10.2 The labor supply of married women has been a subject of a great deal of economic research. Consider the following supply equation specification

 $HOURS = \beta_1 + \beta_2 WAGE + \beta_3 EDUC + \beta_4 AGE + \beta_5 KIDSL6 + \beta_6 NWIFEINC + e$

where *HOURS* is the supply of labor, *WAGE* is hourly wage, *EDUC* is years of education, *KIDSL6* is the number of children in the household who are less than 6 years old, and *NWIFEINC* is household income from sources other than the wife's employment.

- a. Discuss the signs you expect for each of the coefficients.
- b. Explain why this supply equation cannot be consistently estimated by OLS regression.
 c. Suppose we consider the woman's labor market experience EXPER and its square, EXPER², to be
- c. Suppose we consider the woman's labor market experience *EXPER* and its square, *EXPER*², to the instruments for *WAGE*. Explain how these variables satisfy the logic of instrumental variables.
- d. Is the supply equation identified? Explain.e. Describe the steps [not a computer command] you would take to obtain IV/2SLS estimates.

B4:不一定,因各個年龄顾氖多哭芳勒市场的数可能不一致

Bb·一,有non-wife income 1支,可能更加wied nomen IT系原附低 b-田WAGE是为生變數,可能與決差項相關、了多Ability等未納入

迎转换型的复数可能易等 WAGE & HOURS *

C. 国 EXPER LEXPER 學 WAGE 有相附性, PP EXPERT, WAGE 敬端越多。 且 EXPER、EXPER 不管直接 勢等 Hours, 只象键由WAGE 問接處生勢等

因此 EXPER. EXPER 是好的工具變數,(且COV(EXPER, ei)=0、

COV(EXPER2, ei) =0)

d.

因 NAGE 是 的 生變數,工具變數有 EXPER、EXPER 因 2>1,因 比 Snpply equation 是 identified

电、省先是选定工具變數,即EXPER、EXPERT 接著對 WAGE 迴歸

) WAGE= BU+BIEXPER+BZEXPER+BZEDUC+...+U

HOWYS = BUT BIWAGE + BZEDUC + 1 + Q

- 10.3 In the regression model $y = \beta_1 + \beta_2 x + e$, assume x is endogenous and that z is a valid instrument. In Section 10.3.5, we saw that $\beta_2 = \text{cov}(z, y)/\text{cov}(z, x)$. a. Divide the denominator of $\beta_2 = \frac{\cot(z, y)}{\cot(z, x)}$ by $\frac{\cot(z, x)}{\cot(z, x)}$ is the coefficient of the simple regression with dependent variable x and explanatory variable z, $x = \gamma_1 + \theta_1 z + v$. [Hint: See Section 10.2.1.] Note that this is the first-stage equation in two-stage
 - **b.** Divide the numerator of $\beta_2 = \text{cov}(z, y)/\text{cov}(z, x)$ by var(z). Show that cov(z, y)/var(z) is the coefficient of a simple regression with dependent variable y and explanatory variable z, $y = \pi_0 + \pi_1 z + u$. [Hint: See Section 10.2.1.] c. In the model $y = \beta_1 + \beta_2 x + e$, substitute for x using $x = \gamma_1 + \theta_1 z + v$ and simplify to obtain $y = \pi_0 + \pi_1 z + u$. What are π_0 , π_1 , and u in terms of the regression model parameters and error and the first-stage parameters and error? The regression you have obtained is a reduced-form
 - **d.** Show that $\beta_2 = \pi_1/\theta_1$.
 - e. If $\hat{\pi}_1$ and $\hat{\theta}_1$ are the OLS estimators of π_1 and θ_1 , show that $\hat{\beta}_2 = \hat{\pi}_1/\hat{\theta}_1$ is a consistent estimator of $\beta_2 = \pi_1/\theta_1$. The estimator $\hat{\beta}_2 = \hat{\pi}_1/\hat{\theta}_1$ is an **indirect least squares** estimator.

$$\pi_{l} = \frac{E(Z - E(Z))(Y - E(Y))}{E(Z - E(Z))} \cdot \frac{cov(Z, Y)}{Var(Z)}$$

A

C.
$$y_{1} = \beta_{1} + \beta_{2} + \gamma_{1} + e_{1} = \beta_{1} + \beta_{2} + \gamma_{1} + e_{1} = \gamma_{1} + \gamma_{2} + e_{1} = \gamma_{1} + \beta_{2} + \gamma_{1} + e_{2} + e_{2} + e_{2} = \gamma_{1} + \gamma_{1} + e_{2} + e_{2} = \gamma_{1} + \gamma_{1} + e_{2} + e_{2} = \gamma_{1} + e_{2} + e_{2} = \gamma_{1} + e_{2} = \gamma_{2} = \gamma$$

$$\frac{1}{\left(\frac{1}{2}\right)^{2}} = \frac{\left(\frac{1}{2}\right)^{2}}{\left(\frac{1}{2}\right)^{2}} = \frac{\sum_{i=1}^{2}}{\sum_{i=1}^{2}} \left(\frac{1}{2}\right)^{2}$$

= (ov (3,4)

$$\frac{\partial I}{\partial x} = \frac{\cos(3x)}{\cos(3x)} = \frac{\sum (3x)}{\sum (3x)}$$

$$\widehat{T}_{N} = \frac{\widehat{(av(z,y))}}{\widehat{(av(z))}} = \frac{\sum (\overline{z}_{1} - \overline{z}_{2})(\gamma_{1} - \overline{\gamma})/N}{\sum (\overline{z}_{1} - \overline{z}_{2})^{2}} = \frac{\sum (\overline{z}_{1} - \overline{z}_{2})(\gamma_{1} - \overline{\gamma})}{\sum (\overline{z}_{1} - \overline{z}_{2})^{2}}$$

$$\frac{\widehat{\beta}_{2}}{\widehat{\theta}_{1}} = \frac{\underline{\Gamma(\overline{z}_{1} - \overline{z}_{1})(\overline{y}_{1} - \overline{y}_{1})}}{\underline{\Gamma(\overline{z}_{1} - \overline{z}_{1})}} = \frac{\underline{\Gamma(\overline{z}_{1} - \overline{z}_{1})(\overline{y}_{1} - \overline{y}_{1})}}{\underline{\Gamma(\overline{z}_{1} - \overline{z}_{1})(\overline{y}_{1} - \overline{y}_{1})}} = \frac{\underline{\Gamma(\overline{z}_{1} - \overline{z}_{1})(\overline{y}_{1} - \overline{y}_{1})}}{\underline{\Gamma(\overline{z}_{1} - \overline{z}_{1})(\overline{y}_{1} - \overline{y}_{1})}} = \frac{\underline{\Gamma(\overline{z}_{1} - \overline{z}_{1})(\overline{y}_{1} - \overline{y}_{1})}}{\underline{\Gamma(\overline{z}_{1} - \overline{z}_{1})(\overline{y}_{1} - \overline{y}_{1})}} = \frac{\underline{\Gamma(\overline{z}_{1} - \overline{z}_{1})(\overline{y}_{1} - \overline{y}_{1})}}{\underline{\Gamma(\overline{z}_{1} - \overline{z}_{1})(\overline{y}_{1} - \overline{y}_{1})}} = \frac{\underline{\Gamma(\overline{z}_{1} - \overline{z}_{1})(\overline{y}_{1} - \overline{y}_{1})}}{\underline{\Gamma(\overline{z}_{1} - \overline{z}_{1})(\overline{y}_{1} - \overline{y}_{1})}} = \frac{\underline{\Gamma(\overline{z}_{1} - \overline{z}_{1})(\overline{y}_{1} - \overline{y}_{1})}}{\underline{\Gamma(\overline{z}_{1} - \overline{z}_{1})(\overline{y}_{1} - \overline{y}_{1})}} = \frac{\underline{\Gamma(\overline{z}_{1} - \overline{z}_{1})(\overline{y}_{1} - \overline{y}_{1})}}{\underline{\Gamma(\overline{z}_{1} - \overline{z}_{1})(\overline{y}_{1} - \overline{y}_{1})}} = \frac{\underline{\Gamma(\overline{z}_{1} - \overline{z}_{1})(\overline{y}_{1} - \overline{y}_{1})}}{\underline{\Gamma(\overline{z}_{1} - \overline{z}_{1})(\overline{y}_{1} - \overline{y}_{1})}}$$

 $\beta_{2} = \frac{c_{V}}{6_{1}} = \frac{c_{OV}(\overline{z}, Y)}{c_{OV}(\overline{z}, Y)} = \beta_{2}$