(1) 计算T2统计量控制限和SPE统计量控制限;

$$T^{2}_{\text{UCL}} = \frac{k(n-1)}{n-k} \cdot F_{a}(k, n-k)$$

$$\vec{\mathbb{E}}T^{2}_{\text{UCL}} = \frac{k(n-1)(n+1)}{n(n-k)} \cdot F_{a}(k, n-k)$$

检验水平为 a 的 SPE 统计量控制上限为:

$$\begin{split} Q_{UCL} &= \theta_1 \big[1 + \frac{h_0 C_{\mathrm{a}} \sqrt{2\theta_2}}{\theta_1} + \frac{\theta_2 h_0 (h_0 - 1)}{{\theta_1}^2} \big]^{1/h_0} \\ \theta_1 &= \sum_{i=k+1}^m \lambda_i \,, \;\; \theta_2 = \sum_{i=k+1}^m \lambda_i^2 \,, \; \theta_3 = \sum_{i=k+1}^m \lambda_i^3 \,\,, h_0 = \frac{1 - 2\theta_2 \theta_3}{3{\theta_2}^2} \,, \end{split}$$

 C_a 是与(1-a)分位点对应的标准差

(2) 计算测试样本的T2统计量和SPE统计量

$$T_{(i)}^{2} = t_{(i)} \Lambda_{k}^{-1} t_{(i)}^{T} = X_{(i)_{S}} p_{k} \Lambda_{k}^{-1} p_{k}^{T} X_{(i)_{S}}^{T}$$

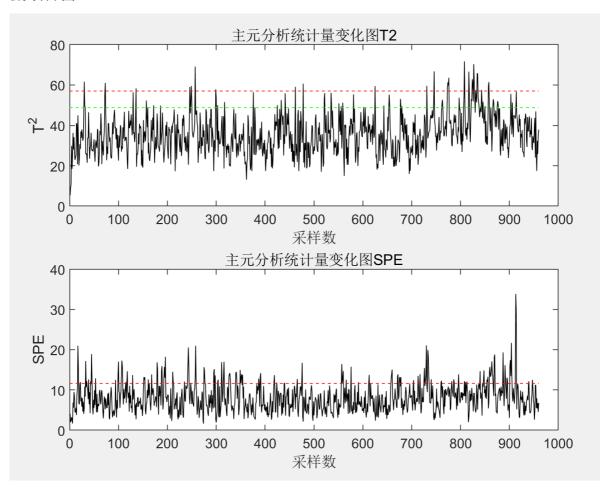
$$Q_{(i)} = X_{(i)_{S}} (I - p_{k} p_{k}^{T}) X_{(i)_{S}}^{T}$$

```
data=load('TE_data.mat');
%数据读取
data = struct2cell(data);
testdata = data(1:22);
train = cell2mat(data(23));
train = train';
train_mean = mean(train); %按列 Xtrain 平均值
train_std = std(train);
                       %求标准差
[train_row,train_col] = size(train); %求 train 行、列数
train=(train-repmat(train_mean,train_row,1))./repmat(train_std,train_row,1);
%归一化
%求协方差矩阵
sigmatrain = cov(train);
%对协方差矩阵进行特征分解, lamda 为特征值构成的对角阵, T的列为单位特征向量, 且与 lamda 中的特
[T,lamda] = eig(sigmatrain);
disp('特征根(由小到大)');
```

```
disp(lamda);
disp('特征向量: ');
disp(T);
%取对角元素(结果为一列向量),即 lamda 值,并上下反转使其从大到小排列,主元个数初值为 1,若累计
贡献率小于 90
%则增加主元个数
D = flipud(diag(lamda));
num_pc = 1;
while sum(D(1:num_pc))/sum(D) < 0.9
num\_pc = num\_pc +1;
end
%取与 lamda 相对应的特征向量
P = T(:,train_col-num_pc+1:train_col);
%每一列代表一个特征向量
%求置信度为 99%、95%时的 T2 统计控制限
T2UCL1=num_pc*(train_row-1)*(train_row+1)*finv(0.99,num_pc,train_row -
num_pc)/(train_row*(train_row - num_pc));
T2UCL2=num_pc*(train_row-1)*(train_row+1)*finv(0.95,num_pc,train_row -
num_pc)/(train_row*(train_row - num_pc));
%开始计算SPE统计量
for i = 1:3
   theta(i) = sum((D(num_pc+1:train_col)).^i);
h0 = 1 - 2*theta(1)*theta(3)/(3*theta(2)^2);
ca = norminv(0.99, 0, 1);
SPE = theta(1)*(h0*ca*sqrt(2*theta(2))/theta(1) + 1 + theta(2)*h0*(<math>h0 - 1)
1)/theta(1)^{2}/(1/h0);
%计算出了SPE统计量的界限
for k = 1:22
   %22组测试数据
   test = cell2mat(testdata(k));
   %开始在线检测
   n = size(test,1);
   test=(test-repmat(train_mean,n,1))./repmat(train_std,n,1);
   %测试样本归一化
   [r,y] = size(P*P');
   I = eye(r,y); %单位矩阵
   T2\_test = zeros(n,1);
   SPE\_test = zeros(n,1);
   for i = 1:n
       T2_test(i)=test(i,:)*P*inv(lamda(52-num_pc+1:52,52-
num_pc+1:52))*P'*test(i,:)';
       SPE\_test(i) = test(i,:)*(I - P*P')*test(i,:)';
   end
   %绘图
   figure (k);
   subplot(2,1,1);
   plot(1:n,T2_test,'k');
   title('主元分析统计量变化图T2');
   xlabel('采样数');
   ylabel('T^2');
   hold on;
   line([0,n],[T2UCL1],'LineStyle','--','Color','r');%画出标志线
   line([0,n],[T2UCL2,T2UCL2],'LineStyle','--','Color','g');
   subplot(2,1,2);
   plot(1:n,SPE_test,'k');
   title('主元分析统计量变化图SPE')
```

```
xlabel('采样数');
ylabel('SPE');
hold on;
line([0,n],[SPE,SPE],'LineStyle','--','Color','r');
end
```

仿真结果图:



这是测试te_00的仿真结果。

上述代码运行会输出所有数据的仿真结果, (这里粘贴了te_00为例子)