

2.11.1 Problems

2.1 Consider the following five observations. You are to do all the parts of this exercise using only a

x	у	$x - \overline{x}$	$(x-\overline{x})^2$	$y - \overline{y}$	$(x-\overline{x})(y-\overline{y})$
3	4	7	Y	7	Y
2	2			0	ΰ
1	3	0	0	1	O
-1	1	- 2	÷	-1	٨
0	0)		ーン	2
$\sum x_i =$	$\sum y_i =$	$\sum (x_i - \overline{x}) =$	$\sum (x_i - \overline{x})^2 =$	$\sum (y_i - \overline{y}) =$	$\sum (x_i - \overline{x})(y_i - \overline{y}) =$
5	10	0	10	O	8

Complete the entries in the table. Put the sums in the last row. What are the sample means \bar{x} and \bar{y} ?

b. Calculate b_1 and b_2 using (2.7) and (2.8) and state their interpretation.

Compute $\sum_{i=1}^5 x_i^2, \sum_{j=1}^5 x_j y_j$. Using these numerical values, show that $\sum (x_i - \overline{x})^2 = \sum x_i^2 - N \overline{x}^2$ and $\sum (x_i - \overline{x})(y_i - \overline{y}) = \sum x_i y_i - N \overline{x} \overline{y}$.

d. Use the least squares estimates from part (b) to compute the fitted values of y, and complete the remainder of the table below. Put the sums in the last row.

Calculate the sample variance of y, $s_y^2 = \sum_{i=1}^{N} (y_i - \overline{y})^2 / (N - 1)$, the sample variance of x, $s_x^2 = \sum_{i=1}^N (x_i - \overline{x})^2 / (N - 1)$, the sample covariance between x and y, $s_{xy} = \sum_{i=1}^N (y_i - \overline{y}) (x_i - \overline{x}) / (N - 1)$ (N-1), the sample correlation between x and y, $r_{xy} = s_{xy}/(s_x s_y)$ and the coefficient of variation of x, $CV_x = 100(s_x/\bar{x})$. What is the median, 50th percentile, of x?

X _i	y_i	ŷį	\hat{e}_{i}	\hat{e}_{i}^{2}	$x_i \hat{e}_i$
3	4	3-6	0-4	0.16	1.>
2	2	2 -8	-08	064	-(.6
1	3	2.0	1-0	1.0	1-0
-1	1	0.4	0-6	0-78	-0.6
0	0	(-2	-1-2	1-44	0
$\sum x_i =$	$\sum y_i =$	$\sum \hat{y}_i =$	$\sum \hat{e}_i =$	$\sum \hat{e}_i^2 =$	$\sum x_i \hat{e}_i =$
		()	_	I	0

$$\alpha$$
, $\pm x_i = s$. $x = \frac{s}{s} = 1$. $\pm x_i = \frac{s}{s} = 1$.

x	у	$x - \overline{x}$	$(x-\overline{x})^2$	$y - \overline{y}$	$(x-\overline{x})(y-\overline{y})$
3	4	3-1,5	シュル	4-2-2	2.224
2	2	2-1=1	(2=	2-2=0	-0"0
1	3	1-1=0	0 0	3-2-1	0-1=0
-1	1	-(-(=-)	(-2)2 · 4	1-2=-1	(->).(<)=?
0	0	0-12-1	417	0-2=-2	(-17.1-2)=

10

be means that for each unit increase in x, y is expected to

increase by 0-8 units, holding all else constant. b1=1-2 is

On estimated value of y when
$$\chi = 0$$
. #

 $\sum_{i=1}^{5} \chi_{i} \chi_{i}^{-1}$
 $\sum_{i=1}^{5} \chi_{i}^{-1} \chi_{i}^{-1}$
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 $\sum_{i=1}^{5} \chi_{i}^{-1} \chi_{i$

e. On graph paper, plot the data points and sketch the fitted regression line
$$\hat{y}_1 = b_1 + b_2 x_1$$
.

f. On the sketch in part (e), locate the point of the means (\bar{x}, \bar{y}) . Does your fitted line pass through that point? If not, go back to the drawing board, literally.

g. Show that for these numerical values $\bar{y} = \bar{y}$, where $\bar{y} = \bar{y}$, \bar{y} .

h. Show that for these numerical values $\bar{y} = \bar{y}$, where $\bar{y} = \bar{y}$, \bar{y} .

i. Compute $\hat{\sigma}^2$.

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j. Above the fitted $\hat{\sigma}^2$.

 $\hat{\sigma}^2 = 1 - 2 + 0 - 8 \times 1$.

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 $\hat{\sigma}^2 = 1$

$$\int_{-\infty}^{\infty} \frac{\sum e^{i}}{N-2} = \frac{3.6}{5.2} = \frac{1-2}{10} = 0.$$

Se (b2) = JVar (b) - J0.12 = 0.346 #

2.14 Consider the regression model $WAGE = \beta_1 + \beta_2 EDUC + e$, where WAGE is hourly wage rate in U.S. 2013 dollars and EDUC is years of education, or schooling. The regression model is estimated twice using the least squares estimator, once using individuals from an urban area, and again for individuals in a rural area. $\widehat{WAGE} = -10.76 + 2.46 \, EDUC, \quad N = 986$ Urban (2.27) (0.16) $\widehat{WAGE} = -4.88 + 1.80 \, EDUC, \quad N = 214$ (3.29) (0.24) a. Using the estimated rural regression, compute the elasticity of wages with respect to education at the "point of the means." The sample mean of WAGE is \$19.74. b. The sample mean of EDUC in the urban area is 13.68 years. Using the estimated urban regression, compute the standard error of the elasticity of wages with respect to education at the "point of the means." Assume that the mean values are "givens" and not random. What is the predicted wage for an individual with 12 years of education in each area? With 16 years of education? a. Yural: WAGE = - 4-88 + 1.80 EDUC DWAGE = 1.8 (b1) mean of WAGE = \$19.74.

elasticity,
$$\frac{\delta WAGE}{\delta EDUC}$$
 $\frac{EDUC}{WAGE}$, 1-8. $\frac{13.68}{(9.74)} \approx 1.247$.

SE (elasticity)=
$$\frac{EDUC}{WAGE}$$
 SE (b) = $\frac{13-68}{19.74}$ [0.1 b \approx 0.11]

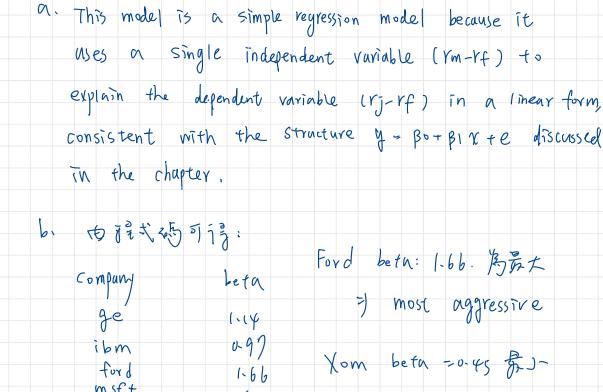
C. urban: WAGE - - (0. 16 + 2.46 EDUC when EDUC = 12, wage = -(0,16+2-46 x12 = 18.76 (\$) When EDUC: (b, WAGE = -(0.76+2,46x16=28.6C\$) rura / ? WAGE = -488 + 1.80 EDUC When EDUC=12, WAGE= (6,72 (\$)
When EDUC=16, WAGE= 23,92 (\$)

2.16 The capital asset pricing model (CAPM) is an important model in the field of finance. It explains variations in the rate of return on a security as a function of the rate of return on a portfolio consisting of all publicly traded stocks, which is called the market portfolio. Generally, the rate of return on any investment is measured relative to its opportunity cost, which is the return on a risk-free asset. The resulting difference is called the risk premium, since it is the reward or punishment for making a risky investment. The CAPM says that the risk premium on security j is proportional to the risk premium on the market portfolio. That is, $r_i - r_f = \beta_i (r_m - r_f)$ where r_i and r_f are the returns to security j and the risk-free rate, respectively, r_m is the return on the market portfolio, and β_i is the jth security's "beta" value. A stock's beta is important to investors since it reveals the stock's volatility. It measures the sensitivity of security j's return to variation in the whole stock market. As such, values of beta less than one indicate that the stock is "defensive" since its variation is less than the market's. A beta greater than one indicates an "aggressive stock." Investors usually want an estimate of a stock's beta before purchasing it. The CAPM model shown above is the "economic model" in this case. The "econometric model" is obtained by including an intercept in the model (even though theory says it should be zero) and an error term $r_i - r_f = \alpha_i + \beta_i (r_m - r_f) + e_i$

- a. Explain why the econometric model above is a simple regression model like those discussed in this b. In the data file capm5 are data on the monthly returns of six firms (GE, IBM, Ford, Microsoft,
- Disney, and Exxon-Mobil), the rate of return on the market portfolio (MKT), and the rate of return on the risk-free asset (RISKFREE). The 180 observations cover January 1998 to December 2012. Estimate the CAPM model for each firm, and comment on their estimated beta values. Which firm appears most aggressive? Which firm appears most defensive? c. Finance theory says that the intercept parameter α_i should be zero. Does this seem correct given
- your estimates? For the Microsoft stock, plot the fitted regression line along with the data scatter.
- **d.** Estimate the model for each firm under the assumption that $\alpha_i = 0$. Do the estimates of the *beta* values change much?

dis

Kom



1-0

0-45

3 m-st defensive.

