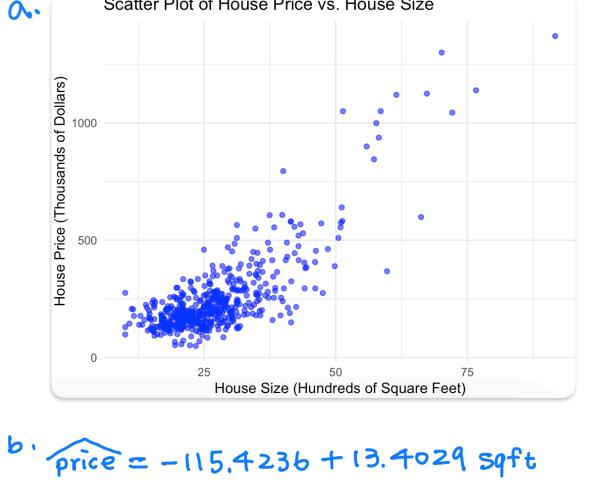
- **2.17** The data file *collegetown* contains observations on 500 single-family houses sold in Baton Rouge, Louisiana, during 2009–2013. The data include sale price (in thousands of dollars), *PRICE*, and total interior area of the house in hundreds of square feet, SQFT.
  - **a.** Plot house price against house size in a scatter diagram.
  - **b.** Estimate the linear regression model  $PRICE = \beta_1 + \beta_2 SQFT + e$ . Interpret the estimates. Draw a sketch of the fitted line.
  - c. Estimate the quadratic regression model  $PRICE = \alpha_1 + \alpha_2 SQFT^2 + e$ . Compute the marginal effect of an additional 100 square feet of living area in a home with 2000 square feet of living space.
  - d. Graph the fitted curve for the model in part (c). On the graph, sketch the line that is tangent to the curve for a 2000-square-foot house.
  - e. For the model in part (c), compute the elasticity of PRICE with respect to SQFT for a home with 2000 square feet of living space.

**f.** For the regressions in (b) and (c), compute the least squares residuals and plot them against SQFT.

- Do any of our assumptions appear violated? g. One basis for choosing between these two specifications is how well the data are fit by the model.
  - Compare the sum of squared residuals (SSE) from the models in (b) and (c). Which model has a lower SSE? How does having a lower SSE indicate a "better-fitting" model?



Scatter Plot of House Price vs. House Size

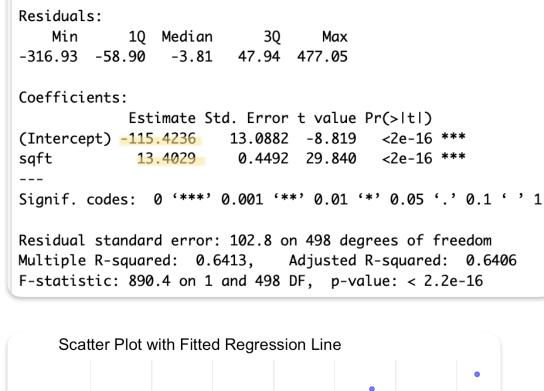
Intercept (b1 = -115.4236):

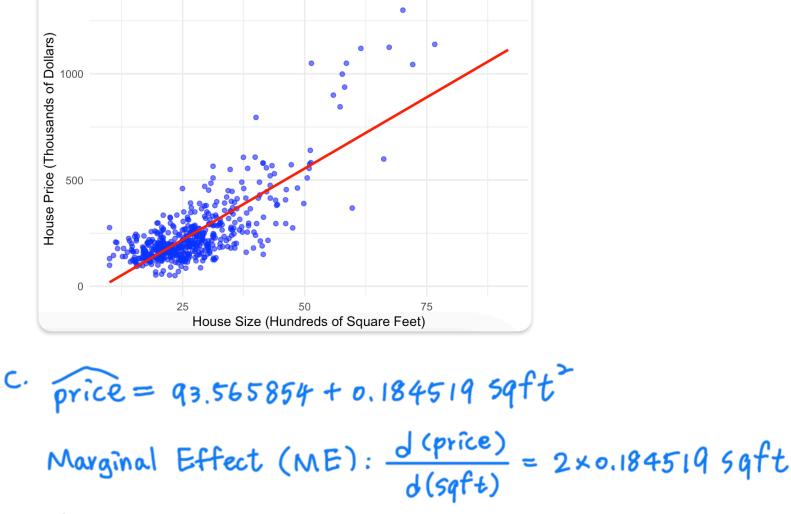
a house with zero square feet has an expected

price of \$-115,423.6 Slope ( b2 = 13.4029):

for every 100 square feet increase in house size, the expected house price increases by \$ 13,402.9

Call: lm(formula = price ~ sqft, data = collegetown) Residuals: Min 1Q Median 3Q





when sqft=20: ME= 2x0.184519 x 20 = 7.38076

lm(formula = price ~ I(sqft^2), data = collegetown)

3Q

Estimate Std. Error t value Pr(>|t|)

38.75 469.70

1Q Median

-383.67 -48.39 -7.50

Interpretation:

Residuals: Min

Coefficients:

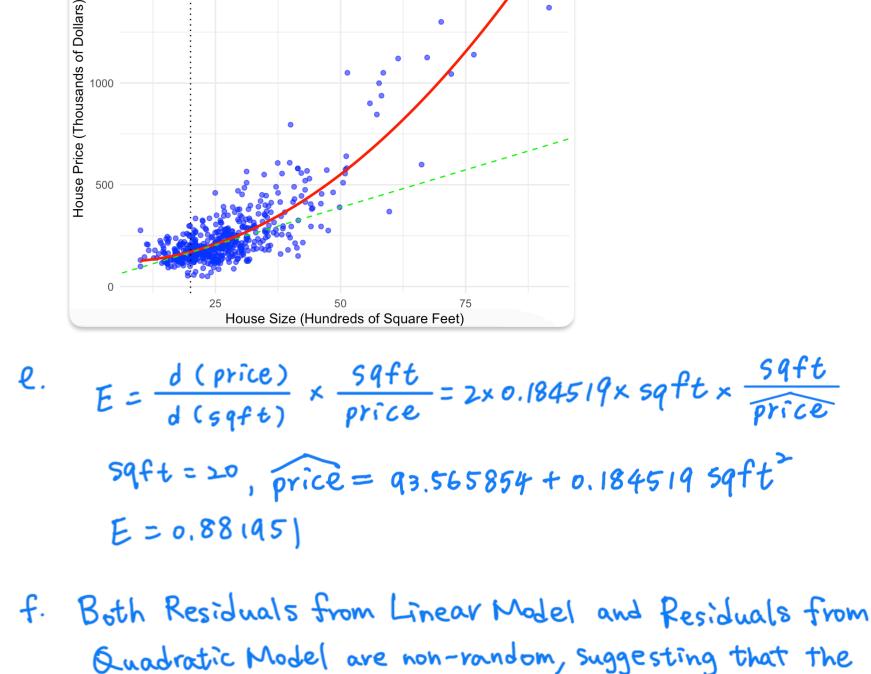
9.

When the house size is 2000 square feet, increasing the size by 100 square feet is expected to increase the house

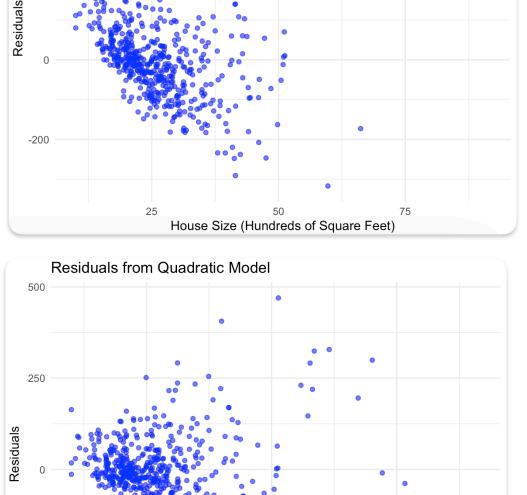
Max

price by approximately \$ 138.016 Call:

(Intercept) 93.565854 6.072226 15.41 <2e-16 \*\*\* <2e-16 \*\*\* I(sqft^2) 0.005256 35.11 0.184519 Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' '1 Residual standard error: 92.08 on 498 degrees of freedom Multiple R-squared: 0.7122, Adjusted R-squared: 0.7117 F-statistic: 1233 on 1 and 498 DF, p-value: < 2.2e-16 Quadratic Regression with Tangent Line at sqft = 20 1500



homoscedasticity assumption may be violated. Residuals from Linear Model



House Size (Hundreds of Square Feet)

9. SSE (linear) = 5, 262,847 SSE (quadratic) = 4,222,356 . '. SSE (quadratic) < SSE (linear) The quadratic model has a lower SSE.

> SSE表示模型對 data 的擬合程度,SSE 越小,表示模型 的預測值和實際值越接近,誤差值越小。