

$$WAGE = \beta_1 + \beta_2 EDUC + \beta_3 EXPER + \beta_4 METRO + e_i$$

$N = 1,000$ . WAGE in \$/hr.

a.

$$n_m = 577 \quad n_f = 423$$

$$\textcircled{1} H_0: \sigma_m^2 = \sigma_f^2 \quad SSE_M = 97161.9174, \quad df_m = 577 - 4 = 573$$

$$H_a: \sigma_m^2 \neq \sigma_f^2 \quad \hat{\sigma}_f^2 = 12,024, \quad df_w = 423 - 4 = 419$$

$$MSE_M \rightarrow \hat{\sigma}_m^2 = \frac{97161.9174}{573} = 169.57$$

$$\hat{\sigma}_f^2 = 1445766.$$

$$F_0 = \frac{\hat{\sigma}_m^2}{\hat{\sigma}_f^2} = 1.17, \quad RR \in \left\{ F \geq F_{\alpha/25}^{1.2/111}(573, 419), F \leq F_{\alpha/25}^{1.2/111}(573, 419) \right\}$$

$F_0 = 1.17 < 1.2 \Rightarrow$  don't reject  $H_0 \Rightarrow$  男女間的工資未存在異質 1hr.



b. Model:  $WAGE = \beta_1 + \beta_2 EDUC + \beta_3 EXPER + \beta_4 METRO + \beta_5 FEMALE + e_i$

$N_S = 400$

$SSE_S = 56231.0382$

$N_M = 600$

$SSE_M = 100703.0471$

$\alpha = 0.05$

$H_0: \sigma_{single}^2 = \sigma_{married}^2$

①

②  $\alpha = 0.05$

$H_a: \sigma_{single}^2 < \sigma_{married}^2$

③ Test statistic:  $F_0 = \frac{\hat{\sigma}_M^2}{\hat{\sigma}_S^2} \sim F_{1,0.05} (600-5, 400-5)$

④  $RR \leftarrow \{ F_0 > F_{0.05} (595, 395), F \leq F_{0.975} (595, 395) \}$

⑤  $F_0 = \frac{\left( \frac{SSE_M}{595} \right)}{\left( \frac{SSE_S}{395} \right)} = 1.19$   $\hookrightarrow 1.2$

⑥ 未存在異質變異.



c.

$$NR \text{ test statistic} = nR^2 = 59.03 \sim \chi^2(2)$$

(只檢查 FEMALE & MARRIED)

$$\chi^2_{0.05}(2) = 5.99$$

$59.03 > 5.99 \Rightarrow \text{reject } H_0$ , 此 2 變數與異質變異數  
高度相關

此輔助迴歸並未將 Married 納入, 無法回答 b 題

d.

$$4 + 4 + \binom{4}{2} = 4 + 4 + 6 = 14 \text{ (df)}$$

$$\chi^2_{0.05}(14) \sim nR^2$$

11  
23.9

$78.82 > 23.9 \Rightarrow \text{Reject } H_0$ , 存在異質變異數



e. 誰的 SE 大, 誰的 CI 寬

Wider: EDUC,

Narrower: EXPER, METERO, FEMALE

} 不一致.

f.

(b) 的模型中並未發現已婚 or 未婚存在異質變異數

而在 (f) 中, 加入主迴歸後  $t_0 = 1 < 1.96$ ,

表示結婚 or 未婚並無顯著差異

兩者並不矛盾