

## 1. APPENDIX A

To estimate the travelling area of each detected nearby vehicle, the position relations between the real position of the target vehicle and its nearby vehicles are firstly provided. Given an assumed real position  $P_T^i = [X(T_i), Y(T_i)]$  of the target vehicle  $T_i$ . Then, the real position  $P_N^{ij} = [X(N_i^j), Y(N_i^j)]$  of the nearby vehicle  $N_i^j$  can be expressed as:

$$(1.1) \quad \begin{aligned} X(N_i^j) &= X(T_i) + PD(T_i, N_i^j)_X \\ &= X(T_i) + d(T_i, N_i^j) \cos(a(T_i, N_i^j)), \end{aligned}$$

$$(1.2) \quad \begin{aligned} Y(N_i^j) &= Y(T_i) + PD(T_i, N_i^j)_Y \\ &= Y(T_i) + d(T_i, N_i^j) \sin(a(T_i, N_i^j)), \end{aligned}$$

where  $[PD(T_i, N_i^j)_X, PD(T_i, N_i^j)_Y]$  is the *real position difference* ( $PD$ ) between the target vehicle  $T_i$  and nearby vehicle  $N_i^j$

The real position difference between the target vehicle  $T_i$  and nearby vehicle  $N_i^j$  can be expressed as:

$$(1.3) \quad \begin{aligned} PD(T_i, N_i^j)_X &= [\hat{d}(T_i, N_i^j) - \varepsilon_d] \cos(\hat{a}(T_i, N_i^j) - \varepsilon_a), \\ PD(T_i, N_i^j)_Y &= [\hat{d}(T_i, N_i^j) - \varepsilon_d] \sin(\hat{a}(T_i, N_i^j) - \varepsilon_a), \end{aligned}$$

where  $\varepsilon_d$  and  $\varepsilon_a$  are the measurement errors of relative distance and bearing angle, and  $\varepsilon_d$  and  $\varepsilon_a$  follow Gaussian distributions with the standard deviations  $\rho$  and  $\omega$  respectively.

Eq. 1.3 can be approximately estimated using the 1<sup>st</sup> Taylor expansion as follows:

$$(1.4) \quad \begin{aligned} PD(T_i, N_i^j)_X &\approx \hat{d}(T_i, N_i^j) \cos(\hat{a}(T_i, N_i^j)) + \varepsilon_x^{PD} \\ &= \hat{P}D(T_i, N_i^j)_X + \varepsilon_x^{PD}, \\ PD(T_i, N_i^j)_Y &\approx \hat{d}(T_i, N_i^j) \sin(\hat{a}(T_i, N_i^j)) + \varepsilon_y^{PD} \\ &= \hat{P}D(T_i, N_i^j)_Y + \varepsilon_y^{PD}, \end{aligned}$$

where  $\varepsilon_x^{PD}$  and  $\varepsilon_y^{PD}$  are the estimated errors of the measured position difference in order to offset the measurement errors of relative positions.  $\varepsilon_x^{PD}$  and  $\varepsilon_y^{PD}$  are determined as follows:

$$(1.5) \quad \begin{aligned} \varepsilon_x^{PD} &= -\varepsilon_d \cos(\hat{a}(T_i, N_i^j)) + \varepsilon_a \hat{d}(T_i, N_i^j) \sin(\hat{a}(T_i, N_i^j)), \\ \varepsilon_y^{PD} &= -\varepsilon_d \sin(\hat{a}(T_i, N_i^j)) - \varepsilon_a \hat{d}(T_i, N_i^j) \cos(\hat{a}(T_i, N_i^j)), \end{aligned}$$

According to Trigonometric Equations, Eq. 1.5 can be expressed as:

$$(1.6) \quad \begin{aligned} \varepsilon_x^{PD} &= R \cos(\hat{a}(T_i, N_i^j) + \alpha), \\ \varepsilon_y^{PD} &= -R \sin(\hat{a}(T_i, N_i^j) + \alpha), \end{aligned}$$

where

$$(1.7) \quad \begin{aligned} R &= \sqrt{(-\varepsilon_d)^2 + (\varepsilon_a \hat{d}(T_i, N_i^j))^2}, \\ \alpha &= \tan^{-1} \left( \frac{\varepsilon_a \hat{d}(T_i, N_i^j)}{\varepsilon_d} \right). \end{aligned}$$

## 2. APPENDIX B

To determine the probability density function (PDF) of displacement difference in terms of the real position of the target vehicle, the displacement of the target vehicle in terms of the real position is determined as:

$$(2.1) \quad \text{Vec}(P_T^i \rightarrow \hat{P}_T^i) = \hat{P}_T^i - P_T^i,$$

where  $\hat{P}_T^i$  is the GPS position of the target vehicle  $T_i$  and  $P_T^i$  is the real position of the target vehicle.

Similarly the displacement of the nearby vehicle  $N_i^j$  in terms of real position is determined as follows:

$$(2.2) \quad \text{Vec}(P_N^{ij} \rightarrow \hat{P}_N^{ij}) = \hat{P}_N^{ij} - P_N^{ij},$$

where  $P_N^{ij}$  and  $\hat{P}_N^{ij}$  are the real position and GPS position of the nearby vehicle  $N_i^j$ .

As the accuracy of GPS measurements depends on the quality of the pseudorange measurement between the satellites and GPS receivers with the consideration of common error sources (e.g., atmospheric delay, satellite clock and ephemeris errors, etc.), and uncommon error sources (e.g., the noise of GPS receivers). When vehicles are driving in a vicinity, these vehicles are assumed to have the GNSS data coming from the same constellation of satellites. However, as non-common errors vary from vehicle to vehicle, the bias in GPS positioning caused by uncommon errors is usually modelled following an vehicle-dependent zero-mean Gaussian distribution.

Therefore, given the target vehicle  $T_i$ , the measured GPS position of the target vehicle  $T_i$  can be formulated as:

$$(2.3) \quad \hat{P}_T^i = P_T^i + B_T^i + NB_T^i,$$

where  $P_T^i$  represents the real position of  $T_i$ ,  $B_T^i$  represents the position bias caused by common errors, and  $NB_T^i$  denotes the position bias caused by non-common errors.  $NB_T^i$  is modelled following a Gaussian distribution  $N(0, \sigma_{NB_T^i}^2)$ , where  $\sigma_{NB_T^i}$  is the standard deviation of  $NB_T^i$ .

Similarly, the measured GPS position of its  $j^{th}$  nearby vehicle  $N_i^j$  can be written as:

$$(2.4) \quad \hat{P}_N^{ij} = P_N^{ij} + B_N^{ij} + NB_N^{ij},$$

where  $P_N^{ij}$  represents the real position of  $N_i^j$ ,  $B_N^{ij}$  represents the position bias caused by common errors,  $NB_N^{ij}$  represents the position bias caused by non-common errors.  $NB_N^{ij}$  follows a Gaussian distribution  $N(0, \sigma_{NB_N^{ij}}^2)$ , where  $\sigma_{NB_N^{ij}}$  is the corresponding standard deviation of  $NB_N^{ij}$ .

As the bias caused by common error sources  $B_T^i \approx B_N^{ij}$  when the target vehicle  $T_i$  and nearby vehicle  $N_i^j$  in a vicinity. Therefore, by subtracting Eq. 2.4 from Eq. 2.3, we have:

$$(2.5) \quad \hat{P}_T^i - \hat{P}_N^{ij} \approx P_T^i - P_N^{ij} + NB_T^i - NB_N^{ij}.$$

where the difference of the GPS position of the target vehicle and nearby vehicle can be determined as the real position difference and the difference of the independent position bias caused by the uncommon errors.

Therefore, the displacement difference  $DD$  in terms of the real position of the target vehicle can be computed from Eq. 2.1, Eq. 2.2 and Eq. 2.5 as follows:

$$\begin{aligned}
 DD(T_i, N_i^j, P_T^i) &= \text{Vec}(P_T^i \rightarrow \hat{P}_T^i) - \text{Vec}(P_N^{ij} \rightarrow \hat{P}_N^{ij}) \\
 &= (\hat{P}_T^i - P_T^i) - (\hat{P}_N^{ij} - P_N^{ij}) \\
 (2.6) \quad &= (\hat{P}_T^i - \hat{P}_N^{ij}) + (P_N^{ij} - P_T^i) \\
 &\approx (NB_T^i - NB_N^{ij}).
 \end{aligned}$$

Since  $NB_T^i$  and  $NB_N^{ij}$  are assumed as independent Gaussian distributions  $N(0, \sigma_{NB_T^i}^2)$  and  $N(0, \sigma_{NB_N^{ij}}^2)$ , therefore  $(NB_T^i - NB_N^{ij})$  follows a Gaussian distribution  $N(0, \sigma_{NB_T^i}^2 + \sigma_{NB_N^{ij}}^2)$ , where  $\sigma_{NB_T^i}$  and  $\sigma_{NB_N^{ij}}$  are the standard deviations of  $NB_T^i$  and  $NB_N^{ij}$  respectively.