d. To estimate the parameters of the reduced-form equation for y2 using the method of moments (MOM), which was introduced in Section 10.3, the two moment equations are  $N^{-1}\sum x_{ij}(y_2 - \pi_1x_{ij} - \pi_2x_{i2}) = 0$  $N^{-1}\sum x_{i2}(y_2 - \pi_1x_{i1} - \pi_2x_{i2}) = 0$ Explain why these two moment conditions are a valid basis for obtaining consistent estimators of

e. Are the MOM estimators in part (d) the same as the OLS estimators? Form the sum of squared that they are equivalent to the two equations in part (d).

errors function for  $y_2 = \pi_1 x_1 + \pi_2 x_2 + v_2$  and find the first derivatives. Set these to zero and show f. Using  $\sum x_{i1}^2 = 1$ ,  $\sum x_{i2}^2 = 1$ ,  $\sum x_{i1}x_{i2} = 0$ ,  $\sum x_{i1}y_{1i} = 2$ ,  $\sum x_{i1}y_{2i} = 3$ ,  $\sum x_{i2}y_{1i} = 3$ ,  $\sum x_{i2}y_{2i} = 4$ ,

and the two moment conditions in part (d) show that the MOM/OLS estimates of  $\pi_1$  and  $\pi_2$  are g. The fitted value  $\hat{y}_2 = \hat{\pi}_1 x_1 + \hat{\pi}_2 x_2$ . Explain why we can use the moment condition  $\sum \hat{y}_{i2}(y_{i1} - \alpha_1 y_{i2}) = 0$  as a valid basis for consistently estimating  $\alpha_1$ . Obtain the IV estimate

h. Find the 2SLS estimate of  $\alpha_1$  by applying OLS to  $y_1 = \alpha_1 \hat{y}_2 + e_1^*$ . Compare your answer to that in

are exougenous.

f. moment conditions .

d. These moment conditions arise from the assumptions that the X's

1) E(X71 VII (X) = E(X12 VIZ (X) =0

reduced form error T3 uncorrelated with X

e. 35(T1,Th/y,x) - 25(y=Thx1-Thx2)x1=0

N = 5x11 ( Y2 - TL1 X11 - TL2 X12) = 0

N = Xi> ( Y2-TUXII-TUZXI2)=0

> IXII YI2- TI IXII -TI = IXIIXI2 =0

3-8,=0=1 21=3

4-92=04 92=4

5 x12 x11 - x11 xx1 11 - x12 = 0

35 (TI, TIZ14,X) = 25 ( y2-TI, X1-TOZ /2) /2-0

91: 1-112 x1+ 1-1/2+ d>e1+e2 = TV1x1+TI2x2+V=

= E[Xik[ dzel+ex ] |x] = E[(1-didz) xikex |x] + E[dz / (1-didz) xikex |x] = 0+0

g. y1=21y=e1 E[(T(1x1+T(2x2)e1)x)= E[(T(1x1+T(2x2)(y-d,y2))x]=0 N I (TIXTI + TI>XT>)(YII-dy)>)=0 In large samples the consistent estimators converge to true parameter values pilm ? = Ti, pilm ? 2 Th ) I(R1X11+R1X12)(YT1-21Y12) = IPi2(Y11-21Y12) =0 I gizyil - 2, Igizyil = 0 = II . Iv: Igizyil Igizyil 21. IV: I (P1 xi1+ P2xi2) Yil = P2 IXi1Yil + P2 IXi2Yil 1P I Yî = I Yî ( 12- V2) = I Yî , 12- I Yî vî = I Yî , 13. I 912 012 = I (8, 1/1 + 82 xiz) R2 = 8, IX71 P2 +8, IX12 P2 = 0 S IXII G , I XILVIL SO

Demand:  $Q_i = \alpha_1 + \alpha_2 P_i + e_{di}$ , Supply:  $Q_i = \beta_1 + \beta_2 P_i + \beta_3 W_i + e_{si}$ 

where Q is the quantity, P is the price, and W is the wage rate, which is assumed exogenous. Data on these variables are in Table 11.7.

TABLI	11.7	Data for Exercise 11.16
Q		W
4	2	2
6	4	3
9	3	1
3	5	1
8	8	3

- a. Derive the algebraic form of the reduced-form equations,  $Q = \theta_1 + \theta_2 W + \nu_2$  and  $P = \pi_1 + \pi_5 W + \nu_1$ , expressing the reduced-form parameters in terms of the structural parameters.

  b. Which structural parameters can you solve for from the results in part (a)? Which equation is
- "identified"?

  c. The estimated reduced-form equations are  $\hat{Q} = 5 + 0.5W$  and  $\hat{P} = 2.4 + 1W$ . Solve for the identified structural parameters. This is the method of indirect least squares.
- tified structural parameters. This is the method of **indirect least squares**. **d.** Obtain the fitted values from the reduced-form equation for *P*, and apply 2SLS to obtain estimates

Q2: 42. Th

G1: 
$$5$$
 $0 \rightarrow 2 \times 5$ 
 $0 \rightarrow 3 \rightarrow 3$ 
 $0 \rightarrow 3 \rightarrow$ 

C. Q: 5+0.5 W Th Th

d. first - stage -Second Stuge : d2= 1 P= 24+1W þi 44 ρî o. abla5.4 4.4 3-4 5.4 d1= To. d2. Pi 6- 6.5 x4.4 544 3 544 PF = 4.4 Q -Q = 3.8 + 0.5 P 25L5: 11.17 Example 11.3 introduces Klein's Model I. a. Do we have an adequate number of IVs to estimate each equation? Check the necessary condition for the identification of each equation. The necessary condition for identification is that in a system of M equations at least M-1 variables must be omitted from each equation. b. An equivalent identification condition is that the number of excluded exogenous variables from the equation must be at least as large as the number of included right-hand side endogenous variables. Check that this condition is satisfied for each equation. c. Write down in econometric notation the first-stage equation, the reduced form, for W., wages of workers earned in the private sector. Call the parameters  $\pi_1, \pi_2,...$ d. Describe the two regression steps of 2SLS estimation of the consumption function. This is not a question about a computer software command. e. Does following the steps in part (d) produce regression results that are identical to the 2SLS estimates provided by software specifically designed for 2SLS estimation? In particular, will the t-values be the same? There are Mc & equations requiring ) omitted variables in each equation There is a total of 16 variables in the system. The consumption equation includes 6 variable and omit 10. The necessary condition is sutisfied, investment equation includes 5 variable and omit 11. The necessary condition is satisfied. The private sector mage equation includes 5 variables and omit 11necessary condition is sutisfied. consumption equation has 2PHS endogenous variables and exclude 5 exougenous variables. The investment and private mage equitions have 1 PHS andogenous variable and omit 5 exogenous variables.

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