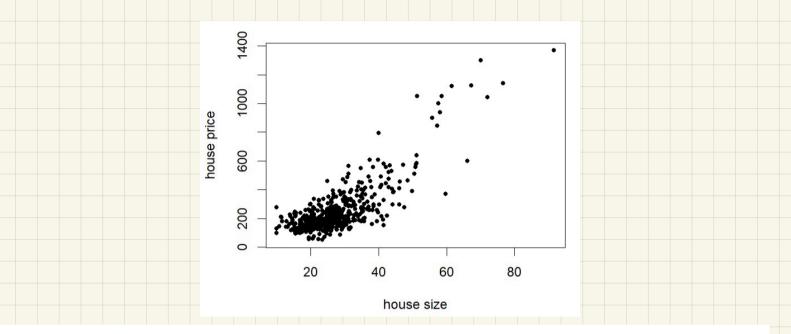
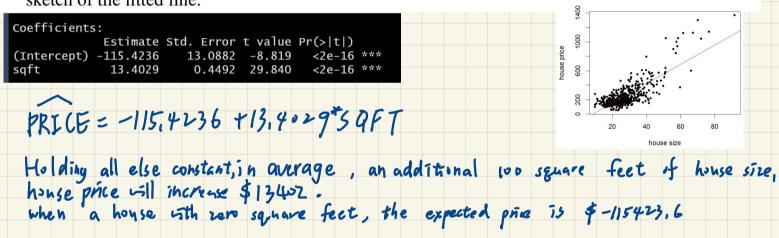
- **2.17** The data file *collegetown* contains observations on 500 single-family houses sold in Baton Rouge, Louisiana, during 2009–2013. The data include sale price (in thousands of dollars), *PRICE*, and total interior area of the house in hundreds of square feet, *SQFT*.
  - a. Plot house price against house size in a scatter diagram.



**b.** Estimate the linear regression model  $PRICE = \beta_1 + \beta_2 SQFT + e$ . Interpret the estimates. Draw a sketch of the fitted line.



Estimate the quadratic regression model  $PRICE = \alpha_1 + \alpha_2 SQFT^2 + e$ . Compute the marginal effect of an additional 100 square feet of living area in a home with 2000 square feet of living space.

Coefficients:

Estimate Std. Error t value 
$$Pr(>|t|)$$

(Intercept) 93.565854 6.072226 15.41 <2e-16 \*\*\*

sqft\_square 0.184519 0.005256 35.11 <2e-16 \*\*\*

PRICE = 97.5659 + 0.184519\*5 9FT

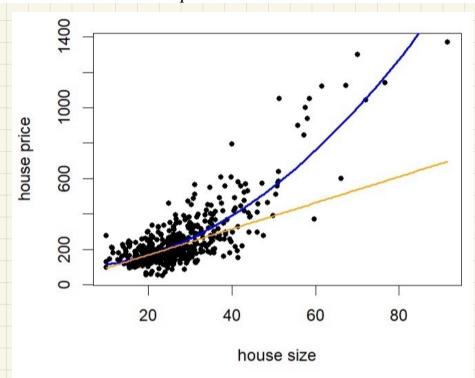
PRICE = 2x0.184519 x 5QFT

PRICE = 2x0.184519 x 5QFT

PRICE = 1,38076

marginal effect = \$7380.76

**d.** Graph the fitted curve for the model in part (c). On the graph, sketch the line that is tangent to the curve for a 2000-square-foot house.

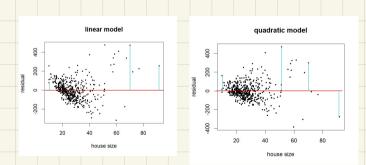


**e.** For the model in part (c), compute the elasticity of *PRICE* with respect to *SQFT* for a home with 2000 square feet of living space.

$$\mathcal{L} = \frac{\partial PRICE}{\partial SQFT} \times \frac{SQFT}{PRICE} = 2 \times 0.184519 \times 20 \times \frac{20}{97.5659 + 0.184519 \times 20^{2}}$$

$$= 0.882$$

**f.** For the regressions in (b) and (c), compute the least squares residuals and plot them against *SQFT*. Do any of our assumptions appear violated?



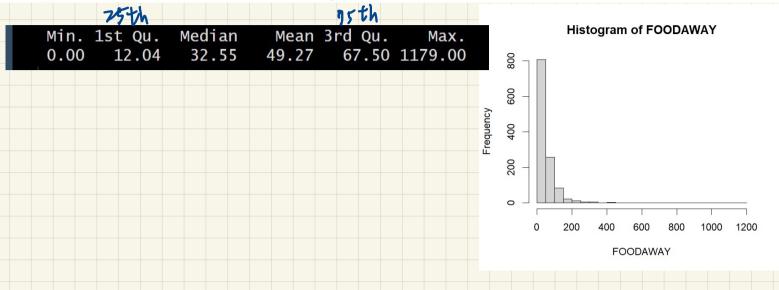
SR 3: Conditional Homoskedasticity 
$$Var(e_i | \mathbf{x}) = \sigma^2$$

In both models, the residual patterns do not appear random. The variation in the residuals increases as SQFT increases, suggesting that the homoskedasticity assumption may be violated.

- **g.** One basis for choosing between these two specifications is how well the data are fit by the model. Compare the sum of squared residuals (*SSE*) from the models in (b) and (c). Which model has a lower *SSE*? How does having a lower *SSE* indicate a "better-fitting" model?
  - (b) 55E , 5262847 (c) 55E : 4222356

In this case the quadratic model has the lower SSE. The lower SSE means that the data values are closer to the fitted line for the quadratic model than for the linear .

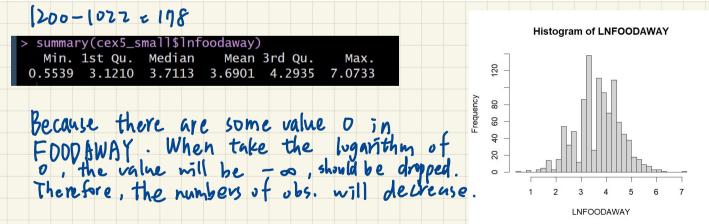
- **2.25** Consumer expenditure data from 2013 are contained in the file *cex5\_small*. [Note: *cex5* is a larger version with more observations and variables.] Data are on three-person households consisting of a husband and wife, plus one other member, with incomes between \$1000 per month to \$20,000 per month. *FOODAWAY* is past quarter's food away from home expenditure per month per person, in dollars, and *INCOME* is household monthly income during past year, in \$100 units.
  - **a.** Construct a histogram of *FOODAWAY* and its summary statistics. What are the mean and median values? What are the 25th and 75th percentiles?



**b.** What are the mean and median values of *FOODAWAY* for households including a member with an advanced degree? With a college degree member? With no advanced or college degree member?

	Mean	Median
advanced	13,15	48115
college	48,60	36,11
None	3910	26.02

**c.** Construct a histogram of ln(FOODAWAY) and its summary statistics. Explain why FOODAWAY and ln(FOODAWAY) have different numbers of observations.



**d.** Estimate the linear regression  $ln(FOODAWAY) = \beta_1 + \beta_2 INCOME + e$ . Interpret the estimated slope.

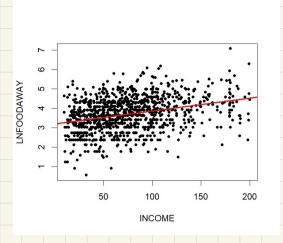
```
Coefficients:

Estimate Std. Error t value Pr(>|t|)
(Intercept) 3.1884908 0.0541157 58.92 <2e-16 ***
income 0.0066381 0.0006265 10.60 <2e-16 ***

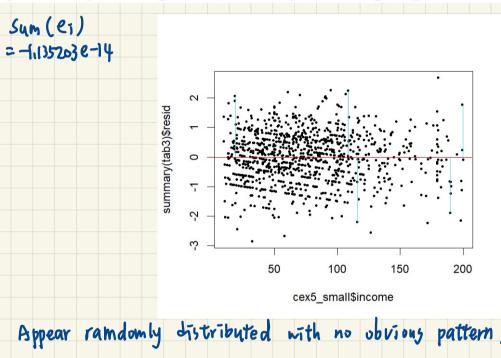
expenditure per person of about 0.66
```

In (FDODAWAY) = 3,1885 + 0,0166 "INCOME

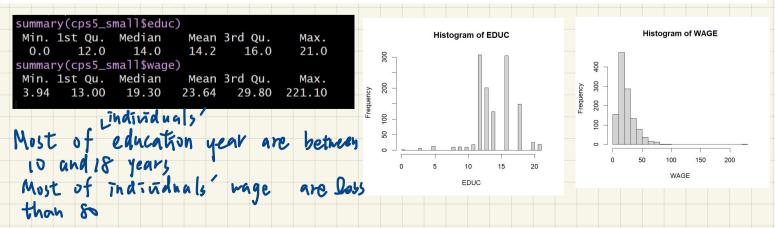
e. Plot ln(FOODAWAY) against INCOME, and include the fitted line from part (d).



**f.** Calculate the least squares residuals from the estimation in part (d). Plot them vs. *INCOME*. Do you find any unusual patterns, or do they seem completely random?



- **2.28** How much does education affect wage rates? The data file *cps5\_small* contains 1200 observations on hourly wage rates, education, and other variables from the 2013 Current Population Survey (CPS). [Note: *cps5* is a larger version.]
  - **a.** Obtain the summary statistics and histograms for the variables *WAGE* and *EDUC*. Discuss the data characteristics.



**b.** Estimate the linear regression  $WAGE = \beta_1 + \beta_2 EDUC + e$  and discuss the results.

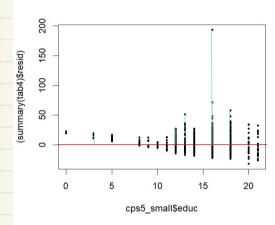
Holding all else constant, in average, an additional I year of education income will increase 213968 units.

when an individual with a year eduction, the expected income is \$-10.4 units

**c.** Calculate the least squares residuals and plot them against *EDUC*. Are any patterns evident? If assumptions SR1–SR5 hold, should any patterns be evident in the least squares residuals?

```
Sum (e;) = 9.824919e-13
```

In the model, the residual patterns do not appear random. The variation in the residuals increases as EDUC increases, suggesting that the homoskedasticity assumption may be violated.

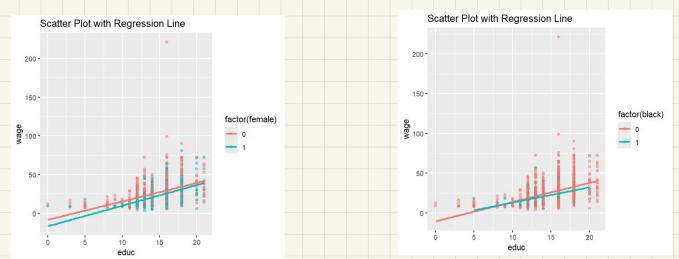


d. Estimate separate regressions for males, females, blacks, and whites. Compare the results.

```
call: Male
lm(formula = wage ~ educ, data = cps5_small, subset = (female =
    0))
Residuals:
               10 Median
    Min
                                 30
                                         Max
         -9.279
                              5.663 191.329
-27.643
                   -2.957
Coefficients:
             Estimate Std. Error t value Pr(>|t|)
-8.2849 2.6738 -3.099 0.00203
                                     -3.099 0.00203 **
(Intercept)
                             0.1881 12.648 < 2e-16 ***
                2.3785
educ
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 14.71 on 670 degrees of freedom
Multiple R-squared: 0.1927, Adjusted R-squared: 0.F-statistic: 160 on 1 and 670 DF, p-value: < 2.2e-16
                                   Adjusted R-squared: 0.1915
F-statistic:
```

```
call: temale
lm(formula = wage ~ educ, data = cps5_small, subset = (female ==
     1))
Residuals:
Min 1Q Median
-30.837 -6.971 -2.811
                                5.102 49.502
Coefficients:
               Estimate Std. Error t value Pr(>|t|)
                               2.7837
                                        -5.964 4.51e-09 ***
(Intercept) -16.6028
                               0.1876 14.174 < 2e-16 ***
                 2.6595
educ
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 11.5 on 526 degrees of freedom
Multiple R-squared: 0.2764, Adjusted R-squared: 0.275
Multiple R-squared: 0.2764, Adjusted R-squared: 0.7
F-statistic: 200.9 on 1 and 526 DF, p-value: < 2.2e-16
```

```
call: White
lm(formula = wage ~ educ, data = cps5_small, subset = (black ==
     0))
Residuals:
                 1Q Median
 -32.131 -8.539
                                    5.960 192.890
                       -3.119
Coefficients:
                Estimate Std. Error t value Pr(>|t|)
-10.475 2.081 -5.034 5.6e-07 ***
(Intercept)
                    2.418
                                   0.143 16.902
                                                        < 2e-16 ***
educ
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 13.79 on 1093 degrees of freedom
Multiple R-squared: 0.2072, Adjusted R-squared: 0.2065
F-statistic: 285.7 on 1 and 1093 DF, p-value: < 2.2e-16
```



The growth speeds of mage in white is a little bit higher than black.

(slope)

The growth speeds if mage in white is a little bit higher than black.

(slope)

e. Estimate the quadratic regression  $WAGE = \alpha_1 + \alpha_2 EDUC^2 + e$  and discuss the results. Estimate the marginal effect of another year of education on wage for a person with 12 years of education and for a person with 16 years of education. Compare these values to the estimated marginal effect of education from the linear regression in part (b).

WAGE = 4.9165 + 0.0891 EDUC

Marginal effect: \( \frac{\text{DWAGE}}{\text{DEDUC}} = \text{2d} \) EDUC

= 2x 0.089 \( \text{MEDUC} \)

(Intercept) 4.916477 1.091864 4.503 7.36e-06 \*\*\*\*

educ\_square 0.089134 0.004858 18.347 < 2e-16 \*\*\*

Marginal effect: \( \frac{\text{DWAGE}}{\text{DEDUC}} = \text{2x 0.089 \( \text{MEDUC}} \)

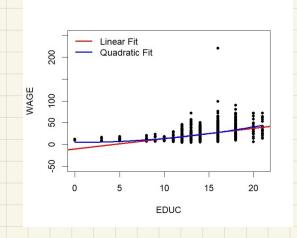
(Intercept) - 10.4000 1.9624 - 5.3 1.38e-07 \*\*\*

educ 2.3968 0.1354 17.7 < 2e-16 \*\*\*

Marginal effect in thear: \( \frac{\text{WAGE}}{\text{VEDUC}} = \text{Cl} \) = 2,3968

In a quadratic model, the marginal effect of another year of education on mage for a person with 12 years of education is smaller than in a linear model; for a person with 16 years of education, it is larger than in a linear model.

**f.** Plot the fitted linear model from part (b) and the fitted values from the quadratic model from part (e) in the same graph with the data on *WAGE* and *EDUC*. Which model appears to fit the data better?



Quadratic model fit the data better

