

3.1

$$a. \begin{cases} H_0: \beta_2 = 0 \\ H_1: \beta_2 > 0 \end{cases}$$

$$b. t = b_2 / \text{se}(b_2) \sim t(b_2)$$

c. shift to right

$$d. t_{62, 0.01} = 2.388.$$

if $t > 2.388$, we reject H_0 .

if $t < 2.388$ we fail to reject H_0 .

$$e. t = \frac{0.01309}{0.00215} = 6.088 > 2.388$$

we reject H_0 , Medals and GDP is significantly positive.

3.7.
(a)

$$\frac{a}{2.672} = 4.31, \quad a = 11.51632$$

(b) Income and Bachelor is increasing at constant rate.

(c) $t = \frac{1.029}{c} = 10.75, \quad c = 0.0957$

(d) $t = \frac{11.51632 - 10}{2.092} = 0.5675$

(e) $t \geq 2.0096, \quad t \leq -2.0096$

(f) $1.029 \pm t_{0.05, 0.005} \times se$
 $= [0.7725, 1.2855]$

(g)
$$\begin{cases} H_0: \beta_2 = 1 \\ H_1: \beta_2 \neq 1 \end{cases}$$

$$\frac{1.029 - 1}{0.0957} = 0.3030 < t_{0.025, 4}$$

3. 17

$$(a) \begin{cases} H_0: \beta_2 = 1.8 \\ H_1: \beta_2 > 1.8 \end{cases}$$

$$t = \frac{2.46 - 1.8}{0.16} = 4.125$$

$$t_{984, 0.05} = 1.6464$$

$4.125 > 1.6464$, so, we reject H_0

$$b) \mu = -4.88 + 1.8 \times 16 = 23.92$$

$$\mu \pm t_{(212, 0.025)} \times se = [22.28, 25.553]$$

$$\begin{aligned} se(Wage) &= \sqrt{se(\hat{\beta}_0)^2 + (EDUC)^2 se(\hat{\beta}_1)^2} \\ &\quad + 2 \cdot EDUC \cdot cov(\hat{\beta}_0, \hat{\beta}_1) \\ &= -0.761 \end{aligned}$$

(c)

$$\mu = -10.76 + 2.46 \times 16 = 28.6$$

$$\begin{aligned} se(Wage) &= \sqrt{(2.27)^2 + (16)^2 \times (0.16)^2 + 2 \times 16 \times (-0.14)} \\ &= 0.8164 \end{aligned}$$

$$\mu \pm t_{(0.05)} \times se = 28.6 \pm 1.96 \times 0.8164 = [27.00, 30.20]$$

d.

$$H_0: \beta_1 \geq 4$$

$$H_1: \beta_1 < 4$$

$$\begin{aligned} t &= \frac{-6.88 - 4}{3.29} = -2.6991 < t_{(212, 0.01)} \\ &= -2.3441 \end{aligned}$$