($\geq 10~{\rm kpc}$).

4.3. Radial variation of halo flattening

Previous work found the evidence for the increase of flattening with radii(?). : X-X, I don't understand the following statement. Pls. explain: We also find strong metallicity-dependence on the flattening by fitting to the Einasto profile with a constant flattening as described in §4.3, which we attribute to the increase of the flattening with the distances.

The above fits were restricted to radially constant flattening q. As there is considerable evidence that at least the innermost part of the halo is quite flattened (?), we explore how our sample can inform us about radial variations in the flattening of the stellar halo. Instead of assuming q = const., we fit the following three expressions for q(r):

$$q(r) = q_{inf} - (q_{inf} - q_0) \exp\left(1 - \frac{\sqrt{r^2 + r_0^2}}{r_0}\right),$$
 (8)

where q_0 is the flattening at center, changing to q_{inf} at large radii, with r_0 is the (here, exponential) scale radius, over which the change of flattening occurs.

Alternatively, we use a functional form that has been used by (?) and (?) in a somewhat different context

$$q(r) = \sqrt{q_0^2 + (q_{inf}^2 + q_0^2) \frac{r^2}{r^2 + r_0^2}},$$
(9)

and finally

$$q(r) = q_0 \sqrt{\frac{r^2 + r_0^2}{q_0^2 r^2 + r_0^2}}$$
(10)

following?, which we dub Sluis-Arnold flattening. Note that the flattening in all these cases is a function of the spherical radius, r, not of r_q .

We restrict the possible radial profile Einasto models with above three forms of varying flattening to the data. For all three flattening profiles, we find that the halo is far more flattened at small radii ($q(r=10 \text{ kpc}) \approx 0.6$), becomes nearly round beyond $r_0 \approx 30 \text{ kpc}$) to $q_{inf} \approx 0.95$), and that formally small Einasto scale radii are favored ($r_{eff} \sim 10 \text{ kpc}$). Flattening profiles that correspond to samples of the parameter's PDFs are illustrated Figure 8: the flattening profile depends little on the functional form chose in the modelling. **Question, XX** WHY NOT MOVE THE FOLLOWING INTO A TABLE? The best-fitting Einasto model with an exponential variation of flattening (Eqn. 7) has $q_{inf} = 0.9 \pm 0.04$, $q_0 = 0.3 \pm 0.1$, $r_0 = 8 \pm 2 \text{ kpc}$, $n = 5.4 \pm 1.8$ and $r_{eff} = 7 \pm 3 \text{ kpc}$. The Einasto profile with an Osipkov-Merritt flattening (Eqn. 8) fits well to the data with $q_{inf} = 0.96 \pm 0.05$, $q_0 = 0.2 \pm 0.1$, $r_0 = 15 \pm 3 \text{ kpc}$, $n = 4.6 \pm 1.5$ and $r_{eff} = 8 \pm 3 \text{ kpc}$. When the flattening follows the Sluis-Arnold form (Eqn. 9), the best-fit Einasto profile has $q_0 = 0.3 \pm 0.1$, $r_0 = 6 \pm 3 \text{ kpc}$, $n = 4.2 \pm 1.5$ and $r_{eff} = 8 \pm 3 \text{ kpc}$.

Note that while the formal $q_0 \approx 0.3$ (at r = 0 kpc), we have not used any data within r = 10 kpc.

The change in r_{eff}, when allowing for variable flattening, may seem dramatic. Yet, the implied radial profile is actually not very different, as we will show below (Section 4.4).

4.4. Comparison of Different Functional Forms for the Radial Profile

Analogous to the comparison of the flattening profiles shown in Figure 8 (cf Section 4.3) we now explore how different the actual radial density profiles implied by the various fits above actually are over the radial range where they are constrained by data (10 kpc \leq r \leq 80 kpc). Here, we focus on the local slope of the density profile, i.e. the local power-law exponent, $\frac{\text{dln}\nu}{\text{dlnr}}$, because of its important role in mass estimates M(< r), e.g. through the Jeans Equation (cf. Section 1). Since the stellar halo density distributions we consider here are axisymmetric, effectively oblate, we take an intermediate axis (in cylindrical coordinates) as the radial coordinate in such comparison, $\frac{\text{dln}\nu(R,R/\sqrt{2})}{\text{dln}R}$.

We start by comparing the Einasto profiles with different forms of flattening variation: the upper panel of Figure 9 shows that all three functional forms for the flattening also have consistent density profiles. Since the Einasto profiles with different definitions of flattening variation are consistent, we will only use one of them to compare with the models with constant flattening (WHICH ONE? YOU NEVER SAY). Figure 9 (lower panel) compares the radial profiles between the models with constant or variable flattening: remarkably the Einasto profiles with constant (black) and variable (blue) flattening have consistent radial profile slopes, $\frac{\text{dln}\nu(R,R/\sqrt{2})}{\text{dln}R}$, despite their quite different r_{eff} . However, the broken power-law profile slope differs significantly from the Einasto profile beyond 50 kpc.

5. Summary and Discussion

In this paper, we have presented an analysis of the overall spatial distribution of stars in the Galactic halo in the range 10 kpc < r < 80 kpc, based on over 2,000 spectroscopically confirmed (l-color) K-giants from SEGUE-2 with $-3.5 < [{\rm Fe/H}] < -1.2$. This sample is comparable in size and distance range to previous samples of BHB stars in the Galactic halo, but has the advantage that K-giants are ubiquitous and well-understood tracers of all stellar halo populations across the relevant age and metallicity range. We have laid out a formalism for fitting parameterized models to the spatial distribution of these halo stars that quite rigorously accounts for the selection function of the spectroscopic survey.

We consider a variety of parameterized functional forms for the stellar density distributions with spheroidal density stratifications. These have either Einasto or broken power-law profiles in radius, and have constant or radially variable flattening.

We find that the radial distribution can be reasonably well described by either an Einasto profile or a (once) broken power-law. If the flattening is assumed to be constant, the the halo is overall mildly oblate. We find that a single power-law is clearly ruled out, as the locally determined power-law slope (for either Einasto, or a broken power law) from -2.5 at 15 kpc to -4.5 at 50 kpc. In the radial profile of the K-giants, we found no evidence for a second power-law break at 50 kpc, as seen for the BHB stars (?). Overall, the halo profile slope $\frac{\text{dln}\nu(R,R/\sqrt{2})}{\text{dln}R}$ seen in the K-giants is significantly shallower than than the one measured and claimed for BHB stars (?); whether that is a true discrepancy, or just implies that the population in which BHB stars are more common has a steeper profile is not clear. At any rate, the new, improved information on the radial profile of the stellar halo presented here, should enable better halo mass estimates with stellar kinematics, as the radial profile uncertainties are a more important error source than the velocity dispersion measurements.

The large sample size and good metallicity estimates ($\delta[\text{Fe/H}] \approx 0.2$) allow us to search for an abundance dependence of the overall halo profile: we find little dependence of the

radial profile (e.g. 10% in R_{eff}) on metallicity in the range -3.5 < [Fe/H] < -1.2.

We also explore the shape (i.e. the flattening) of the radial profile. Presuming radially constant flattening ($q = 0.78 \pm 0.02$ for the entire sample), we find that the most metal-poor sub-population of the halo [Fe/H] < -1.9 is considerably less flattened (q = 0.85) than the rest (q = 0.7). We find a distinct radial dependence of the flattening in the observed radial range, rising from $q \approx 0.6$ at 10 kpc to $q \approx 0.95$ at 30 kpc and beyond. This may reflect the transition from the *in situ* formed portion halo to accreted halo stars. Our finding is consistent with early claims? that the halo becomes rounder at large radii, but is inconsistent with findings of ???. This radial variation may reconcile our (constant) flattening q = 0.78, which is less flat than the values found by ?, ;q=0.7 and ?, ;q=0.58 : if q varies radially, then the details of the radial weighting matter in the fitting of q = const. models.

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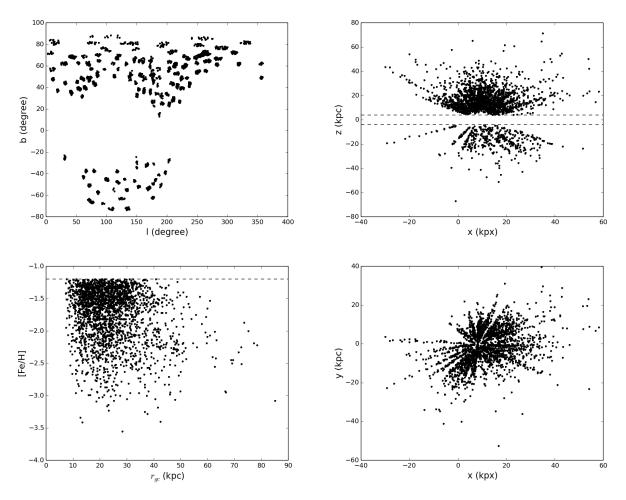


Fig. 1.—: (Upper left) The sky coverage and the spatial distributions (right panel) of SEGUE-2 l-color K giants appear to be pencil-beam due to the nature of SEGUE survey. (Lower left) The distribution of metallicities along with the Galactocentric radii shows the mean metallicity is about -1.75 dex, and some K giants have metallicities of ~ -3.5 . The stars with [Fe/H] > -1.2 and |z| < 4 kpc are culled because they could belong to the disk.

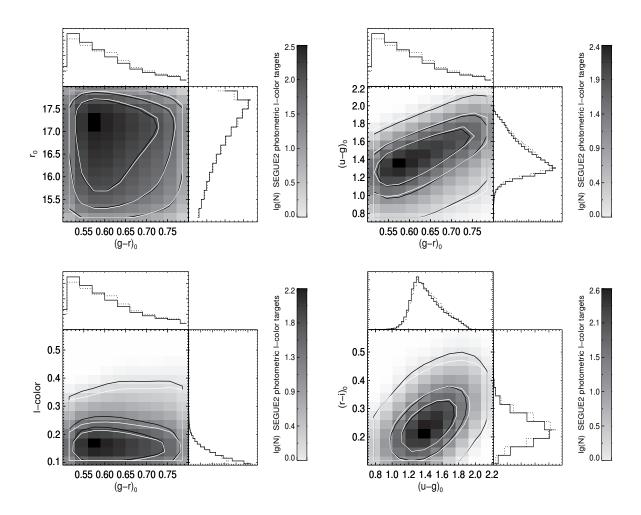


Fig. 2.—: Distribution of SEGUE-2 photometric l-color K-giant candidates (gray map, black contours, solid histogram) and the successfully spectroscopic sample (white contours, dotted histogram). The contours contain 68%, 95% and 99% of the distribution. The spectroscopic sampling is relatively fair in colors and magnitudes.

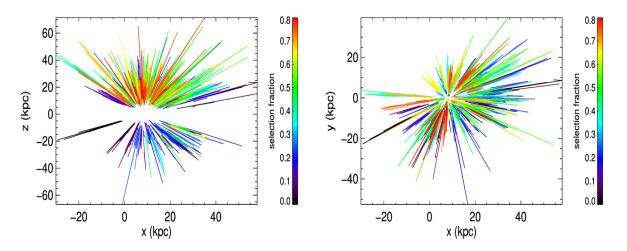


Fig. 3.—: The SEGUE-2 selection function of l-color K giants, as a function of Galactic coordinates X and Y (left panel), and of Galactocentric coordinates X and vertical height Z (right panel).

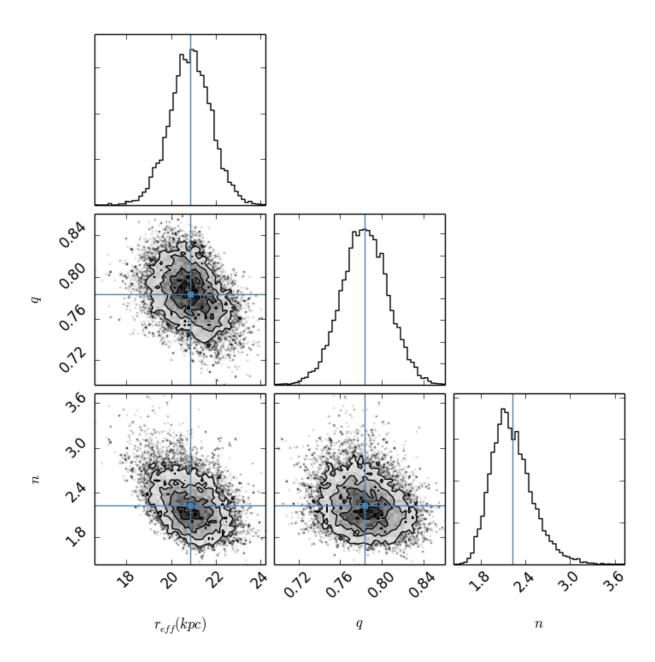


Fig. 4.—: The triangle plot shows all the one and two dimensional projections of the posterior probability distributions of parameters (q, n, r_{eff}) of Einasto profile. The blue lines and squares mark the best value of each parameter.

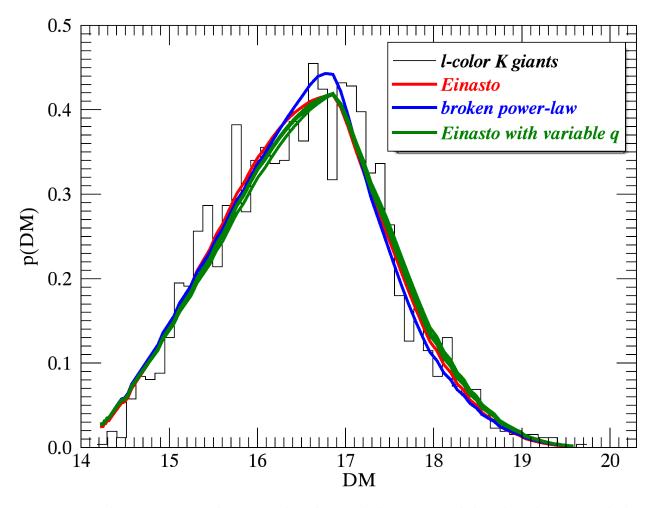


Fig. 5.—: The comparison between the observed distance-modulus distribution and the predicted distributions by the best-fitting models. All of the best-fitting models fit well.

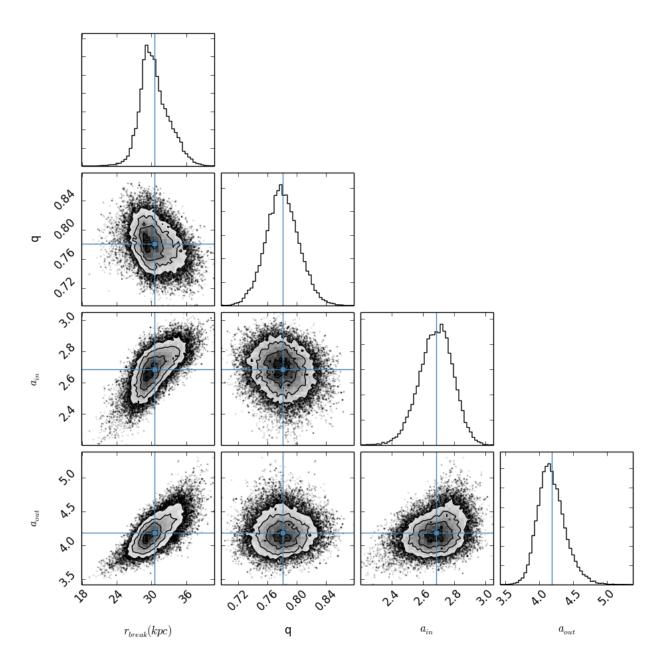


Fig. 6.—: The triangle plot shows all the one and two dimensional projections of the posterior probability distributions of parameters $(q, \alpha_{in}, \alpha_{out}, r_{break})$ of the broken power-law profile. The blue lines and squares mark the best value of each parameter.

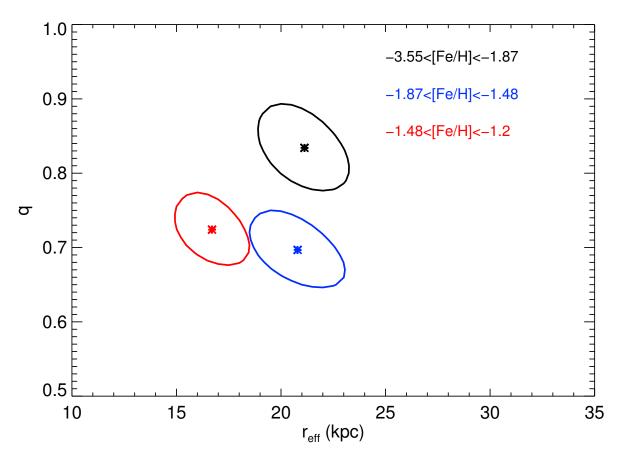


Fig. 7.—: The best-fit values of flattening and effective radii and their 68% confidence levels for three sub-samples in different metallicity bins. The shape of the stellar halo has strong dependence on the metallicity, while the radial profile is independent on metallicity.

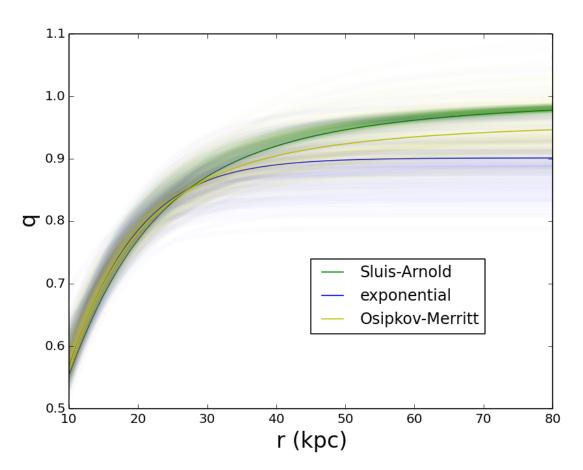


Fig. 8.—: The comparison between three models of flattening variation. They are consistent with each other.

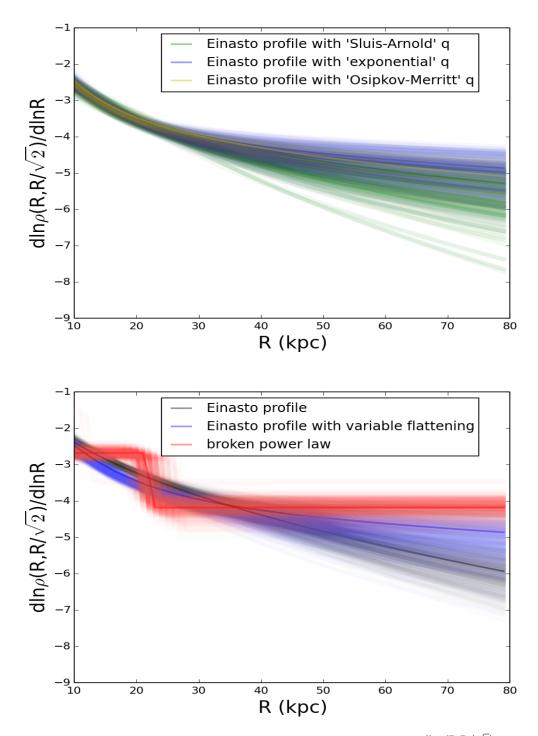


Fig. 9.—: (Upper panel) Comparison of the local power-law slope $\frac{\text{dln}\nu(R,R/\sqrt{2})}{\text{dln}R}$ for the best-fit Einasto profiles with different functional forms of the flattening variation (Section 4.3); the lines correspond to radial profiles created from XX (??) samples of the parameter's PDF. (Lower panel) Comparison between the radial profile $\frac{\text{dln}\nu(R,R/\sqrt{2})}{\text{dln}R}$ for the best-fit broken power-law with constant flattening (red) and the best-fit Einasto profiles with constant (black) or variable (blue) flattening. Despite the fact that the Einasto profiles in the two cases (black and blue) have errective radii that differ by a factor of two, their radial profiles are very similar within the range constrained by the data.

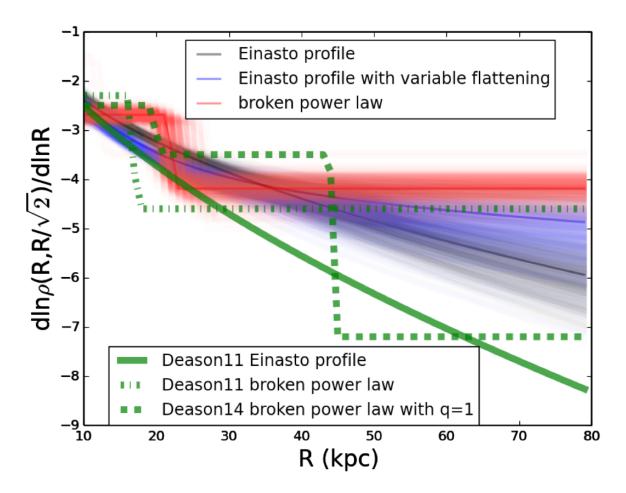


Fig. 10.—: $\frac{\text{dln}\nu(R,R/\sqrt{2})}{\text{dln}R}$ for our best-fit broken power-law with constant flattening (red) and best-fit Einasto profiles with constant flattening (black) or variable flattening (blue) and the best-fit models of ??, green.