

2.1

a.

x	y	$x - \bar{x}$	$(x - \bar{x})^2$	$y - \bar{y}$	$(x - \bar{x})(y - \bar{y})$
3	4	2	4	2	4
2	2	1	1	0	0
1	3	0	0	1	0
-1	1	-2	4	-1	2
0	0	-1	1	-2	2
$\sum x_i = 5$	$\sum y_i = 10$	$\sum (x_i - \bar{x}) = 0$	$\sum (x_i - \bar{x})^2 = 10$	$\sum (y_i - \bar{y}) = 0$	$\sum (x_i - \bar{x})(y_i - \bar{y}) = 8$

$$\bar{x} = \frac{\sum x_i}{n} = \frac{5}{5} = 1 \quad \bar{y} = \frac{\sum y_i}{n} = \frac{10}{5} = 2$$

$$b. \quad b_2 = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{\sum (x_i - \bar{x})^2} = \frac{8}{10} = 0.8$$

$$b_1 = \bar{y} - b_2 \bar{x} = 2 - 0.8 \cdot 1 = 1.2$$

$$y_{\hat{x}} = 1.2 + 0.8x_i$$

$$c. \quad \sum x_i^2 = 15 \quad \sum x_i y_i = 18$$

$$\begin{aligned} \sum (x_i - \bar{x})^2 &= \sum (x_i^2 - 2\bar{x}x_i + \bar{x}^2) \\ &= \sum x_i^2 - 2\bar{x}\sum x_i + \sum \bar{x}^2 \\ &= \sum x_i^2 - 2N\bar{x} + N\bar{x}^2 \\ &= \sum x_i^2 - N\bar{x}^2 \end{aligned}$$

$$\begin{aligned} \sum (x_i - \bar{x})(y_i - \bar{y}) &= \sum (x_i y_i - x_i \bar{y} - \bar{x} y_i + \bar{x} \bar{y}) \\ &= \sum x_i y_i - \bar{y} \sum x_i - \bar{x} \sum y_i + N\bar{x} \bar{y} \\ &= \sum x_i y_i - N\bar{x} \bar{y} \end{aligned}$$

d.

x_i	y_i	\hat{y}_i	\hat{e}_i	\hat{e}_i^2	$x_i \hat{e}_i$
3	4	3.6	0.4	0.16	1.2
2	2	2.8	-0.8	0.64	-1.6
1	3	2	1	1	1
-1	1	0.4	0.6	0.36	-0.6
0	0	1.2	-1.2	1.44	0
$\sum x_i = 5$		$\sum y_i = 10$	$\sum \hat{y}_i = 10$	$\sum \hat{e}_i = 0$	$\sum \hat{e}_i^2 = 3.6$
$\sum x_i \hat{e}_i = 0$					

$$S_y^2 = \frac{\sum (y_i - \bar{y})^2}{N-1} = \frac{10}{5-1} = 2.5$$

$$N = 5, 1, 0, 1, 2, 3$$

$$S_x^2 = \frac{\sum (x_i - \bar{x})^2}{N-1} = \frac{10}{5-1} = 2.5$$

$$5 \div 2 = 2.5 \rightarrow \text{取 } 3$$

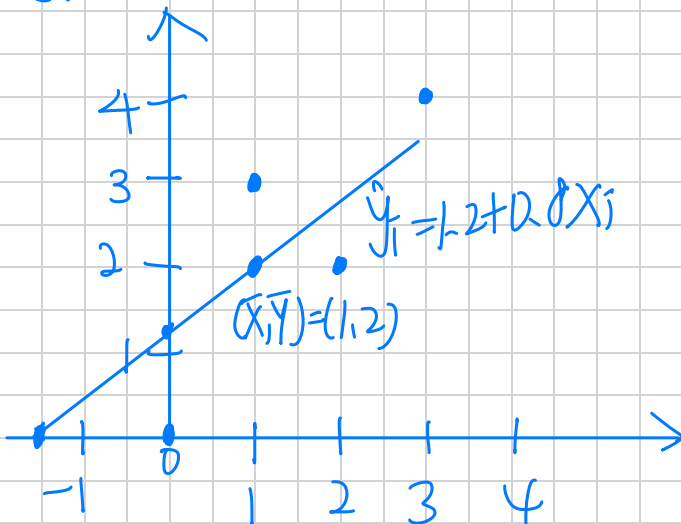
$$S_{xy} = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{N-1} = \frac{8}{5-1} = 2$$

$$\text{media} = 1$$

$$r_{xy} = \frac{S_{xy}}{S_x S_y} = \frac{2}{\sqrt{2.5 \times 2.5}} = 0.8$$

$$C.V._x = 100 \left(\frac{S_x}{\bar{x}} \right) = 158.11$$

e.



$$g. \hat{y}_i = b_1 + b_2 X_i$$

$$\sum \hat{y}_i = n b_1 + b_2 \sum X_i$$

$$\bar{\hat{y}} = b_1 + b_2 \bar{X}$$

$$\begin{aligned} h. \bar{\hat{y}} &= \frac{1}{n} \sum \hat{y}_i = \frac{1}{n} \sum (b_1 + b_2 X_i) \\ &= \frac{1}{n} \times (n b_1 + b_2 n \bar{X}) \\ &= b_1 + b_2 \bar{X} = \bar{y} \end{aligned}$$

$$\text{得證 } \bar{\hat{y}} = \bar{y}$$

$$i. \sigma^2 = \frac{\sum \hat{e}_i^2}{n-2} = \frac{316}{5-2} = 1.2$$

$$j. \text{var}(b_2 | X) = \frac{\sigma^2}{SST_X} = \frac{1.2}{10} = 0.12$$

$$SE(b_2) = \sqrt{0.12} = 0.3464$$

2.14

$$a. \hat{\epsilon} = \hat{\beta}_2 \frac{\bar{X}}{\bar{X} + \bar{X}} = 1.8 \frac{13.68}{19.74} = 1.247$$

$$b. \bar{X} = 13.68 \quad \bar{y} = 22.89$$

$$\begin{aligned} \text{var}(\hat{\epsilon}) &= \text{var}\left(b_2 \frac{\bar{X}}{\bar{y}}\right) \\ &= \left(\frac{\bar{X}}{\bar{y}}\right)^2 \text{var}(b_2) \end{aligned}$$

$$SE(\hat{\epsilon}) = \frac{\bar{X}}{\bar{y}} \cdot SE(b_2) = \frac{13.68}{22.89} \times 0.16 = 0.0956$$

C.

urban:

$$12 \text{ years: } \hat{\text{wage}} = -10.76 + 2.46 \times 12 = 18.76$$

$$16 \text{ years: } \hat{\text{wage}} = -10.76 + 2.46 \times 16 = 28.6$$

Rural:

$$12 \text{ years: } \hat{\text{wage}} = -4.88 + 1.8 \times 12 = 16.72$$

$$16 \text{ years: } \hat{\text{wage}} = -4.88 + 1.8 \times 16 = 23.92$$

2.16

a. A simple linear regression model is any regression equation with just one explanatory variable, a constant and an error term

b.

Firm	Beta	Alpha
1. ge	1.1480	-00010
2. ibm	0.9769	0.0061
3. ford	1.6620	0.0038
4. msft	1.2018	0.0032

5. djs 1.0115 0.0010

6. xom 0.4565 0.0053

defensive firm = min Beta = 0.4565 = Exxon-Mobil

aggressive firm = Max Beta = 1.6620 = Ford

d.

According to the code, the difference between "Beta - with - intercept" and "beta - no - intercept" seem quite small.