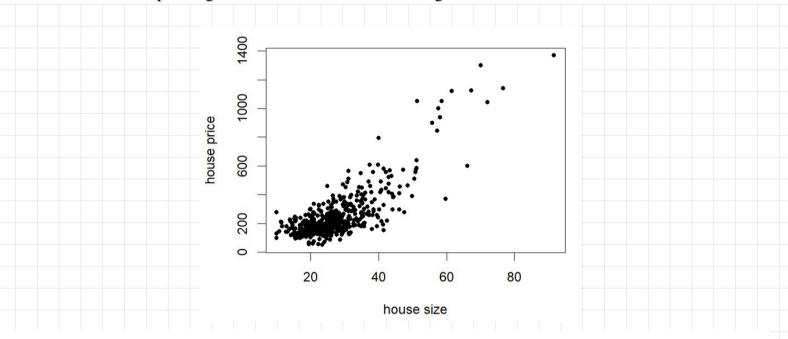
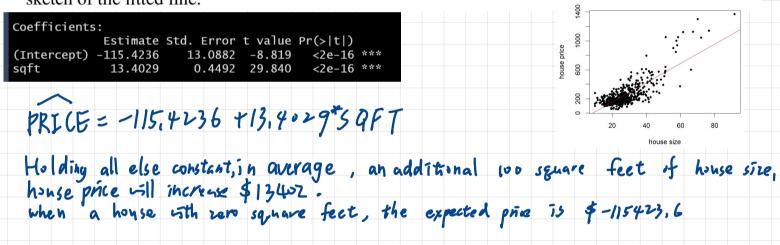
- **2.17** The data file *collegetown* contains observations on 500 single-family houses sold in Baton Rouge, Louisiana, during 2009–2013. The data include sale price (in thousands of dollars), *PRICE*, and total interior area of the house in hundreds of square feet, *SQFT*.
 - a. Plot house price against house size in a scatter diagram.



b. Estimate the linear regression model $PRICE = \beta_1 + \beta_2 SQFT + e$. Interpret the estimates. Draw a sketch of the fitted line.



Estimate the quadratic regression model $PRICE = \alpha_1 + \alpha_2 SQFT^2 + e$. Compute the marginal effect of an additional 100 square feet of living area in a home with 2000 square feet of living space.

Coefficients:

Estimate Std. Error t value
$$Pr(>|t|)$$

(Intercept) 93.565854 6.072226 15.41 $<2e-16$ ***

 $sqft_square$ 0.184519 0.005256 35.11 $<2e-16$ ***

$$PRICE = 97.5659 + 0.184519^*5977$$

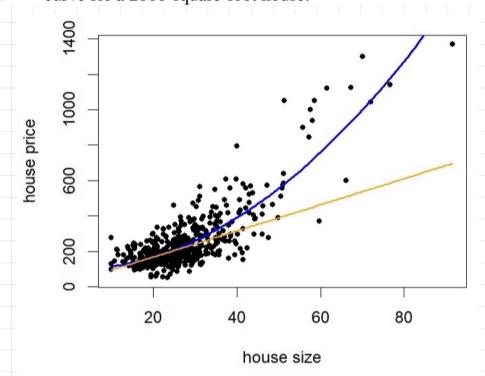
$$\frac{3}{3}PRIE = 2x0.184519 \times 30F7$$

$$\frac{3}{3}PRIE = 2x0.184519 \times 30F7$$

$$\frac{3}{3}PRIE = 7.38076$$

marging effect = \$7380.76

d. Graph the fitted curve for the model in part (c). On the graph, sketch the line that is tangent to the curve for a 2000-square-foot house.

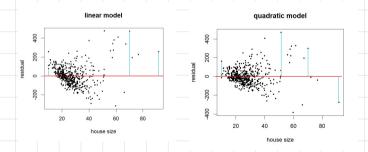


e. For the model in part (c), compute the elasticity of *PRICE* with respect to *SQFT* for a home with 2000 square feet of living space.

$$\mathcal{L} = \frac{\partial PRICE}{\partial SQFT} \times \frac{SQFJ}{PRILE} = 2 \times 0.184519 \times 20 \times \frac{20}{97.5659 + 0.184519 \times 20^{2}}$$

$$= 0.882$$

f. For the regressions in (b) and (c), compute the least squares residuals and plot them against *SQFT*. Do any of our assumptions appear violated?



SR 3: Conditional Homoskedasticity
$$Var(e_i | \mathbf{x}) = \sigma^2$$

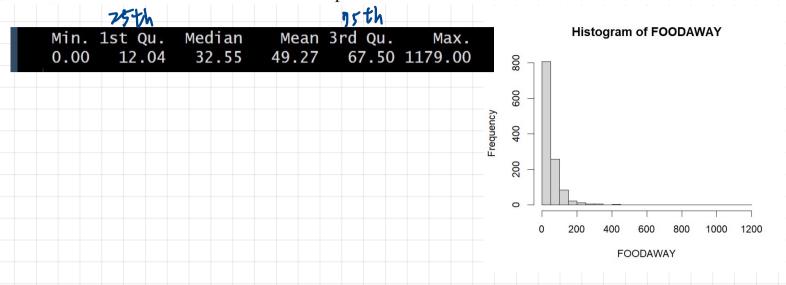
In both models, the residual patterns do not appear random. The variation in the residuals increases as SQFT increases, suggesting that the homoskedasticity assumption may be violated.

- g. One basis for choosing between these two specifications is how well the data are fit by the model. Compare the sum of squared residuals (SSE) from the models in (b) and (c). Which model has a lower SSE? How does having a lower SSE indicate a "better-fitting" model?
 - (b) SSE , 5262847 (c) SSE : 4222356

35Eb 7 55Ec

In this case the quadratic model has the lower SSE. The lower SSE means that the data values are closer to the fitted line for the quadratic model than for the linear.

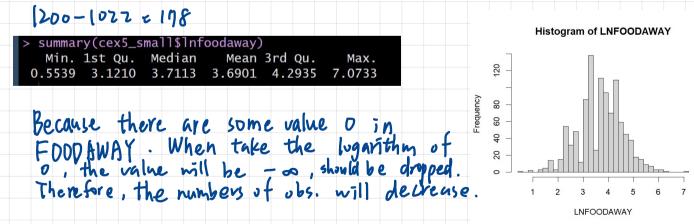
- **2.25** Consumer expenditure data from 2013 are contained in the file *cex5_small*. [Note: *cex5* is a larger version with more observations and variables.] Data are on three-person households consisting of a husband and wife, plus one other member, with incomes between \$1000 per month to \$20,000 per month. *FOODAWAY* is past quarter's food away from home expenditure per month per person, in dollars, and *INCOME* is household monthly income during past year, in \$100 units.
 - **a.** Construct a histogram of *FOODAWAY* and its summary statistics. What are the mean and median values? What are the 25th and 75th percentiles?



b. What are the mean and median values of *FOODAWAY* for households including a member with an advanced degree? With a college degree member? With no advanced or college degree member?

Mean	megian
13,15	48115
48,60	36,11
3910	26.02
	13,15

c. Construct a histogram of ln(*FOODAWAY*) and its summary statistics. Explain why *FOODAWAY* and ln(*FOODAWAY*) have different numbers of observations.

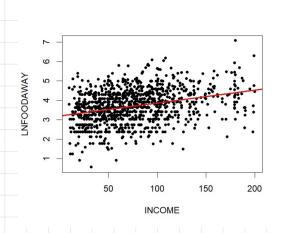


d. Estimate the linear regression $ln(FOODAWAY) = \beta_1 + \beta_2 INCOME + e$. Interpret the estimated slope.

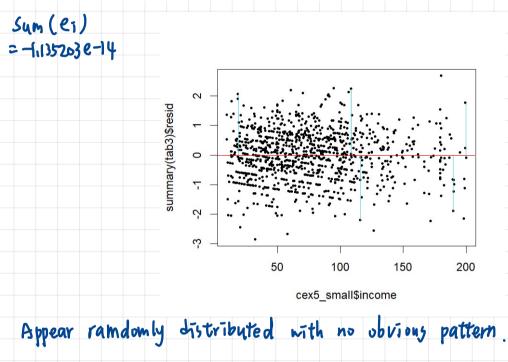
Holding all else constant, in average, an addition \$100 of Thome, food away expenditure perperson of about 0.66%

In (FDODAWAY) = 3,1885 +0,0166 INCOME

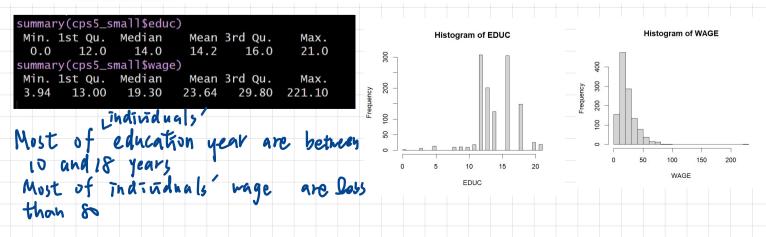
e. Plot ln(FOODAWAY) against INCOME, and include the fitted line from part (d).



f. Calculate the least squares residuals from the estimation in part (d). Plot them vs. *INCOME*. Do you find any unusual patterns, or do they seem completely random?



- **2.28** How much does education affect wage rates? The data file *cps5_small* contains 1200 observations on hourly wage rates, education, and other variables from the 2013 Current Population Survey (CPS). [Note: *cps5* is a larger version.]
 - **a.** Obtain the summary statistics and histograms for the variables *WAGE* and *EDUC*. Discuss the data characteristics.



b. Estimate the linear regression $WAGE = \beta_1 + \beta_2 EDUC + e$ and discuss the results.

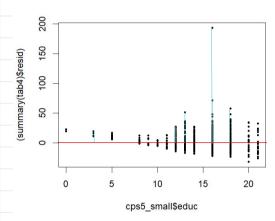
Holding all else constant, in average, an additional I year of education income will increase 23968 units.

when an individual with a year eduction, the expected income is \$-10.4 units

c. Calculate the least squares residuals and plot them against *EDUC*. Are any patterns evident? If assumptions SR1–SR5 hold, should any patterns be evident in the least squares residuals?

```
Sum (e;) = 9.824919e-13
```

In the model, the residual patterns do not appear random. The variation in the residuals increases as EDUC increases, suggesting that the homoskedasticity assumption may be violated.



d. Estimate separate regressions for males, females, blacks, and whites. Compare the results.

```
call: Male
lm(formula = wage ~ educ, data = cps5_small, subset = (female =
    0))
Residuals:
               1Q Median
    Min
                                   30
                                           Max
-27.643 -9.279
                               5.663 191.329
                    -2.957
Coefficients:
              Estimate Std. Error t value Pr(>|t|)
-8.2849 2.6738 -3.099 0.00203
                              2.6738 -3.099 0.00203 **
0.1881 12.648 < 2e-16 ***
(Intercept)
                 2.3785
educ
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 14.71 on 670 degrees of freedom
Multiple R-squared: 0.1927, Adjusted R-squared: 0.F-statistic: 160 on 1 and 670 DF, p-value: < 2.2e-16
                                     Adjusted R-squared: 0.1915
F-statistic:
```

```
ca11: temale
lm(formula = wage ~ educ, data = cps5_small, subset = (female ==
     1))
Residuals:
Min 1Q Median
-30.837 -6.971 -2.811
                                5.102 49.502
Coefficients:
               Estimate Std. Error t value Pr(>|t|)
                               2.7837
                                        -5.964 4.51e-09 ***
(Intercept) -16.6028
                               0.1876 14.174 < 2e-16 ***
                 2.6595
educ
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 11.5 on 526 degrees of freedom
Multiple R-squared: 0.2764, Adjusted R-squared: 0.275
Multiple R-squared: 0.2764, Adjusted R-squared: 0.7
F-statistic: 200.9 on 1 and 526 DF, p-value: < 2.2e-16
```

```
Call: White

Im(formula = wage ~ educ, data = cps5_small, subset = (black == 0))

Residuals:

Min 1Q Median 3Q Max

-32.131 -8.539 -3.119 5.960 192.890

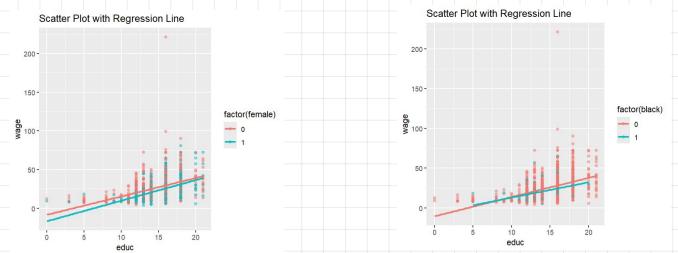
Coefficients:

Estimate Std. Error t value Pr(>|t|)

(Intercept) -10.475 2.081 -5.034 5.6e-07 ***
educ 2.418 0.143 16.902 < 2e-16 ***

---
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 13.79 on 1093 degrees of freedom
Multiple R-squared: 0.2072, Adjusted R-squared: 0.2065
F-statistic: 285.7 on 1 and 1093 DF, p-value: < 2.2e-16
```



The growth speeds of mage in white is a little bit higher than black.

(slope)

The growth speeds if mage in white is a little bit higher than black.

(slope)

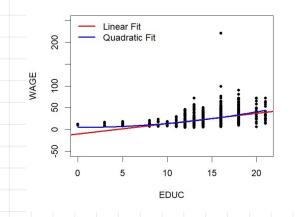
e. Estimate the quadratic regression $WAGE = \alpha_1 + \alpha_2 EDUC^2 + e$ and discuss the results. Estimate the marginal effect of another year of education on wage for a person with 12 years of education and for a person with 16 years of education. Compare these values to the estimated marginal effect of education from the linear regression in part (b).

WAGE = 4.9165+0.0891 EDUC

WAGE = 4.9165+0.0891 EDUC

Marginal effect: \(\frac{2}{3}\text{WAGE} \) = 20 \(\frac{2}{3}\text{EDUC} \) = 20 \(\frac{2}{3}\text{GBUC} \) = 20 \(\frac{2}{3}\text{GBUC} \) = 20 \(\frac{2}{3}\text{968} \) = 30 \(\frac{2}{3}\te

f. Plot the fitted linear model from part (b) and the fitted values from the quadratic model from part (e) in the same graph with the data on *WAGE* and *EDUC*. Which model appears to fit the data better?



Quadratic model fit the data better