

한양대학교 인공지능연구실

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Introduction	

해결하려는 문제: 2 개의 도메인 간 Image-to-Image translation

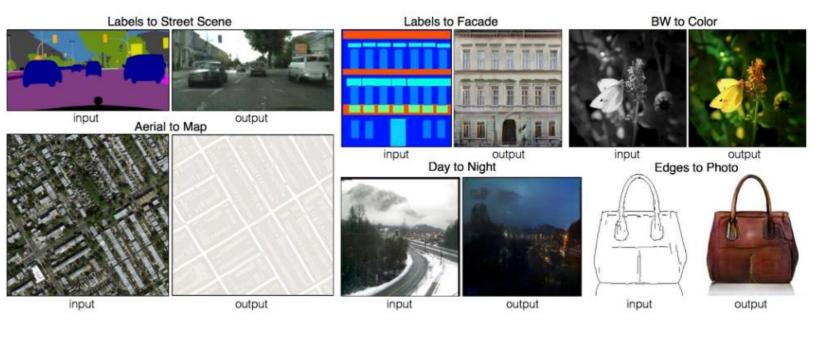


각 도메인 이미지의 pair data 가 존재하지 않음

→ Unsupervised problem!

Image-to-Image translation

"Mapping an image in one domain to a corresponding image in another domain."

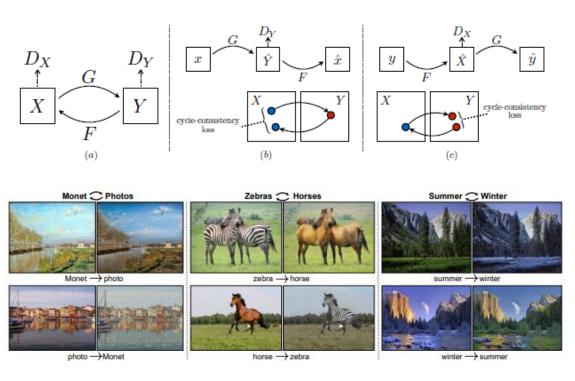


pix2pix[1]

[1]: https://arxiv.org/pdf/1611.07004.pdf

Image-to-Image translation

"Mapping an image in one domain to a corresponding image in another domain."



(b) Handbag images (input) & Generated shoe images (output)

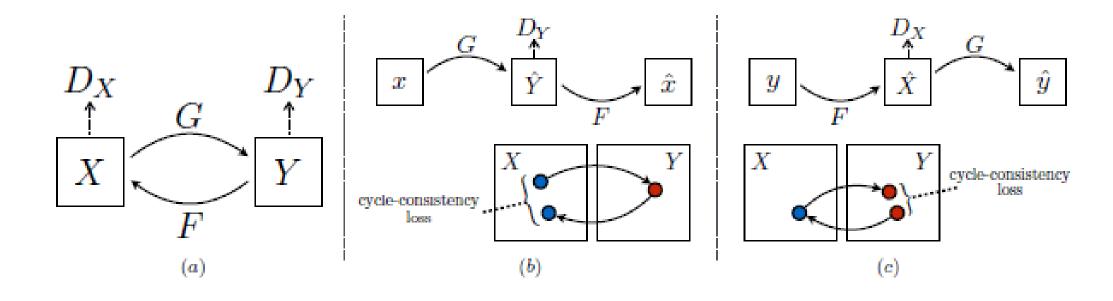
CycleGAN[2]

DiscoGAN[3]

[2]: https://arxiv.org/pdf/1703.10593v6.pdf

[3]: https://arxiv.org/pdf/1703.05192.pdf

CycleGAN 도 unpaired 이미지 변환에 대한 연구

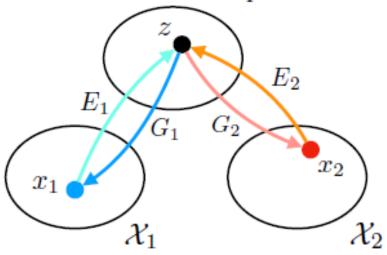


Cycle-consistency loss 이용

X 도메인 → Y 도메인 → X 도메인 으로 변환했을 때 다시 원본 이미지와 비슷해지도록

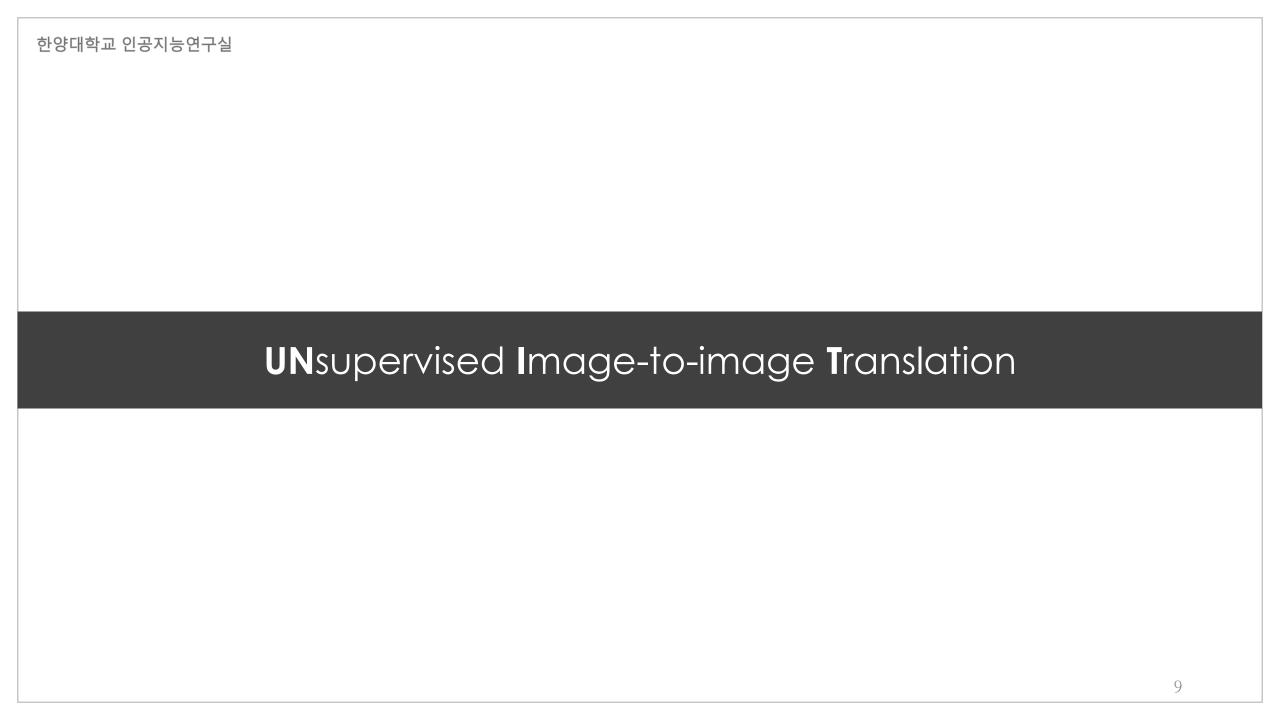
이 연구에서는 어떻게 했을까?

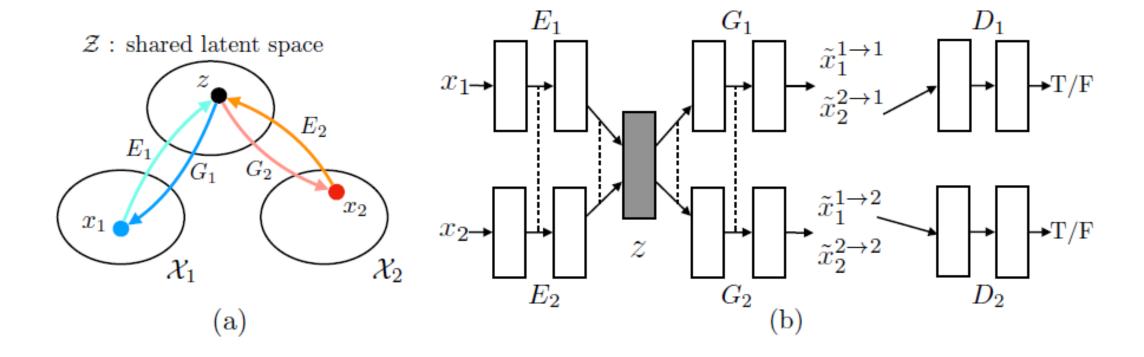
\mathcal{Z} : shared latent space

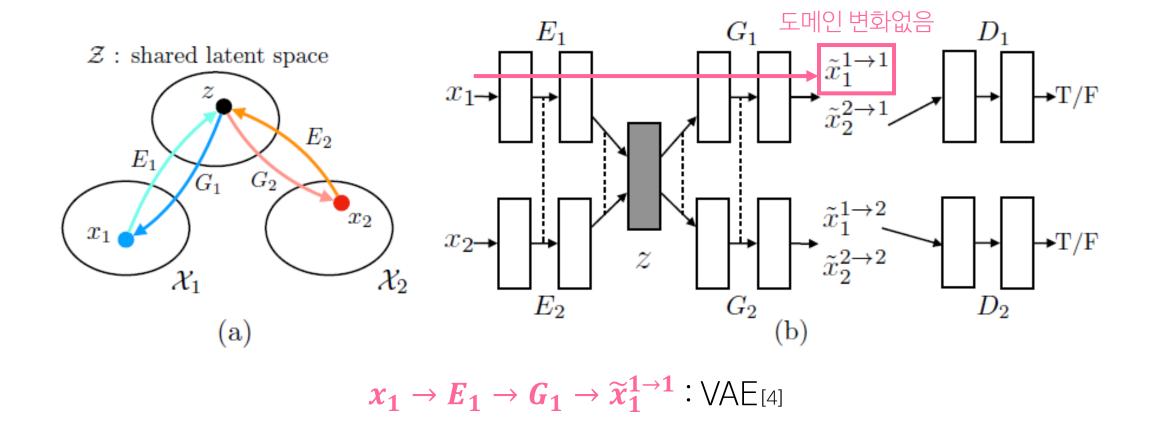


Shared latent space assumption

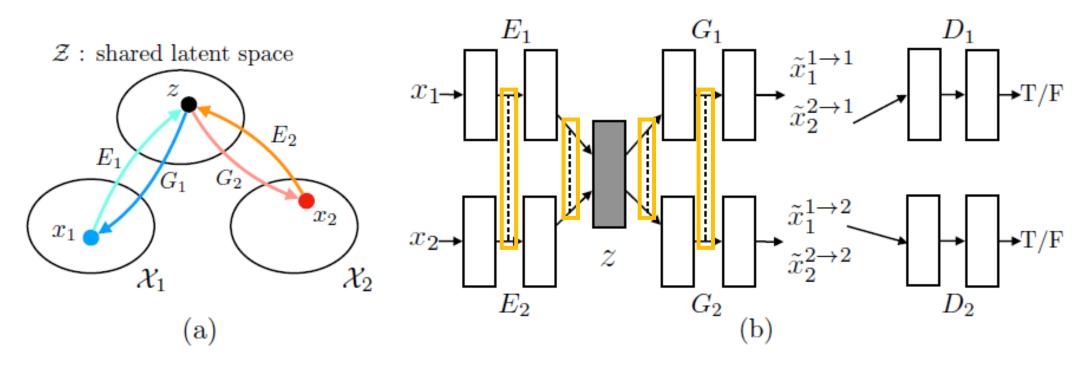
각 도메인에 대한 오토인코더(VAE) 를 학습할 때, 그 latent space 가 동일한 vector space 가 될 수 있지 않을까?





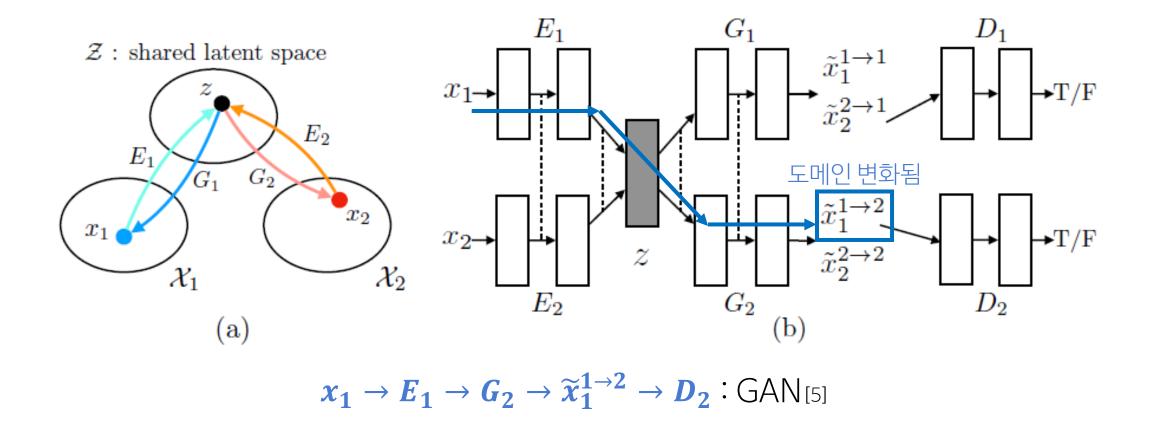


[4]: https://arxiv.org/pdf/1312.6114.pdf

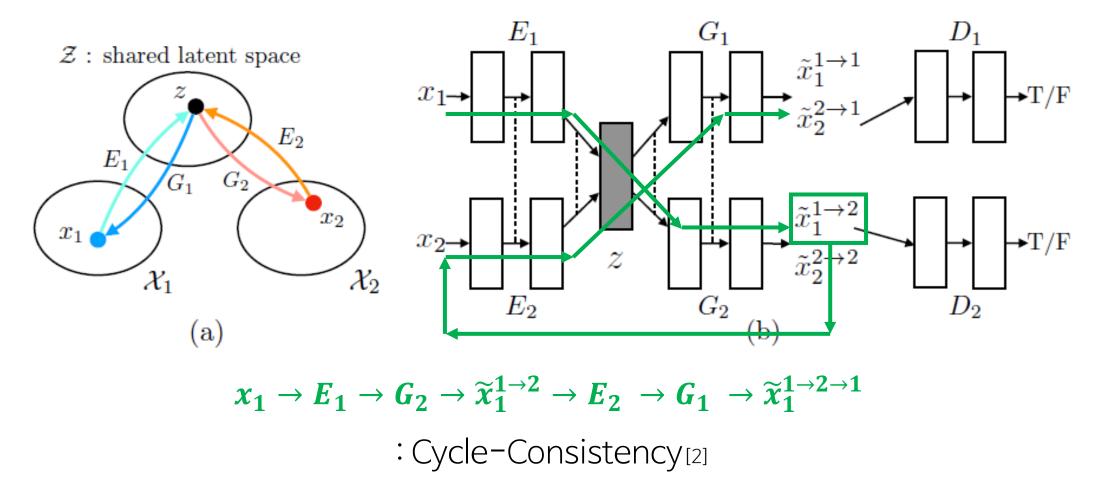


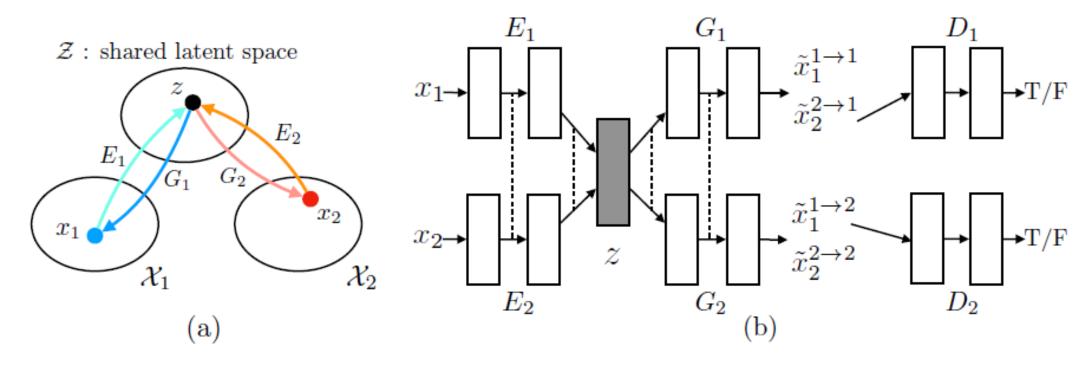
Weight sharing

각 도메인의 인코더 일부 레이어와 디코더(=generator) 일부 레이어의 weight 를 공유하여 두 도메인의 이미지가 common latent code 로 매핑되도록 함



[5]: https://papers.nips.cc/paper/5423-generative-adversarial-nets.pdf





$$\min_{E_1,E_2,G_1,G_2} \max_{D_1,D_2} \begin{array}{l} \mathcal{L}_{VAE_1}(E_1,G_1) + \mathcal{L}_{GAN_1}(E_2,G_1,D_1) + \mathcal{L}_{CC_1}(E_1,G_1,E_2,G_2) + \\ \mathcal{L}_{VAE_2}(E_2,G_2) + \mathcal{L}_{GAN_2}(E_1,G_2,D_2) + \mathcal{L}_{CC_2}(E_2,G_2,E_1,G_1) \end{array}$$

$$\mathcal{L}_{\text{VAE}_{1}}(E_{1}, G_{1}) = \lambda_{1} \text{KL}(q_{1}(z_{1}|x_{1})||p_{\eta}(z)) - \lambda_{2} \mathbb{E}_{z_{1} \sim q_{1}(z_{1}|x_{1})}[\log p_{G_{1}}(x_{1}|z_{1})]$$

$$\mathcal{L}_{\text{VAE}_{2}}(E_{2}, G_{2}) = \lambda_{1} \text{KL}(q_{2}(z_{2}|x_{2})||p_{\eta}(z)) - \lambda_{2} \mathbb{E}_{z_{2} \sim q_{2}(z_{2}|x_{2})}[\log p_{G_{2}}(x_{2}|z_{2})]$$

$$\mathcal{L}_{GAN_1}(E_1, G_1, D_1) = \lambda_0 \mathbb{E}_{x_1 \sim P_{\mathcal{X}_1}} [\log D_1(x_1)] + \lambda_0 \mathbb{E}_{z_2 \sim q_2(z_2|x_2)} [\log(1 - D_1(G_1(z_2)))]$$

$$\mathcal{L}_{GAN_2}(E_2, G_2, D_2) = \lambda_0 \mathbb{E}_{x_2 \sim P_{\mathcal{X}_2}} [\log D_2(x_2)] + \lambda_0 \mathbb{E}_{z_1 \sim q_1(z_1|x_1)} [\log(1 - D_2(G_2(z_1)))]$$

$$\mathcal{L}_{\text{CC}_{1}}(E_{1}, G_{1}, E_{2}, G_{2}) = \lambda_{3} \text{KL}(q_{1}(z_{1}|x_{1})||p_{\eta}(z)) + \lambda_{3} \text{KL}(q_{2}(z_{2}|x_{1}^{1\to2}))||p_{\eta}(z)) - \lambda_{4} \mathbb{E}_{z_{2}\sim q_{2}(z_{2}|x_{1}^{1\to2})}[\log p_{G_{1}}(x_{1}|z_{2})]$$

$$\mathcal{L}_{\text{CC}_{2}}(E_{2}, G_{2}, E_{1}, G_{1}) = \lambda_{3} \text{KL}(q_{2}(z_{2}|x_{2})||p_{\eta}(z)) + \lambda_{3} \text{KL}(q_{1}(z_{1}|x_{2}^{2\to1}))||p_{\eta}(z)) - \lambda_{4} \mathbb{E}_{z_{1}\sim q_{1}(z_{1}|x_{2}^{2\to1})}[\log p_{G_{2}}(x_{2}|z_{1})].$$

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Experiments	

Experiments

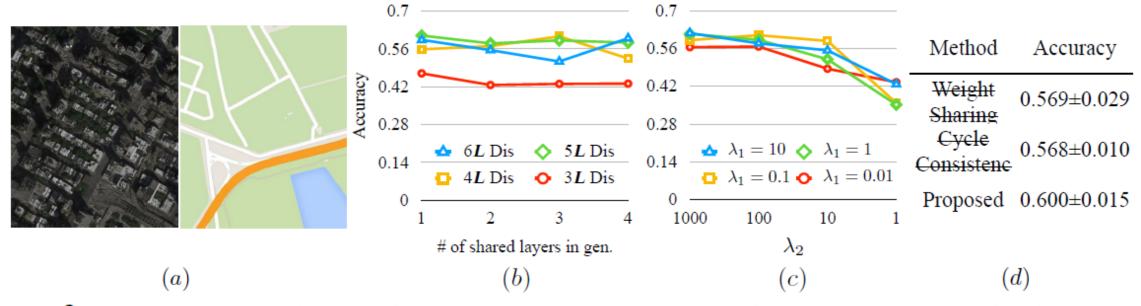


Figure 2: (a) Illustration of the Map dataset. Left: satellite image. Right: map. We translate holdout satellite images to maps and measure the accuracy achieved by various configurations of the proposed framework. (b) Translation accuracy versus different network architectures. (c) Translation accuracy versus different hyper-parameter values. (d) Impact of weight-sharing and cycle-consistency constraints on translation accuracy.

Experiments



Figure 3: Street scene image translation results. For each pair, left is input and right is the translated image.

Experiments

Figure 4: Dog breed translation results.

Input Cougar Cheetah Leopard Lion Tiger Input Leopard

| Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Cheetah Leopard | Che

Figure 5: Cat species translation results.

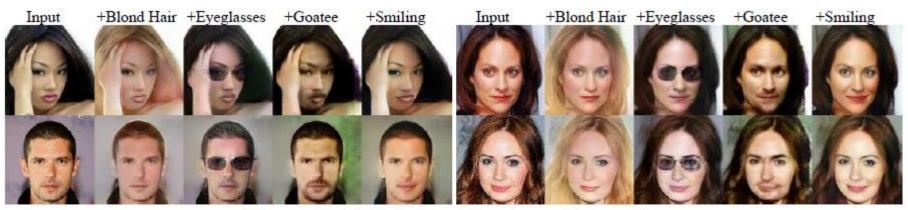
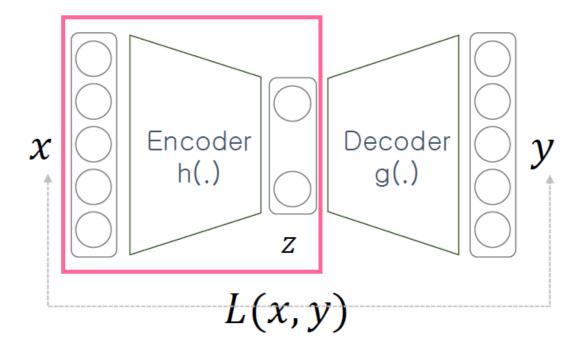


Figure 6: Attribute-based face translation results.

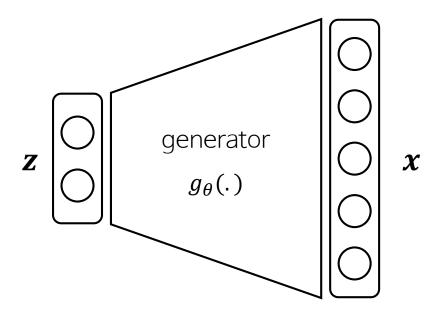
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Auto Encoder



latent code 를 잘 만들기 위해서 디코더를 붙임

VAE 는 generative model

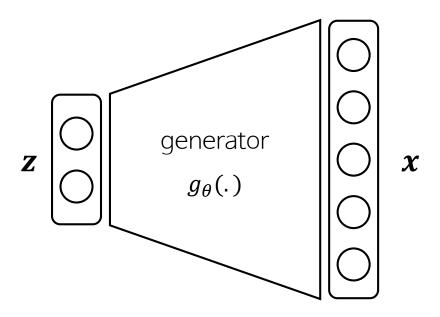


"Generative modeling" is a broad area of machine learning which deals with models of distributions P(X)

학습 데이터셋에 있는 데이터 샘플 x 와 비슷한 것을 생성하려고 함

"producing more examples that are like those already in a database, but not exactly the same."

VAE 는 generative model



We can formalize this setup by saying that we get examples X distributed according to some unknown distribution $P_{gt}(X)$, and our goal is to learn a model P which we can sample from, such that P is as similar as possible to P_{gt} .

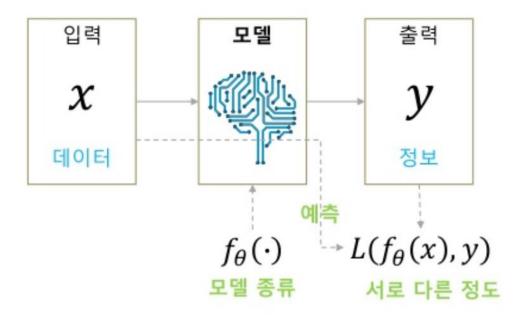
X의 실제 분포(P_{gt})를 모르니 가능한 한 비슷한 분포(P)를 학습하려고 함

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Variational AutoEncoder

네트워크 출력을 계속 "분포"라고 말하는 이유?

네트워크 출력을 Maximum likelihood 관점에서 해석.



$$\theta^* = \operatorname*{argmin}_{\theta} L(f_{\theta}(x), y)$$
 주어진 데이터를 제일 질 설명하는 모델 찾기

$$y_{new} = f_{\theta^*}(x_{new})$$

고정 입력, 고정 출력

네트워크 출력에서 우리가 원하는 y 가 나올 확률(likelihood)이 높아지기(maximum)를 원함

가우시안이라고 가정하면 네트워크 출력값을 **가우시안의 평균값**으로 해석

입력 모델 출력 x데이터 정보 $f_{\theta_1}(x)$ $T_{\theta_2}(x)$ $p(y|f_{\theta_1 2}(x)) < p(y|f_{\theta_1}(x))$

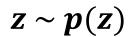
이 관점에서는 y 에 대한 확률 분포가 무슨 모델인지 미리 정함 (가우시안, 베르누이 등)

Loss 에 log 가 붙은 이유는 Backpropagation 알고리즘을 적용하기 위한 조건에 맞추려고

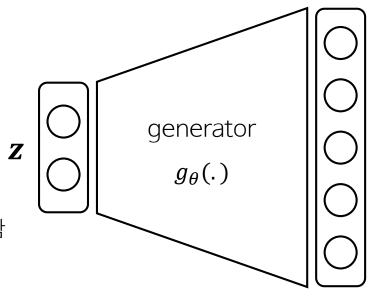
$$\theta^* = \underset{\theta}{\operatorname{argmin}} [-\log(p(y|f_{\theta}(x)))]^{주어진 데이터를 제일 질 설명하는 모델 찾기}$$

 $y_{new} \sim p(y|f_{\theta^*}(x_{new}))$

고정 입력, 고정/다른 출력



z의 확률분포는 다루기 쉬운 확률 분포 중 선택함
Normal / Uniform distribution



모든 training dataset에 대한 확률

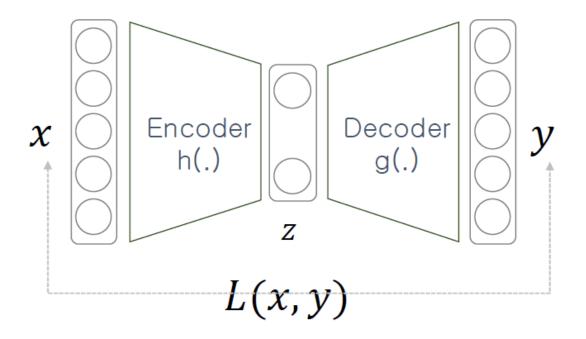
$$p(x) = \int p(x|g_{\theta}(z))p(z)dz$$
$$\approx \sum_{i} p(x|g_{\theta}(z_{i}))p(z_{i})$$

 $p(x|g_{\theta}(z))$

g 가 z 라는 random variable 을 입력 받아 X 를 잘 만들어낼 확률을 높이도록 네트워크 파라미터 θ 를 조정

Manifold 가정

: 고차원의 벡터를 저차원으로 표현할 수 있다는 가정



오토인코더 구조에서는 z 를 latent vector 로 보고 manifold 상에 존재하는 것으로 해석하는데, 이 z의 분포를 단순한 normal distribution 이라고 가정하면 문제가 되지 않을까?

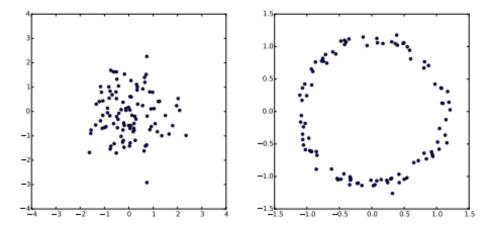
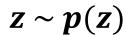


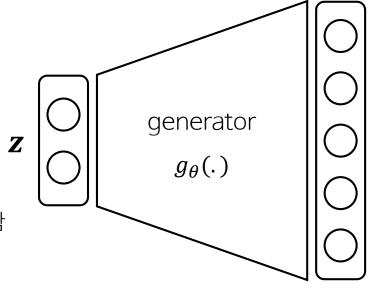
Figure 2: Given a random variable z with one distribution, we can create another random variable X=g(z) with a completely different distribution. Left: samples from a gaussian distribution. Right: those same samples mapped through the function g(z)=z/10+z/||z|| to form a ring. This is the strategy that VAEs use to create arbitrary distributions: the deterministic function g is learned from data.

Generator 가 여러 개의 레이어를 가진 경우 처음 몇 개의 레이어가 latent space 로의 매핑을 수행해주고 나머지 레이어들이 그 latent vector 에 해당하는 이미지를 생성하게 된다고 함



z의 확률분포는 다루기 쉬운 확률 분포 중 선택함

Normal / Uniform distribution



모든 training dataset에 대한 확률

$$p(x) = \int p(x|g_{\theta}(z))p(z)dz$$
$$\approx \sum_{i} p(x|g_{\theta}(z_{i}))p(z_{i})$$

 $p(x|g_{\theta}(z))$

g 가 z 라는 random variable 을 입력 받아 X 를 잘 만들어낼 확률을 높이도록 네트워크 파라미터 θ 를 조정



Figure 3: It's hard to measure the likelihood of images under a model using only sampling. Given an image *X* (a), the middle sample (b) is much closer in Euclidean distance than the one on the right (c). Because pixel distance is so different from perceptual distance, a sample needs to be extremely close in pixel distance to a datapoint *X* before it can be considered evidence that *X* is likely under the model.

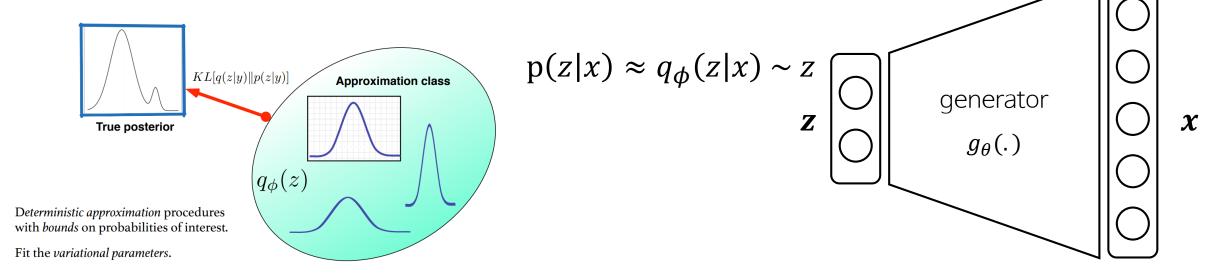
네트워크 출력에 대한 확률 모델을 가우시안으로 할 경우 MSE 관점에서 더 가까운 것으로 학습됨 (c) 가 의미적으로 (a) 에 더 가깝지만, MSE 는 (a)와 (b) 사이가 더 작음

$$||x - g_{\theta}(z_b)||^2 < ||x - g_{\theta}(z_c)||^2$$

이러면 (b) 같은 출력이 likelihood 가 높으므로 학습이 제대로 되지 않음

그래서 z 를 정규분포에서 샘플링하는 게 아니라 x 를 잘 생성해 줄 수 있는 이상적인 샘플링 함수 p(z|x)로부터 샘플링을 해보자 (x 를 evidence 로 줬으니까 x를 잘 만들겠지)

근데 p(z|x) 가 뭔지 모르니까 우리가 다루기 쉬운 확률 분포(예를 들면 가우시안) 중 하나를 가지고 파라미터를 조정해서 비슷하게 만들어 보자(=Variational Inference)



https://www.shakirm.com/papers/VITutorial.pdf

 $p(x), p(z|x), q_{\phi}(z|x)$ 사이의 관계식

$$\log(p(x)) = \int \log(p(x))q_{\phi}(z|x)dz \qquad \leftarrow \int q_{\phi}(z|x)dz = 1$$

$$= \int \log\left(\frac{p(x,z)}{p(z|x)}\right)q_{\phi}(z|x)dz \leftarrow p(x) = \frac{p(x,z)}{p(z|x)}$$

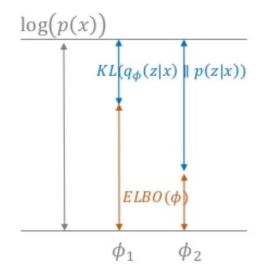
$$= \int \log\left(\frac{p(x,z)}{q_{\phi}(z|x)} \cdot \frac{q_{\phi}(z|x)}{p(z|x)}\right)q_{\phi}(z|x)dz$$

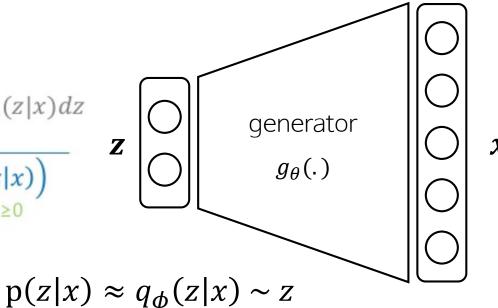
$$= \int \log\left(\frac{p(x,z)}{q_{\phi}(z|x)}\right)q_{\phi}(z|x)dz + \int \log\left(\frac{q_{\phi}(z|x)}{p(z|x)}\right)q_{\phi}(z|x)dz$$

$$ELBO(\phi) \qquad KL\left(q_{\phi}(z|x) \parallel p(z|x)\right)$$

$$= \frac{1}{2} \log \frac{p(z|x)}{p(z|x)} \log \frac{p(z|x)}{p(z|x)}$$

Evidence Lower Bound (ELBO)





KL term 을 최소화하는 것은 ELBO 를 최대화 하는 것과 동일함

$$\log \big(p(x)\big) = ELBO(\phi) + KL\big(q_\phi(z|x)\big|p(z|x)\big)$$

$$q_{\phi^*}(z|x) = \operatorname*{argmax}_{\phi} ELBO(\phi)$$

이상적인 샘플링 함수를 approximation 하기 위해 파라미터 ϕ 를 조절하여 ELBO 를 최대화 해야함

$$\begin{split} ELBO(\phi) &= \int \log \left(\frac{p(x,z)}{q_{\phi}(z|x)}\right) q_{\phi}(z|x) dz \\ &= \int \log \left(\frac{p(x|z)p(z)}{q_{\phi}(z|x)}\right) q_{\phi}(z|x) dz \\ &= \int \log \left(p(x|z)\right) q_{\phi}(z|x) dz - \int \log \left(\frac{q_{\phi}(z|x)}{p(z)}\right) q_{\phi}(z|x) dz \\ &= \mathbb{E}_{q_{\phi}(z|x)} \left[\log (p(x|z))\right] - KL \left(q_{\phi}(z|x) \middle| p(z)\right) \ \ \mathfrak{L} \Rightarrow 0. \end{split}$$

ELBO 를 다시 전개한 최종수식

Optimization problem 1 on ϕ

$$q_{\phi^*}(z|x) = \operatorname*{argmax}_{\phi} ELBO(\phi)$$

$$ELBO(\phi) = \mathbb{E}_{q_{\phi}(z|x)} \left[\log(p(x|z)) \right] - KL(q_{\phi}(z|x) | |p(z))$$

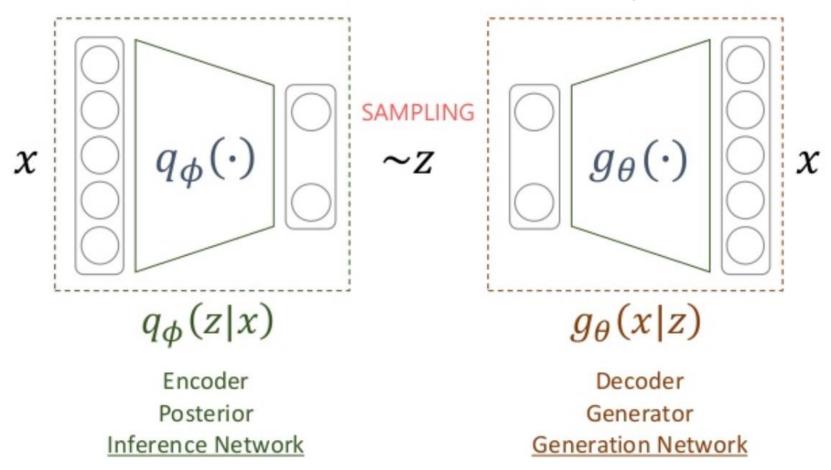
Optimization problem 2 on θ (Maximum likelihood 관점)

$$\arg\min_{\theta} \left(-\sum_{i} \log(p(x_i)) \right) = \arg\min_{\theta} \left(-\sum_{i} \left\{ ELBO(\phi) + KL(q_{\phi}(z|x)||p(z|x) \right\} \right)$$

Final Optimization problem

$$\arg\min_{\phi,\theta} \sum_{i} -\mathbb{E}_{q_{\phi}(z|x_{i})} \left[\log \left(p(x_{i}|g_{\theta}(z))\right)\right] + KL(q_{\theta}(z|x)||p(z))$$

이상적인 샘플링함수를 approximation 하는 함수가 $q_{\phi}(.)$



The mathematical basis of VAEs actually has relatively little to do with classical autoencoders.

원 데이터에 대한 likelihood 선택

Variational inference를 위한 approximation class 중 선택

다루기 쉬운 확률 분포 중 선택

$$L_i(\phi, \theta, x_i) = -\mathbb{E}_{q_{\phi}(z|x_i)} \left[\log \left(p_{\theta}(x_i|z) \right) \right] + KL \left(q_{\phi}(z|x_i) \middle| |p(z) \right)$$

Reconstruction Error

- 현재 샘플된 z에 대한 negative log 현재 샘플된 z에 대한 대한 추가 likelihood
- x_i 에 대한 복원 오차 (AutoEncoder 관점)

Regularization

- 조건
- 샘플링되는 z들에 대한 통제성을 prior를 통해 부여, Variational distribution q(z|x)가 p(z)와 유사해야 한다는 조건을 부여

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References

Paper

https://arxiv.org/pdf/1703.00848.pdf

- VAE 관련
 - Tutorial on Varialtional Autoencoders

https://arxiv.org/pdf/1606.05908.pdf

■ 오토인코더의 모든 것 - 2/3

https://www.youtube.com/watch?v=rNh2CrTFpm4&list=PLD7i1I-

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