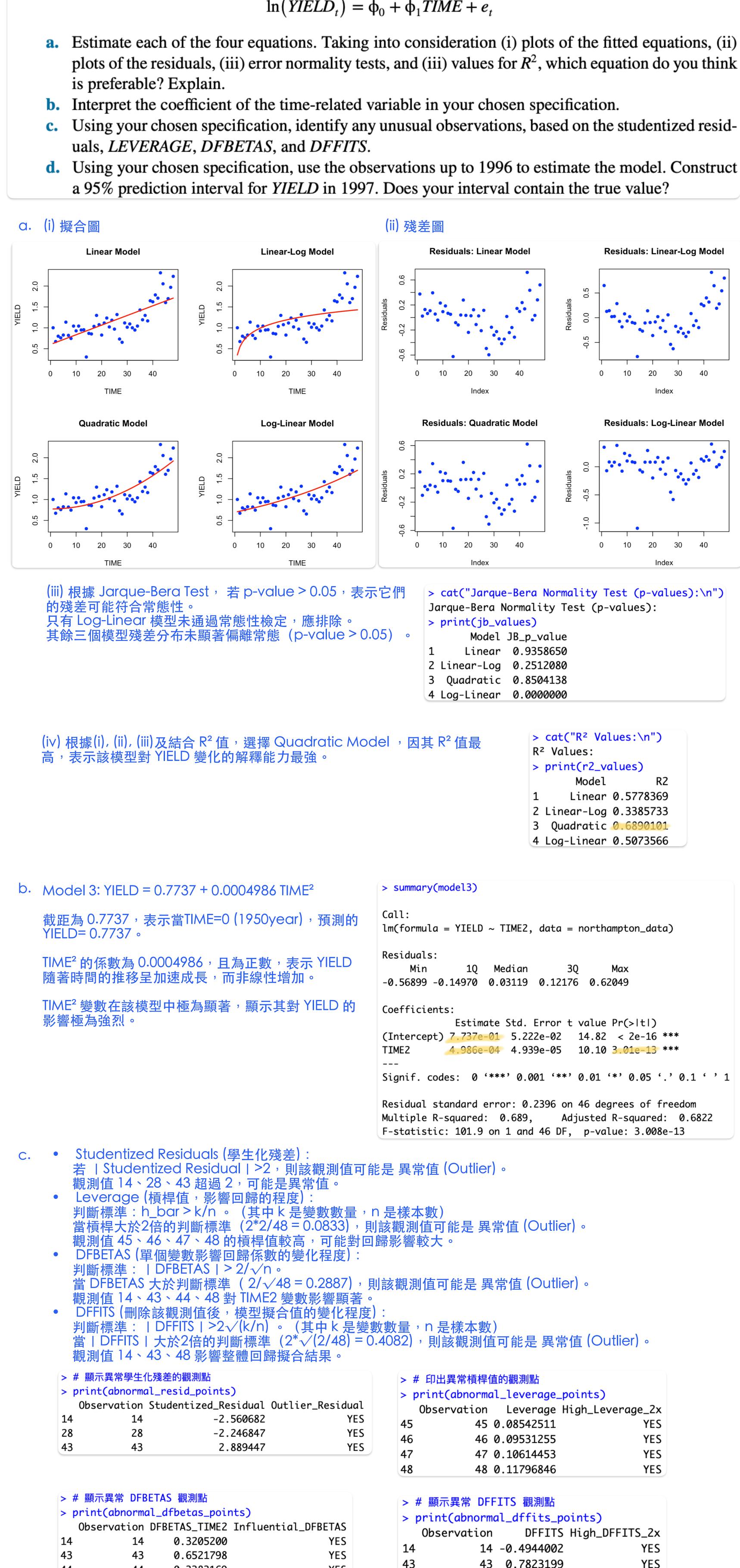
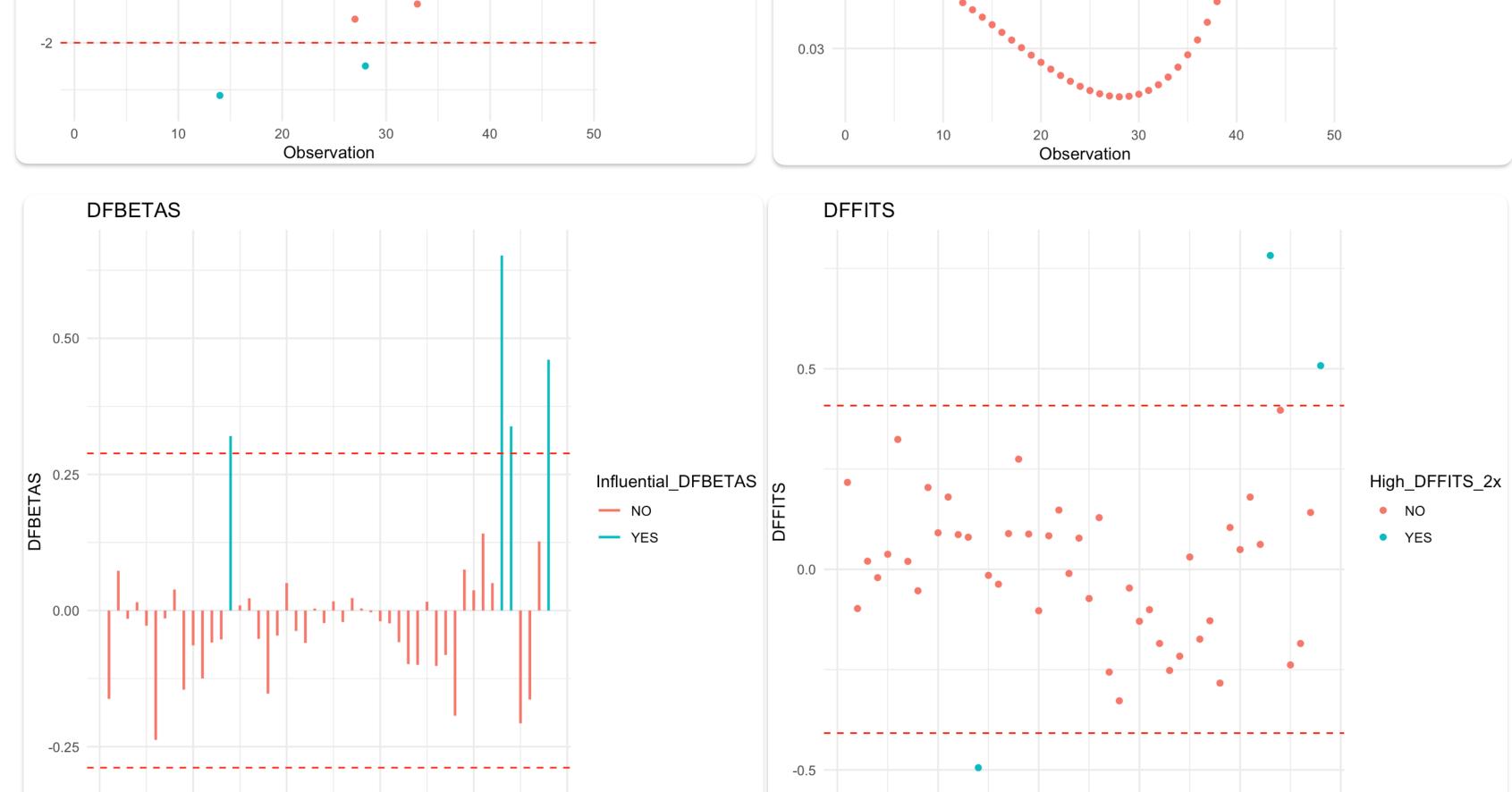
4.28 The file *wa-wheat.dat* contains observations on wheat yield in Western Australian shires. There are 48 annual observations for the years 1950–1997. For the Northampton shire, consider the following four equations:

```
YIELD_{t} = \beta_{0} + \beta_{1}TIME + e_{t}
YIELD_{t} = \alpha_{0} + \alpha_{1}\ln(TIME) + e_{t}
YIELD_{t} = \gamma_{0} + \gamma_{1}TIME^{2} + e_{t}
\ln(YIELD_{t}) = \phi_{0} + \phi_{1}TIME + e_{t}
```



```
43 0.7823199
                                                                                                                                        YES
                                                                                   43
                                 0.3383169
        44
                                                                   YES
                        44
                                                                                   48
                                                                                                     48 0.5077802
                                                                                                                                        YES
        48
                                 0.4607666
                                                                   YES
                        48
    Studentized Residuals
                                                                                      LEVERAGE
                                                                                   0.12
                                                                                   0.09
Studentized Residual
                                                                Outlier_Residual
                                                                                                                                               High Leverage 2x
                                                                                 Leverage
                                                                 NO
                                                                                                                                                NO
                                                                 YES
                                                                                                                                                YES
                                                                                   0.06
                                                                                   0.03
                10
                                                 40
                            Observation
                                                                                                             Observation
```



```
40
                                                               10
                                                                      Observation
                   Observation
d. 95%預測區間 = [1.372403, 2.389819]
   1997年的真實值 = 2.2318
   1997 年的真實值落在 95% 預測區間內 (1.372403 ≤ 2.2318 ≤ 2.389819),表示模型對該年度的預測是合理的。
   > # 計算 95% 預測區間
   > prediction_1997 <- predict(model_restricted, newdata = new_data_1997, interval =
    "prediction", level = 0.95)
    > print(prediction_1997) # 顯示預測結果
          fit
                  lwr
                          upr
    1 1.881111 1.372403 2.389819
   > # 檢查 1997 年的真實值是否落在預測區間內
   > true_value_1997 <- northampton_data$YIELD[northampton_data$TIME == 48]</pre>
   > cat("1997 年的真實值:", true_value_1997, "\n")
    1997 年的真實值: 2.2318
```